

Unit No 1. Introduction to Data Structures and Algorithm.

Data refers to raw facts and figures that can be processed to extract meaningful information. It is unprocessed and unorganized, often existing in various forms such as numbers, text, images, or sounds. In the context of computing and data management, data serves as the foundation upon which information and knowledge are built.

Key Characteristics of Data:

- **Raw and Unprocessed:** Data has not been subjected to any manipulation, processing, or interpretation.
- **Variety of Forms:** Data can exist in multiple forms such as numbers, characters, images, etc.
- **Contextual Value:** The significance of data depends on the context in which it is used.

Concept of Data Object

Data Object refers to a collection of data elements that are grouped together because they share a common context or purpose. A data object can be considered as an instance of a data type, encapsulating both the structure and the values of the data.

Key Characteristics of Data Objects:

- **Encapsulation:** Data objects encapsulate data elements and the operations that can be performed on them.
- **Defined Structure:** The structure of a data object is defined by its data type.
- **Identity and State:** Data objects have a unique identity and a state defined by the values of their attributes.

Example:

- A data object representing a 'Person' might include attributes such as name, age, and address.

Concept of Data Structure

Data Structure is a specific way of organizing and storing data in a computer so that it can be accessed and modified efficiently. Data structures define the layout of data elements and the relationships between them, facilitating efficient data operations.

Key Characteristics of Data Structures:

- **Organization:** Data structures organize data in a manner that reflects its logical or physical relationships.
- **Efficiency:** Proper data structures allow for efficient data access and manipulation.
- **Abstract Data Types (ADTs):** Data structures often implement abstract data types, which define the behavior of data independently of its implementation.

Common Types of Data Structures:

1. **Arrays:** A collection of elements identified by index or key.
2. **Linked Lists:** A sequence of elements, where each element points to the next.
3. **Stacks:** A collection of elements that follows the Last In, First Out (LIFO) principle.
4. **Queues:** A collection of elements that follows the First In, First Out (FIFO) principle.
5. **Trees:** A hierarchical structure with nodes connected by edges.
6. **Graphs:** A collection of nodes and edges, representing relationships between pairs of nodes.
7. **Hash Tables:** A structure that maps keys to values for efficient lookup.

Summary

- **Data:** Raw and unorganized facts that require processing to become meaningful.
- **Data Object:** An instance of a data type that encapsulates data and operations.
- **Data Structure:** A specific way of organizing data for efficient access and manipulation, with various types such as arrays, linked lists, stacks, queues, trees, graphs, and hash tables.

Understanding these concepts is fundamental for effectively managing, processing, and utilizing data in computing and information systems.

2. Primitive Data Structures are the most basic forms of data storage. These structures are directly operated upon by the machine-level instructions and are generally built-in types provided by a programming language.

Examples of Primitive Data Structures:

- **Integer:** Whole numbers, e.g., 1, 2, 3.
- **Float:** Numbers with fractional parts, e.g., 1.5, 2.75.
- **Character:** Single characters, e.g., 'a', 'b', 'c'.
- **Boolean:** True or false values.

Non-Primitive Data Structures are more complex and are derived from primitive data structures. They are used to store a collection of values or more complex relationships among data.

Examples of Non-Primitive Data Structures:

- **Arrays:** A collection of elements of the same type, stored in contiguous memory locations.
- **Lists:** Ordered collections of elements, can be implemented as linked lists.
- **Stacks:** LIFO (Last In, First Out) collections.
- **Queues:** FIFO (First In, First Out) collections.
- **Trees:** Hierarchical structures with nodes connected by edges.
- **Graphs:** Collections of nodes and edges representing relationships.

Concept of Linear and Nonlinear Data Structures

Linear Data Structures store data in a sequential manner, where elements are adjacent to each other. Each element has a unique predecessor and successor except for the first and last elements.

Examples of Linear Data Structures:

- **Arrays:** Fixed-size, sequential collections of elements.
- **Linked Lists:** Sequential collections where each element points to the next.
- **Stacks:** Elements are added or removed from one end (top).
- **Queues:** Elements are added from one end (rear) and removed from the other (front).

Nonlinear Data Structures store data in a hierarchical manner. They do not follow a sequential arrangement, and elements can be connected in multiple ways.

Examples of Nonlinear Data Structures:

- **Trees:** Hierarchical structures with a root and child nodes.
- **Graphs:** Collections of nodes (vertices) connected by edges.

