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1 clear; close all; clc;
2
3 %% Parameters
4 % Leg geometry
5 L_thigh = 0.3;
6 L_shin = 0.3;
7
8 % PD Controller gains for shin
9 Kp = 150;    % Proportional gain (increased for better tracking)
10 Kd = 35;     % Derivative gain (increased for better damping)
11
12 % Simulation parameters
13 dt = 0.001;    % Time step (s) - smaller for stability
14 t_end = 10;     % Simulation duration (s)
15 t = 0:dt:t_end;
16 N = length(t);
17
18 % Walking gait parameters
19 stride_freq = 0.4; % Hz (walking frequency - even slower)
20 thigh_amplitude = 30 * pi/180; % Thigh swing amplitude (rad)
21
22 %% Initialize variables
23 theta_thigh = zeros(1, N);          % Thigh angle (absolute)
24 theta_shin_abs = zeros(1, N);        % Shin angle (absolute)
25 theta_knee = zeros(1, N);           % Knee angle (shin relative to thigh)
26 omega_knee = zeros(1, N);           % Knee angular velocity
27 tau_thigh = zeros(1, N);            % Thigh torque
28 tau_knee = zeros(1, N);             % Knee control torque
29
30 % Initial conditions
31 theta_thigh(1) = 0;
32 theta_knee(1) = 50 * pi/180;       % Initial knee bend (50 degrees)
33 omega_knee(1) = 0;
34
35 % Shin dynamics parameters
36 I_knee = 0.05;      % Moment of inertia (kg*m^2)
37 b_knee = 8;         % Damping coefficient (increased for stability with higher gains)
38
39 %% Simulation loop
40 for i = 1:N-1
41     % Generate thigh motion with MODERATE VARYING AMPLITUDE (realistic disturbance)
42     % Reduced number of components and amplitudes for smoother variation
43     amp_modulation = 0.7 + 0.5*sin(0.8*2*pi*stride_freq*t(i)) + ...
44                     0.2*cos(1.6*2*pi*stride_freq*t(i));
45
46     % Ensure amplitude doesn't go negative
47     amp_modulation = max(0.2, amp_modulation);
48
49     theta_thigh(i) = thigh_amplitude * amp_modulation * sin(2*pi*stride_freq*t(i));
50
51     % Torque includes amplitude modulation effects
52     amp_deriv = 0.5*0.8*(2*pi*stride_freq)*cos(0.8*2*pi*stride_freq*t(i)) - ...
53                     0.2*1.6*(2*pi*stride_freq)*sin(1.6*2*pi*stride_freq*t(i));
54
55     tau_thigh(i) = thigh_amplitude * amp_modulation * (2*pi*stride_freq)^2 *
56                     sin(2*pi*stride_freq*t(i)) + ...
57                     thigh_amplitude * amp_deriv * sin(2*pi*stride_freq*t(i));
58
58     phase = 2*pi*stride_freq*t(i);
59     theta_knee_base = (50 - 30*sin(phase + pi/4)) * pi/180;
60     thigh_nominal = thigh_amplitude * sin(phase);

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61     thigh_error = theta_thigh(i) - thigh_nominal;
62     compensation_gain = -1.5; % Increased for stronger compensation
63
64     theta_knee_desired = theta_knee_base + compensation_gain * thigh_error;
65
66     % Derivative includes compensation
67     omega_knee_base = -30*(pi/180)*(2*pi*stride_freq)*cos(phase + pi/4);
68     omega_thigh_nominal = thigh_amplitude * (2*pi*stride_freq) * cos(phase);
69
70     % Calculate actual thigh velocity (handle first timestep)
71     if i > 1
72         omega_thigh_actual = (theta_thigh(i) - theta_thigh(i-1)) / dt;
73     else
74         omega_thigh_actual = omega_thigh_nominal; % Use nominal for first step
75     end
76
77     omega_knee_desired = omega_knee_base + compensation_gain * (omega_thigh_actual -
78     omega_thigh_nominal);
79
79     % PD Controller for knee
80     error = theta_knee_desired - theta_knee(i);
81     error_dot = omega_knee_desired - omega_knee(i);
82
83     tau_knee(i) = Kp * error + Kd * error_dot;
84
85     % Knee dynamics: I*alpha = tau - b*omega
86     alpha_knee = (tau_knee(i) - b_knee*omega_knee(i)) / I_knee;
87
88     % Integration (Euler method with smaller timestep for stability)
89     omega_knee(i+1) = omega_knee(i) + alpha_knee * dt;
90     theta_knee(i+1) = theta_knee(i) + omega_knee(i+1) * dt;
91
92     % Apply realistic constraints (10° to 120°)
93     theta_knee(i+1) = max(10*pi/180, min(120*pi/180, theta_knee(i+1)));
94
95     % If constraint hit, zero the velocity
96     if theta_knee(i+1) <= 10*pi/180 || theta_knee(i+1) >= 120*pi/180
97         omega_knee(i+1) = 0;
98     end
99
100    % Calculate absolute shin angle
101    theta_shin_abs(i) = theta_thigh(i) + theta_knee(i);
102 end
103
104 % Final values
105 theta_thigh(N) = thigh_amplitude * sin(2*pi*stride_freq*t(N));
106 tau_thigh(N) = tau_thigh(N-1);
107 theta_knee(N) = theta_knee(N-1);
108 theta_shin_abs(N) = theta_thigh(N) + theta_knee(N);
109
110 %% Real-time Animation and Plotting
111 figure('Position', [100 100 1200 600]);
112
113 % Animation subplot
114 subplot(1, 2, 1);
115 h_leg = subplot(1, 2, 1);
116 axis equal;
117 grid on;
118 xlim([-0.4 0.4]);
119 ylim([-0.8 0.1]);
120 xlabel('X Position (m)');

