

Hydrodynamic Origin of the Hydrogen Ground State

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Abstract

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Circulation as a Fundamental Quantity in Physics and SST

Historically, the idea of *circulation* as a primitive physical quantity dates back to 19th-century hydrodynamics. In 1858, Hermann von Helmholtz proved that vortex lines in an inviscid fluid move as indestructible tubes—their vorticity and circulation are conserved in time. A decade later, William Thomson (Lord Kelvin) formalized the conservation of circulation with his famous theorem:

$$\frac{d\Gamma}{dt} = 0 \quad (1)$$

for any material loop in a barotropic ideal fluid. Kelvin went further to propose that atoms might in fact be knotted vortex rings in a universal ether, each with a quantized circulation “charge”. This bold vortex atom model elevated the line-integral of velocity (circulation) to a candidate fundamental invariant of nature. The legacy of Helmholtz and Kelvin is a recognition that *circulation can be treated as a basic building block*—a concept that Swirl String Theory (SST) adopts as a central postulate.

In SST, matter is modeled as stable swirl strings (closed vortex filaments) in a pervasive incompressible medium. It is thus natural to take circulation (the strength of these vortices) as a primitive quantity. We seek a fundamental circulation constant, Γ_0 , that characterizes the swirl medium. To pin down Γ_0 quantitatively, we start from a remarkable relativistic scale: the maximum electromagnetic force. Consider the ratio of an electron’s rest energy to its classical radius,

$$r_e = \frac{\alpha \hbar}{m_e c} \quad (2)$$

This yields a force magnitude:

$$F_{\max} = \frac{m_e c^2}{r_e} = \frac{m_e^2 c^3}{\alpha \hbar} \approx 2.905 \times 10^1 \text{ N} \quad (3)$$

where m_e is the electron mass, c the speed of light, \hbar Planck’s constant, and $\alpha \approx 1/137$ the fine-structure constant. This $F_{\max} \sim 29 \text{ N}$ is an empirical force scale appearing in the SST canon (listed as the EM-sector maximum force). Physically, it represents the self-interaction force scale of an electron’s charge in classical electromagnetism, and in some formulations it’s viewed as an upper limit for force transmissible in that sector. In the context of the swirl medium, we posit that an equivalent force scale should emerge from the medium’s fundamental parameters. Dimensional analysis suggests that the combination $\rho_{!f} \Gamma_0^2$ (fluid density times circulation-squared) has units of force:

- Dimensions check: $[\rho_{!f} \Gamma_0^2] = \left[\frac{M}{L^3} \right] \left[\frac{L^4}{T^2} \right] = \frac{ML}{T^2}$, the dimensions of force.

We therefore impose the relation

$$F_{\max} = \chi_F \rho_{!f} \Gamma_0^2 \quad (4)$$

where $\rho_{!f}$ is the mass density of the swirl medium and χ_F is a dimensionless proportionality factor to be fixed by convention. Solving for the circulation constant gives

$$\Gamma_0 = \sqrt{\frac{F_{\max}}{\chi_F \rho_{!f}}} \quad (5)$$

By choosing Γ_0 as a defining constant of the theory, we can absorb any order-unity factor χ_F into its value. In other words, Γ_0 is defined such that $\chi_F = 1$, making it the exact circulation needed to reproduce the 29.05 N force when combined with the medium density. Using the calibrated SST density $\rho_{!f} = 7.0 \times 10^{-7} \text{ kg/m}^3$, we find:

- Numerical value:

$$\Gamma_0 \approx \sqrt{\frac{29.05 \text{ N}}{7.0 \times 10^{-7} \text{ kg/m}^3}} \approx 6.4 \times 10^3 \frac{\text{m}^2}{\text{s}} \quad (6)$$

This fundamental circulation scale Γ_0 is on the order of $10^3 \text{ m}^2/\text{s}$. Such a value may seem large compared to, say, the quantum of circulation in superfluid helium ($\sim 10^{-7} \text{ m}^2/\text{s}$), but it reflects the extremely low density of the vacuum medium in SST. Because $\rho_{!f}$ is so small, a much larger circulation is required to yield the same force—a direct consequence of the medium’s tenuousness. Indeed, $\rho_{!f}$ in SST is set fourteen orders below water’s density; intuitively, swirling such an “ultralight” medium demands a very strong circulation to accumulate significant inertia. The chosen Γ_0 ensures that $\rho_{!f}\Gamma_0^2$ matches a known physical scale (29 N), anchoring the theory’s single circulation constant to empirical reality. Moreover, this choice is consistent with particle physics scales: if we also take the core radius r_c of a swirl string to be $1.4089 \times 10^{-15} \text{ m}$ (a value calibrated to half the classical electron radius, as discussed below), then one finds

$$2\rho_{!f}\Gamma_0^2 r_c \approx m_e c^2 \quad (7)$$

i.e., on the order of the electron’s rest energy ($\sim 0.511 \text{ MeV}$). In essence, by fitting Γ_0 to F_{\max} we simultaneously guarantee that the swirl energy available in one “quantum” of circulation (within a core-sized volume) is of the right order of magnitude for particle rest energies. This is a compelling consistency check: *the circulation needed to hit the EM force limit, together with the tiny vacuum density and Fermi-scale core size, naturally encodes the rest-mass scale of matter.* No ad-hoc scales are introduced; Γ_0 is fixed by one physical requirement and then everything else falls into line.