Concept of Static and Dynamic Data Structures

Static Data Structures have a fixed size, determined at the time of declaration. Their size cannot be altered during runtime, which makes them less flexible but simpler to manage.

Example:

- **Array:** The size of the array is fixed and cannot be changed once declared.

Dynamic Data Structures can grow or shrink in size during runtime. They provide more flexibility in memory management but require more complex handling.

Examples:

- **Linked List:** Can grow or shrink as elements are added or removed.
- **Dynamic Arrays:** Arrays that can resize themselves as needed (e.g., vectors in C++ or Array Lists in Java).

Concept of Persistent and Ephemeral Data Structures

Persistent Data Structures preserve the previous versions of themselves when modified. Instead of updating the structure in place, a new version is created with the changes, keeping the old version intact. This is often used in functional programming.

Example:

- **Immutable Lists:** Modifying the list creates a new list, preserving the old version.

Ephemeral Data Structures do not preserve previous versions. When modified, the changes are made in place, and the old version is lost.

Example:

- **Mutable Lists:** Modifying the list updates the existing structure without preserving the old version.

Summary

- **Primitive Data Structures:** Basic data types like integers, floats, characters, and Booleans.
- **Non-Primitive Data Structures:** More complex structures like arrays, lists, stacks, queues, trees, and graphs.
- **Linear Data Structures:** Sequential data storage like arrays, linked lists, stacks, and queues.
- **Nonlinear Data Structures:** Hierarchical data storage like trees and graphs.
- **Static Data Structures:** Fixed-size structures like arrays.
- **Dynamic Data Structures:** Resizable structures like linked lists and dynamic arrays.
- **Persistent Data Structures:** Preserve old versions on modification, creating new versions (e.g., immutable lists).
- **Ephemeral Data Structures:** Update in place, losing old versions (e.g., mutable lists).

Understanding these concepts helps in choosing the right data structure based on the requirements of memory usage, data access patterns, and performance needs.

Abstract Data Type (ADT) is a model for data structures that defines the type of data it can hold, the operations that can be performed on the data, and the behavior of these operations, independently of any specific implementation. ADTs provide a theoretical framework for designing and analyzing data structures and algorithms without worrying about implementation details.

Key Characteristics of ADT:

- **Encapsulation:** Hides the implementation details and only exposes the interface.
- **Operations:** Specifies a set of operations that can be performed on the data.
- **Behavior:** Describes the expected behavior of the operations in terms of their inputs and outputs.

Examples of ADTs:

- **List ADT:** Operations might include insert, delete, find, etc.
- **Stack ADT:** Operations might include push, pop, top, etc.
- **Queue ADT:** Operations might include enqueue, dequeue, front, etc.

Analysis of Algorithm

Analysis of an Algorithm is the process of determining the computational complexity of algorithms, the amount of resources required, and their efficiency. It is crucial for understanding the performance and scalability of algorithms.

Frequency Count

Frequency count refers to counting the number of times a particular operation is executed within an algorithm. It is an essential step in understanding an algorithm's behavior and efficiency.

Importance of Frequency Count:

- **Performance Evaluation:** Helps in assessing the performance of an algorithm.
- **Identifying Bottlenecks:** Points out which operations are the most time-consuming.
- **Optimization:** Provides insights into which parts of the algorithm need optimization.

Time Complexity

Time Complexity is a measure of the amount of time an algorithm takes to complete as a function of the size of its input. It provides an estimate of the running time of an algorithm in the worst, average, and best cases.

Notations Used:

- **Big O (O):** Upper bound on the time, representing the worst-case scenario.
- **Omega (Ω):** Lower bound on the time, representing the best-case scenario.
- **Theta (Θ):** Tight bound on the time, representing the average-case scenario.

Common Time Complexities:

- **$O(1)$:** Constant time.
- **$O(\log n)$:** Logarithmic time.
- **$O(n)$:** Linear time.
- **$O(n \log n)$:** Log-linear time.
- **$O(n^2)$:** Quadratic time.
- **$O(2^n)$:** Exponential time.

Space Complexity

Space Complexity is a measure of the amount of memory space an algorithm uses as a function of the size of its input. It includes both the space needed to store the input and the auxiliary space used by the algorithm.

Notations Used:

- Similar to time complexity, space complexity can be expressed using Big O, Omega, and Theta notations.

