

$$\text{Q2. } \begin{bmatrix} 1 & h & -3 \\ h & 4 & 6 \end{bmatrix} \quad \text{--- (1)}$$

$$\checkmark hR_1 - R_2 \begin{bmatrix} 1 & h & -3 \\ 0 & 4-h^2 & -3h-6 \end{bmatrix} \quad \text{--- (2)}$$

~~Q2~~ ~~Q2~~ ~~Q2~~ ~~Q2~~

Considering (1), if $h = -2$
we get $\begin{bmatrix} 1 & -2 & -3 \\ -2 & 4 & 6 \end{bmatrix}$

$$-2R_1 = R_2$$

$$\text{R}_2 / -2 \begin{bmatrix} 1 & -2 & -3 \\ 1 & -2 & -3 \end{bmatrix}$$

~~Q2~~

Considering (2), if ~~we get~~ $h = 2$
we get $\begin{bmatrix} 1 & 2 & -3 \\ 0 & 0 & -12 \end{bmatrix}$

- (i) exactly one solution when $h \neq 2$ and $h \neq -2$
- (ii) no solution when $h = 2$ since REF is inconsistent
- (iii) infinitely many solutions when $h = -2$ because $R_1 = R_2$ (after scaling)