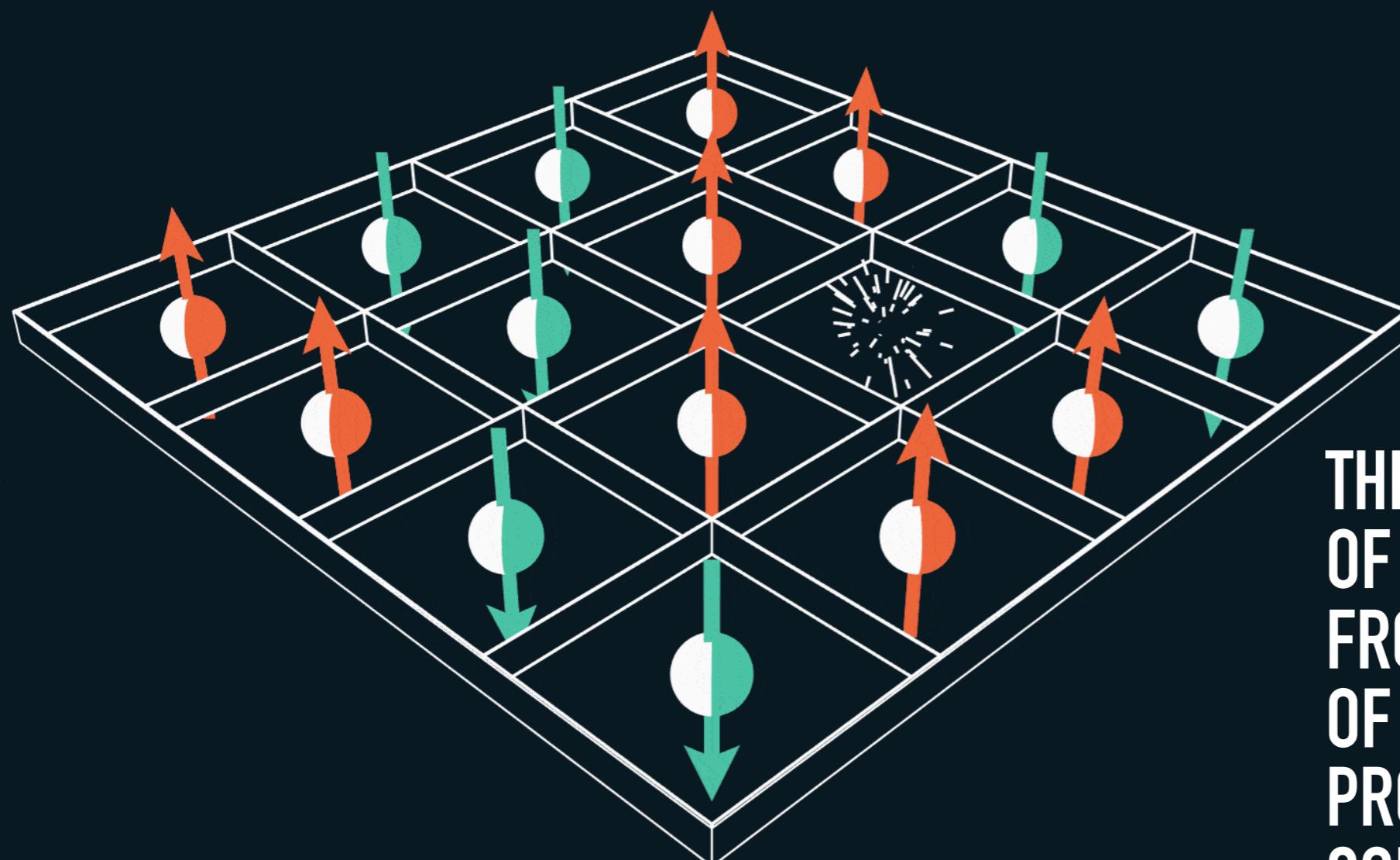


NICOLÁS VERGARA - NANOMAGNETISM  
LABORATORY

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MONTECARLO SIMULATION OF MAGNETIC  
NANOSTRUCTURES .