Common Space Complexities:

- **$O(1)$:** Constant space.
- **$O(n)$:** Linear space.
- **$O(n^2)$:** Quadratic space.

Summary

- **Abstract Data Type (ADT):** A model defining data type operations and behavior abstractly, independent of implementation.
- **Frequency Count:** Counting operation executions to analyze algorithm efficiency.

Sequential Organization: Arrays

Single Dimensional Array (1D Array)

- A single-dimensional array is a linear data structure that stores elements of the same type in a contiguous block of memory.
- Each element is accessed using a unique index, typically starting from 0.

Address Calculation in 1D Array:

The address of an element in a 1D array can be calculated using the formula:
 $\text{Address}(A[i]) = \text{Base Address} + i \times \text{Size of each element}$

Multidimensional Array

- A multidimensional array is an array of arrays. The most common are 2D arrays (matrices), but higher dimensions are also possible.
- Elements are accessed using multiple indices, e.g., $A[i][j]$ for a 2D array.

Address Calculation in 2D Array:

For a 2D array stored in row-major order (the most common method), the address of an element can be calculated using:

$\text{Address}(A[i][j]) = \text{Base Address} + (i \times \text{Number of columns} + j) \times \text{Size of each element}$

For column-major order:
 $\text{Address}(A[i][j]) = \text{Base Address} + (j \times \text{Number of rows} + i) \times \text{Size of each element}$

Linked Organization: Linked Lists

Concept of Linked Organization

- In linked organization, elements (nodes) are stored in non-contiguous memory locations. Each node contains data and a reference (or link) to the next node in the sequence.
- This structure allows for efficient insertion and deletion of elements since it does not require shifting elements like arrays.

Singly Linked List

- A singly linked list is a linear collection of nodes where each node points to the next node.
- Operations include creating the list, displaying elements, searching for an element, inserting a node, and deleting a node.

Doubly Linked List

- A doubly linked list has nodes that contain references to both the next and the previous nodes.
- This allows traversal in both directions and makes operations like insertion and deletion more flexible.

Circular Linked List

- A circular linked list is similar to a singly linked list but with the last node pointing back to the first node, forming a circle.
- This allows for cyclic traversal of the list.

Operations on Linked Lists

1. Create

- To create a linked list, we initialize an empty list and then add nodes to it one by one.

2. Display

- Traverse the list from the head node to the end, printing each node's data.

3. Search

- Traverse the list from the head node, comparing each node's data with the target value until the value is found or the end of the list is reached.

4. Insert

- **At the beginning:** Create a new node and set its next reference to the current head node. Update the head to this new node.
- **At the end:** Traverse to the last node, create a new node, and set the last node's next reference to this new node.
- **At a specific position:** Traverse to the node after which the new node is to be inserted, update the new node's next reference to point to the next node, and update the previous node's next reference to point to the new node.

5. Delete

- **From the beginning:** Update the head to the next node of the current head.
- **From the end:** Traverse to the second-to-last node and set its next reference to null.
- **From a specific position:** Traverse to the node before the one to be deleted, update its next reference to skip the node to be deleted.

Examples of Linked List Operations

Singly Linked List:

```
python
class Node:
    def __init__(self, data):
```

```
    self.data = data
    self.next = None

class SinglyLinkedList:
    def __init__(self):
        self.head = None

    def insert_at_beginning(self, data):
        new_node = Node(data)
        new_node.next = self.head
        self.head = new_node

    def insert_at_end(self, data):
        new_node = Node(data)
        if not self.head:
            self.head = new_node
            return
        last = self.head
        while last.next:
            last = last.next
        last.next = new_node

    def display(self):
        current = self.head
        while current:
            print(current.data, end=" -> ")
            current = current.next
        print("None")

    def search(self, target):
        current = self.head
        while current:
            if current.data == target:
                return True
            current = current.next
        return False

    def delete_node(self, key):
        temp = self.head
        if temp is not None:
            if temp.data == key:
                self.head = temp.next
                temp = None
                return
        while temp is not None:
            if temp.data == key:
                break
            prev = temp
            temp = temp.next
        if temp == None:
```

```
        return  
    prev.next = temp.next  
    temp = None
```

