# Exercise: K-Means Clustering

Machine Learning and Prediction Modelling

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## Exercise 1: Wine quality data

The wine quality data set summarizes various properties of different wines. The variables include amongst others the amount of alcohol, the ph-value, the density, the residual sugar and a quality-score (ranging from 0-10). There are two data sets, one for red wines and one for white wines.

a) Load the two data sets contained in the wine\_data.rda file using the load command. Inspect the two data sets to get a first impression of the data. You can also draw pairs plots for the two data sets to get a visual impression.

```
load('wine data.rda')
head(wine_red, 3)
                   # Only showing 3 rows to save space
##
     fixed.acidity volatile.acidity citric.acid residual.sugar chlorides
## 1
               7.4
                                 0.70
                                                               1.9
                                             0.00
                                                                       0.076
## 2
               7.8
                                 0.88
                                             0.00
                                                                       0.098
                                                               2.6
## 3
               7.8
                                 0.76
                                             0.04
                                                               2.3
                                                                       0.092
##
     free.sulfur.dioxide total.sulfur.dioxide density
                                                           pH sulphates alcohol
## 1
                                                  0.9978 3.51
                                                                    0.56
                                                                              9.4
## 2
                       25
                                             67
                                                  0.9968 3.20
                                                                    0.68
                                                                              9.8
## 3
                       15
                                                  0.9970 3.26
                                                                    0.65
                                                                              9.8
##
     quality
## 1
           5
## 2
           5
           5
## 3
head(wine white, 3)
##
     fixed.acidity volatile.acidity citric.acid residual.sugar chlorides
## 1
                7.0
                                 0.27
                                              0.36
                                                              20.7
                                                                       0.045
## 2
                6.3
                                 0.30
                                              0.34
                                                               1.6
                                                                       0.049
               8.1
                                 0.28
                                             0.40
                                                               6.9
                                                                       0.050
##
     free.sulfur.dioxide total.sulfur.dioxide density
                                                           pH sulphates alcohol
## 1
                       45
                                            170
                                                1.0010 3.00
                                                                    0.45
                                                                              8.8
## 2
                       14
                                            132
                                                  0.9940 3.30
                                                                    0.49
                                                                              9.5
## 3
                       30
                                                 0.9951 3.26
                                                                    0.44
                                                                             10.1
     quality
##
## 1
           6
## 2
           6
## 3
           6
str(wine_red)
```

```
'data.frame':
                    1599 obs. of 12 variables:
##
    $ fixed.acidity
                                 7.4 7.8 7.8 11.2 7.4 7.4 7.9 7.3 7.8 7.5 ...
                          : num
    $ volatile.acidity
                          : num
                                  0.7 0.88 0.76 0.28 0.7 0.66 0.6 0.65 0.58 0.5 ...
                                 0 0 0.04 0.56 0 0 0.06 0 0.02 0.36 ...
##
    $ citric.acid
                          : num
##
    $ residual.sugar
                           : num
                                  1.9 2.6 2.3 1.9 1.9 1.8 1.6 1.2 2 6.1 ...
##
    $ chlorides
                                  0.076 0.098 0.092 0.075 0.076 0.075 0.069 0.065 0.073 0.071 ...
                           : num
                                  11 25 15 17 11 13 15 15 9 17 ...
    $ free.sulfur.dioxide : num
                                 34 67 54 60 34 40 59 21 18 102 ...
##
    $ total.sulfur.dioxide: num
##
    $ density
                          : num
                                 0.998 0.997 0.997 0.998 0.998 ...
##
                                 3.51 3.2 3.26 3.16 3.51 3.51 3.3 3.39 3.36 3.35 ...
    $ pH
                           : num
##
    $ sulphates
                                 0.56 0.68 0.65 0.58 0.56 0.56 0.46 0.47 0.57 0.8 ...
                          : num
##
    $ alcohol
                                  9.4 9.8 9.8 9.8 9.4 9.4 9.4 10 9.5 10.5 ...
                            num
                                  5 5 5 6 5 5 5 7 7 5 ...
    $ quality
                           : int
str(wine_white)
##
   'data.frame':
                    4898 obs. of 12 variables:
##
    $ fixed.acidity
                          : num
                                 7 6.3 8.1 7.2 7.2 8.1 6.2 7 6.3 8.1 ...
##
    $ volatile.acidity
                                  0.27 0.3 0.28 0.23 0.23 0.28 0.32 0.27 0.3 0.22 ...
                           : num
##
                                  0.36 0.34 0.4 0.32 0.32 0.4 0.16 0.36 0.34 0.43 ...
    $ citric.acid
                           : num
##
    $ residual.sugar
                                  20.7 1.6 6.9 8.5 8.5 6.9 7 20.7 1.6 1.5 ...
                           : num
                                  0.045\ 0.049\ 0.05\ 0.058\ 0.058\ 0.05\ 0.045\ 0.045\ 0.049\ 0.049\ \dots
    $ chlorides
##
                           : num
##
    $ free.sulfur.dioxide : num
                                  45 14 30 47 47 30 30 45 14 28 ...
    $ total.sulfur.dioxide: num
                                  170 132 97 186 186 97 136 170 132 129 ...
                                  1.001 0.994 0.995 0.996 0.996 ...
    $ density
                           : num
                                  3 3.3 3.26 3.19 3.19 3.26 3.18 3 3.3 3.22 ...
##
    $ pH
                            num
    $ sulphates
                                 0.45 0.49 0.44 0.4 0.4 0.44 0.47 0.45 0.49 0.45 ...
##
                          : num
    $ alcohol
                                 8.8 9.5 10.1 9.9 9.9 10.1 9.6 8.8 9.5 11 ...
##
                           : num
    $ quality
                           : int
                                 6666666666...
```