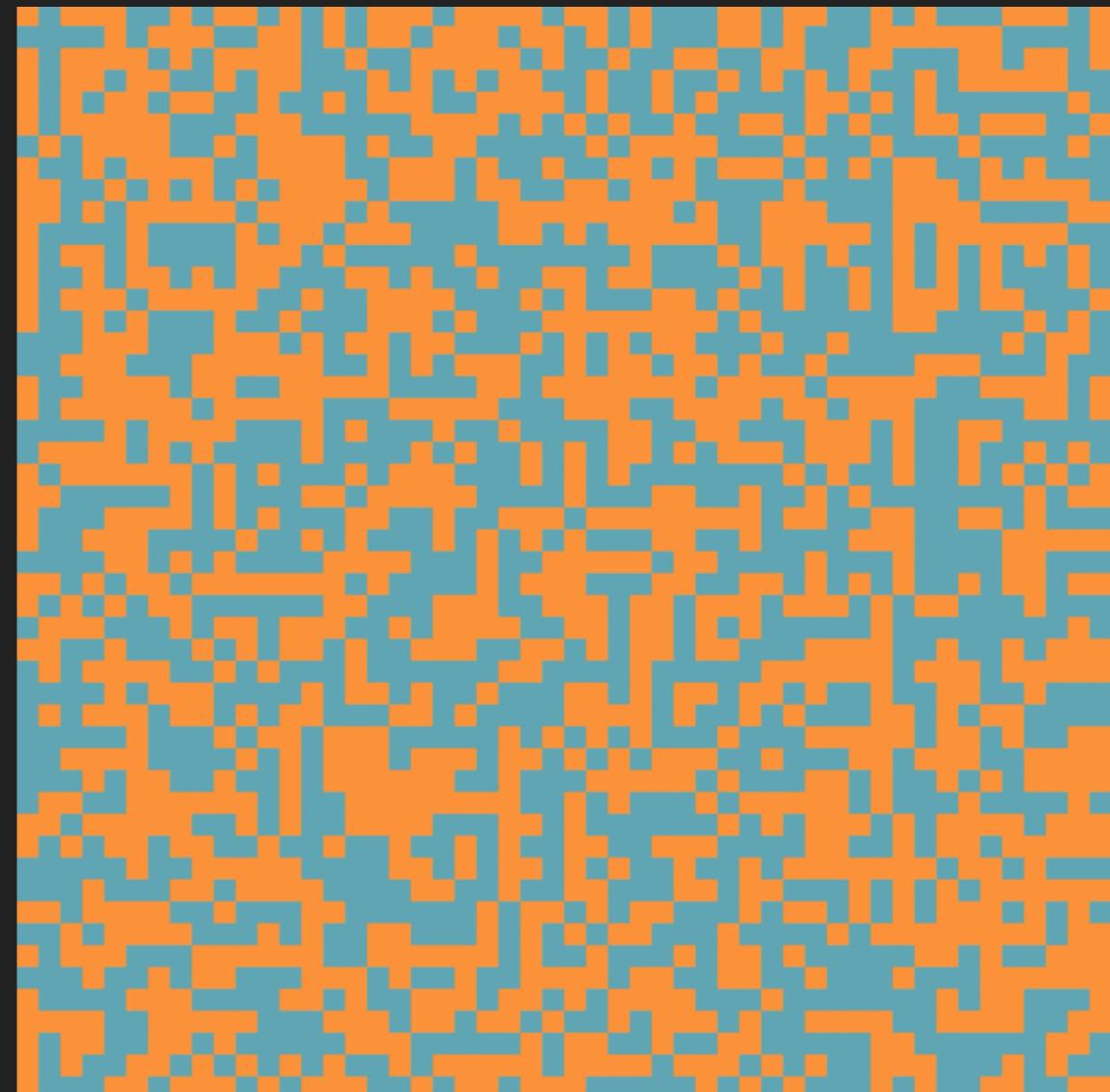
# MAGNETS



THE MAGNETIC PROPERTIES OF THE MATERIALS ARISES FROM ELECTRONS. THE SUM OF THE ELECTRONS PROPERTIES DESCRIBES COMPLETELY THE MAGNET

