

## Vectors

$$\begin{aligned}
 \mathbf{u} &= \langle u_x, u_y, u_z \rangle, \mathbf{w} = \langle w_x, w_y, w_z \rangle \\
 \|\mathbf{u}\| &= \sqrt{(u_x)^2 + (u_y)^2 + (u_z)^2} \\
 \mathbf{u} \cdot \mathbf{w} &= (u_x w_x) + (u_y w_y) + (u_z w_z) = \|\mathbf{u}\| \|\mathbf{w}\| \cos \theta \\
 \mathbf{u} \times \mathbf{w} &= \langle (u_y w_z - u_z w_y), (-[u_x w_z - u_z w_x]), (u_x w_y - u_y w_x) \rangle \\
 \|\mathbf{u} \times \mathbf{w}\| &= \|\mathbf{u}\| \|\mathbf{w}\| \sin \theta \\
 \text{proj}_{\mathbf{w}} \mathbf{u} &= \frac{\mathbf{u} \cdot \mathbf{w}}{\|\mathbf{u}\| \|\mathbf{w}\|} \mathbf{w}
 \end{aligned}$$

## Surfaces

$$\begin{aligned}
 (ax + by^2 = c) &\Rightarrow \text{parabola} \\
 (ax^2 + by^2 = c) &\Rightarrow \text{circle/ellipse} \\
 (ax^2 - by^2 = k^2 + c) &\Rightarrow \text{hyperbola (one-sheet)} \\
 (ax^2 - by^2 = k^2 - c) &\Rightarrow \text{hyperbola (two-sheets)}
 \end{aligned}$$

## Vector value functions

$$\begin{aligned}
 \mathbf{r}(t) &= \langle x(t), y(t), z(t) \rangle \\
 \mathbf{v}(t) &= \mathbf{r}'(t) = \langle x'(t), y'(t), z'(t) \rangle \\
 \mathbf{a}(t) &= \mathbf{v}'(t) = \langle x''(t), y''(t), z''(t) \rangle \\
 L &= \int_a^b \|\mathbf{v}(t)\| dt \\
 \mathbf{T}(t) &= \frac{1}{\|\mathbf{v}\|} \mathbf{v} \\
 \mathbf{N}(t) &= \frac{1}{\|\mathbf{T}'(t)\|} \mathbf{T}'(t) \\
 k &= \|\mathbf{T}'(t)\| \frac{1}{\|\mathbf{v}\|} \\
 \mathbf{a}(t) &= a_{\mathbf{T}} \mathbf{T} + a_{\mathbf{N}} \mathbf{N} \\
 \text{linear component: } a_{\mathbf{T}} &= \frac{d^2 s}{dt^2} = \frac{\mathbf{v} \cdot \mathbf{a}}{\|\mathbf{v}\|} \\
 \text{angular component: } a_{\mathbf{N}} &= \left( \frac{ds}{dt} \right)^2 k = \frac{\|\mathbf{v} \times \mathbf{a}\|}{\|\mathbf{v}\|}
 \end{aligned}$$