The two data sets for white and red wines have the same variables. All variables are numeric variables. There are fewer observations for red (1599) than white wines (4898). The pairs plots of the two data sets (not shown) reveals that there are some extreme points in some of the variables. For further analyses one could think about removing these potential outliers, but here we will leave them as they are.

b) We want to add a colour column to both data sets. For the white wine data, this column should only have the value "white" and for the red wine data "red". (Hint: wine\_red\$colour <- ...)

```
wine_red$colour <- 'red'</pre>
wine_white$colour <- 'white'</pre>
head(wine_white, 3)
     fixed.acidity volatile.acidity citric.acid residual.sugar chlorides
## 1
                7.0
                                 0.27
                                              0.36
                                                               20.7
                                                                         0.045
## 2
                6.3
                                 0.30
                                              0.34
                                                                1.6
                                                                         0.049
## 3
                8.1
                                 0.28
                                              0.40
                                                                6.9
                                                                         0.050
                                                             pH sulphates alcohol
##
     free.sulfur.dioxide total.sulfur.dioxide density
## 1
                                                  1.0010 3.00
                                                                     0.45
                                                                               8.8
                        45
                                             170
## 2
                        14
                                                  0.9940 3.30
                                                                     0.49
                                                                               9.5
## 3
                        30
                                              97 0.9951 3.26
                                                                     0.44
                                                                              10.1
     quality colour
##
## 1
           6 white
           6
## 2
              white
## 3
           6
              white
```

c) Combine the two data sets into one big data set called wines using the rbind command. The rbind command can take multiple data frames as arguments and combines them rowwise. Check what the dimensions of the new data set are to make sure the combination worked.

```
wines <- rbind(wine_red, wine_white)
dim(wines)</pre>
```

```
## [1] 6497 13
```

We now have all the data combined in one data frame, which now has 1599 + 4898 = 6497 rows.

d) Turn the colour variable in the wines data frame into a factor.

```
wines$colour <- factor(wines$colour)</pre>
```

e) Although the colour variable will be of use later, for k-means clustering we can only use numerical variables. Create a copy of the data frame with the name wines\_nocol which does not include the colour column. (Hint wines\_nocol\$... <- NULL)

```
wines_nocol <- wines
wines_nocol$colour <- NULL</pre>
```

f) The wines\_nocol data frame only includes numeric variables. We want to scale this data before we apply any cluster algorithm to it. The reason is that the variables are on rather different scales, and we don't want variables with larger variance to dominate any measures of distance between points. To scale all columns of a data frame, we can use the scale function, which takes a data frame as an argument. Because the scale function automatically changes the data into a matrix, we will apply the data.frame function to the result again, so that we retain the data as a data frame. (Hint: data.frame( scale(...) ))

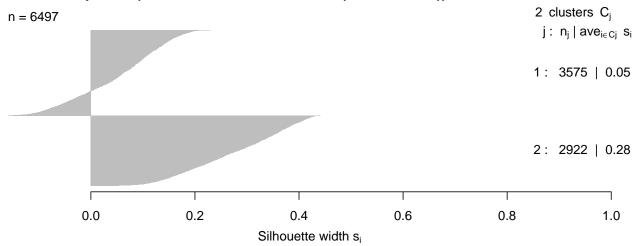
```
wines_nocol <- data.frame(scale(wines_nocol))</pre>
```

Now all variables have a variance of 1 and a mean of 0.

