

長庚大學期中、期末考試答案用紙

科目 _____

學年度 第 _____ 學期 _____ 考 電機通訊三系 姓名 朱豐任 學號 B0621142

[1] (a) $\mu = 70, \sigma = 8$
 $n = 25 \rightarrow \bar{x} = 73$
 $\alpha = 5\%$

$70 \times 5\% = 70 \times \frac{5}{100} = 3.5$
 $70 + 3.5 = 73.5$
 $70 - 3.5 = 66.5$

$s = 8 = \sqrt{\frac{\sum x^2}{25} - 70^2}$
 $x = \sqrt{8^2 + 70^2} = 70.4557$
 在誤差內

誤差在 66.5 ~ 73.5 歲之間可被接受

$\therefore \bar{x} = 73$ 歲不能推翻 $\mu = 70$ 歲之認知

(b) $s = 9 = \sqrt{\frac{\sum x^2}{25} - 73^2}$
 $9^2 + 73^2 = x^2$

code:
 import numpy as np
 import scipy.stats as st
 import pandas as pd

st.norm.sf(73, loc=70, scale=8/5)
 $\Rightarrow 0.0303963 < 0.5$
 不能

$x = 73.55 > 73.5 \rightarrow$ 已超出 73.5 $\therefore s = 9$ 且 $\bar{x} = 73$ 能推翻 $\mu = 70$ 歲之認知
 能

[2] (a) $E(\hat{p}) = E\left(\frac{\sum x}{n}\right) = \frac{1}{n} E(\sum x) = \frac{1}{n} \cdot n \cdot p = p$

(b) $std(\hat{p}) = \sqrt{Var(\hat{p})} = \sqrt{Var\left(\frac{\sum x}{n}\right)} = \sqrt{\frac{1}{n^2} Var(\sum x)} = \sqrt{\frac{1}{n} \cdot n \cdot p \cdot q} = \sqrt{\frac{p \cdot q}{n}}$

(c) $E = \frac{\sigma}{\sqrt{n}} = \frac{\sqrt{\frac{p \cdot q}{n}}}{\sqrt{n}} = \frac{\sqrt{p \cdot q}}{n} = \frac{\sqrt{0.6 \cdot 0.4}}{100} = \frac{0.4899}{100}$

$0.6 - (1.96) \frac{0.4899}{100} < \mu < 0.6 + (1.96) \frac{0.4899}{100}$
 $p = 0.6, q = 0.4$

$0.5904 < \mu < 0.6096$

(d) $0.6 - (1.645) \frac{0.4899}{100} < \mu < 0.6 + (1.645) \frac{0.4899}{100}$

$0.5919 < \mu < 0.6081$

[3] (a) $n = 100, p = 0.6$
 $p(\bar{x} = 66) = 0.03908$

(b) $st.binom.cdf(66, 100, 0.6)$
 $\Rightarrow 0.908746$

import numpy as np

$1 - 0.908746 = 0.091254$

import scipy.stats as st

(c) 60

import pandas as pd

(d) 不拒絕接受 H_0

st.binom.pmf(66, 100, 0.6)

(e) 0.91

$\Rightarrow 0.03908 >$

(f) $\beta = 0.0391$

(g)

(請翻面繼續作答)