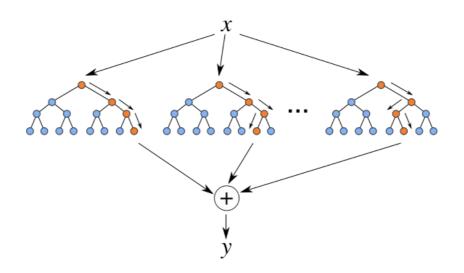


Workshop: Machine Learning and Prediction Modelling

Ensemble Methods



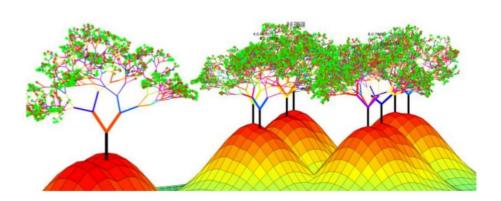
Yannick Rothacher

SPF, HS2025



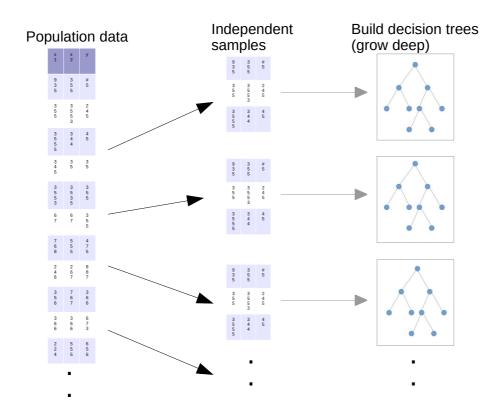
Ensemble methods

- Why not combine multiple models to improve prediction?
- Given some training data and a test-observation:
 - ➤ You could apply multiple, different classifiers to the data (logistic regression, KNN, decision tree, neural network, ...) and incorporate each classifier's prediction into your final prediction of the test observation (e.g. majority vote)
- ► Ensemble methods are based on a similar intuition: Combine multiple (simple) models of the same type to improve performance
- With regard to decision trees there are two ensemble methods, which are mostly applied:
 - Bagging
 - Random Forest



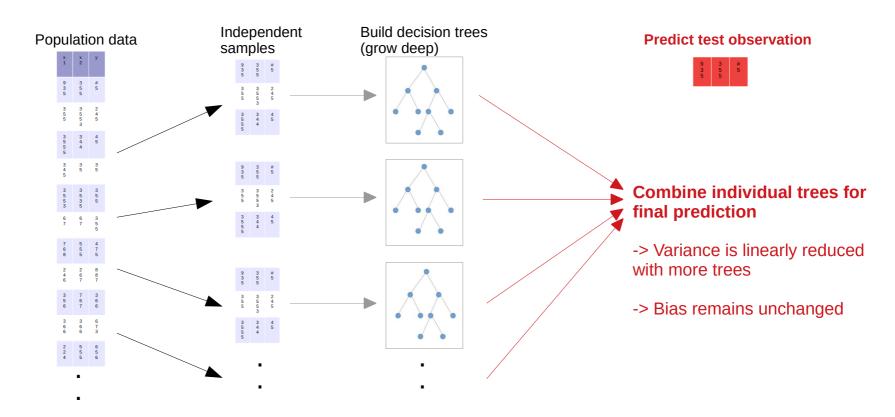


- Bagging (bootstrap aggregating) is an ensemble method typically applied to decision trees (but can be applied to all classifiers)
- Main idea: Fully grown decision trees have low bias but high variance...
 - ...it would be nice to have multiple independent samples from the same population to reduce variance by taking the mean of prediction



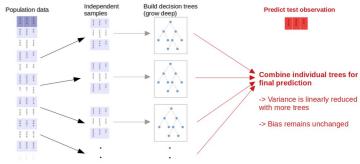


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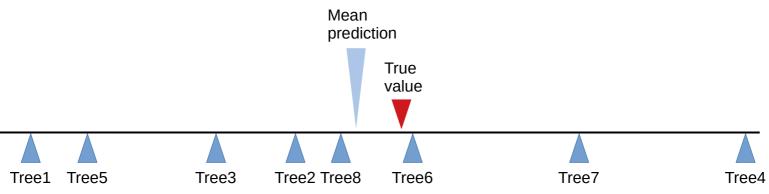




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- By averaging the individual trees the variance of the estimation is reduced

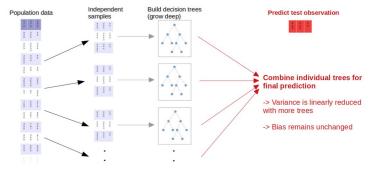


Predictions

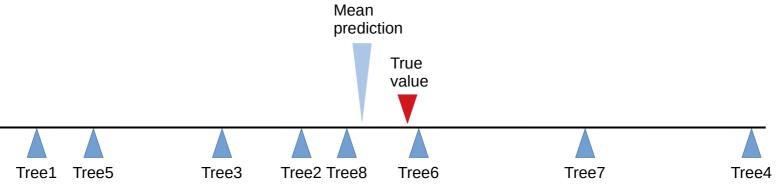




- ▶ **Bagging** (bootstrap aggregating) is an ensemble method typically applied to decision trees (but can be applied to all classifiers)
- Main idea: Fully grown decision trees have low bias but high variance...
 - ...it would be nice to have multiple independent samples from the same population to reduce variance by taking the mean of prediction
- By averaging the individual trees the variance of the estimation is reduced
- However: In reality we usually only have one training sample from the population

