

## Sheet 8

Submission of the solutions: 21.12.2021, 14:00

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This exercise sheet is concerned with the topics

- Ordinary differential equations (ODEs)
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1. Solve the following ODEs

- a)  $(1 - x^2)u'(x) - xu(x) = 0;$
- b)  $u'(x) = \frac{1+u(x)}{1+x};$
- c)  $x \cos(xu)u' + (u \cos(xu) + 2x) = 0.$

2. Find the solutions for the ODEs

- a)  $u' = \frac{x^2-u}{x};$
- b)  $(x^2 - u^2)u' - 2xu = 0,$

by computing an integrating factor.

3. Find the solutions to the following linear ODEs with initial conditions  $u(0) = 0$ ,  $u'(0) = 1$

- a)  $u'' + u' - 6u = 0;$
- b)  $u'' - 4u' + 5u = 0.$