WE SIMULATE A  
MAGNET AS AN  
ARRAY OF SPINS.  
EVERY TIME WE  
INITIALIZE IT WE  
MUST ASSURE A  
RANDOM STATE

ORANGE IS SPIN UP AND BLUE IS SPIN DOWN



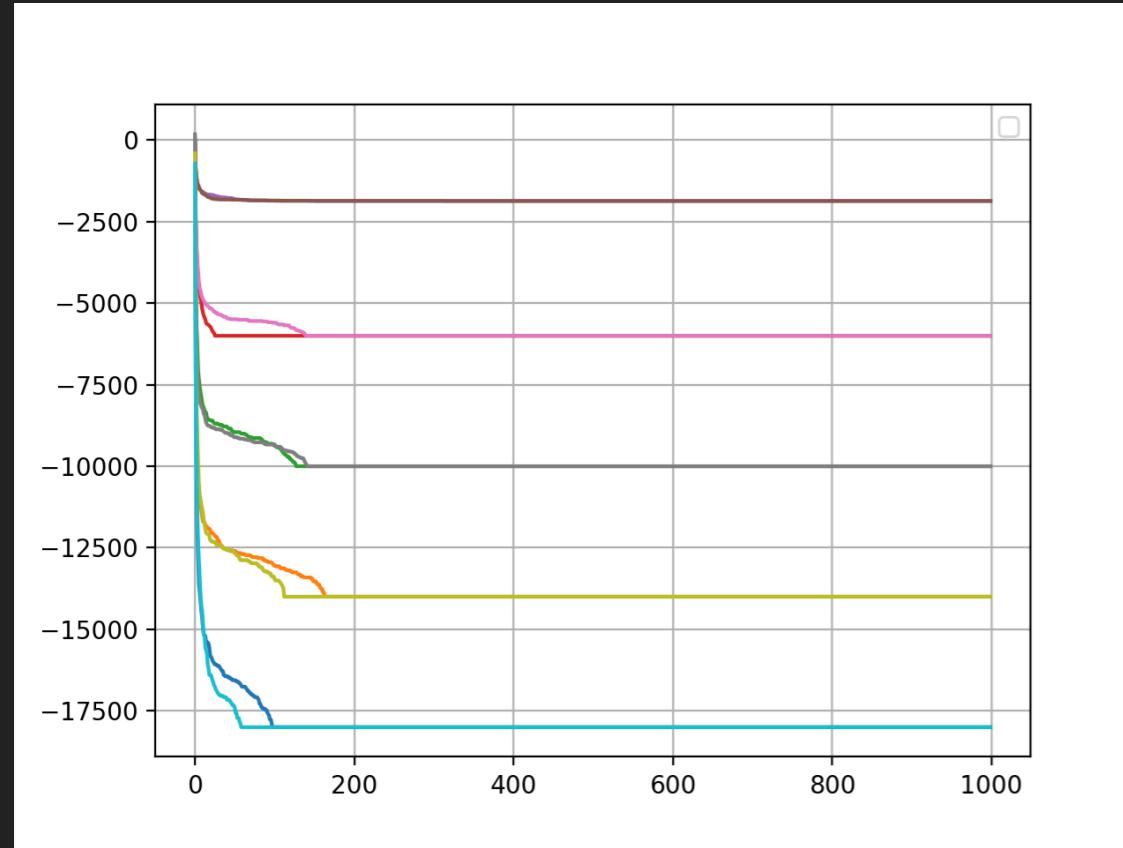
# 2D MODEL

```
SYSTEM = HBAR*2 * (0.5 - NP.RANDOM.RANDINT(0, 2,SIZE=[L, L, L]))
```

