

# There Is No Largest Prime Number

With an introduction to a new proof technique

Euklid of Alexandria

Department of Mathematics  
University of Alexandria

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## 1 Results

- Proof of the Main Theorem

# There Is No Largest Prime Number

The proof uses *reductio ad absurdum*.

## Theorem

*There is no largest prime number.*

## Proof.

- ① Suppose  $p$  were the largest prime number.
- ② Let  $q$  be the product of the first  $p$  numbers.
- ③ Then  $q + 1$  is not divisible by any of them.
- ④ Thus  $q + 1$  is also prime and greater than  $p$ . □