Doubly Linked List:

```
python  
class Node:  
    def __init__(self, data):  
        self.data = data  
        self.next = None  
        self.prev = None  
  
class DoublyLinkedList:  
    def __init__(self):  
        self.head = None  
  
    def insert_at_beginning(self, data):  
        new_node = Node(data)  
        new_node.next = self.head  
        if self.head is not None:  
            self.head.prev = new_node  
        self.head = new_node  
  
    def insert_at_end(self, data):  
        new_node = Node(data)  
        if self.head is None:  
            self.head = new_node  
        else:  
            last = self.head  
            while last.next:  
                last = last.next  
            last.next = new_node  
            new_node.prev = last  
  
    def display(self):  
        current = self.head  
        while current:  
            print(current.data, end=" <-> ")  
            current = current.next  
        print("None")  
  
    def search(self, target):  
        current = self.head  
        while current:  
            if current.data == target:  
                return True  
            current = current.next  
        return False
```

```

def delete_node(self, key):
    temp = self.head
    if temp is not None and temp.data == key:
        self.head = temp.next
        if self.head:
            self.head.prev = None
        temp = None
        return
    while temp is not None and temp.data != key:
        temp = temp.next
    if temp is None:
        return
    if temp.next:
        temp.next.prev = temp.prev
    if temp.prev:
        temp.prev.next = temp.next
    temp = None

```

Circular Linked List:

```

python
class Node:
    def __init__(self, data):
        self.data = data
        self.next = None

class CircularLinkedList:
    def __init__(self):
        self.head = None

    def insert_at_beginning(self, data):
        new_node = Node(data)
        if not self.head:
            self.head = new_node
            self.head.next = self.head
        else:
            temp = self.head
            while temp.next != self.head:
                temp = temp.next
            new_node.next = self.head
            temp.next = new_node
            self.head = new_node

    def insert_at_end(self, data):
        new_node = Node(data)
        if not self.head:
            self.head = new_node
            self.head.next = self.head
        else:
            temp = self.head
            while temp.next != self.head:
                temp = temp.next
            temp.next = new_node
            new_node.next = self.head

```

```

while temp.next != self.head:
    temp = temp.next
temp.next = new_node
new_node.next = self.head

def display(self):
    if not self.head:
        return
    temp = self.head
    while True:
        print(temp.data, end=" -> ")
        temp = temp.next
        if temp == self.head:
            break
    print("HEAD")

def search(self, target):
    temp = self.head
    while True:
        if temp.data == target:
            return True
        temp = temp.next
        if temp == self.head:
            break
    return False

def delete_node(self, key):
    if not self.head:
        return
    temp = self.head
    prev = None
    while True:
        if temp.data == key:
            if prev:
                prev.next = temp.next
            else:
                if temp.next == self.head:
                    self.head = None
                else:
                    self.head = temp.next
                    tail = self.head
                    while tail.next != temp:
                        tail = tail.next
                    tail.next = self.head
            return
        prev = temp
        temp = temp.next
        if temp == self.head:
            break

```

These examples demonstrate the basic operations for singly, doubly, and circular linked lists. Understanding these concepts and operations is fundamental for managing and manipulating dynamic data structures effectively.

- **Time Complexity:** Measures the time an algorithm takes relative to input size, using Big O, Omega, and Theta notations.
- **Space Complexity:** Measures the memory space an algorithm uses relative to input size, also expressed using Big O, Omega, and Theta notations.

Analyzing algorithms in terms of time and space complexity helps in selecting the most efficient algorithm for a given problem, ensuring optimal use of computational resources.

Unit No.2 : Searching And Sorting

Searching and **Sorting** are fundamental operations in computer science, crucial for organizing and managing data efficiently.

Need for Searching:

- **Data Retrieval:** Finding a specific item in a dataset, such as a record in a database.
- **Efficiency:** Enabling quick access to information, which is critical for performance in applications like search engines.
- **Data Management:** Facilitating the organization of data by locating duplicates, ensuring data integrity, and managing storage.

Need for Sorting:

- **Data Presentation:** Organizing data in a readable and logical order, such as alphabetical order in a list.
- **Efficiency:** Improving the efficiency of other algorithms, such as binary search, which requires sorted data.
- **Data Processing:** Facilitating efficient data processing tasks, like merging datasets or finding the median.

Concept of Internal and External Sorting

Internal Sorting: Sorting that is performed within the main memory (RAM) of the computer. It is used when the entire dataset fits into the memory.