**BUT WHAT ABOUT  
THE DYNAMICS ?**

# MINIMIZATION OF ENERGY

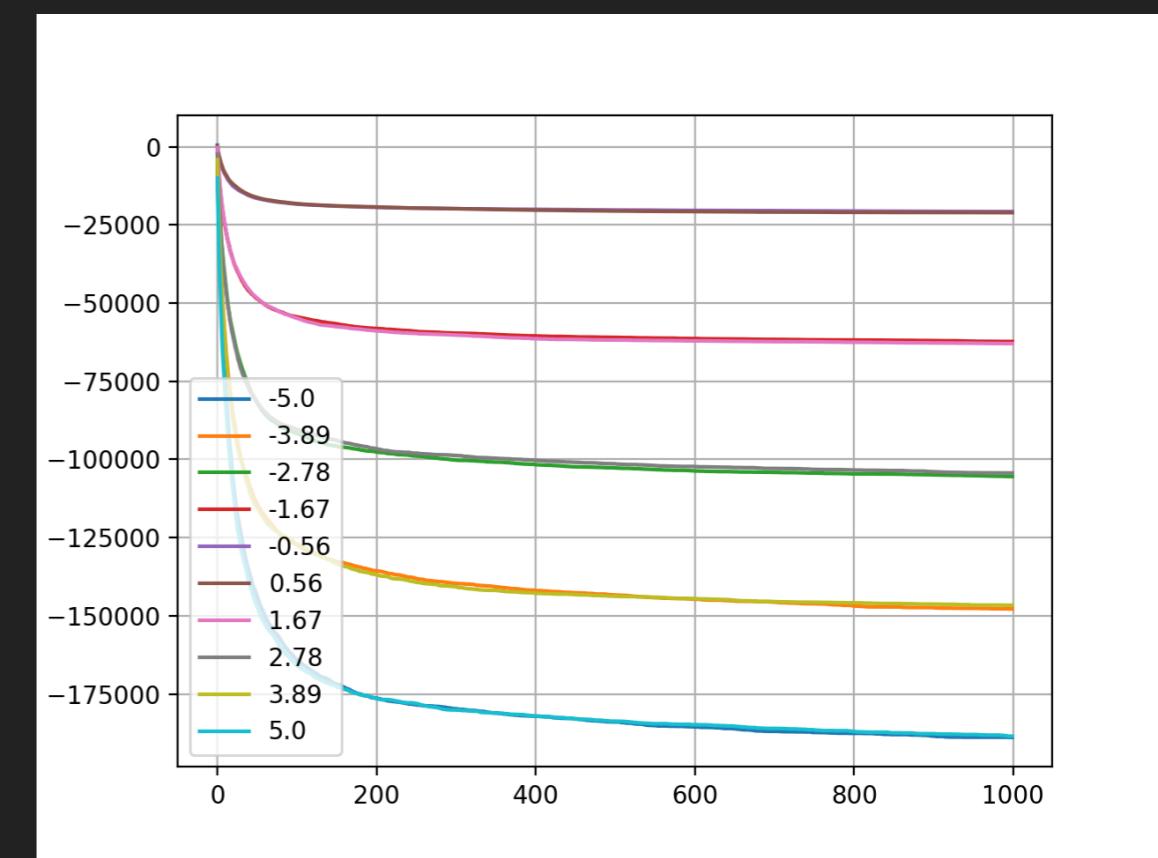
Energy



Iterations

 $M=30 \times 30$ 

Energy



Iterations

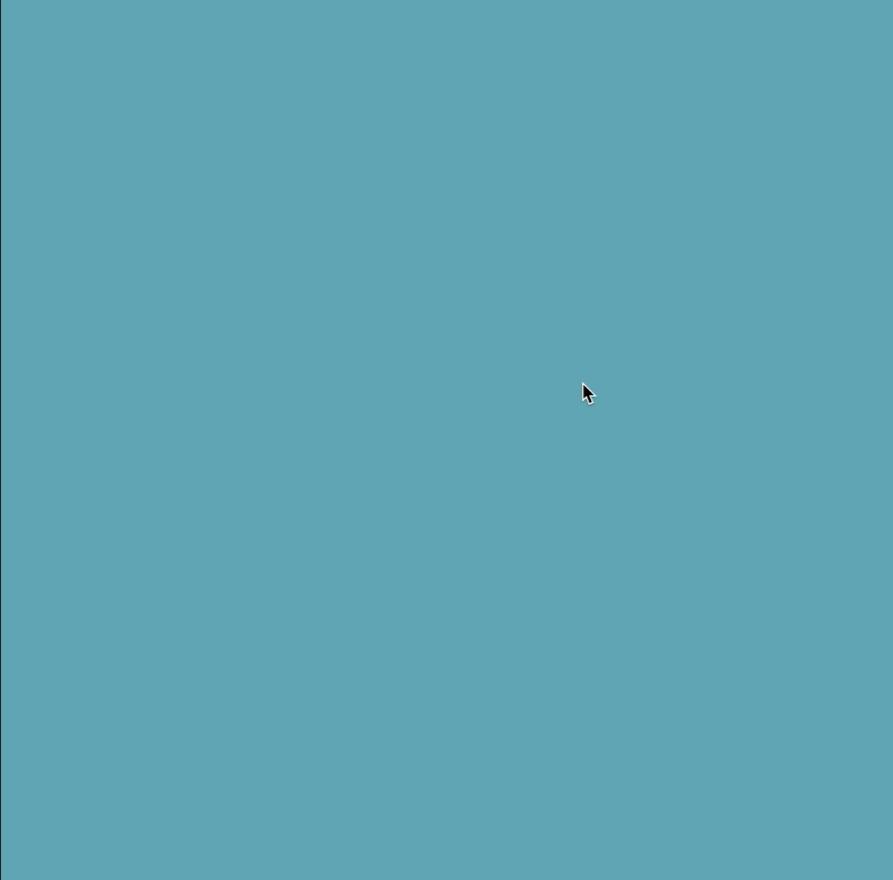
 $M=100 \times 100$

$$p_i = \frac{1}{Z} e^{-E_i/(K_B T)}$$

