## GATE 2023 EC 48

## EE23BTECH11061 - SWATHI DEEPIKA\*

**Question:** Let an input x[n] having discrete time Fourier transform  $X(e^{j\omega})=1-e^{-j\omega}+2e^{-3j\omega}$  be passed through an LTI system. The frequency response of the LTI system is  $H(e^{j\omega})=1-\frac{1}{2}e^{-2j\omega}$ . The output y[n] of the system is

## **Solution:**

Parameter	Value
$X(e^{j\omega})$	$1 - e^{-j\omega} + 2e^{-3j\omega}$
$H(e^{j\omega})$	$1 - \frac{1}{2}e^{-2j\omega}$
$Y(e^{j\omega})$	$X(e^{j\omega}) \cdot H(e^{j\omega})$
<i>y</i> [ <i>n</i> ]	?

TABLE I Parameters

$$y[n] = x[n] * h[n]$$
 (1)

$$x(n) * h(n) \longleftrightarrow X(e^{j\omega}) \cdot H(e^{j\omega})$$

$$Y(e^{j\omega}) = X(e^{j\omega}) \cdot H(e^{j\omega})$$
 (2)

$$Y(e^{j\omega}) = (1 - e^{-j\omega} + 2e^{-3j\omega}) \cdot \left(1 - \frac{1}{2}e^{-2j\omega}\right)$$
(3)

$$= (1 - e^{-j\omega} + \frac{5}{2}e^{-3j\omega} - \frac{1}{2}e^{-2j\omega} - e^{-5j\omega}) \quad (4)$$

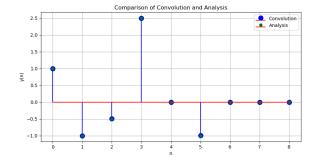


Fig. 1. y(n) vs n