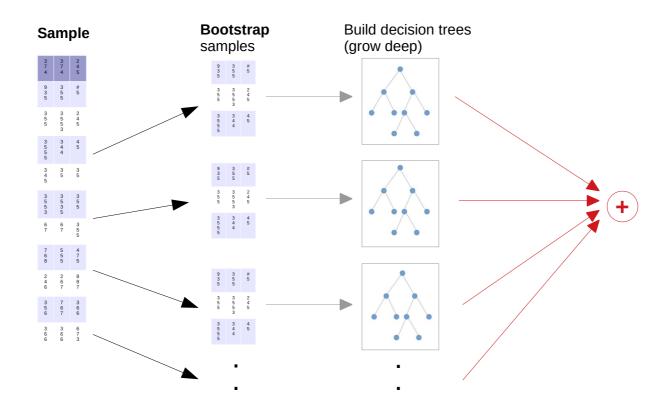


Predictions



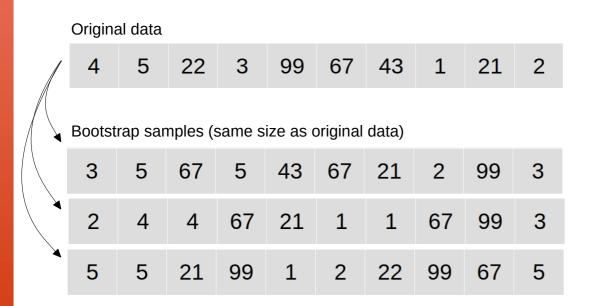


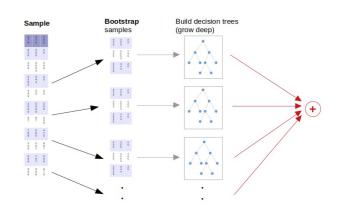
- In reality we usually only have only **one sample** from the population
 - Solution: We now take **bootstrap samples** from our training data (originally suggested by Breiman 1996)
 - Grow deep decision trees on bootstrap samples and combine the trees for prediction





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 - Grow deep decision trees on bootstrap samples and combine the trees for prediction
- Bootstrap samples are samples drawn with replacement:

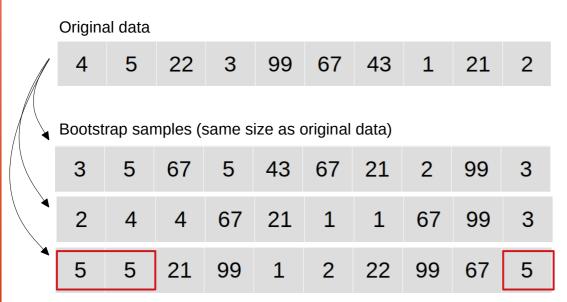


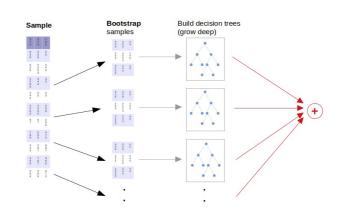


Breiman L: Bagging Predictors. Machine Learning 1996, 24(2):123-140.



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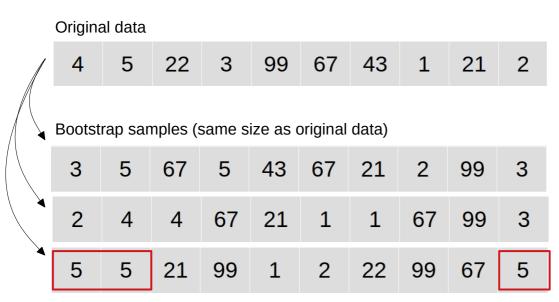




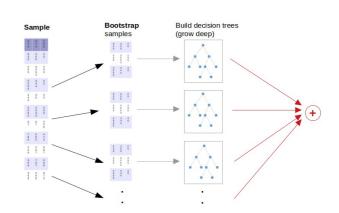
Same observation can appear multiple times!



- In reality we usually only have only **one sample** from the population
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Same observation can appear multiple times!



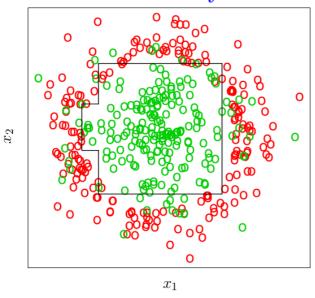
Bagging shows better performance than one decision tree applied to original data (why?)

Note: Individual bootstrap samples are not independent!

