

05/03/19

## ( Production and cost )

→ Production is value addition process.

\* Short term:  $Q = f(L, \bar{K})$  ↑ fixed.  
L: Labour  
 long run:  $Q = f(L, K)$  K: capital

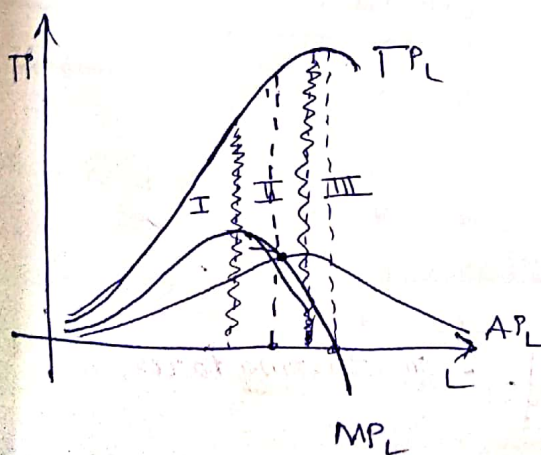
→  $Q$ : Total Product

→ Average Product =  $\frac{TP}{L}$

Marginal Product<sub>L</sub> =  $\frac{dTP}{dL}$

\*  $Q = -L^3 + 15L^2 + 10L$  (Short run)

∴ for different L: different Q



\* Law of diminishing marginal ~~labour~~ <sup>return.</sup> (something)

\* → more and more amount of variable input to fixed input then rate of output increase decreases.

\* All other factors constant : If Average production decreases then, no more labour input.

\*  $Q = AK^\alpha L^\beta$  Cobb Douglas functional form.

dim of returns to scale

$$\begin{aligned} hQ &= A(kK)^\alpha (kL)^\beta \\ hQ &= k^{\alpha+\beta} AK^\alpha L^\beta \end{aligned} \quad \left\{ \begin{array}{l} \text{Homogeneous of degree } \alpha+\beta. \end{array} \right.$$

If  $\alpha+\beta > 1$  : law of increasing return to scale ( $h > k$ )

$\alpha+\beta = 1$  : law of constant return to scale ( $h = k$ )

$\alpha+\beta < 1$  : " " decreasing " " " ( $h < k$ )

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$$\begin{aligned} MP_K &= \frac{dQ}{dK} = \alpha AK^{\alpha-1} L^\beta \\ &= \alpha A \left( \frac{K}{L} \right)^{\alpha-1} \end{aligned}$$

$$MP_L = \beta A \left( \frac{K}{L} \right)^{1-\beta}$$

$$\boxed{\ln Q = \ln A + \alpha \ln K + \beta \ln L} \rightarrow \text{smoothing factor.}$$

$$\frac{dQ}{dK} \cdot \frac{K}{Q} = \alpha \text{ (elasticity)}$$

\*  $\alpha$  and  $\beta$  represent distributive share of production to wrt capital and labour.

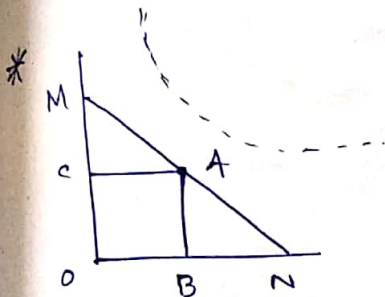
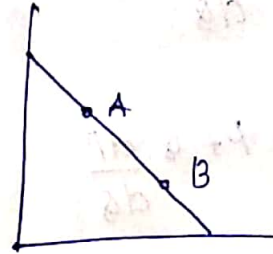


## Price elasticity of demand

$$e_p = \frac{\% \text{ change in quant demanded}}{\% \text{ change in price of commodity}}$$

$$Arc = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q}$$

$$\text{Point Elasticity: } -\frac{dQ}{dP} \cdot \frac{P}{Q}$$



$$e = -\frac{dQ}{dP} \cdot \frac{P}{Q} = \frac{BN}{AB} = \frac{\Delta B}{\Delta B} = \frac{AM}{\Delta M}$$

$$e_p = \frac{\text{Lower segment}}{\text{Upper segment}}$$

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## Determinants of Elasticity

$e=1 \Rightarrow$  unitary elasticity

~~$e=1$~~

$$* Q = a - bP \Rightarrow e = -b \frac{P}{Q}$$

$$Q = aP^{-b} \Rightarrow e = -b$$

→ Luxury good: high elasticity

\* for profit: at high elasticity reduce price marginally

∴ (i) Nature of Commodity.

