ASSIGNMENT-1 (F.M. 50 Marks)

Overall Mars Balance: (1)

15 Marks

Tank 1: A, oth = F, -F2.

Tank 2: Az dhe = F2-F3

Using deviational variables and in laplace domain.

Tank 1: A, S T, (s) = F, (s) - F_2 (s)

 $A_2 S \overline{h}_2 (S) = \overline{f}_2 (S) - \overline{f}_3 (S)$ Tank 2:

Measured output / controlled variable: h_(s)

Manipulated input/ Control variable: F,(s), F2(s), F3(s)

(a) Controller (PE): Gie = Kc (1+1)

Case1: Fi (s) is the manipulated variable

 $F_{5}(s) = \alpha_{1}h_{1}(s)$; $F_{3}(s) = \alpha_{2}h_{2}(s)$

From (1) and (2); Substituting the value of F2 (3) and F3 (5)

A1 Sh, (8) = F, (8) - d, h, (5)

 $\overline{h}_{1}(s) = \frac{(1/\alpha_{1})}{(\frac{A_{1}}{\alpha_{1}})s+1} \overline{F}_{1}(s) \Rightarrow \overline{h}_{1}(s) = \frac{(1/\alpha_{1})}{(\overline{T}_{1}s+1)} \overline{F}_{1}(s)$

where, 7,2 A1/0/

Also, A25 h2(s) = 0, h, (s) - 02 h2(s)

 $= A_{2} S h_{2} (S) = \frac{\alpha_{1} (\sqrt{\alpha_{1}})}{(75+1)} \bar{F}_{1} (S) - \alpha_{2} \bar{h}_{2} (S)$

 $\frac{1}{42} = \frac{1}{42} = \frac{1}{42}$

where, $z_2 = \frac{A_2}{\alpha_0}$.

Let (1/42) = Gp(s) .. h2 (s) = Gp (s) F, (s)

h2, sp + & & Gre = 1 F1 1/02 (75+1) (75+1)

closed - loop block diagram.

$$\begin{array}{llll} \frac{Cau2}{\bar{F}_{3}(s)} & = \mathcal{A}_{2} \, \bar{h}_{2}(s) \\ & = \mathcal{A}_{2} \, \bar{h}_{2}(s) \\ & = \mathcal{A}_{1} \, \bar{h}_{1}(s) & = \bar{F}_{1}(s) - \bar{F}_{2}(s) \\ & \Rightarrow & \bar{h}_{1}(s) & = \bar{f}_{1}(s) - \bar{f}_{2}(s) \\ & \Rightarrow & \bar{h}_{1}(s) & = \bar{f}_{1}(s) - \bar{f}_{2}(s) \\ & \Rightarrow & \bar{h}_{1}(s) & = \bar{f}_{2}(s) - \bar{f}_{3}(s) \\ & & & & & & & & & & & & & & & \\ & & & & & & & & & & & \\ & & & & & & & & & & \\ & & & & & & & & & \\ & & & & & & & & & \\ & & & & & & & & \\ & & & & & & & & \\ & & & & & & & & \\ & & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & & \\ &$$

Closed loop block diagram.

(b) General form of Closed loop transfer function

$$y = \frac{Gp G_1 G_2}{|1+ Gp G_1 G_1 G_1 G_2} y_{Sp} + \frac{Gd}{|1+ Gp G_2 G_1 G_2 G_2 G_2} x_{Sp} = \frac{Gd}{|1+ Gp G_2 G_1 G_2 G_2 G_2} x_{Sp} + \frac{Gd}{|1+ Gp G_2 G_1 G_2 G_2 G_2} x_{Sp} + \frac{Gd}{|1+ Gp G_2 G_2 G_2 G_2 G_2} x_{Sp} + \frac{Gd}{|1+ Gp G_2 G_2 G_2 G_2} x_{Sp} + \frac{Gd}{|1+ Gp G_2 G_2} x_{Sp} + \frac{Gd}{$$

