Exercise-6.R

B-C-Herbert

2019-10-05

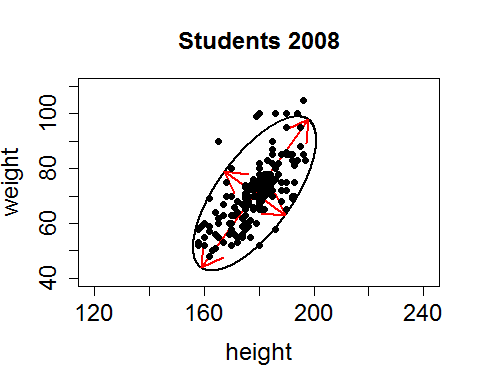
### Exercise 6  
  
remove(list = ls())  
  
students = read.table(file = "students2008.txt", header = T, dec =",")  
attach(students)

## The following object is masked from package:datasets:  
##   
## sleep

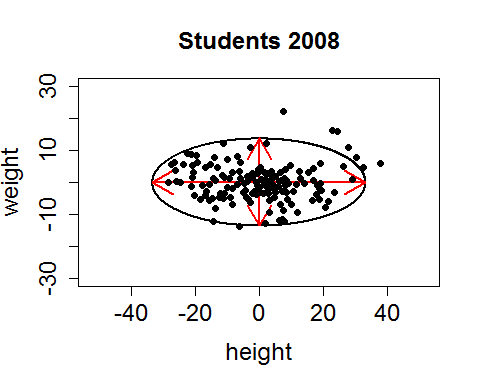
heightweight=data.frame(height,weight)  
heightweight=na.omit(heightweight)  
attach(heightweight)

## The following objects are masked from students:  
##   
## height, weight

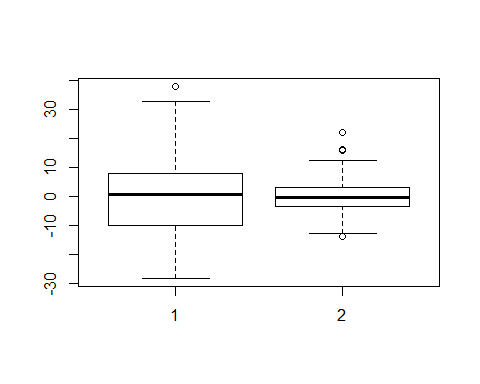
m1=mean(height)  
m2=mean(weight)  
c2=qchisq(0.95,2)  
S=cov(heightweight)  
Sinv=solve(S)  
a11=Sinv[1,1]  
a12=Sinv[1,2]  
a22=Sinv[2,2]  
x1=seq(150,210,le=1000)  
x2=seq(40,110,le=1000)  
f=function(x1,x2)  
{  
 a11\*(x1-m1)^2+a22\*(x2-m2)^2+2\*a12\*(x1-m1)\*(x2-m2)  
}  
z=outer(x1,x2,f)  
  
# a)  
  
contour(x1,x2,z,asp=1,levels=c2,drawlabels=FALSE,lwd=2,  
 cex.axis=1.5,cex.lab=1.5,cex.main=1.5,  
 xlab="height",ylab="weight",main="Students 2008")  
reseigen=eigen(S)  
lambda=reseigen$values  
E=reseigen$vectors  
lambda1=lambda[1]  
lambda2=lambda[2]  
e1=E[,1]  
e2=E[,2]  
arrows(m1,m2,sqrt(c2\*lambda1)\*e1[1]+m1,sqrt(c2\*lambda1)\*e1[2]+m2,lwd=2, col = "red")  
arrows(m1,m2,sqrt(c2\*lambda2)\*e2[1]+m1,sqrt(c2\*lambda2)\*e2[2]+m2,lwd=2, col = "red")  
arrows(m1,m2,-sqrt(c2\*lambda1)\*e1[1]+m1,-sqrt(c2\*lambda1)\*e1[2]+m2,lwd=2, col = "red")  
arrows(m1,m2,-sqrt(c2\*lambda2)\*e2[1]+m1,-sqrt(c2\*lambda2)\*e2[2]+m2,lwd=2, col = "red")  
  
points(height,weight,pch=16)



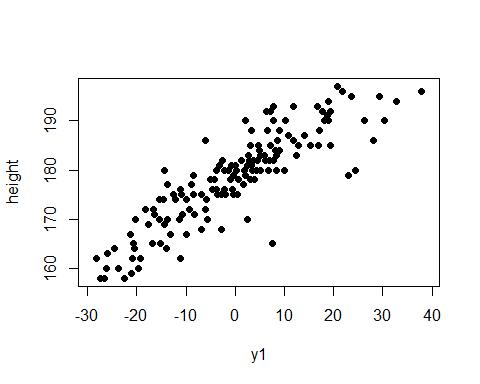
# ii)  
X = scale(heightweight, TRUE, FALSE)  
S = cov(heightweight)  
Ee = eigen(S)  
S = matrix(c(Ee$values[1],0,0,Ee$values[2]),2,2)  
Sinv = solve(S)  
lam1 = eigen(S)$values[1]  
lam2 = eigen(S)$values[2]  
  