Characteristics of Internal Sorting:

- **Speed:** Generally faster due to direct access to memory.
- **Data Size:** Limited by the size of the available RAM.
- **Examples:**
 - **Bubble Sort:** Simple comparison-based sorting algorithm.
 - **Insertion Sort:** Builds the final sorted array one item at a time.
 - **Selection Sort:** Repeatedly selects the smallest element from the unsorted part and moves it to the sorted part.

- **Quick Sort:** Divides the array into sub-arrays and sorts them recursively.
- **Merge Sort:** Divides the array into halves, sorts each half, and merges them.

External Sorting: Sorting that involves external storage (disk) due to the dataset being too large to fit into the main memory. It is used for large datasets that exceed the capacity of RAM.

Characteristics of External Sorting:

- **Data Size:** Handles very large datasets.
- **Efficiency:** Optimizes the number of disk accesses, which are slower than memory accesses.
- **Examples:**
 - **External Merge Sort:** Divides data into chunks that fit into memory, sorts each chunk in memory, and then merges the sorted chunks.
 - **Multiway Merge Sort:** Extends the merge sort to handle multiple sorted chunks simultaneously.

Summary

- **Searching:** Essential for data retrieval and management, improving efficiency and organization.
- **Sorting:** Important for data presentation, improving the efficiency of search algorithms, and facilitating data processing.
- **Internal Sorting:** Conducted within main memory, faster and suitable for smaller datasets.
- **External Sorting:** Utilizes external storage, designed for handling very large datasets efficiently by minimizing disk access.

Linear Search

Linear Search is the simplest search algorithm that checks each element of the list sequentially until the desired element is found or the list ends.

Algorithm:

1. Start from the first element.
2. Compare the current element with the target element.
3. If they match, return the index.
4. If not, move to the next element.
5. Repeat steps 2-4 until the target element is found or the list ends.

Time Complexity:

- **Worst-case:** $O(n)$
- **Best-case:** $O(1)$
- **Average-case:** $O(n)$

Example (C++):

```
cpp
int linearSearch(int arr[], int n, int target) {
```

```

for (int i = 0; i < n; i++) {
    if (arr[i] == target) {
        return i;
    }
}
return -1;
}

```

Binary Search

Binary Search is an efficient search algorithm that works on sorted arrays by repeatedly dividing the search interval in half.

Algorithm:

1. Start with the entire array.
2. Find the middle element.
3. If the middle element is equal to the target, return the index.
4. If the target is less than the middle element, narrow the interval to the left half.
5. If the target is greater, narrow the interval to the right half.
6. Repeat steps 2-5 until the target is found or the interval is empty.

Time Complexity:

- **Worst-case:** $O(\log n)$
- **Best-case:** $O(1)$
- **Average-case:** $O(\log n)$

Example (C++):

```

cpp
int binarySearch(int arr[], int left, int right, int target) {
    while (left <= right) {
        int mid = left + (right - left) / 2;
        if (arr[mid] == target) {
            return mid;
        }
        if (arr[mid] < target) {
            left = mid + 1;
        } else {
            right = mid - 1;
        }
    }
    return -1;
}

```

Sorting Methods

Bubble Sort

Bubble Sort repeatedly swaps adjacent elements if they are in the wrong order. It is known for its simplicity but is inefficient for large datasets.

Algorithm:

1. Compare adjacent elements.
2. Swap if they are in the wrong order.
3. Repeat until no swaps are needed.

Time Complexity:

- **Worst-case:** $O(n^2)$
- **Best-case:** $O(n)$ (when the array is already sorted)
- **Average-case:** $O(n^2)$

Example (C++):

```
cpp
void bubbleSort(int arr[], int n) {
    for (int i = 0; i < n-1; i++) {
        for (int j = 0; j < n-i-1; j++) {
            if (arr[j] > arr[j+1]) {
                swap(arr[j], arr[j+1]);
            }
        }
    }
}
```

Insertion Sort

Insertion Sort builds the final sorted array one item at a time. It is efficient for small data sets or partially sorted data.

Algorithm:

1. Start from the second element.
2. Compare it with the elements before it.
3. Insert it into its correct position.
4. Repeat for all elements.

