

```
!git clone https://github.com/SwastikGorai/NN-from-scratch.git
```

```
fatal: destination path 'NN-from-scratch' already exists and is not an empty directory.
```

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
```

```
dataset = pd.read_csv("dataset/train.csv")
```

```
dataset.head(10)
```

	label	pixel0	pixel1	pixel2	pixel3	pixel4	pixel5	pixel6
0	1	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0
2	1	0	0	0	0	0	0	0
3	4	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0	0
6	7	0	0	0	0	0	0	0
7	3	0	0	0	0	0	0	0
8	5	0	0	0	0	0	0	0
9	3	0	0	0	0	0	0	0

	pixel8	...	pixel774	pixel775	pixel776	pixel777	pixel778
0	0	...	0	0	0	0	0
1	0	...	0	0	0	0	0
2	0	...	0	0	0	0	0
3	0	...	0	0	0	0	0
4	0	...	0	0	0	0	0
5	0	...	0	0	0	0	0

```

0
6      0 ...      0      0      0      0      0
0
7      0 ...      0      0      0      0      0
0
8      0 ...      0      0      0      0      0
0
9      0 ...      0      0      0      0      0
0

```

```

      pixel780  pixel781  pixel782  pixel783
0           0         0         0         0
1           0         0         0         0
2           0         0         0         0
3           0         0         0         0
4           0         0         0         0
5           0         0         0         0
6           0         0         0         0
7           0         0         0         0
8           0         0         0         0
9           0         0         0         0

```

```
[10 rows x 785 columns]
```

```
data = np.array(dataset)
```

```
data
```

```

array([[1, 0, 0, ..., 0, 0, 0],
       [0, 0, 0, ..., 0, 0, 0],
       [1, 0, 0, ..., 0, 0, 0],
       ...,
       [7, 0, 0, ..., 0, 0, 0],
       [6, 0, 0, ..., 0, 0, 0],
       [9, 0, 0, ..., 0, 0, 0]], dtype=int64)

```

```
row,column = data.shape
```

```
print(row,column)
```

```
42000 785
```

```
train, test = train_test_split(data, test_size = 0.2)
```

```
train, test = train.T , test.T
```

```
train_y = train[0]
```

```
train_x = train[1:]
```

```
train_x = train_x/255.
```

```
test_x = test[0]
test_y = test[1:]
test_y = test_y/255.

train_x[:,0].shape # or train_x.shape[0]
(784,)
```

## Create parameters, weights, functions

### Initialize the weights and Biases

```
def initialize():

    weight_1 = np.random.rand(10,784) -0.5
    bias_1 = np.random.rand(10,1) -0.5

    weight_2 = np.random.rand(10,10) -0.5
    bias_2 = np.random.rand(10,1) -0.5

    weight_3 = np.random.rand(10,10) -0.5
    bias_3 = np.random.rand(10,1)-0.5

    return weight_1, bias_1, weight_2, bias_2, weight_3, bias_3
```

### Define the Rectified Linear Unit (ReLU) function:

$\text{Relu}(z) = \max(0, z)$

```
def ReLU(x):
    return np.maximum(x,0)

def derivative_ReLU(x):
    return x>0
```

### Define the softmax function

$$\sigma(z_i) = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_j}} \text{ for } i=1,2,\dots,K$$

```
def Softmax(x):
    # x = np.float128(x)
    e = np.exp(x) / sum(np.exp(x))
    return e
```

## Define the Forward Propagation function

```
def forward_propagation(w1, b1, w2, b2, w3, b3, layer):
    Z1 = w1.dot(layer) + b1
    L1 = ReLU(Z1)

    Z2 = w2.dot(L1) + b2
    L2 = ReLU(Z2)

    Z3 = w3.dot(L2) + b3
    L3 = Softmax(Z3)

    return Z1, L1, Z2, L2, Z3, L3
```

## Define a One-Hot-Encoding Function

```
def one_hot_encode(Y):
    one_hot_Y = np.zeros((Y.size, Y.max() + 1))
    one_hot_Y[np.arange(Y.size), Y] = 1
    one_hot_Y = one_hot_Y.T
    return one_hot_Y
```

### Explanation:

1. `one_hot_Y = np.zeros((Y.size, Y.max() + 1))`:

Creates a matrix of size `Y.size` and `Y.max() + 1`. `Y.max() + 1` means that if there are 3 distinct values, say `Y = [3, 1, 2]` then there would be 4 columns and 3 rows created (incl. 0) like `[[0, 0, 0, 0], [0, 0, 0, 0], [0, 0, 0, 0], ]`

2. `one_hot_Y[np.arange(Y.size), Y] = 1`

- `np.arange(Y.size)` creates a range of values starting from 0, For example, if `Y` is `[3, 1, 2]` then `np.arange` would create `[0, 1, 2, 3]`
- `one_hot_Y[np.arange(Y.size), Y]` will be like:
  - i. `one_hot[0, 3] = 1`
  - ii. `one_hot[1, 1] = 1`
  - iii. `one_hot[2, 2] = 1`

3. Next, transposing the values, to bring labels to column headers. Here, each row is a record (or value). We need each column to be a record (or value).

## Define the Backward Propagation Function

