# spBeamer Demo

**Sweet Pastry** 

Fudan University, Shanghai, China

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# Summary

Introduction

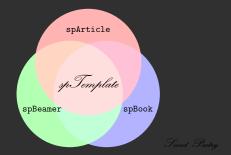
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## Definition (Linear Functional)

A linear functional on a vector space X over  $\mathbb R$  or  $\mathbb C$  is a map  $f:X\to\mathbb R$  (or  $\mathbb C$ ) such that:

$$f(\alpha x + \beta y) = \alpha f(x) + \beta f(y) \quad \forall x, y \in X, \ \alpha, \beta \in \mathbb{R} \ (\text{or} \ \mathbb{C})$$

## Definition (Sublinear Functional)

A map  $p: X \to \mathbb{R}$  is called sublinear if:

$$p(x+y) \le p(x) + p(y)$$
 and  $p(\lambda x) = \lambda p(x) \quad \forall x, y \in X, \ \lambda \ge 0$ 

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# Theorem (Hahn-Banach, Normed Space Version)

Let X be a normed space, M a subspace of X, and  $f:M\to\mathbb{R}$  a bounded linear functional. Suppose  $p:X\to\mathbb{R}$  is a sublinear functional such that:

$$f(x) \le p(x) \quad \forall x \in M$$

Then, there exists an extension  $F: X \to \mathbb{R}$  of f such that:

$$F(x) \le p(x) \quad \forall x \in X$$

and F is linear and bounded.

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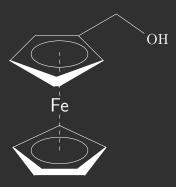
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#### References

- [1] L. Lamport, LaTeX: A Document Preparation System, 2nd. Boston, MA: Addison-Wesley, 1994, An excellent introduction to LaTeX., ISBN: 978-0201529838. https://latex-project.org/.
- [2] A. Einstein, "Zur elektrodynamik bewegter körper," Annalen der Physik, vol. 322, no. 10, pp. 891–921, 1905, This paper introduces the theory of special relativity. DOI: 10.1002/andp.19053221004.
- [3] D. E. Knuth, *Knuth: Computers and typesetting*, http://www-cs-faculty.stanford.edu/~knuth/, Accessed: 2025-01-01.
- [4] A. M. Turing, "On computable numbers, with an application to the entscheidungsproblem," in *Proceedings of the London Mathematical Society*, A landmark paper in computer science., vol. s2-42, 1936, pp. 230–265. DOI: 10.1112/plms/s2-42.1.230.

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