Assignment 2 Probability and Random Variables

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I. Problem

In a meeting, 70% of the members favour and 30% oppose a certain proposal. A member is selected at random and we take X = 0 if he opposed, and X = 1 if he is in favour. Find E(X) and Var(X).

II. SOLUTION

A member opposes the proposal : X=0; A member favours the proposal : X=1;

$$P(X=0) = 70 \% = 0.7$$

 $P(X=1) = 30 \% = 0.3$

$$E(X) = \sum_{i=1}^{n} x_i p_i \tag{1}$$

$$= 1 \times 0.7 + 0 \times 0.3 = 0.7 \tag{2}$$

$$\implies E(X) = 0.7$$
 (3)

$$E(X^{2}) = \sum_{i=1}^{n} (x_{i})^{2} p_{i}$$
 (4)

$$= 1^2 \times 0.7 + 0^2 \times 0.3 = 0.7 \tag{5}$$

$$Var(X) = E(X^{2}) - [E(X)]^{2}$$
 (6)

$$= 0.7 - 0.7^2 = 0.21 \tag{7}$$

$$\implies Var(X) = 0.21$$
 (8)

Similar result is also obtained with random samples generated using the python code.

Figure 1: Result obtained from python code

Download python code from here

https://github.com/Swati-Mohanty/AI5002/blob/main/Assignment%202/codes/bernoullidist.py

Download latex code from here-

https://github.com/Swati-Mohanty/AI5002/blob/main/Assignment%202/codes/assignment2.tex