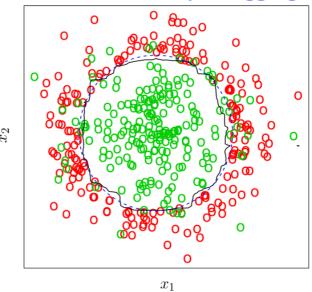
-> Variance is only reduced sublinearly



Decision Boundary: Tree



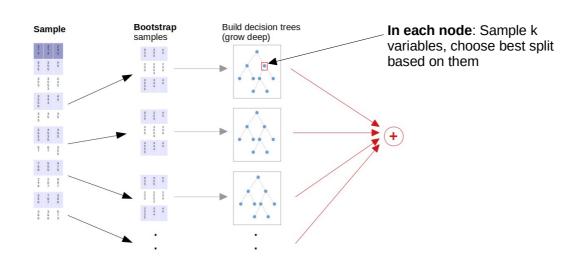
Decision Boundary: Bagging



Source: Ji Zhu, University of Michigan

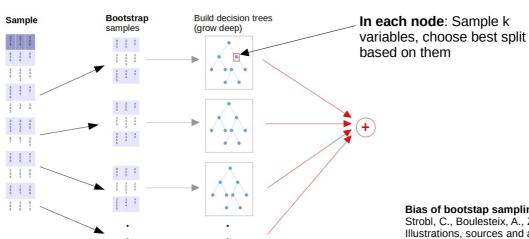


- Random forest is an extension of bagging
 - Main idea: Do not only sample from the data but also from the variables, which are used for splitting
- In random forest the trees are generated in the following way
 - Generate bootstrap samples from original data (same like bagging)
 - Build a decision tree on each bootstrap sample, but...
 - ... at each node of a decision tree, randomly select k variables, which are evaluated for splitting. Choose the best split (using only the k variables).





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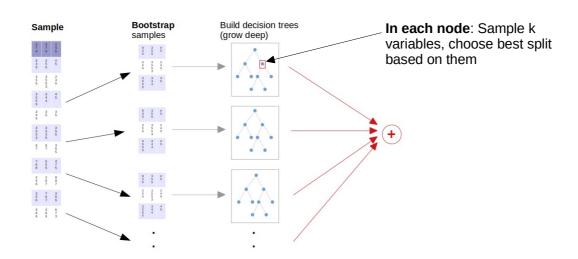


Can also use **sub- samples** instead
of bootstrap
samples. Bootstrap
sampling can also
induce bias in
variable selection.

Bias of bootstap sampling in RF:Strobl, C., Boulesteix, A., Zeileis, A. et al. Bias in random forest variable importance measures: Illustrations, sources and a solution. BMC Bioinformatics 8, 25 (2007)

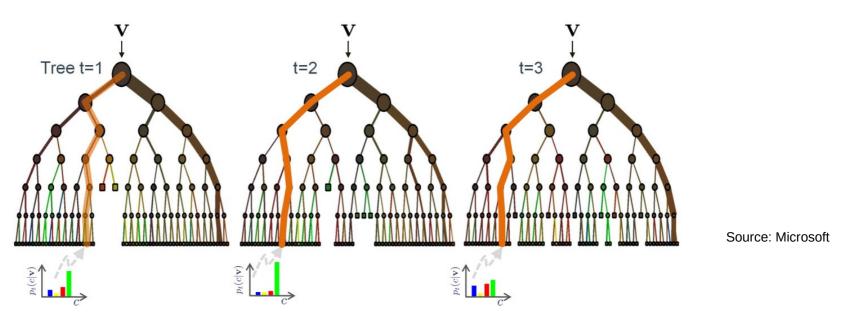


- What is the point of sampling the variables?
 - Sampling variables de-correlates the individual trees, makes them more diverse (this increases variance reduction)
 - ▶ Intuition: By restricting the variable selection at each node, some variables are incorporated in the analysis which might otherwise never be considered
 - This can reveal interactions in the data, which would otherwise not be detected





- Prediction of a new observation same like in bagging:
 - Run observation through all trees and incorporate each tree's prediction in the final prediction (e.g. majority vote for classification or mean for regression)
- Example of aggregating the tree's results for classification:



Average probability: $\overrightarrow{\underbrace{\frac{\mathbf{v}}{\mathbf{v}}}} p(c|\mathbf{v}) = \frac{1}{T} \sum_{t}^{T} p_{t}(c|\mathbf{v})$

Predicted category: green



Random Forest in R

We will use the cforest() function from the package "partykit" (unbiased variable selection)

```
### Cforest with partykit:
library("partykit")
set.seed(123)
rf smoke <- cforest(intention to smoke ~., data = dat smoking, ntree=500, mtry=2)</pre>
### Confusion matrix (OOB predictions):
preds oob <- predict(rf smoke, 00B = TRUE)</pre>
confT <- table(dat smoking$intention to smoke, preds oob)</pre>
confT
     preds_oob
      no yes
  no 93 20
 yes 25 62
### Calculate (00B) misclassification rate:
confT_mis <- confT</pre>
diag(confT_mis) <- 0</pre>
sum(confT mis)/sum(confT)
0.23
### Make predictions for "new" observations:
predict(rf_smoke, newdata = dat_smoking[1:4,], type = 'response')
 1 2 3 4
 no yes no yes
Levels: no yes
```

The used "smoking" data includes data from teenagers and the target variable is whether a person intends to start smoking (yes/no). The predictor variables are:

lied_to_parents,
alcohol_per_month,

age, friends smoke





Random Forest in R

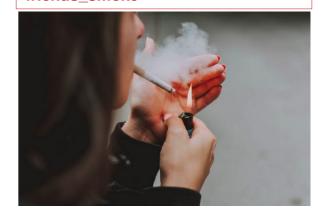
We will use the cforest() function from the package "partykit" (unbiased) variable selection)

```
ntree: How many trees to grow
### Cforest with partykit:
library("partykit")
set.seed(123)
rf smoke <- cforest(intention to smoke ~., data = dat smoking, ntree=500, mtry=2)</pre>
### Confusion matrix (OOB predictions):
                                                             What is OOB?
preds oob <- predict(rf smoke, 00B = TRUE)</pre>
confT <- table(dat smoking$intention to smoke, preds oob)</pre>
confT
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      no yes
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The used "**smoking**" data includes data from teenagers and the target variable is whether a person intends to start smoking (yes/no). The predictor variables are: lied to parents, alcohol per month, age, friends smoke

mtry: How many variables

to sample at each node



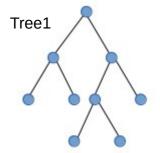


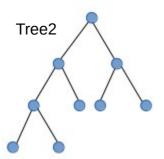
- Random Forest comes with its own integrated evaluation tool!
- Each tree is fitted to a bootstrap sample (or sub-sample) of original data
 - Thus, every tree in the forest has only seen a part of the data
- To calculate the OOB-error:
 - Predict each observation in the data using only the trees, which have not seen the observation when they were generated

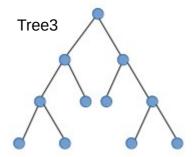


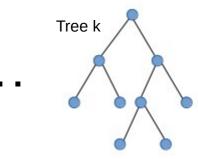
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e.g. observation #24: $\begin{pmatrix} x1 & x2 & x3 & y \\ 23.4 & 66.3 & 2 & A \end{pmatrix}$



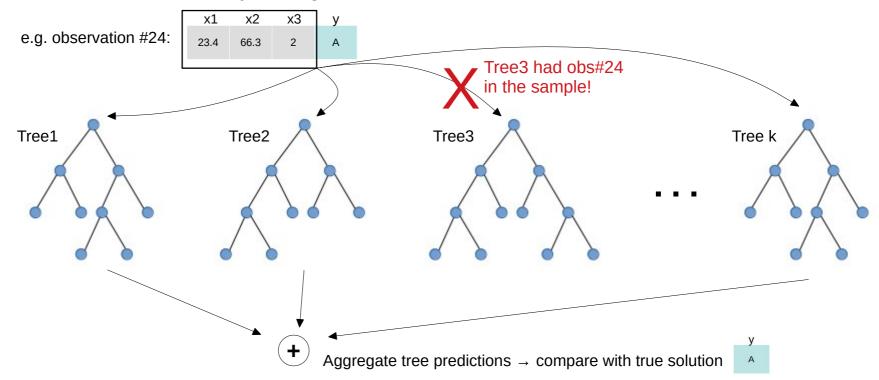








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 - Predict each observation in the data using only the trees, which have not seen the observation when they were generated





- Create OOB confusion table to look at the OOB-performance (see R-code slide)
- Use predict()-function and set OOB=TRUE, give no "newdata" argument

```
### Fit forest and calculate 00B misclassification rate:

rf_smoke <- cforest(intention_to_smoke ~., data = dat_smoking, ntree=500, mtry=2)
preds_oob <- predict(rf_smoke, 00B = TRUE)

confT <- table(dat_smoking$intention_to_smoke, preds_oob)

confT_mis <- confT

    preds_oob

    no yes

no 93 20
    yes 25 62

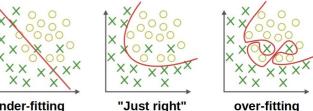
diag(confT_mis) <- 0
sum(confT_mis)/sum(confT)

0.23</pre>
```



Tuning of Random Forests

- In machine learning, we usually tune the hyperparameters of a model to find a setting which is neither under- nor overfitting the data.
 - Use crossvalidation to evaluate model performance

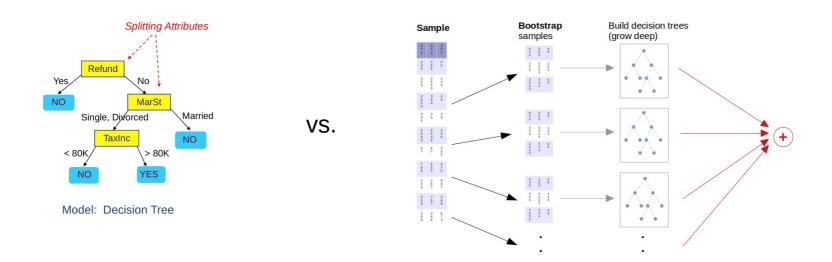


- We will look at model tuning in more detail for neural networks (next topic)
- Random forests are perhaps slightly "special" in this regard, since they are less prone to overfitting
 - Average of ensemble removes variance in predictions (RFs can still overfit in certain scenarios)
 - Random forests are said to work "off-the-shelf" (usually reach good performance with default parameter values)
- The hyperparameter **ntree** cannot be too high (only cost is computational effort)
- Ideally mtry (number of variables considered for splitting in each node) should be tuned.
 - There are further hyperparameters, which control the growing of the individual trees, that could be tuned



Interpretability of Random Forest

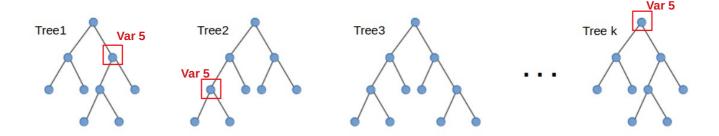
- One advantage of decision trees are their good interpretability
 - Can easily track how each variable affects the prediction
- In Random Forest we somewhat lose the interpretability ("black box")
 - Difficult to track how each variable is active in each of the e.g. 500 trees...
- How can we assess which variables are important for prediction?





Variable importance in RF

- How could variable importance be scored?
 - Simple idea: Count the number of times a variable is chosen for splitting throughout all trees
- Two more elaborate approaches:
- ➤ Variable importance 1: Average score improvement at splits
 - ➤ For each node where variable x was used for splitting, record the achieved improvement in the splitting score (e.g. Gini-index -> **Gini-importance score**)
 - ➤ Variable x's importance 1 score is the average of all score improvements (can be weighted with the number of data points in each node)





Variable importance in RF

- ➤ Variable importance 2: Permutation importance
- Permutation importance is a very intuitive importance score
- Main idea: Mix up the values of variable x to break up any meaningful relation between x and the response variable (permutation)
 - Check how much the performance (usually the OOB-error) drops after permutation of x

	Predict	oredicts	y Predicted	, Laide ra			Predict	or Predicto	nedictor	rade ^{t val}
Original data	X1	X2	Х3	Υ		X1 permuted	X1	X2	Х3	Y
	2.3	33.1	67	Α	VS.		5.1	33.1	67	Α
	5.1	35.8	70.3	В			2.3	35.8	70.3	В
	3.3	34.0	96	Α			2.8	34.0	96	Α
	2.8	37.7	85	С			1.3	37.7	85	С
	1.3	38.3	84.9	Α			3.3	38.3	84.9	Α
Calculate OOB-error							Calculate OOB-error			

Permutation importance:
Difference in OOB-error

Calculate OOB-error (using RF fitted to original data)

With stronger relation between x1 and target variable, the more should the OOB-error grow



Variable importance with R

To calculate the variable importance after fitting a Random Forest use the varimp()-function (default is permutation importance score)

lied to parents

alcohol per month

friends smoke