SO IF WE FIX THE ENERGY, ASSUMING IT'S ALREADY MINIMUM , WE CAN EXPECT THAT THE TEMPERATURE GIVE INFORMATION ABOUT THE MOST PROBABLE STATE OF THE SYSTEM

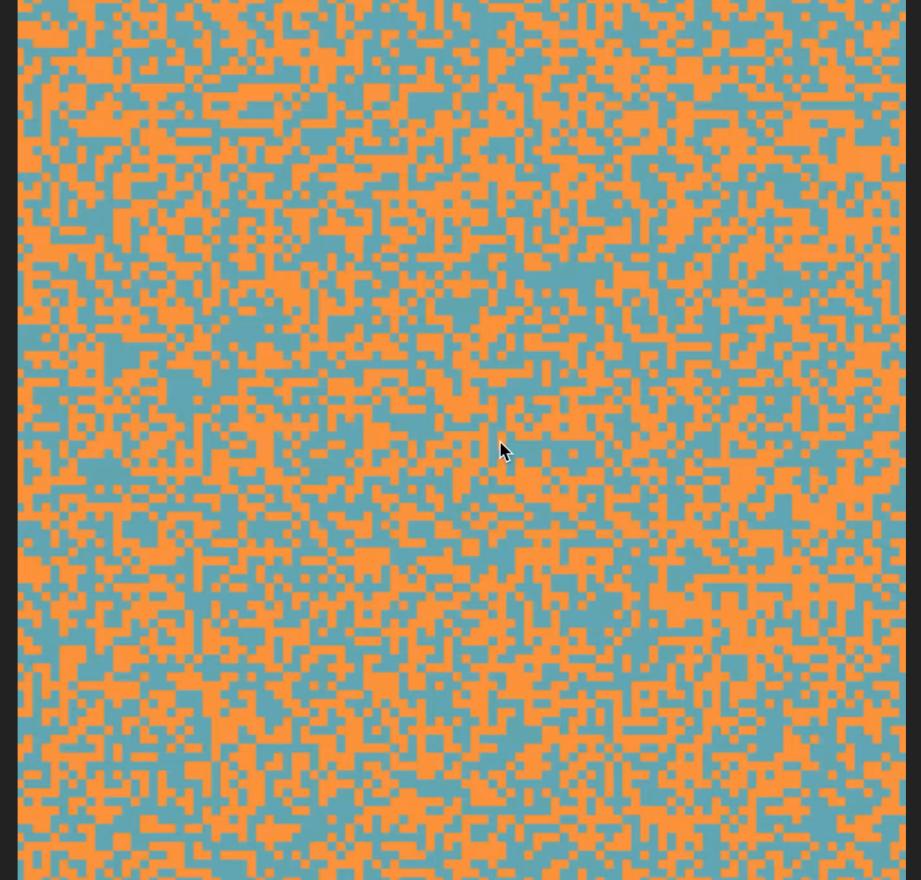
$$T \rightarrow 0 \Rightarrow p_i \approx 1$$