Time Complexity:

- **Worst-case:** $O(n^2)$
- **Best-case:** $O(n)$ (when the array is already sorted)
- **Average-case:** $O(n^2)$

Example (C++):

```
cpp
void insertionSort(int arr[], int n) {
    for (int i = 1; i < n; i++) {
        int key = arr[i];
```

```

int j = i - 1;
while (j >= 0 && arr[j] > key) {
    arr[j + 1] = arr[j];
    j--;
}
arr[j + 1] = key;
}
}

```

Quick Sort

Quick Sort is a divide-and-conquer algorithm that selects a 'pivot' element and partitions the array around the pivot.

Algorithm:

1. Choose a pivot.
2. Partition the array into two sub-arrays: elements less than the pivot and elements greater than the pivot.
3. Recursively apply the above steps to the sub-arrays.

Time Complexity:

- **Worst-case:** $O(n^2)$ (when the pivot is the smallest or largest element)
- **Best-case:** $O(n \log n)$
- **Average-case:** $O(n \log n)$

Example (C++):

```

cpp
int partition(int arr[], int low, int high) {
    int pivot = arr[high];
    int i = (low - 1);
    for (int j = low; j <= high - 1; j++) {
        if (arr[j] <= pivot) {
            i++;
            swap(arr[i], arr[j]);
        }
    }
    swap(arr[i + 1], arr[high]);
    return (i + 1);
}

```

```

void quickSort(int arr[], int low, int high) {
    if (low < high) {
        int pi = partition(arr, low, high);
        quickSort(arr, low, pi - 1);
        quickSort(arr, pi + 1, high);
    }
}

```

Merge Sort

Merge Sort is a divide-and-conquer algorithm that divides the array into two halves, sorts them, and then merges the sorted halves.

Algorithm:

1. Divide the array into two halves.
2. Recursively sort each half.
3. Merge the two sorted halves.

Time Complexity:

- **Worst-case:** $O(n \log n)$
- **Best-case:** $O(n \log n)$
- **Average-case:** $O(n \log n)$

Example (C++):

```
cpp
void merge(int arr[], int l, int m, int r) {
    int n1 = m - l + 1;
    int n2 = r - m;
    int L[n1], R[n2];
    for (int i = 0; i < n1; i++)
        L[i] = arr[l + i];
    for (int j = 0; j < n2; j++)
        R[j] = arr[m + 1 + j];
    int i = 0, j = 0, k = l;
    while (i < n1 && j < n2) {
        if (L[i] <= R[j]) {
            arr[k] = L[i];
            i++;
        } else {
            arr[k] = R[j];
            j++;
        }
        k++;
    }
    while (i < n1) {
        arr[k] = L[i];
        i++;
        k++;
    }
    while (j < n2) {
        arr[k] = R[j];
        j++;
        k++;
    }
}
```

```

void mergeSort(int arr[], int l, int r) {
    if (l < r) {
        int m = l + (r - l) / 2;
        mergeSort(arr, l, m);
        mergeSort(arr, m + 1, r);
        merge(arr, l, m, r);
    }
}

```

Shell Sort

Shell Sort is an optimization of insertion sort that allows the exchange of items that are far apart. It uses a gap sequence to determine which elements to compare.

[Algorithm:](#)

1. Initialize a gap sequence.
2. Perform insertion sort for elements at each gap distance.
3. Reduce the gap and repeat until the gap is 1.

[Time Complexity:](#)

- **Worst-case:** $O(n^2)$
- **Best-case:** $O(n \log n)$
- **Average-case:** $O(n^{1.5})$ (depends on gap sequence)

[Example \(C++\):](#)

```

cpp
void shellSort(int arr[], int n) {
    for (int gap = n / 2; gap > 0; gap /= 2) {
        for (int i = gap; i < n; i++) {
            int temp = arr[i];
            int j;
            for (j = i; j >= gap && arr[j - gap] > temp; j -= gap) {
                arr[j] = arr[j - gap];
            }
            arr[j] = temp;
        }
    }
}

```

Comparison of Sorting Methods

Algorithm	Time Complexity (Worst)	Time Complexity (Best)	Time Complexity (Average)	Space Complexity	Stability	Adaptive
Bubble Sort	$O(n^2)$	$O(n)$	$O(n^2)$	$O(1)$	Yes	Yes

Algorithm	Time Complexity (Worst)	Time Complexity (Best)	Time Complexity (Average)	Space Complexity	Stability	Adaptive
Insertion Sort	$O(n^2)$	$O(n)$	$O(n^2)$	$O(1)$	Yes	Yes
Quick Sort	$O(n^2)$	$O(n \log n)$	$O(n \log n)$	$O(\log n)$	No	No
Merge Sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(n)$	Yes	No
Shell Sort	$O(n^2)$	$O(n \log n)$	$O(n^{1.5})$	$O(1)$	No	No

- **Bubble Sort** and **Insertion Sort** are simple but inefficient for large datasets.

