

There Is No Largest Prime Number

With an introduction to a new proof technique

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27th International Symposium on Prime Numbers, –280

1 Results

Proof of the Main Theorem

There Is No Largest Prime Number

The proof uses *reductio ad absurdum*.

Theorem

There is no largest prime number.

Proof.

- ① Suppose p were the largest prime number.
- ② Let q be the product of the first p numbers.
- ③ Then $q + 1$ is not divisible by any of them.
- ④ Thus $q + 1$ is also prime and greater than p . □