```
rf smoke <- cforest(intention to smoke ~., data = dat smoking, ntree=500, mtry=2)
# Calculate variable importance scores:
set.seed(123)
imps <- varimp(rf smoke)</pre>
imps
lied to parents alcohol per month
                                                           friends smoke
                                                  age
    -0.02591487
                           0.14622240
                                        -0.04417460
                                                              0.48487966
                                                                      Permutation importance scores (smoking data)
# Create barplot:
                                                       9.0
barplot(imps, col='lightblue',
        main = 'Permutation importance
                 scores (smoking data)',
                                                     permutation importance
        ylab = 'permutation importance',
        ylim = c(-0.1, 0.6))
abline(h = 0, col=1, ltv=1, lwd=3)
```



Variable importance with R

➤ To calculate the variable importance after fitting a Random Forest use the varimp()-function (default is permutation importance score)

```
rf smoke <- cforest(intention to smoke ~., data = dat smoking, ntree=500, mtry=2)
# Calculate variable importance scores:
                                                                             Because importance scores are based
set.seed(123)
                                                                             on random permutation we should fix
                                                                             the random seed when calculating them
imps <- varimp(rf smoke)</pre>
imps
lied to parents alcohol per month
                                                           friends smoke
                                                  age
    -0.02591487
                           0.14622240
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        ylab = 'permutation importance',
        ylim = c(-0.1, 0.6))
abline(h = 0, col=1, ltv=1, lwd=3)
                   Permutation importance
                   scores can also be negative!
                    → Why?
                                                              lied to parents
                                                                           alcohol per month
                                                                                                        friends smoke
```



lines(x=steps, y=apply(predic, 2, mean), col=1, lwd=4)

Partial Dependence (and ICE) Plots

- Partial dependence plots are another method to "bring light" into what is happening in the forest
- Main idea: See how the prediction of the response variable changes when only one predictor is shifted in its value
- Example of partial dependence plot for the smoking data (response: intention_to_smoke; predictor: alcohol_per_month):