g) Apply k-means clustering to the scaled data looking for two clusters. Do not set the random seed before applying the kmeans function. To get an idea of how good the found cluster pattern is, create a silhouette plot of the found solution. Interpret the result. Now run the used code a couple of times again. Do the results always turn out the same way? Why not?

```
km_2 <- kmeans(wines_nocol, centers = 2)
library(cluster)
plot(silhouette(x = km_2$cluster, dist = dist(wines_nocol)), border=NA)</pre>
```

## Silhouette plot of (x = km\_2\$cluster, dist = dist(wines\_nocol))



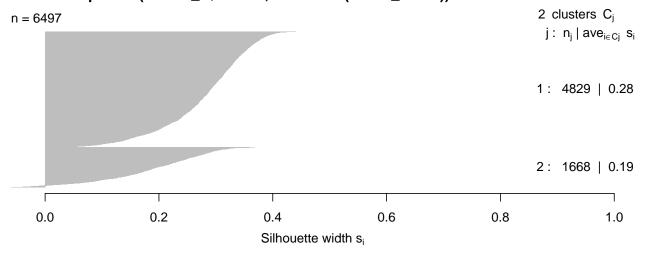
#### Average silhouette width: 0.15

We get different solutions because k-means clustering can depend on the randomly selected starting values (only one solution shown here). The solutions we get do not achieve very good silhouette scores.

h) We can force the kmeans function to try out multiple random starting positions and choose among the achieved solutions the best one. This can be done with the nstart option. Apply again k-means clustering to the scaled data looking for two clusters, but trying out 10 random starting positions (Hint: kmeans(..., nstart=10)). Draw again a silhouette plot to inspect the solution.

```
set.seed(4890)
km_2 <- kmeans(wines_nocol, centers = 2, nstart = 10)
plot(silhouette(x = km_2$cluster, dist = dist(wines_nocol)), border=NA)</pre>
```

## Silhouette plot of $(x = km \ 2\ cluster, dist = dist(wines \ nocol))$

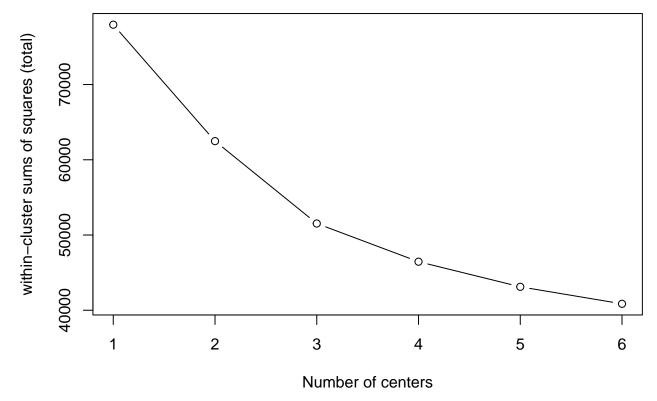


### Average silhouette width: 0.26

Although the solution is better than the previously shown one, according to the usual rules of thumb the silhouette plot still shows rather bad average cluster scores. However, as we will see later, for our data this is actually not such a bad solution as one might think based on the silhouette plot alone.

i) To investigate whether a different number of clusters fits our data better, we want to calculate the within-cluster SSQ for different values of k. Visualize the resulting SSQ when using the values 1 to 6 for k. Use again multiple random starting positions when applying kmeans. Interpret the resulting figure.

```
wss <- rep(NA, 6)  # Initialize
set.seed(2145)
for(i in 1:6){ # Check for up to 6 clusters
  wss[i] <- kmeans(wines_nocol, centers = i, nstart = 10)$tot.withinss
}
plot(1:6, wss, type = 'b', xlab = 'Number of centers',
ylab = 'within-cluster sums of squares (total)')</pre>
```

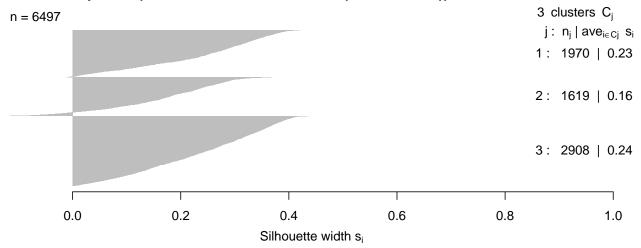


The figure doesn't show a very clear bend in the line. There might to be a bit of an 'elbow' at the value k=3.

j) Based on the previous exercise, apply k-means clustering to the data looking for three clusters and create the associated silhouette plot.

```
set.seed(8893)
km_3 <- kmeans(wines_nocol, centers = 3, nstart = 10)
plot(silhouette(x = km_3$cluster, dist = dist(wines_nocol)), border=NA)</pre>
```