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121 ylabel('Y Position (m)');
122 title('Spot Leg Walking Motion');
123 hold on;
124
125 % Initialize leg plot objects
126 h_thigh = plot([0 0], [0 0], 'b-', 'LineWidth', 4);
127 h_shin = plot([0 0], [0 0], 'r-', 'LineWidth', 4);
128 h_hip = plot(0, 0, 'ko', 'MarkerSize', 10, 'MarkerFaceColor', 'k');
129 h_knee = plot(0, 0, 'go', 'MarkerSize', 8, 'MarkerFaceColor', 'g');
130 h_foot = plot(0, 0, 'ro', 'MarkerSize', 8, 'MarkerFaceColor', 'r');
131 h_ground = plot([-0.4 0.4], [-0.75 -0.75], 'k--', 'LineWidth', 1);
132
133 % Plotting subplot - Angles
134 subplot(2, 2, 2);
135 h_thigh_plot = plot(t(1), theta_thigh(1)*180/pi, 'b-', 'LineWidth', 2);
136 hold on;
137 h_knee_plot = plot(t(1), theta_knee(1)*180/pi, 'r-', 'LineWidth', 2);
138 xlabel('Time (s)');
139 ylabel('Angle (degrees)');
140 title('Joint Angles vs Time');
141 legend('Thigh Angle (absolute)', 'Knee Angle (relative)');
142 grid on;
143 xlim([0 t_end]);
144 ylim([-40 80]);
145
146 % Plotting Torque
147 subplot(2, 2, 4);
148 h_torque_plot = plot(t(1), tau_thigh(1), 'b-', 'LineWidth', 2);
149 xlabel('Time (s)');
150 ylabel('Torque (N·m)');
151 title('Thigh Input Torque');
152 grid on;
153 xlim([0 t_end]);
154 ylim([min(tau_thigh)-2 max(tau_thigh)+2]);
155
156 %% Animation
157 skip = 20;
158 for i = 1:skip:N
159     % leg positions
160     hip = [0; 0];
161     % Thigh extending
162     knee = hip + L_thigh * [sin(theta_thigh(i)); -cos(theta_thigh(i))];
163     % Shin bending
164     foot = knee + L_shin * [sin(theta_shin_abs(i)); -cos(theta_shin_abs(i))];
165
166     % Update
167     set(h_thigh, 'XData', [hip(1) knee(1)], 'YData', [hip(2) knee(2)]);
168     set(h_shin, 'XData', [knee(1) foot(1)], 'YData', [knee(2) foot(2)]);
169     set(h_knee, 'XData', knee(1), 'YData', knee(2));
170     set(h_foot, 'XData', foot(1), 'YData', foot(2));
171
172     % Update plots
173     set(h_thigh_plot, 'XData', t(1:i), 'YData', theta_thigh(1:i)*180/pi);
174     set(h_knee_plot, 'XData', t(1:i), 'YData', theta_knee(1:i)*180/pi);
175     set(h_torque_plot, 'XData', t(1:i), 'YData', tau_thigh(1:i));
176
177     drawnow;
178     pause(0.02); % Longer pause for slower animation
179 end
180
181

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182 desired_knee = (50 - 30*sin(2*pi*stride_freq*t + pi/4)) * pi/180;
183 fprintf('==> PD Controller Performance ==\n');
184 fprintf('Kp: %.2f, Kd: %.2f\n', Kp, Kd);
185 fprintf('Mean tracking error: %.2f degrees\n', ...
186     mean(abs((desired_knee - theta_knee)*180/pi)));
187 fprintf('Max knee angle: %.2f degrees\n', max(theta_knee)*180/pi);
188 fprintf('Min knee angle: %.2f degrees\n', min(theta_knee)*180/pi);
189 fprintf('Knee angle range: %.2f degrees\n', (max(theta_knee) - min(theta_knee))*180/pi);
```