THERE IS ONE REALLY PROBABLE STATE



$$T \rightarrow \infty \Rightarrow p_i \approx 0$$

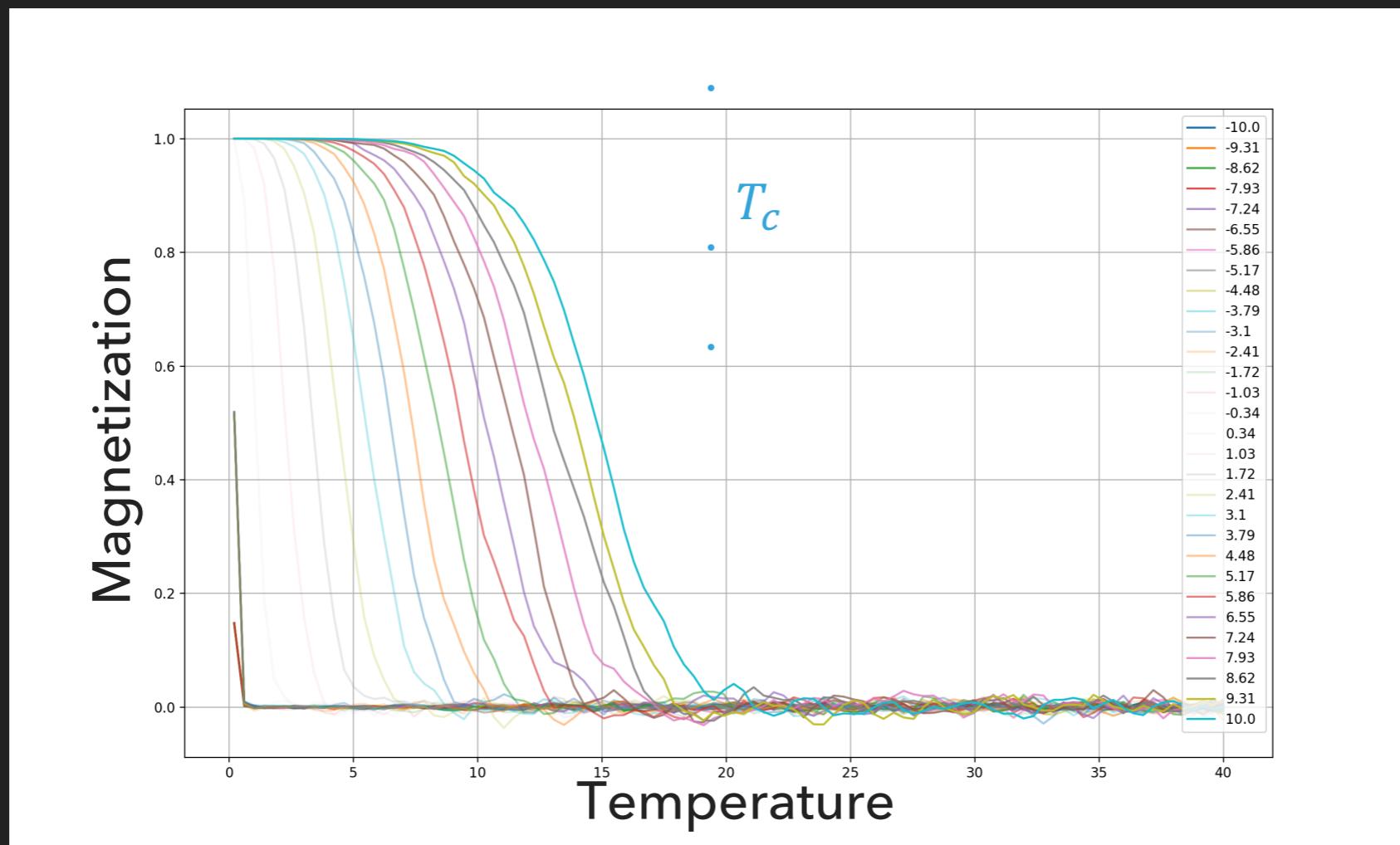
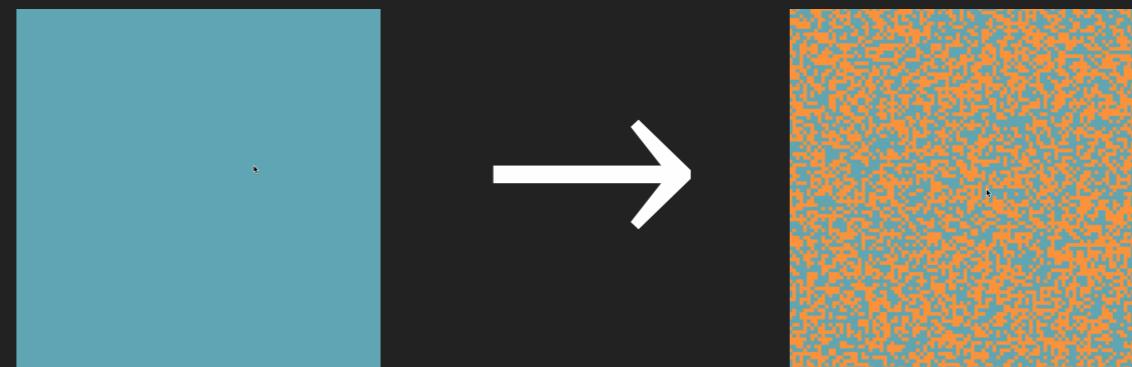
THERE ARE MANY PROBABLE MICRO-STATES



