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PES University, Bangalore (Established under Karnataka Act No. 16 of 2013)

UE16CS311

END SEMESTER ASSESSMENT (ESA) B.Tech. V SEMESTER - Dec. 2018

UE16CS311 - Advanced Algorithms

I - I	S Answer All Questions	Max Marks: 1
1a Algo	rithm Run(n) count ← 0 i ← n while(i > 0) j ← 1 while(j <= i) for k ← 1 to n count ← count + 1 j ← j + 2 i ← floor(i / 2) return count	06
Find	the worst-case asymptotic time complexity of the above algorithm in	- G-notation
Using	<pre>EMENT(A[0k-1]) i ← 0 while i < k and A[i] = 1 A[i] ← 0 (toggles the bit) i ← i + 1 if i < k then A[i] ← 1 (toggles the bit) "Aggregate Method", find the amortized cost of the above of the abov</pre>	06
increr	ments a binary number A[0k-1].	08
TAI 1 2 3 4 5 6 7 8 9	if $size[T] = 0$ then allocate $table[T]$ with 1 slot $size[T] \leftarrow 1$ if $num[T] = size[T]$ then allocate new -table with $2 \cdot size[T]$ slots insert all items in $table[T]$ into new -table free $table[T]$ $table[T] \leftarrow new$ -table $size[T] \leftarrow 2 \cdot size[T]$	

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2a	Find the pattern "31415" in the text "2359023141526739921" using the Rabin-Karp method. Use radix-10 with "mod 13" for finding the hash values.	06
2b	KMP-MATCHER (T, P) 1 $n = T.length$ 2 $m = P.length$ 3 $\pi = \text{Compute-Prefix-Function}(P)$ 4 $q = 0$	06
	while $q > 0$ and $P[q + 1] \neq T[i]$ $q = \pi[q]$ // next character does not match if $P[q + 1] == T[i]$ $q = q + 1$ // next character matches if $q == m$ // is all of P matched?	
	print "Pattern occurs with shift" $i-m$ $q=\pi[q] \qquad \text{look for the next match}$ For the KMP-MATCHER algorithm given above, write the COMPUTE-PREFIX-FUNCTION procedure it requires.	
2c	Explain an O(n) method of finding the longest common substring of two strings T1 and T2 of length O(n) using generalized suffix trees. Use the method to find the longest common substring of T1 = "nonsense" and T2 = "offense".	08
За	Find the integers \mathbf{x} and \mathbf{y} in the equation $840\mathbf{x} + 462\mathbf{y} = \gcd(840, 462)$ using the extended Euclid's algorithm.	06
3b	Explain the procedure of generating a pair of public-private keys for a participant in the RSA public-key cryptosystem.	06
3c	Let P _A , S _A , P _B , S _B are public-key and secret-key of Alice, and public-key and secret-key of Bob, respectively. Explain with a block diagram, a procedure for: (i) Bob to send message M to Alice confidentially, (ii) Alice to send a short message M [*] to Bob authenticating it is her who sent the message.	08

4a	What is memoization technique? Write an algorithm using memoization technique to find the binomial coefficient C(n, k) in O(nk) time. Use Pascal's identity given below to find the binomial coefficient.	06
	C(n, k) = C(n-1, k-1) + C(n-1, k) for $n > k > 0C(n, 0) = 1, C(n, n) = 1 for n \ge 0$	

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4b	Using dynamic programming, find the longest common subsequence of two strings T1	06
	= "GCCCTAGCG" and T2 = "GCGCAATG".	×
4c	Apply dynamic programming to solve the problem of fully parenthesizing for optimally multiplying a chain of n matrices. Find the optimal substructure, recursive solution and write the procedure to find the optimal value (finding an optimal solution is not necessary, just the optional value is needed).	08
5a	Convert the polynomial $A(x) = a_0 + a_1x + a_2x^2 + a_3x^3$ from the coefficient representation to the point-value representation.	06
5b	Explain the addition of two polynomials in point-value representation.	06
5c	RECURSIVE-FFT(a) 1 $n = a.length$ 2 if $n = 1$ 3 return a 4 $\omega_n = e^{2\pi i/n}$ 5 $\omega = 1$ 6 $a^{[0]} = (a_0, a_2,, a_{n-2})$ 7 $a^{[1]} = (a_1, a_3,, a_{n-1})$	08
	8 $y^{[0]} = \text{RECURSIVE-FFT}(a^{[0]})$ 9 $y^{[1]} = \text{RECURSIVE-FFT}(a^{[1]})$ 10 for $k = 0$ to $n/2 - 1$ 11 $y_k = y_k^{[0]} + \omega y_k^{[1]}$ 12 $y_{k+(n/2)} = y_k^{[0]} - \omega y_k^{[1]}$ 13 $\omega = \omega \omega_n$	
	14 return y Explain the working of the above FFT algorithm to evaluate coefficient vector a into its value vector y .	