

Q4.1: In the Quant test of CAT exam, the population standard deviation is known to be 100. A sample of 25 test takers has a mean of 520. Construct a 80% confidence interval about mean.

Solution:- Given,

$$\text{Population S.D} = 100 = \sigma, n = 25$$

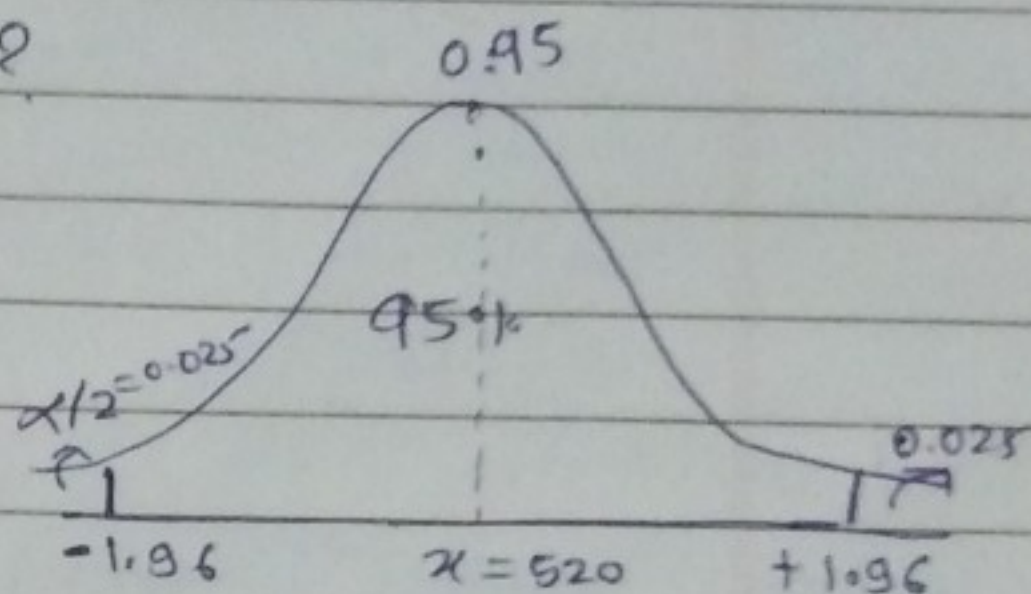
$$\bar{x} = 520$$

∴ Construct 80% C.I @ mean = ?

∴ Confidence Interval :-

Point estimate \pm margin of error

$$\text{i.e. } \boxed{\bar{x} \pm Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}}$$



$$\therefore \alpha = 1 - \text{C.I} = 1 - 0.95 = 0.05$$

$$\therefore \text{Margin of error} = Z_{\alpha/2} = Z_{0.05/2} = Z_{0.025}$$

∴ From Z table, $Z_{0.025}$

$$+ve, Z_{\alpha/2} = 1 - 0.025 = 0.9750 = +1.96$$

$$-ve, Z_{0.025} = -1.96$$

⇒ Confidence Interval is

$$\therefore \text{Lower fence} = \bar{x} - Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$$

$$= 520 - 1.96 (100/\sqrt{25})$$

$$= \underline{\underline{480.8}}$$

$$\therefore \text{Higher fence} = \bar{x} + Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$$

$$= 520 + 1.96 \cdot 20$$

$$= \underline{\underline{559.2}}$$