```
# Self generated:
set.seed(123)
rf_smoke <- cforest(intention_to_smoke ~., data = dat_smoking, ntree=500, mtry=2)
steps <- seg(min(dat smoking$alcohol per month), max(dat smoking$alcohol per month),</pre>
              length.out=20)
predic <- matrix(NA, nrow=nrow(dat_smoking), ncol = length(steps))</pre>
for(i in 1:nrow(dat smoking)){
 obs <- dat smoking[i,]</pre>
                                                                                  predicted P(intention_to_smoke = yes)
  obs$alcohol per month <- NULL
  for(s in 1:length(steps)){
    obs$alcohol per month <- steps[s]
    predic[i,s] <- predict(rf smoke, newdata=obs, type = 'prob')[2]</pre>
    print(paste0('Done with step ', s, ' of observation ', i))
 }
plot(NULL, xlim=c(min(dat_smoking$alcohol_per_month),
     max(dat smoking$alcohol per month)),
     vlim=c(0, 1),
     xlab='alcohol_per_month', ylab='predicted P(intention_to_smoke = yes)')
for(l in 1:nrow(predic)){
                                                                                                                         alcohol per month
 lines(x = steps, y = predic[l,], col='grey')
```



Partial Dependence (and ICE) Plots

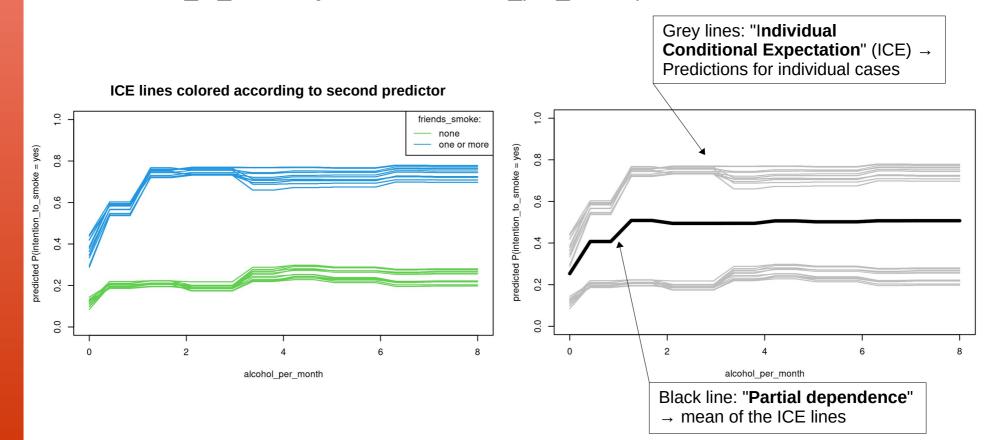
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```
# Self generated:
                                                                                                       Grey lines: "Individual
set.seed(123)
                                                                                                       Conditional Expectation" (ICE) →
rf_smoke <- cforest(intention_to_smoke ~., data = dat_smoking, ntree=500, mtry=2)
                                                                                                       Predictions for individual cases
steps <- seg(min(dat smoking$alcohol per month), max(dat smoking$alcohol per month),</pre>
             length.out=20)
predic <- matrix(NA, nrow=nrow(dat_smoking), ncol = length(steps))</pre>
for(i in 1:nrow(dat smoking)){
  obs <- dat smoking[i,]</pre>
                                                                              predicted P(intention_to_smoke = yes)
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    print(paste0('Done with step ', s, ' of observation ', i))
  }
plot(NULL, xlim=c(min(dat_smoking$alcohol_per_month),
     max(dat smoking$alcohol per month)),
    vlim=c(0, 1),
     xlab='alcohol_per_month', ylab='predicted P(intention_to_smoke = yes)')
for(l in 1:nrow(predic)){
                                                                                                                  alcohol per month
  lines(x = steps, y = predic[l,], col='grey')
                                                                                                       Black line: "Partial dependence"
                                                                                                       → mean of the ICE lines
lines(x=steps, y=apply(predic, 2, mean), col=1, lwd=4)
```



Partial Dependence (and ICE) Plots

- Partial dependence plots are another method to "bring light" into what is happening in the forest
- Main idea: See how the prediction of the response variable changes when only one predictor is shifted in its value
- Example of partial dependence plot for the smoking data (response: intention_to_smoke; predictor: alcohol_per_month):

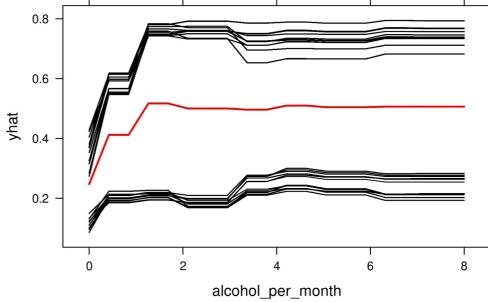




Partial dependence plots with "pdp"

- "pdp" is an R package to construct partial dependence plots
- Can be applied to different Machine Learning methods
 - Also works for Random Forests fitted with cforest()

See also the iml R package for a collection of interpretation techniques





Summary Random Forest

Advantages:

- Random Forest is a very effective ML method (good performance in ML-competitions)
- Is non-parametric, poses no assumption regarding distribution of variables or residuals
- Comes with included performance evaluation (OOB-error)
- Random Forests less prone to overfitting
- Can handle thousands of input variables
- Can handle lots of noise variables with only few relevant variables
- Random Forest can detect strong and local interactions
- Is robust against outliers
- It can handle imbalanced data (e.g. using weighted sampling)
- >



Summary Random Forest

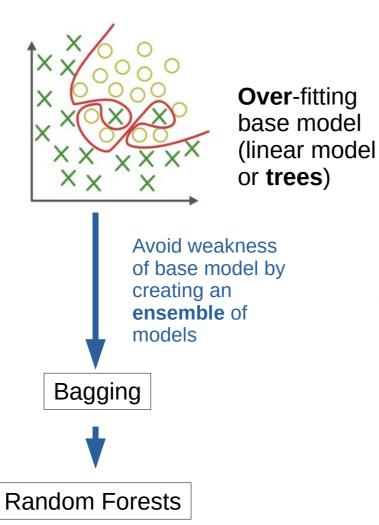
Disadvantages:

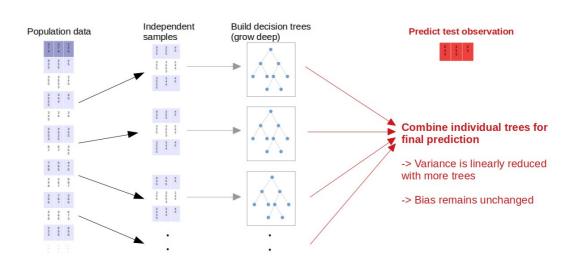
- Less interpretability, feeling of a "black box"
- Can not extrapolate predictions beyond the range of training data well
- Takes more time to train than e.g. decision tree



Ensemble methods: Boosting

Bagging + RF:

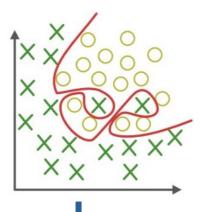






Ensemble methods: Boosting

Bagging + RF:



Over-fitting base model (linear model or **trees**)

