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“Strassen Theorem”

$$T(n) = 7^{\log_2 n} \quad n = 2^i; i \in \mathbb{N} \cup \{0\}$$

$$\text{Let } n = 2^0 = T(7^{\log_2 n}) \mid \geq T(1) \approx 1$$

Induction Hypothesis

Suppose $n = 2^k, k \in \mathbb{N}$ and that $T(2^k) = 7^{\log_2(2^k)}$ satisfies

$$T(n) = 7T\left(\frac{n}{2}\right)$$

Statement to prove:

Let $n = 2^{k+1} \geq T(2^{k+1}) = 7^{\log_2(2^{k+1})}$ which satisfies

$$T(n) = 7T\left(\frac{n}{2}\right)$$

$$\text{Let } T(2^{kn}) = 7^{\log_2(2^{k+1})}$$

Let us also compute the value of

$$7T\left(\frac{n}{2}\right) \mid n = 2^{k+1}$$

$$7T\left(\frac{n}{2}\right) \mid = 7T\left(\frac{2^{k+1}}{2}\right) = 7T(2^k)$$

We know

$$\begin{aligned} T(2^k) &= 7^{\log_2(2^k)} = 7^{k \log_2(2)} = 7^{k(1)} = 7T(2^k) = 7^1 \circ 7k = 7^{k+1} = 7^{k+1(1)} \\ &= 7^{k+1(\log(0))} \\ &= 7^{\log_0(2^{k+1})} \end{aligned}$$