(ii) Proportion of income spent on commodity.

(iii) Time factor for adjusting to change.

(iv) Possibility of reduction in consumption of a commodity.

$$T.R. = P \times Q$$

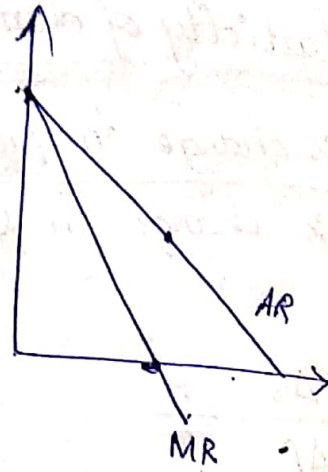
$$A.R. = \frac{TR}{Q} = P$$

$$MR = \frac{d(TR)}{dQ}$$

$$= P + Q \cdot \frac{dP}{dQ}$$

$$= P \left( 1 + \frac{Q}{P} \cdot \frac{dP}{dQ} \right)$$

$$MR = P \left( 1 - \frac{1}{e_p} \right) = AR \left( 1 - \frac{1}{e} \right)$$



Income elasticity

$$e_i = \frac{\% \text{ change in demand}}{\% \text{ change in income}}$$

$$= \frac{dQ}{dH} \cdot \frac{H}{Q}$$

Cross Elasticity

$$e_c = \frac{\% \text{ change in demand of } X}{\% \text{ change in demand price of } Y}$$

$$e_{t,c} = \frac{dQ_t}{dP_c} \cdot \frac{P_c}{Q_t}$$

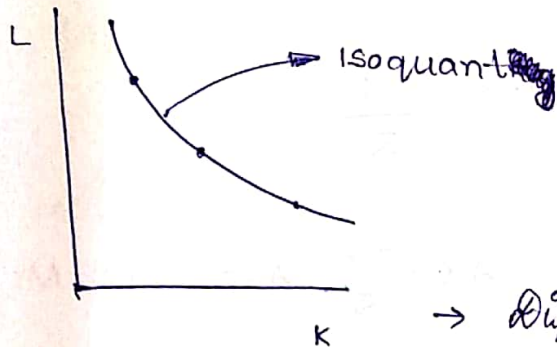


## Elasticity of supply

$$e_s = \frac{\% \text{ change in quantity supplied}}{\% \text{ change price of good.}}$$

