## 1

(15)

(18)

## NCERT Discrete 11.9.1 Q7

## EE23BTECH11061 - SWATHI DEEPIKA\*

**Question:** If a,b,c are in A.P.;b,c,d are in G.P. and  $\frac{1}{c}$ ,  $\frac{1}{d}$ ,  $\frac{1}{e}$  are in A.P. prove that a,c,e are in G.P. **Solution:** 

Symbol	Value	Description
$x_1(n)$	$\{a,b,c\}$	A.P Sequence
$x_2(n)$	$\{b,c,d\}$	G.P Sequence
$x_3(n)$	$\left\{\frac{1}{c}, \frac{1}{d}, \frac{1}{e}\right\}$	A.P Sequence
y(n)	$\{a,c,e\}$	Sequence

TABLE I **PARAMETERS** 

Using Z-transform,

$$X_1(z) = \frac{x_1(0)}{1 - z^{-1}} + \frac{(x_1(1) - x_1(0))z^{-1}}{(1 - z^{-1})^2}, \quad |z| > 1$$
(12)

For  $x_2(n)$ ,

$$x_2(n) = x_2(0) \left(\frac{x_2(1)}{x_2(0)}\right)^n u(n)$$
 (13)

Using Z-transform,

$$X_2(z) = \frac{x_2(1)}{1 - \frac{x_2(1)}{x_2(0)}z^{-1}}, \quad |z| > \left|\frac{x_2(1)}{x_2(0)}\right|$$
 (14)

For  $x_3(n)$ ,

$$b - a = c - b \tag{1}$$

$$2b = a + c$$

$$c^2 = b \times d$$

$$d = \frac{c^2}{b}$$

3) 
$$X_3(z) = \frac{x_3(0)}{1 - z^{-1}} + (x_3(1) - x_3(0)) \frac{z^{-1}}{(1 - z^{-1})^2}, \quad |z| > 1$$

 $x_3(n) = (x_3(0) + n(x_3(0) - x_3(1))) u(n)$ 

(4) For 
$$y(n)$$
,

 $Y(z) = \frac{y(1)}{1 - \frac{y(1)}{y(0)}z^{-1}}, \quad |z| > \left|\frac{y(1)}{y(0)}\right|$ 

$$\frac{1}{d} - \frac{1}{c} = \frac{1}{e} - \frac{1}{d} \tag{5}$$

$$\frac{2}{d} = \frac{1}{c} + \frac{1}{e}$$

$$y(n) = y(0) \left(\frac{y(1)}{y(0)}\right)^n u(n)$$
 (17)

Using Z-transform,

(6)

From (4),

$$\frac{2b}{c^2} = \frac{1}{c} + \frac{1}{e} \tag{7}$$

From (2),

$$\frac{a+c}{c^2} = \frac{1}{c} + \frac{1}{e} \tag{8}$$

$$\frac{a}{c^2} + \frac{1}{c} = \frac{1}{c} + \frac{1}{e} \tag{9}$$

$$a \times e = c^2 \tag{10}$$

So, a,c,e are in G.P

For  $x_1(n)$ ,

$$x_1(n) = (x_1(0) + n(x_1(1) - x_1(0)))u(n)$$
 (11)