[Case 2]
$$(a, b) = \frac{kc(1+\frac{1}{2}s)(\frac{1/4c}{2s+1})}{1+ kc(1+\frac{1}{2}s)(\frac{1/4c}{2s+1})} [From \]$$
 $1+ kc(1+\frac{1}{2s})(\frac{1/4c}{2s+1})$
 $1+ kc(1+\frac{1}{2s+1})(\frac{1/4c}{2s+1})$
 $1+ kc(1+\frac{1}{2s+1})(\frac{1/4c}{2s+1})$
 $1+ kc(1+\frac{1}{2s+1})(\frac{1}{2s+1})$
 $1+ kc(1+\frac{1}{2s+1})(\frac{1/4c}{2s+1})$
 $1+ kc(1+\frac{1}{2s+1})(\frac{1/4c}{2s+1$

(d)

2) For a feedback control system the Characteristic equation is give by. 1+ Gip Gif Ge Gim. Gm = Gf = 1, Gre = Ke (: proportional controller) Gp(S) = 10 (a) Characteristic equation: 1+ 10kc. To find the roots of the characteristic equation. A feedback control system is said to be stable if all the roots of its characteristic equation have negetive real parts. To produce Stable closed loop response -10ket/20 > | Kc > 10 Gp(3) = 2 (b) Characteristic equation: 1+ 2KC 0.18+1 $1 + \frac{2kc}{0.1s+1} = 0 \Rightarrow 0.1s+1+2kc=0 \Rightarrow s = \frac{(2kc+1)}{0.1}$.. Any value of ke will result in Stable Closed loop response. (c) characteristic equation: 1+ 10kc 252+35-4 1+ 10ke =0 => 2s2+3s+(10ke-4)=0 -3 ± \(\q - 8 \) (10 kc-4) To produce Stable closed loop responer - 8 (10ki-4) LO >> Kc > 2/5 (d) Characteristic equation: 1+ kc 1+ Kc 20 >> 353+252+5+6 (Kc-5)=0. From Routh - Hurwitz criterion. 2 (kc-5) 2-3(kc-5)70 => kc < 5+2 => kc < 17. Also, ke-5>0 > ke>5 5 < Ke < \frac{17}{3}

Cop(5) =
$$\frac{1}{105^3 + 25^2 + 5 - 5}$$

Characteristic equation: $1 + \frac{Kc}{105^3 + 25^2 + 5 - 5}$
 $1 + \frac{Kc}{105^3 + 25^2 + 5 - 5} = 0 \implies 105^3 + 25^2 + 5 + (Kc - 5) = 0$
From Routh - Hurwitz stability culterion:
 $Kc - 5 > 0 \implies Kc > 5$
 $10 \quad 1$
 $2 \quad (Kc - 5)$
 $2 - 10(Kc - 5) > 0$
 $2 \quad (Kc - 5)$
 $2 \quad (Kc - 5)$

Characteristic equation: 1+ GpGcGgGm

1+
$$\frac{kc}{(S+1)(2S+1)} = 0$$
 to find the roots of the Characteristic $(S+1)(2S+1)+kc=0$
 $2S^2+3S+(kc+1)=0$
 $S=-3\pm\sqrt{9-8(kc+1)}$: Roots are $-3\pm\sqrt{9-8(kc+1)}$

Let the two roots be represented as $\sqrt{9}$ and $\sqrt{2}$

We vary the value of ke in the range 0< Ke < so and evaluate the values of of and of.