Having established Γ_0 as the circulation quantum of the swirl medium, we now examine the other two primitive constants that SST must posit: the medium’s mass density $\rho_{!f}$ and the vortex core length r_c . These serve as the natural complementary scales (of mass-density and length) alongside Γ_0 (of circulation) to span all relevant dimensions in the theory. Indeed, $(\Gamma_0, \rho_{!f}, r_c)$ can be viewed as an alternative fundamental trio in place of, say, (c, \hbar, G) —one tailored to a fluidic ontology:

- **Swirl medium density $\rho_{!f}$:** This represents the inertial mass per volume of the vacuum condensate. It is an empirically calibrated constant in SST, set to $\rho_{!f} = 7.0 \times 10^{-7} \text{ kg/m}^3$. Notably, this value corresponds to 1×10^{-7} in SI units (mirroring the vacuum permeability $\mu_0/4\pi$) by design. The choice was made to anchor electromagnetic coupling in the swirl model—in effect, normalizing $\rho_{!f}$ such that the fluid’s response reproduces Coulombic strength. Physically, $\rho_{!f}$ is extremely small—about 10^{-19} times the density of water—reflecting a nearly void vacuum that nevertheless carries momentum and energy. Such a low density means the medium imparts only a feeble resistance to motion, which is why cosmic-scale circulation is needed to manifest substantial forces. In the SST Canon, $\rho_{!f}$ is treated as a fundamental constant (not derived from deeper theory) but its value is crucial for matching observed phenomena (e.g., atomic spectral lines, as it enters into formulas for wave impedance and force constants).
- **Core radius r_c :** This length scale sets the characteristic thickness of a swirl string—roughly the radius of the “tube” of circulating fluid that makes up a particle. SST takes r_c to be on the order of a Fermi (10^{-15} m), which is the size of a nucleon and coincidentally half the classical electron radius. In fact, the canonical value $r_c = 1.40897 \times 10^{-15} \text{ m}$ was chosen to calibrate the model’s mass predictions: by giving the smallest swirl (unknotted loop) a core of about $0.5r_e$, the self-energy stored in its vortex matches the electron’s mass. The introduction of a finite r_c is also essential for consistency—it regularizes the fluid vortex solutions by removing the singularity at $r = 0$. In classical vortex dynamics, a finite core radius cuts off the $1/r$ velocity divergence, thereby capping the maximum swirl speed. The

same is true in SST: r_c provides an inner cutoff and ensures that the fluid velocity of a swirl string remains finite (and in practice sub-relativistic). Using the above values, the tangential speed at the core boundary is $v_{\text{core}} \sim \Gamma_0/(2\pi r_c)$. Plugging in $\Gamma_0 \approx 6.4 \times 10^3 \text{ m}^2/\text{s}$ and $r_c = 1.4 \times 10^{-15} \text{ m}$, we get $v_{\text{core}} \sim 1.1 \times 10^6 \text{ m/s}$, about $3 \times 10^{-3}c$. This aligns with the characteristic swirl speed listed in the SST constants ($v \approx 1.09 \times 10^6 \text{ m/s}$). Thus, the chosen r_c guarantees that no point in the vortex approaches light-speed motion—a vital check on the theory’s internal consistency (no Lorentz violations at the mechanical level). Additionally, r_c sets the scale of the smallest structures in the theory (the “thickness” of strings), playing a role analogous to the Planck length in quantum gravity or string length in string theory, albeit at a nuclear scale here.

In summary, by starting from the electron’s force/mass scales and classical vortex principles, we justify the adoption of $(\Gamma_0, \rho_{!f}, r_c)$ as the primitive dimensional constants of SST. Γ_0 provides the link between circulation and force (anchoring the overall scale of vortex strength to known physics), while $\rho_{!f}$ and r_c supply the natural density and length cutoffs to define the medium’s properties. *All other dimensional quantities in SST can be constructed from these three:* for example, a characteristic energy scale can be formed as $\rho_{!f}\Gamma_0^2 r_c$ (on the order of 10^{-14} J , corresponding to hundreds of keV), and a characteristic time scale as r_c^2/Γ_0 (on the order of 10^{-30} s , which relates to high-frequency swirl excitations). In the next section, we formalize the circulation-based canon of SST by detailing these three primitive constants and showing how they underpin the theory’s postulates and benchmarks. This will lead directly into the section “Primitive dimensional constants,” where we enumerate Γ_0 , $\rho_{!f}$, and r_c and outline their defined values and roles in the SST framework.

References

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