c2=qchisq(0.95,2)  
  
x1 = seq(-40,40, le = 1000)  
x2 = seq(-30,30, le = 1000)  
  
f=function(x1,x2)  
{  
 1/(lam1)\*(x1)^2+1/lam2\*(x2)^2  
}  
z=outer(x1,x2,f)  
  
contour(x1,x2,z,asp=1,levels=c2,drawlabels=FALSE,lwd=2,  
 cex.axis=1.5,cex.lab=1.5,cex.main=1.5,  
 xlab="height",ylab="weight",main="Students 2008")  
  
reseigen=eigen(S)  
  
lambda=reseigen$values  
E=reseigen$vectors  
lambda1=lambda[1]  
lambda2=lambda[2]  
e1=E[,1]  
e2=E[,2]  
m1 = 0  
m2 = 0  
arrows(m1,m2,sqrt(c2\*lambda1)\*e1[1]+m1,sqrt(c2\*lambda1)\*e1[2]+m2,lwd=2, col = "red")  
arrows(m1,m2,sqrt(c2\*lambda2)\*e2[1]+m1,sqrt(c2\*lambda2)\*e2[2]+m2,lwd=2, col = "red")  
arrows(m1,m2,-sqrt(c2\*lambda1)\*e1[1]+m1,sqrt(c2\*lambda1)\*e1[2]+m2,lwd=2, col = "red")  
arrows(m1,m2,sqrt(c2\*lambda2)\*e2[1]+m1,-sqrt(c2\*lambda2)\*e2[2]+m2,lwd=2, col = "red")  
  
y1 = X%\*%Ee$vectors[,1]  
y2 = X%\*%Ee$vectors[,2]  
  
Y = cbind(y1,y2)  
points(Y, pch = 16)



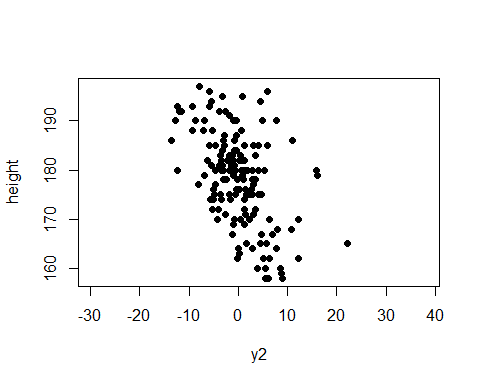
boxplot(c(y1),c(y2))



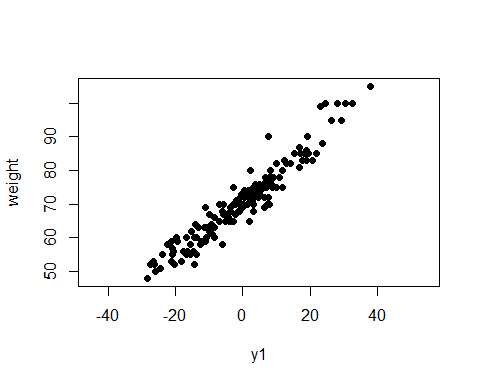
plot(y1,height, pch = 16, asp = 1)



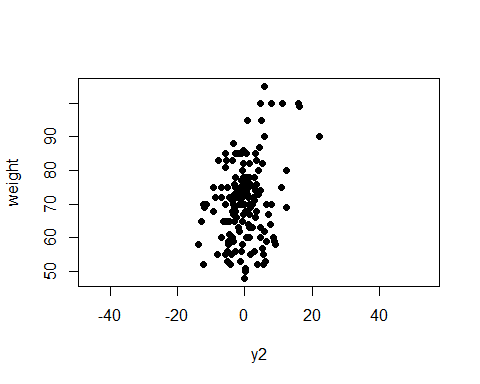
plot(y2,height, pch = 16, asp = 1)



plot(y1, weight, pch = 16, asp = 1)



plot(y2, weight, pch = 16, asp = 1)



# b)   
round(Ee$vectors, digits = 4)

## [,1] [,2]  
## [1,] 0.5875 -0.8092  
## [2,] 0.8092 0.5875

round(Ee$values, digits = 4)

## [1] 184.7198 30.8903

round(cor(y1,height), digits = 4)

## [,1]  
## [1,] 0.8713

round(cor(y1,weight), digits = 4)

## [,1]  
## [1,] 0.9586

round(cor(y2,height), digits = 4)

## [,1]  
## [1,] -0.4908

round(cor(y2,weight), digits = 4)

## [,1]  
## [1,] 0.2846

round(Ee$values[1]/sum(Ee$values), digits = 4)

## [1] 0.8567

round(sum(Ee$values)/sum(Ee$values), digits = 4)

## [1] 1