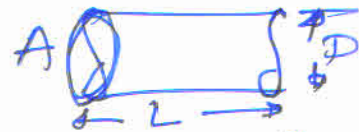


# Pneumatic Transport



Net force  $= \frac{1}{2} \rho_g \bar{U}_{g,superc}^2 A \epsilon + \frac{1}{2} \rho_p \bar{U}_{p,superc}^2 A (1 - \epsilon)$

$(\Delta P_{net}) A - F_{g,w} - F_{p,g,single} \times n$  - gravity force (for both gas & solid)

$f_{g,w} \rightarrow Re_{g,w} = \frac{\rho_g \bar{U}_{g,superc} D}{\mu_g}$

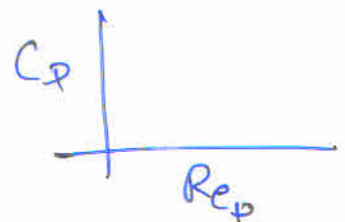
$F_{gw} = (\Delta P_{gw}) A \epsilon$   
 $= \frac{1}{2} f_{gw} \rho_g \bar{U}_{g,superc}^2 \frac{L}{D} A \epsilon$   
 $= \left( \frac{1}{2} f_{gw} \bar{U}_{g,superc}^2 \frac{L}{D} A \right) \underbrace{\rho_g \epsilon}_{\text{also known as dispersed gas density } \rho_{gd}}$

$d_p$  = particle diameter

$F_{g,p,single}$

$= \frac{1}{2} C_D \rho_g (\bar{U}_{g,superc} - \bar{U}_{p,superc})^2 \pi \frac{d_p^2}{4}$

$Re_p$



$Re_p = \frac{\rho_g (\bar{U}_{g,superc} - \bar{U}_{p,superc}) d_p}{\mu_g}$

$n$  = no of particles

$= \frac{A (1 - \epsilon)}{\frac{4}{3} \pi d_p^3}$

# Slurry Transport

## Homogeneous:-

If constitutive equation is not known, in that case one has to use Moody chart for knowing  $f$  (friction factor), which needs  $Re$  calculation.

$$Re = \frac{\rho_b U_s D}{\mu_l}$$

$\rho_b$  = bulk density of slurry.

if feed composition is  $a:b$  by mass% (liquid:solid)

$$\rho_b = \frac{a+b}{\frac{a}{\rho_l} + \frac{b}{\rho_s}}$$

$U_s$  = slurry superficial velocity

$$= \frac{\dot{m}_{\text{total of slurry}}}{A}$$



$\mu_l$  = liquid density

(although one should take  $\mu$  of slurry, however many times we approximate it with viscosity of carrying liquid)

## Heterogeneous

$$\frac{(\Delta P)_{\text{slurry}}}{(\Delta P)_{\text{carrying liquid}}} = f(\dots, C_D)$$

$\Delta P_{\text{carrying liquid}}$  needs

slurry superficial velocity  $\rightarrow$  need  $Re$  for liquid only.

$$Re = \frac{\rho_l U_s D}{\mu_l}$$

$U_s$  = slurry superficial velocity (means if liquid will flow with  $U_s$ , what will be  $Re$ )

$C_D$  is particle level calculation

$$Re_{\text{particle}} = Re_p$$

$$Re_p = \frac{\rho_l U_s d_p}{\mu_l} \quad (\text{particle diameter})$$