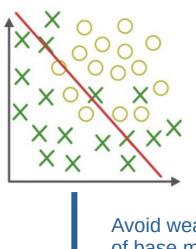
Avoid weakness of base model by creating an ensemble of models

Bagging



Random Forests

Boosting:



Under-fitting base model (linear model or trees)

Avoid weakness of base model by creating an **ensemble** of models

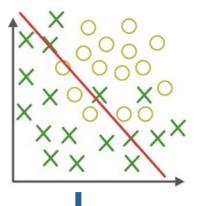
Adaptive boosting





- General intuition behind gradient boosting:
 - Fit a weak learner (usually shallow tree) to your data and check training error
 - Express through "residuals" (more specifically gradient of loss, later) the shortcomings of the initial model
 - Fit a new shallow tree to the "residuals" of the initial model
 - The predictions of the model now consist of the sum of the predictions from the first and the second tree
 - Add further trees following this procedure...

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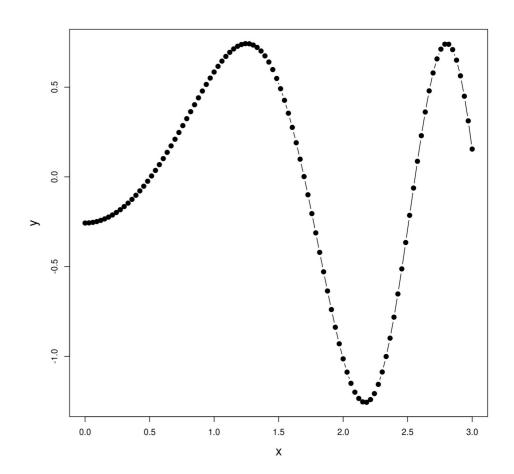
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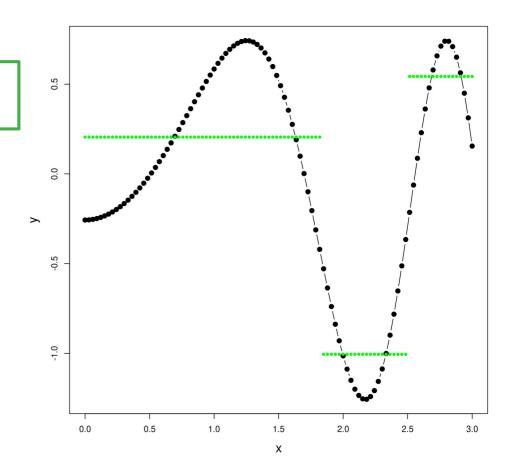


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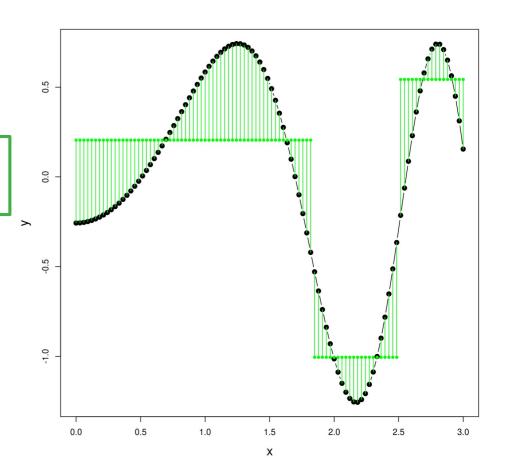


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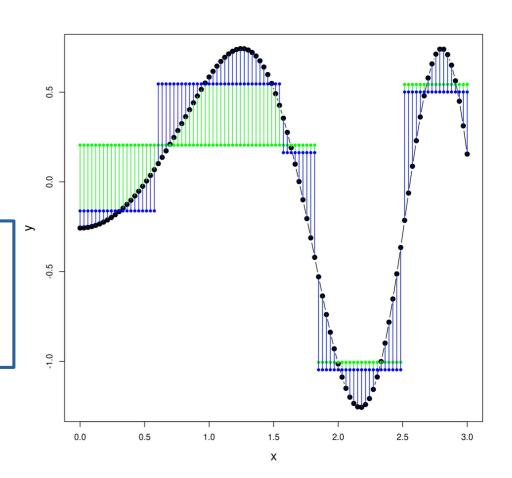


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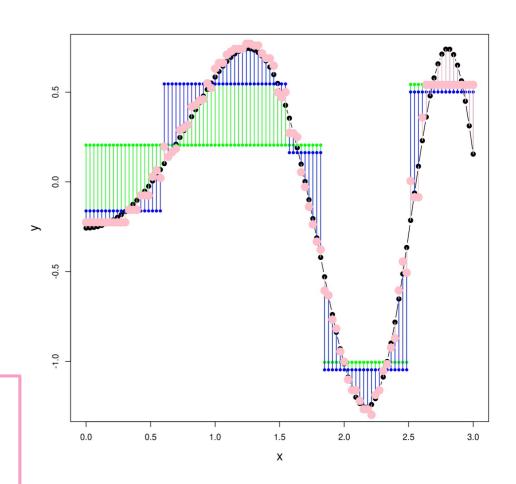


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$$M = M_1 + \eta \sum_i \gamma_i T_i$$

The final prediction of the model is updated by adding (scaled) predictions of following trees.

