

Q1. Algorithm for working kth node from end and front in a doubly linked list.

$\therefore \text{swaps}(\text{int } i) \rightarrow // \text{taking } i \text{ as } k$

Taking \*temp as header and \*temp2 as trailer and then Traversing through the list  $i-1$  times to pointa ~~now~~ to the kth node from front and end.

from front  
 while (counter <  $i-1$ )  
 {  
   temp = temp → next;  
   counter++;  
 }  
 temp = temp → next;

from the end  
 while (count <  $i-1$ )  
 {  
   temp2 = temp2 → prev;  
   count++;  
 }  
 temp2 = temp2 → prev;

while we traverse  $i-1$  times we point to  $i-1$ th node  
 $\therefore$  the index starts from 0. then we take one more traversal like pointing which goes to the next or the previous of that particular pointer.

like:- temp = temp → next; now temp points to the kth node from the front and temp2 then points to the kth node from the back.

We have a boundary condition of header and trailer



Taking the boundary condition.

```
if (temp == header || temp2 == header).  
{  
    if (temp == header).
```

// Now taking the condition for temp to point to header.  
We have already taken a pointer which  $\phi$  is address equal to NULL.

Swapping (header, temp2  $\rightarrow$  prev  $\rightarrow$  next).  
// We are storing header into the NULL pointer  
sw = header;

and now we will take the predecessor next of the second node and store in header.

and also take the original header stored in sw and now store it in the predecessor next of the second node.



sw = header

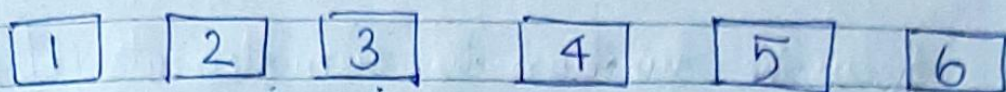


swapping these two pointers.

Now swapping (temp  $\rightarrow$  prev, temp2  $\rightarrow$  prev).  
and swapping (temp  $\rightarrow$  next, temp2  $\rightarrow$  next).

Basically, we have broken the ~~ex~~ existing links and swapped the nodes creating new links.



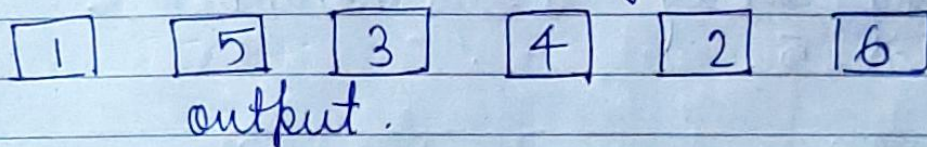


Taking value of  $k$  as 3.

Now we are breaking links by first storing address of 2 in the prev of pointer of 5..  
And prev of 6 into address of 2.

Doing the same with next of 2 and next of 5  
and prev of 2 and prev of 5.

~~We are have pointing the next.~~





Q2. Recursive function to sum elements of an array:

```
int sum(int a[], int n) {  
    if (n == 0) // boundary condition.  
        return 0;  
    return a[n-1] + sum(a, n-1);  
}
```

$n \rightarrow$  size of the array .  
 $a \rightarrow$  array .

Taking array  $a = \{1, 2, 3, 4, 5\}$ .  
 $n = 5$ .

sum(a)

sum(1)

sum(2)

sum(3)

sum(4)

$$n=1 \rightarrow a[1-1] + 0 \rightarrow a[0] + 0 = 1$$

$$n=2 \rightarrow a[2-1] + 1 = 3$$

$$n=3 \rightarrow a[3-1] + 3 = a[2] + 3 = 6$$

$$n=4 \rightarrow a[4-1] + 6 = a[3] + 6 = 10$$

$$n=5 \rightarrow a[5-1] + 10 = a[4] + 10 = 15$$

now sum = 15



Q3. Array of integers  
12, 14, 9, 18, 120, 30, 40, 35, 60.

Insertion sort will be best suited because the array is almost sorted and only 9, 120 and 35 are in the wrong position.

Algorithm:-

```
for (int i = 1; i < n; i++)  
{  
    T tmp = data[i];  
    for (j = i; j > 0; && tmp < data[j-1]; j--)  
    {  
        data[j] = data[j-1];  
    }  
    data[j] = tmp;  
}
```

Also, In average case bubble sort makes approximately twice as many comparisons and same number of moves as insertion sort, as many comparisons as selection sort and  $n$  times more than selection sort.

Insertion sort is fast among these two sorting algorithms.



## Comparison of runtime of random numbers.

Insertion sort  $\rightarrow$  .438

Selection sort  $\rightarrow$  .818

Bubble sort  $\rightarrow$  17.700.

array = {12, 14, 9, 18, 120, 30, 40, 35, 60}.

$i=1$   
 $j=1$

12	14	9	18	120	30	40	35	60
----	----	---	----	-----	----	----	----	----

tmp = 14. 14 is not less than 12

no swapping.

$i=2$   
 $j=2$

12	14	9	18	120	30	40	35	60
----	----	---	----	-----	----	----	----	----

tmp = 9. 9 is less than 14

swapping.

