Landau symbol ("big O"): O(") for order of magnitude of complexity

O(Na) - exponential computational complexity

 $\lim_{N \to \infty} \frac{O(N^2)}{N^2} = A \neq 0$, ∞ i.e. $O(N^2)$ means AN^2 is the biggest contributer to the complexity $AN^2 + O(N)$, $A \neq 0 = constant$

4.2.2 k NN (k-Nearest Neighbours)

Idea: Follow the majority of k nearest training samples. $k \in IN$ k = 1: look for the closest neighbour. $To this case <math>w_2$ k = 3: We have 2 from <math>w, and 1 from w_2 . $So \ \hat{y} \ (\cancel{b}) = w$,

k=1 leads to overfitting and should not be bed

4.3 Bayes Plug-in

We use Bayes decision theory here Ch 2.

Bayesian decision theory:

P(X/Wj), P(Wj) -> MBR/MAP/ML/NP decision rule

In practice $\rho(2|w_j), \rho(w_j) \rightarrow unknown$

Idea: $p(X|W_j)$ known except for some unknown parameters Y_j .

i.e. $p(X|W_j; Y_j)$

eg. $2 lw_j \sim N(\underline{\mu}_j, \subseteq_j)$ $2 l = \{ \underline{\mu}_j, \subseteq_j \}$

Training:

Estimate 2;, P(W;) from N; training samples of class w;

 $\Rightarrow \hat{\gamma}_i, \hat{\rho}(\omega_i)$

Classification

use $\rho(x|w_j, \hat{y}_j)$ and $\hat{\rho}(w_j)$ in Bayesian decision

How to use estimate Li, P(W;)?

4.3.1 ML parameter estimation
A crash course: see SASP.

$$\frac{\mathcal{I}_{ml}(\mathcal{X})}{\mathcal{I}} = \underset{\mathcal{Y}}{\operatorname{arg max}} \ \rho(\mathcal{X}; \mathcal{Y}) \longrightarrow \underset{\operatorname{log-likelihood}}{\operatorname{likelihood}}$$

$$= \underset{\mathcal{Y}}{\operatorname{arg max}} \ \ln \rho(\mathcal{X}; \mathcal{Y}) \longrightarrow \underset{\operatorname{log-likelihood}}{\operatorname{log-likelihood}}$$

Necessary condition:

$$P \ln P(X; Y) \Big|_{Y = \frac{2}{2}mc} \stackrel{!}{=} 0$$

$$\nabla = \begin{bmatrix} \frac{\partial}{\partial v_i} \\ \frac{\partial}{\partial v_i} \end{bmatrix} \rightarrow \text{gradient vector}$$

E4.4 ML estimation for Gaussian distribution.

$$Z_n \in \mathbb{R}^d$$
 ($1 \leq n \leq N$), iid $N(\underline{M}, \underline{\subseteq})$

$$P\left(\underline{x}_{n};\underline{y}\right) = \frac{1}{(2\pi)^{d/2}} \sqrt{|\underline{c}|} \exp\left(-\frac{1}{2}\left(\underline{x}_{n} - \underline{u}\right)\right)$$

$$P(\chi_{1}...\chi_{N}; \underline{Y}) \stackrel{iid}{=} \frac{N}{1!} p(\chi_{0}; \underline{Y})$$

$$\log - \text{likelihood}:$$

$$L(Y) = \ln P(X_1 \dots X_N; Y)$$

$$\approx \text{constant} - \frac{N}{2} \ln |\mathcal{L}| - \frac{1}{2} \sum_{n=1}^{\infty} (X_n - \frac{N}{2}) \mathcal{L}(X_n - \frac{N}{2})$$

$$V = S \mathcal{U} \quad (C) \quad$$

$$V = \{ \underline{\mathcal{M}}, \subseteq \} \text{ contains } d \text{ elements } of \underline{\mathcal{M}} \quad \exists$$
and
$$\frac{d(d+1)}{2} \quad \exists \quad \subseteq \subseteq \subseteq \mathsf{T} \quad \mathsf{T}$$

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1.24.1

$$\hat{M} = \frac{1}{N} \frac{E}{2n} \frac{\pi}{2n}$$
 for $M = E(x)$

$$\hat{\zeta} = \frac{1}{N} \sum_{n=1}^{N} (x_n - \hat{n}) (x - \hat{a})^{T}$$
 for $\zeta = E[(x - \hat{b})(x - \hat{b})^{T}]$

stide 423

429.1

E4.5 cont : Solution

Method of Lagrange multiplier :

$$\frac{\partial \lambda}{\partial P_{j}} \Big| = \frac{N_{j}}{P_{j}} + \lambda \stackrel{!}{=} 0 \implies \hat{P}_{j} = -\frac{1}{\lambda} N_{j} \sim N_{j}$$

$$\frac{2}{2} = \frac{1}{2} = \frac{2}{2} = \frac{1}{2} = \frac{2}{2} = \frac{1}{2} = \frac{1}$$

4.3.9 Gaussian classifier

Idea: Bayes plug-in method . Assumption: Gaussian likelihood <u>L</u> | w; ~ N (u; , ⊆;)

ML estimate of Mj, Sj, P(Wj) according to \$ 4.4, E4.5 from training examples.

Stide 4-30

4-30.1

Comparision to nearest mean (4.2.1)

· nearest mean :

min Dmahe = (2-4;) 7 5; (x-4;)

or min max - Dmaha = - (2-4;) [= ; (1 - 4;)

· Gaussian classifier + MAP decision rule:

 $P(2|w_j, \widetilde{\mathcal{P}}_j) = \sim N(\widehat{\mathcal{A}}_j, \widehat{\mathcal{L}}_j)$ max $h P(1|w_i; \underline{\mathcal{V}}_j). \widehat{P}(\omega_j)$

= - \frac{1}{2} (x-4j) G' (x-4j) - \frac{1}{2} \land |\hat{C} | + \land \hat{g};

ch5: Advanced Optimization Techniques

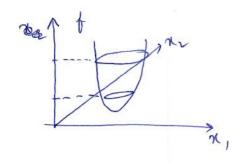
5.1 Challenges in Optimization

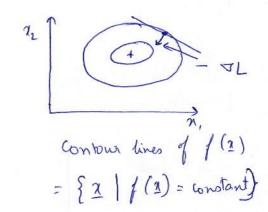
Slide 5-1

515.4.1

2 D visualization

$$f(\underline{x}) = f(x_1, x_2)$$





Slide 5-5