$$= \frac{dQ_s}{dP} \cdot \frac{P}{Q_s}$$

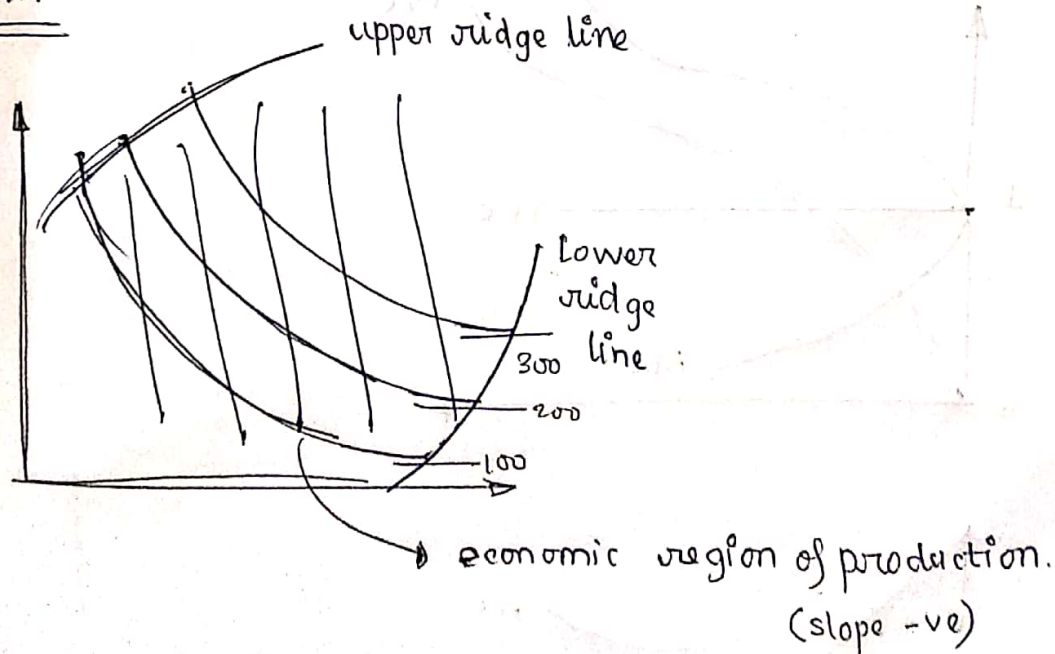
## \* Isoquant



→ Output same but some labour intensive, some capital intensive.

→ Different combinations of labour and capital to produce same output.  
Properties same as indifference curve.

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## Short Run Production (all inputs fixed)

$$\text{Total cost} = 10 + 6Q - 0.9Q^2 + 0.05Q^3$$

$\downarrow$  total fixed cost       $\downarrow$  total variable cost.

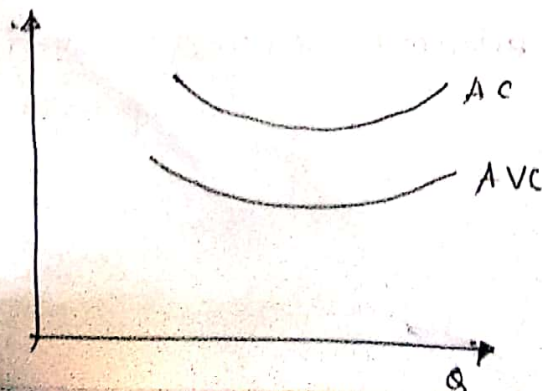
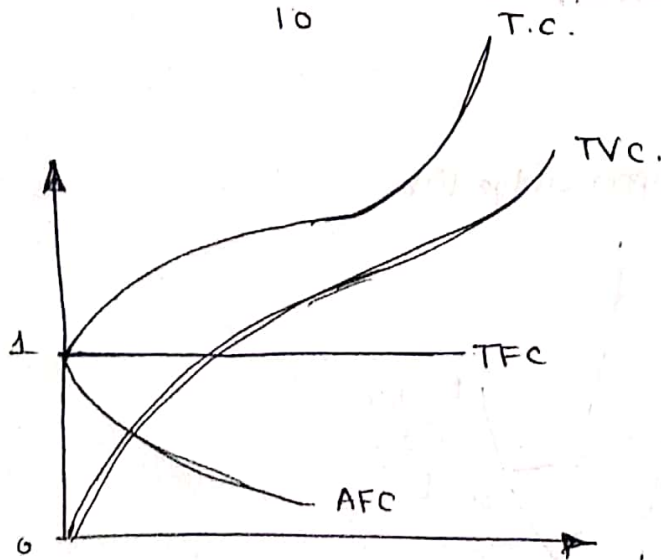
$$\text{Average cost} = \frac{T.C}{Q}$$