```
def backward_propagation(Z1, L1, W1, Z2, L2, W2, Z3, L3, W3, X, Y):
    one_hot_y = one_hot_encode(Y)
    m = Y.size
    # Find the gradient of loss function wrt to the pre-activated values
    # (Z2) of the output layer
    dz3 = L3 - one_hot_y # This calculation essentially measures the
```

*difference between the predicted output and the true target for each class. It gives us a measure of how much the predictions deviate from the actual target class probabilities.*

*# find the gradient of the loss function wrt to the Weights in the output layers*

*dw3 = 1 / m \* dz3.dot(L2.T) # This multiplication effectively calculates how the gradients of z3 with respect to the weights w3 influence the overall loss. The 1/m rescales the resultant.*

*# Find the gradient of the loss function wrt to the biases in the output layer*

*# db3 = 1 / m \* np.sum(dz3) # Summing its(dz3) elements gives a measure of how the loss function changes with respect to changes in the overall output of the output layer.*

*db3 = 1 / m \* np.sum(dz3, axis=1).reshape(-1, 1)*

*dz2 = W3.T.dot(dz3) \* (derivative\_ReLU(dz3))*

*dw2 = 1 / m \* dz3.dot(L1.T)*

*# db2 = 1 / m \* np.sum(dz2)*

*db2 = 1 / m \* np.sum(dz2, axis=1).reshape(-1, 1)*

*dz1 = W2.T.dot(dz2) \* (derivative\_ReLU(dz2))*

*dw1 = 1 / m \* dz2.dot(X.T)*

*# db1 = 1 / m \* np.sum(dz1)*

*db1 = 1 / m \* np.sum(dz1, axis=1).reshape(-1, 1)*

*return dw3, db3, dw2, db2, dw1, db1*

## Define the function to apply changes to the values

```
def update(W1, W2, W3, B1, B2, B3, dw1, dw2, dw3, db1, db2, db3, learning_rate):
```

```
    W1 = W1 - learning_rate * dw1
```

```
    B1 = B1 - learning_rate * db1
```

```
    W2 = W2 - learning_rate * dw2
```

```
    B2 = B2 - learning_rate * db2
```

```
    W3 = W3 - learning_rate * dw3
```

```
    B3 = B3 - learning_rate * db3
```

```
    return W1, W2, W3, B1, B2, B3
```

## Define function to get predictions and accuracy

```
def predict(output_L):
```

```
    return np.argmax(output_L, axis=0) # axis = 0=> max values along rows
```

```
def accuracy(preds, labels):
```

```
is_correct = np.sum(preds == labels)
return is_correct/labels.size
```

## Using Gradient descent

```
def gradient_descent(X, Y, epochs, learning_rate):
    W1, b1, W2, b2, W3, b3 = initialize()
    for i in range(epochs):
        Z1, L1, Z2, L2, Z3, L3 = forward_propagation(W1, b1, W2, b2, W3,
        b3, X)
        dw3, db3, dw2, db2, dw1, db1 = backward_propagation(Z1, L1, W1,
        Z2, L2, W2, Z3, L3, W3, X, Y)
        W1, W2, W3, b1, b2, b3 = update(W1, W2, W3, b1, b2, b3, dw1, dw2,
        dw3, db1, db2, db3, learning_rate )
        if i%10 == 0:
            print("-----")
            print("Epoch ==> ", i)
            preds = predict(L3)
            acc = accuracy(preds, Y)
            print("Accuracy : ", acc )

    print("-----")
    return W1, b1, W2, b2, W3, b3
```

## Training

```
W1, b1, W2, b2, W3, b3 = gradient_descent(train_x, train_y, 100, 0.1)
```

```
-----
Epoch ==> 0
Accuracy : 0.14098214285714286
```

```
-----
Epoch ==> 10
Accuracy : 0.15142857142857144
```

```
-----
Epoch ==> 20
Accuracy : 0.07639880952380952
```

```
-----
Epoch ==> 30
Accuracy : 0.13848214285714286
```

```
-----  
Epoch ==> 40  
Accuracy : 0.2833333333333333  
-----
```

```
-----  
Epoch ==> 50  
Accuracy : 0.37973214285714285  
-----
```

```
-----  
Epoch ==> 60  
Accuracy : 0.38916666666666666  
-----
```

```
-----  
Epoch ==> 70  
Accuracy : 0.36622023809523807  
-----
```

```
-----  
Epoch ==> 80  
Accuracy : 0.4249107142857143  
-----
```

```
-----  
Epoch ==> 90  
Accuracy : 0.4616369047619048  
-----
```