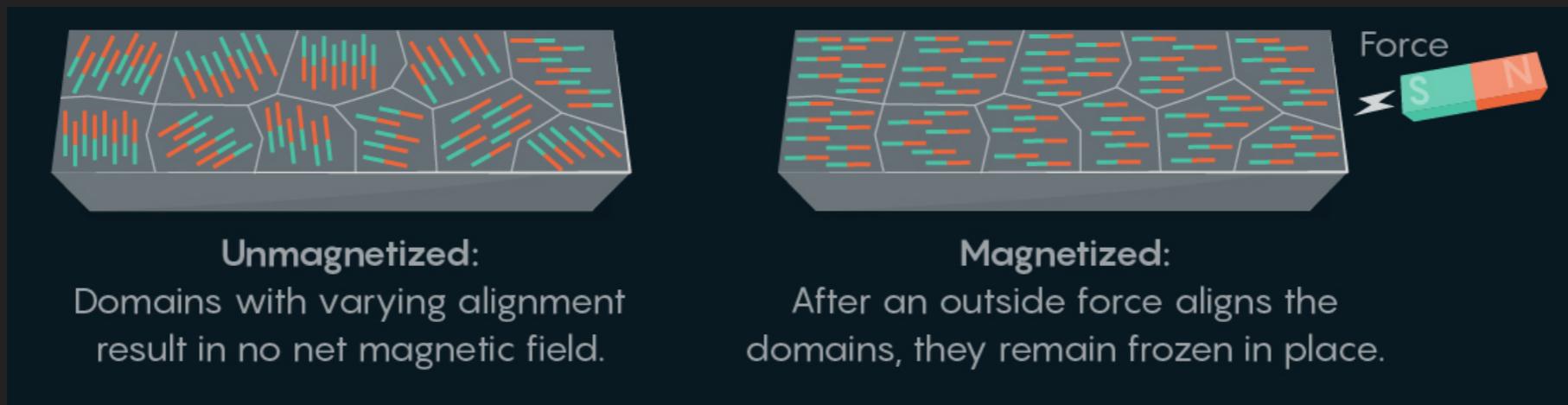
THE TEMPERATURE OF TRANSITION BETWEEN  
THIS TWO STATES, IT'S CALLED THE CURIE  
TEMPERATURE :  $T_c$