Then we plot all the roots in the complex plane.

	kc	81	Y2
-	0	- <u>1</u> (A)	-1 B
	8	$-\frac{3}{4}$ ©	- <u>3</u> ©
	1/4	$-\frac{3}{4}+\dot{j}\frac{1}{4}$	-3 - j 1 E
	1		

(3)

$$Rc \rightarrow \infty$$
 $A \perp m$
 $B \rightarrow C \wedge A$
 $E \rightarrow \infty$
 $E \rightarrow \infty$

- (a) AC, BC & overdamped
- (b) Point C Critically damped
- (C) CD, CE < underdamped.

closed loop transfer function for set point change (suppose)

Generalized form of 2nd order transfer function

mparity
$$\gamma^2 = \frac{1}{V_{K,t+1}}$$

$$2 = \frac{1}{V_{K,t+1}}$$

$$279 = \frac{3}{12} \Rightarrow 9 = \frac{3}{2} \frac{1}{\sqrt{16c+1}}$$

Also, it is given that dream ratio = 4

AHSO, IT IS
$$0 - 2 \times 9$$

$$1 - 2 \times 9$$

$$1 - 3 \times 9$$

$$1 - 4$$

$$\Rightarrow \frac{2\pi y}{\sqrt{1-y^2}} = \frac{1.386}{2} = 0.215 - 2$$

From (1) and (2)

$$\frac{3}{2}\sqrt{\frac{1}{k_{c}+1}}=0.215$$

(5) (and Using Oz as the manipulated Variable

10 Marks

$$\overline{T}_{2}(s) = \frac{1}{4s+1} \overline{T}_{1}(s) + \frac{0.2}{4s+1} \overline{G}_{1}(s)$$

$$\overline{T}_3(s) = \frac{1}{10s+1} \overline{T}_2(s) + \frac{0.1}{10s+1} \overline{Q}_2(s)$$

$$= \frac{1}{10s+1} \cdot \frac{1}{4s+1} \cdot \frac{1}{T_1(s)} + \frac{0.1}{10s+1} \cdot \frac{0}{Q_2(s)} + \frac{1}{10s+1} \cdot \frac{0.2}{4s+1} \cdot \frac{0}{Q_1(s)}$$

Ti (s) vis the disturbance Variable.

Let us neglet the disturbance ((5)

$$\overline{T}_3(s) = \frac{0.1}{105+1} \overline{Q}_2(s) + \frac{1}{(105+1)(45+1)} \overline{T}_1(s)$$

Closed loop response:

For 10%. Step change un the value of disturbance.

When Ti, ss is the Steady State value of disturbane Ti

$$T_3(s) = \frac{1}{(10S+1)(4S+1)} = \frac{0.1 T_{1,55}}{1 + 0.1 \cdot Kc}$$

Offset =
$$0 - dt$$
 S. $\overline{T}_3(s)$
S $\Rightarrow 0$

Minimum offset is obtained at maximum ke value at ke=100.

Case 2 using & as the manipulated variable From O, $\overline{T}_{3}(s) = \frac{1}{10s+1} \cdot \frac{1}{4s+1} \cdot \overline{T}_{1}(s) + \frac{0.1}{10s+1} \cdot \overline{\Theta}_{2}(s) + \frac{1}{10s+1} \cdot \frac{0.2}{4s+1} \cdot \overline{\Theta}_{1}(s)$ T, (S) is the disturbance variable. Let us neglet the disturbance Q (S). $\overline{T}_{3}(s) = \frac{0.2}{(10S+1)(4S+1)} \overline{O}_{1}(s) + \frac{1}{(10S+1)(4S+1)} \overline{T}_{1}(s)$ = Gp(s) Q(s) + Gd(s) T,(s). closed loop response for 10%. Step change in the value of disturbance. $T_3(s) = \frac{1}{(105+1)(45+1)} \cdot \frac{0.1T_{1,55}}{s}$ 1+ 0.2 KC (105+1) (45+1) = (4st) (10st) +0.2kl S. Offset = $0 - \alpha t$ S. $\overline{13}$ (S) $5 \rightarrow 0$ 0.1 Tr, ss $2 \quad 0 - \underline{1}$ 1+0.2 KeMinimum Offset is obtained at Kc=100. Minimum aff set 2-0.0048 T1,55 -3 From @ and 3 it can be concluded that Employing the minimum offset criterion we select Q as the manipulated variable.