# Silhouette plot of (x = km\_3\$cluster, dist = dist(wines\_nocol))

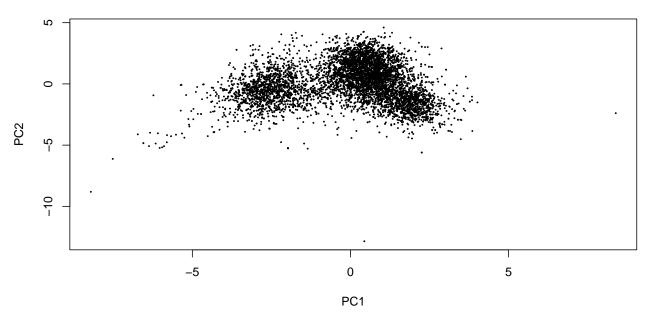


Average silhouette width: 0.22

Again, the silhouette scores are not that good.

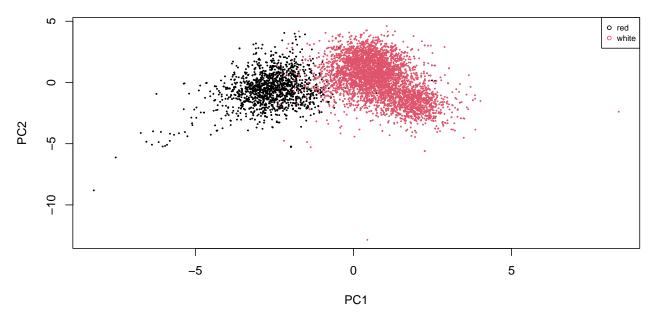
k) We would like to get a visual impression of the data to see what is going on. Perform a dimensionality reduction by applying a PCA to the data and plot the first two PCs (since we have scaled the data before, it doesn't make a difference if we apply the PCA with or without scaling).

```
pc_wine <- prcomp(wines_nocol)
plot(PC2~PC1, data=pc_wine$x, cex=0.2)</pre>
```



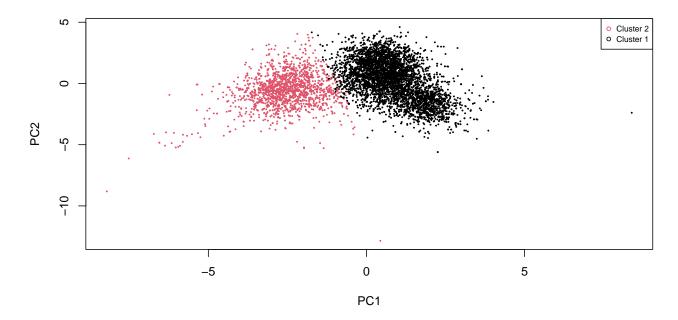
Using the two dimensional representation of the data, we can see that the observations lie pretty close toghether and, therefore, it is indeed difficult to find a clear cluster pattern. From the humen eye it looks like two or three clusters might describe the data best.

l) Create again the same plot but this time colour the points according to whether they represent a white or red wine. (Hint: wines\$colour).



Interestingly, the two clusters which we thought to identify by eye, more or less represent the colour of the wines.

m) Create the plot again but now colour the points according to the assigned cluster numbers of the two-cluster solution found with k-means in exercise h).



The cluster solution of kmeans also heavily overlaps with the wine colour. We can further see this when creating a confusion table of the wine colour and the assigned cluster numbers:

```
table(km_2$cluster, wines$colour)

##

##

red white
```

n) Visualize in the same way the three-cluster solution from exercise j).

##

##

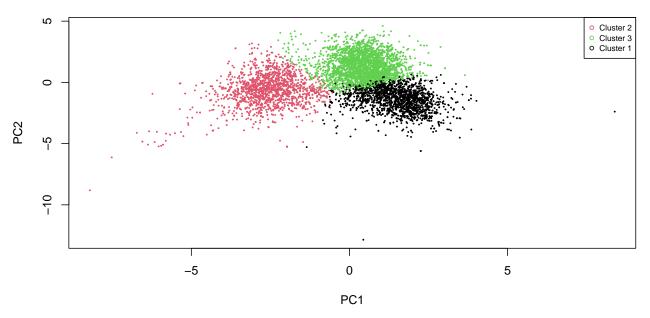
1

25

2 1574

4804

94



In this two-dimensional representation of the data, this solution seems perhaps a bit less appropriate compared to the solution with only two clusters.