$i=3$   
 $j=3$

12	14	14	18	120	30	40	35	60
----	----	----	----	-----	----	----	----	----

tmp = 9. 9 is less than 12.

swapping.

12	12	14	18	120	30	40	35	60
----	----	----	----	-----	----	----	----	----

no swapping.

9	12	14	18	120	30	40	35	60
---	----	----	----	-----	----	----	----	----

$i=3$

9	12	14	18	120	30	40	35	60
---	----	----	----	-----	----	----	----	----

tmp = 18.

18 is less than is not less than 14.

no swapping.



i=4

j=4

9	12	14	18	120	30	40	35	60
---	----	----	----	-----	----	----	----	----

120 is not less than 18

no swapping.

i=5

j=5

9	12	14	18	120	30	40	35	60
---	----	----	----	-----	----	----	----	----

30 is less than 120

swapping.

i=5  
j=4

9	12	14	18	120	120	30	40	35	60
---	----	----	----	-----	-----	----	----	----	----

30 is less than 180  
not

no swapping.

i=6  
j=6

9	12	14	18	30	120	40	35	60
---	----	----	----	----	-----	----	----	----

40 is less than 120

swapping.

i=6  
j=5

9	12	14	18	30	120	40	120	35	60
---	----	----	----	----	-----	----	-----	----	----

40 is not less than 30

no swapping.

i=7  
j=7

9	12	14	18	30	40	120	35	60
---	----	----	----	----	----	-----	----	----

9	12	14	18	30	40	120	120	60
---	----	----	----	----	----	-----	-----	----

9	12	14	18	30	40	35	120	60
---	----	----	----	----	----	----	-----	----

9	12	14	18	30	40	35	120	120
---	----	----	----	----	----	----	-----	-----

9	12	14	18	30	40	35	60
---	----	----	----	----	----	----	----



[9 | 12 | 14 | 18 | 30 | 40 | 40 | 120 | 60]

[9 | 12 | 14 | 18 | 30 | 35 | 40 | 120 | 60]

[9 | 12 | 14 | 18 | 30 | 35 | 40 | 120 | 120]

[9 | 12 | 14 | 18 | 30 | 35 | 40 | 60 | 120]

Q4 (i) (4, 5, 8, 1) (15, 8, 4) (1, 4, 8, 5)  
(1, 4, 5, 8)

→ Selection sort is used here because in intermediate configuration, smallest element is selected and exchanged with the element in 1st position, then the smallest value among the remaining elements is found and put in 2nd position.

Algo:

```
for (int i=0; i < n-1; i++)  
{  
    for (j=i+1, least=i; j < n; j++)  
        if (data[j] < data[least])  
            least = j;  
    swap(data[least], data[i]);  
}
```



4	5	8	1
---	---	---	---

$i = 0$      $j = 1$      $least = 0$

false ( $5 < 4$ )     $least = 1$      $j++ \Rightarrow j = 2$   
 false ( $8 < 5$ )     $least = 1$      $j++ \Rightarrow j = 3$   
 true ( $1 < 5$ )     $least = 3$      $j++ \Rightarrow j = 4$

$(j < n)$  so out from inner loop.  
then swap( $data[3], data[0]$ )

1	5	8	4
---	---	---	---

$i = 1$      $j = 2$      $least = 1$

false ( $8 < 5$ )     $least = 1$      $j++$ ;  $j = 3$   
 true ( $4 < 5$ )     $least = 3$      $j++$ ,  $j = 4$

$(j < n)$  out from inner loop.  
then swap( $data[3], data[1]$ )

1	4	8	5
---	---	---	---

$i = 2$      $j = 3$      $least = 2$

true ( $5 < 8$ )     $least = 3$   
 swap( $data[3], data[2]$ )

1	4	5	8
---	---	---	---



$i=3$  false condition  $i < n-1 ; i < 2$ .

Sorted array 

1	4	5	8
---	---	---	---

(ii) (4, 5, 8, 1) (4, 5, 1, 8) (4, 1, 5, 8) (1, 4, 5, 8)

Bubble sort is used because in bubble sort, the array is scanned from top to bottom up and two adjacent elements are interchanged if they found to be out of order with respect to each other.

first  $data[n-1]$  and  $data[n-2]$  are compared and swapped if they are out of order, next  $data[n-2]$  and  $data[n-3]$  are compared and their order is changed if necessary and so on upto  $data[1]$  and  $data[0]$ .

algorithm:

```
for(int i = 0; i < n-1; i++)  
{  
    for(int j = n-1; j > i; --j)  
    {  
        if(data[j] < data[j-1])  
            swap(data[j], data[j-1])  
    }  
}
```

Array:- {4, 5, 8, 1}

$i=0$   $j=3$   $(1 < 8)$  true swap  $(data[3], data[2])$



4	5	1	8
---	---	---	---

$i = 0$   $j = 2$   $(1 < 5)$  true swap( $\text{data}[2]$ ,  $\text{data}[i]$ )

4	1	5	8
---	---	---	---

$i = 0$   $j = 1$   $(1 < 4)$  true swap( $\text{data}[1]$ ,  $\text{data}[i]$ )

1	4	5	8
---	---	---	---