

Assignment 4

Probability and Random Variables

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I. PROBLEM

Find the probability distribution of

- number of heads in two tosses of a coin.
- number of tails in the simultaneous tosses of three coins.
- number of heads in four tosses of a coin.

II. SOLUTION

(i) Let the event be defined as

X = Number of heads when a coin is tossed twice

Outcomes = {HH, HT, TH, TT}

Hence the probability distribution of X is:

X	0	1	2
$P(X)$	1/4	1/2	1/4

(ii) Let the event be defined as

X = Number of tails in the simultaneous tosses of three coins.

Outcomes = { HHH, HHT, HTH, HTT, THH, TTH, TTT }

Hence the probability distribution of X is:

X	0	1	2	3
$P(X)$	1/8	3/8	3/8	1/8

(iii) Let the event be defined as

X = Number of heads in four tosses of a coin.

Outcomes = { HHHH, HHHT, HHHT, HHTT, HTHH, HTTH, HTTH, HTTT, THHH, THHT, THTH, THTT, TTHH, TTHH, TTTH, TTTT }

Hence the probability distribution of X is:

X	0	1	2	3	4
$P(X)$	1/16	1/4	3/8	1/4	1/16

The PDF graphs were plotted using the python code.

Download python code from here

https://github.com/Swati-Mohanty/AI5002/blob/main/Assignment_4/codes/cointoss.py

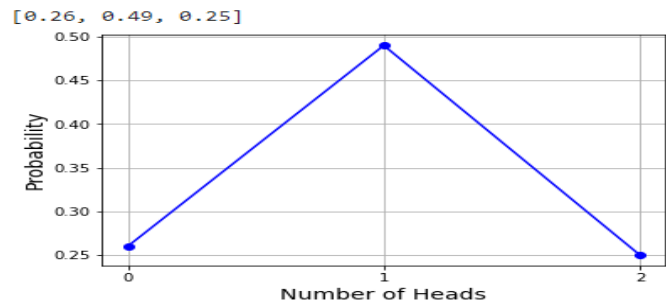


Figure 1: PDF for tossing a fair coin twice

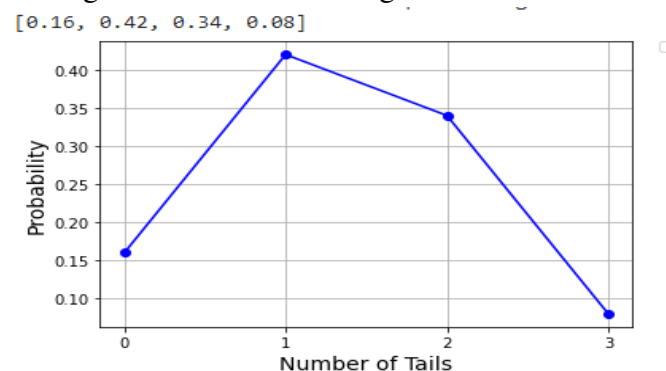


Figure 2: PDF for tossing a fair coin thrice

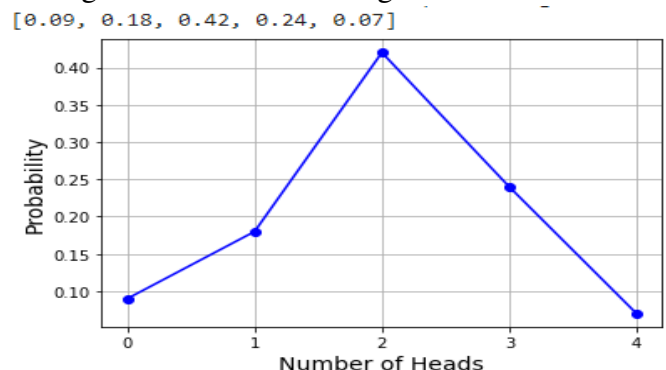


Figure 3: PDF for tossing a fair coin 4 times

Download latex code from here-

https://github.com/Swati-Mohanty/AI5002/blob/main/Assignment_4/codes/assignment4.tex