Insertion Sort

Insertion Sort is a simple and intuitive sorting algorithm that builds the final sorted array one item at a time.

Best Case

- **Time Complexity:** $O(n)$
- **Scenario:** The array is already sorted. Each element is compared only once with the previous element and inserted in its correct position immediately.

Worst Case

- **Time Complexity:** $O(n^2)$
- **Scenario:** The array is sorted in reverse order. Each element must be compared with all previous elements and moved to the beginning of the array.

Average Case

- **Time Complexity:** $O(n^2)$
- **Scenario:** The elements are in random order. On average, each element is compared and shifted half the number of times as the worst case.

Space Complexity

- **Space Complexity:** $O(1)$
- **Scenario:** In-place sorting algorithm that requires no additional memory.

Stability

- **Stability:** Yes

- **Scenario:** Equal elements retain their relative order in the sorted array.

Quick Sort

Quick Sort is a divide-and-conquer algorithm that selects a 'pivot' element and partitions the array around the pivot.

Best Case

- **Time Complexity:** $O(n \log n)$
- **Scenario:** The pivot element always splits the array into two equal halves, ensuring a balanced partitioning.

Worst Case

- **Time Complexity:** $O(n^2)$
- **Scenario:** The pivot element is the smallest or largest element, resulting in an unbalanced partition (one side is empty and the other side has $n-1$ elements).

Average Case

- **Time Complexity:** $O(n \log n)$
- **Scenario:** The pivot element splits the array into reasonably balanced partitions on average.

Space Complexity

- **Space Complexity:** $O(\log n)$
- **Scenario:** Requires space for the stack used in recursion, with the depth of the stack being proportional to the number of recursive calls.

Stability

- **Stability:** No
- **Scenario:** The relative order of equal elements may change.

Binary Search

Binary Search is an efficient search algorithm that works on sorted arrays by repeatedly dividing the search interval in half.

Best Case

- **Time Complexity:** $O(1)$
- **Scenario:** The target element is at the middle position of the array on the first comparison.

Worst Case

- **Time Complexity:** $O(\log n)$

- **Scenario:** The target element is not present, or it is found after $\log n$ comparisons (the array must be halved $\log n$ times).

Average Case

- **Time Complexity:** $O(\log n)$
- **Scenario:** On average, the target element is found in the middle of the array after $\log n$ comparisons.

Space Complexity

- **Space Complexity:** $O(1)$
- **Scenario:** Iterative implementation uses a constant amount of space.

Hashing

Hashing is a technique used to map data of arbitrary size to fixed-size values (hash codes) for efficient search, insert, and delete operations.

Best Case

- **Time Complexity:** $O(1)$
- **Scenario:** There are no collisions, and each element is directly accessible via its hash code.

Worst Case

- **Time Complexity:** $O(n)$
- **Scenario:** All elements hash to the same slot (extreme collision), resulting in a linked list of elements in that slot.

Average Case

- **Time Complexity:** $O(1)$
- **Scenario:** There are few collisions, and the elements are well-distributed across the hash table.

Space Complexity

- **Space Complexity:** $O(n)$
- **Scenario:** Space is required to store the hash table and the elements.

Stability

- **Stability:** Not applicable
- **Scenario:** Hashing is used for direct access rather than sorting, so stability is not a concern.

Summary

- **Insertion Sort:** Best-case $O(n)$, worst-case $O(n^2)$, average-case $O(n^2)$, space $O(1)$, stable.
- **Quick Sort:** Best-case $O(n \log n)$, worst-case $O(n^2)$, average-case $O(n \log n)$, space $O(\log n)$, not stable.
- **Binary Search:** Best-case $O(1)$, worst-case $O(\log n)$, average-case $O(\log n)$, space $O(1)$.
- **Hashing:** Best-case $O(1)$, worst-case $O(n)$, average-case $O(1)$, space $O(n)$, stability not applicable.

These analyses help in understanding the efficiency and applicability of each algorithm in different scenarios, aiding in the selection of the most appropriate algorithm based on the problem requirements.