$$\begin{pmatrix} 1\\4\\1\\1 \end{pmatrix} S = \begin{pmatrix} \mathbf{a}\\1\\4\\1\\1 \end{pmatrix}$$