 η is the learning rate \rightarrow determines how much the model is updated with each tree (small values recommended, e.g. 0.1)



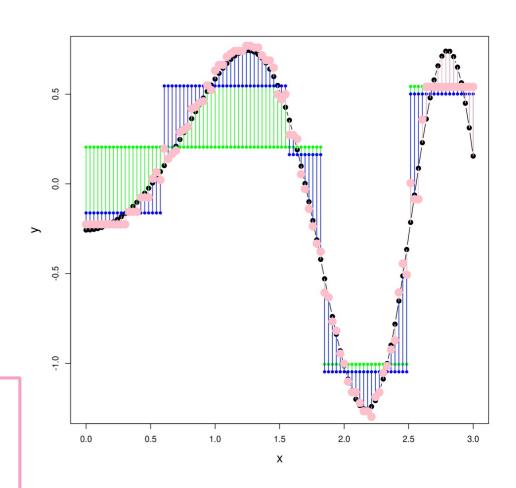


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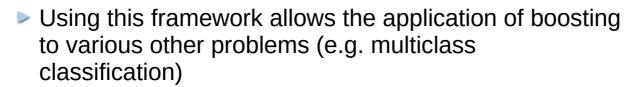
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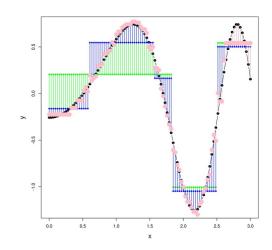


The "residuals" to which subsequent trees are fitted are the negative gradients of the problem-specific Loss (for each data point)

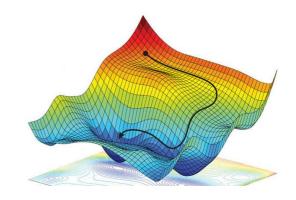
$$-g(x_i) = \frac{-\partial Loss(y_i, M(x_i))}{\partial M(x_i)}$$



- Friedman/Hastie/Tibshirani(2000): Generalization to a variety of loss functions
- Gradient boosting is an iterative gradient descent algorithm



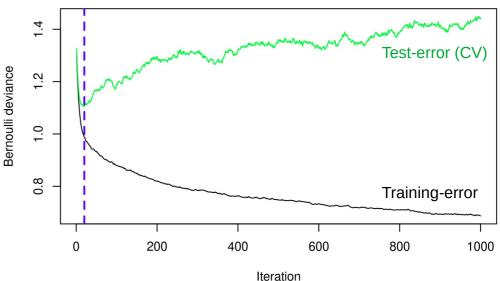
$$M = M_1 + \eta \sum \gamma_i T_i$$





Gradient boosting in R (smoking data)

```
### Gradient boosting with gbm:
library("gbm")
### Turn intention to smoke to 0, 1 variable:
d <- dat smoking
d$intention_to_smoke <- as.numeric(dat_smoking$intention_to_smoke)-1</pre>
### Fit gradient boosting ensemble:
boost_smk <- gbm(intention_to_smoke ~., data=d,</pre>
                 distribution = 'bernoulli',
                 n.trees = 1000,
                 shrinkage = 0.1,
                 interaction.depth = 3,
                 cv.folds = 10)
### Find best number of iterations, i.e. trees:
gbm.perf(boost_smk, method = 'cv')
[1] 22
### Make predictions (probabilites):
                                                     1.2
predict(boost smk, newdata=d[1:3,],
      type = 'response', n.trees = 22)
[1] 0.4046658 0.7258298 0.1103924
```





Gradient boosting in R (smoking data)

```
### Gradient boosting with gbm:
                                                                 For binary classification y must be a
                                                                 numeric variable (0,1)
library("qbm")
### Turn intention to smoke to 0, 1 variable:
d <- dat smoking
d$intention to smoke <- as.numeric(dat smoking$intention to smoke)-1
### Fit gradient boosting ensemble:
boost_smk <- gbm(intention_to_smoke ~., data=d,</pre>
                                                                Specify type of y (will be guessed if not supplied)
                 distribution = 'bernoulli', ◀
                 n.trees = 1000.
                                                           ——— How many trees
                                           Learning rate
                 shrinkage = 0.1, ◀
                 interaction.depth = 3, ___

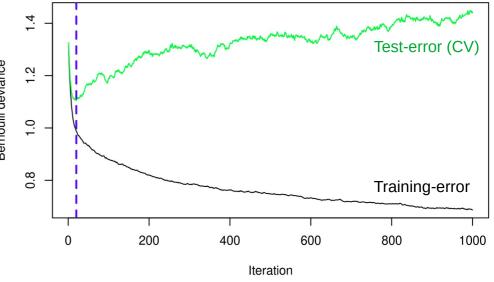
Maximal depth of trees

                 cv.folds = 10)
                                                   Run 10-fold crossvalidation for each iteration
### Find best number of iterations, i.e. trees:
gbm.perf(boost_smk, method = 'cv')
[1] 22
### Make predictions (probabilites):
                                                 Bernoulli deviance
predict(boost_smk, newdata=d[1:3,],
      type = 'response', n.trees = 22)
[1] 0.4046658 0.7258298 0.1103924
```

Alternative R-package:

xqboost ("extreme" gradient boosting)

- → Specific implementation of gradient boosting
- → Theory similar to gradient boosting
- → Faster implementation





Further reading

➤ Strobl, C., Malley, J., & Tutz, G. (2009). **An introduction to recursive partitioning:** Rationale, application, and characteristics of classification and regression trees, bagging, and Random Forests. Psychological Methods, 14(4), 323–348. https://doi.org/10.1037/a0016973