$$M.C = \frac{d(TC)}{dQ}$$

$$A.V.C = \frac{T.V.C}{Q}$$

$$AFC = \frac{TFC}{Q}$$

Q	TC	TFC	TVC	A.C = $\frac{T.C}{Q}$	AFC	AVC	MC
1		10					
2		10					
3		10					



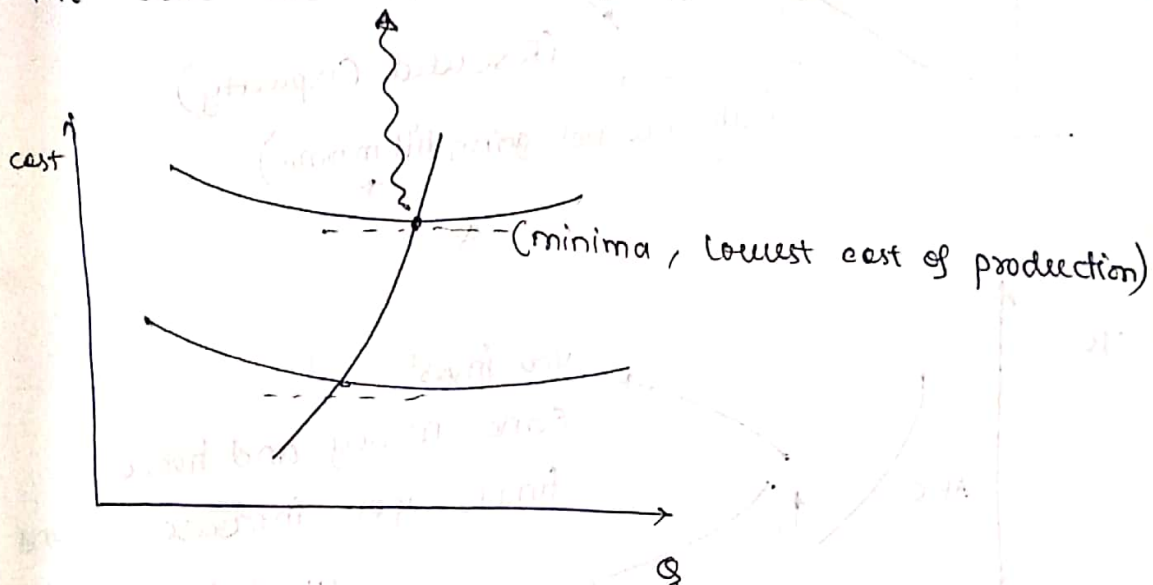
now

$$M.C. = \frac{dT.C}{dQ} = \frac{d(AC \cdot Q)}{dQ}$$

$$= Q \cdot \frac{dAC}{dQ} + AC$$

$$\frac{dAC}{dQ} = \frac{1}{Q} (M.C. - A.C)$$

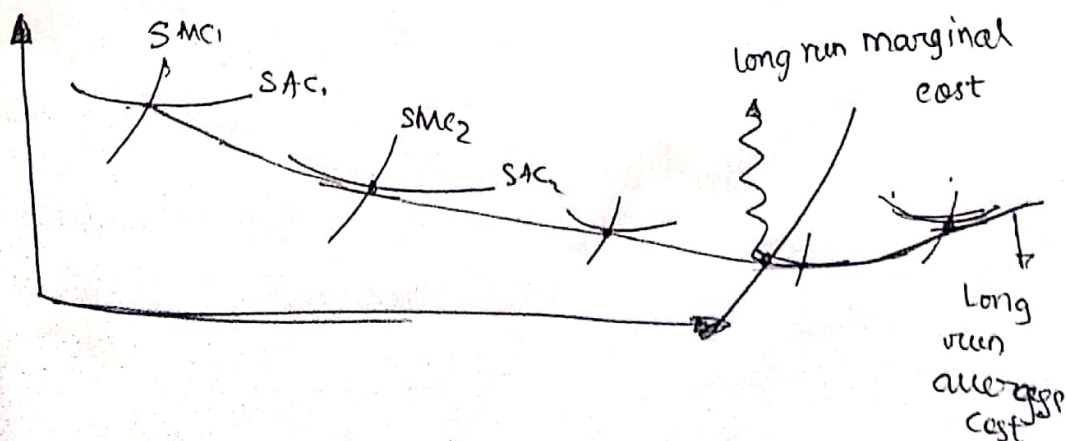
MC cuts AC at its minima



$$\text{Total profit : } \pi = TR - TC$$

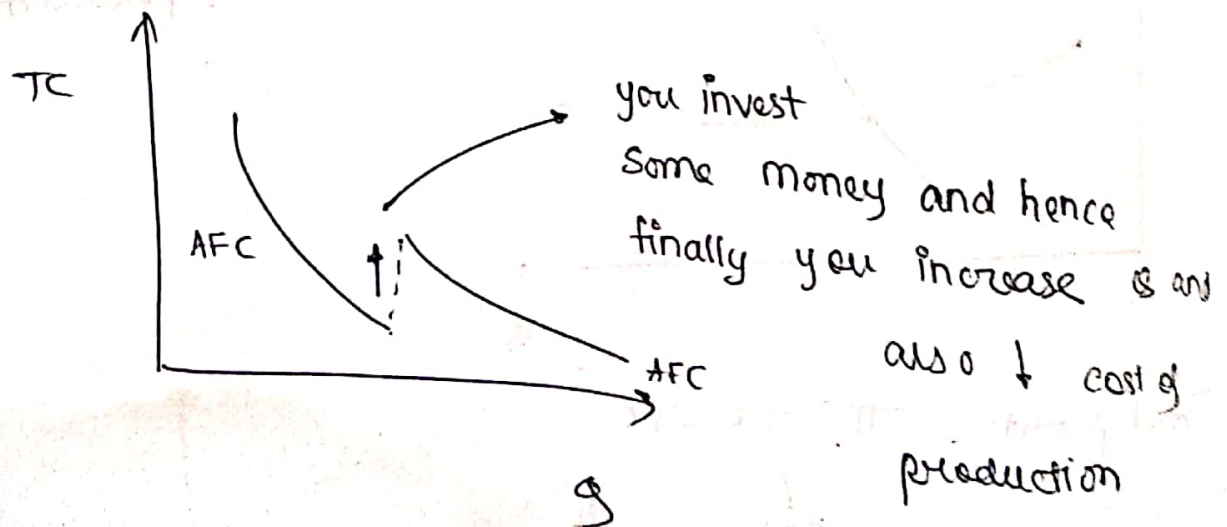
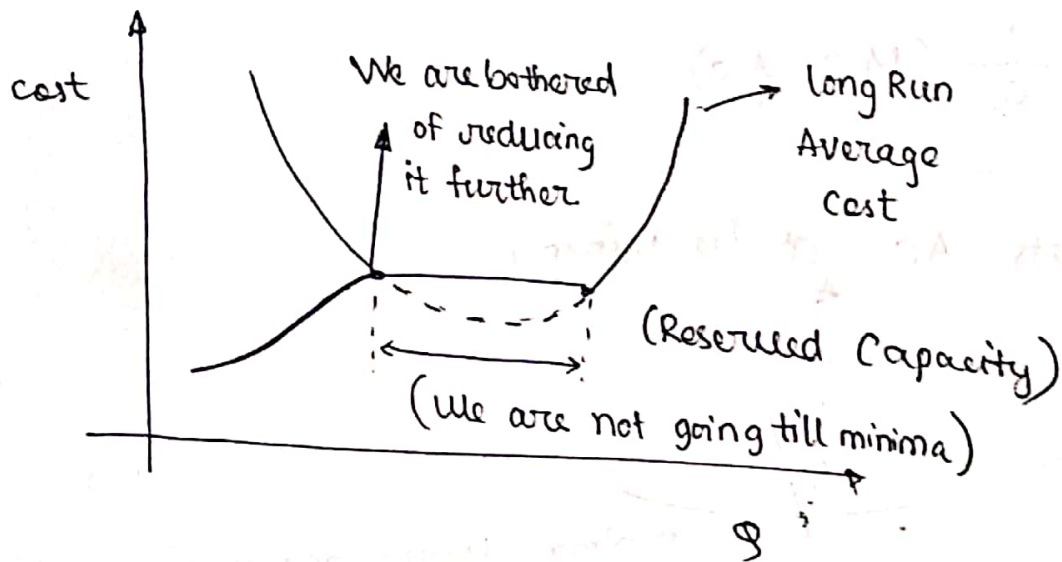
(PQ)

Long Run Production. (sum of short runs)





Due to inefficiencies in the process of production,  
we are always producing in the negatively  
sloped region of cost-s curve





09/01/19

## Opportunity cost

→ return lost by not taking 2nd best preference.

\* Business cost & full cost



along with BC

Opportunity cost and ~~return~~

minimal profit

\* Explicit cost : Appearing on account

Implicit cost : Imputed cost of family labour  
(no salary)

\* private cost, social cost = private + external cost

\* External cost

Economies in scale, diseconomies in scale

↗ average cost goes up

\* Average Cost decreases by increase in scale.

\* Average cost decreases by

→ increase efficiency.

→ Reduce other cost