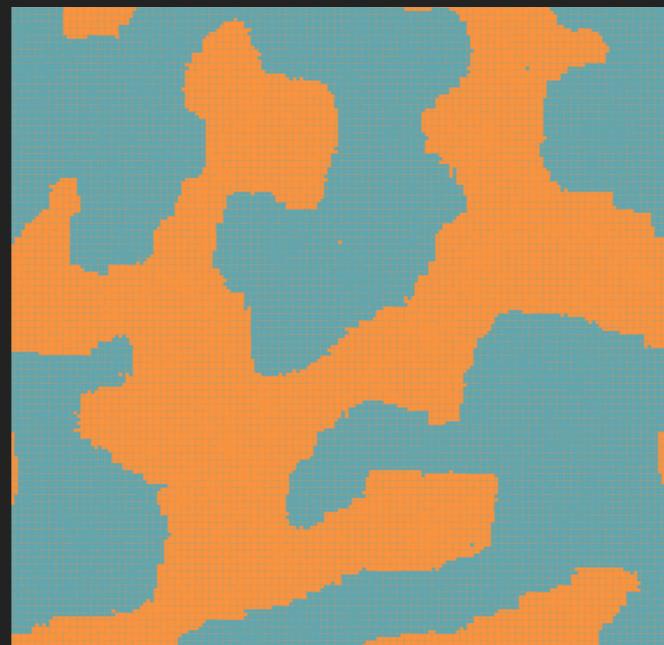
7



## Transition of state, for different simulated systems



THANKS TO THE SIMULATION WE PREDICT THE FORMATION OF DOMAINS FOR TEMPERATURES IN THE RANGE OF THE TRANSITION OF STATE  $0 < T < T_C$



Ernst Ising, Contribution to the Theory of Ferromagnetism. [http://www.hsaugsburg.de/~harsch/anglica/Chronology/20thC/Ising/isi\\_fm00.html](http://www.hsaugsburg.de/~harsch/anglica/Chronology/20thC/Ising/isi_fm00.html)

# WHAT IF THERE IS AN EXTERNAL MAGNETIC FIELD?

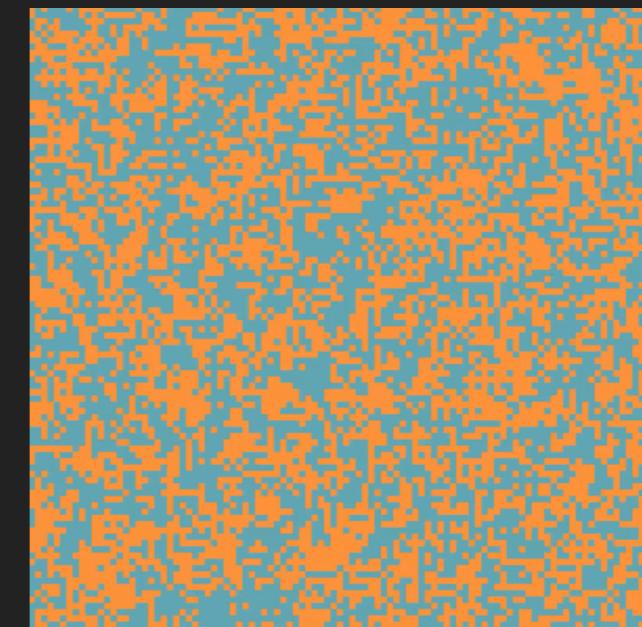
$$E_i \equiv \mathcal{H}_i = s_{iz} \sum_j J_{ij} s_{jz} \rightarrow \mathcal{H}_i = s_{iz} \sum_j J_{ij} s_{jz} + B s_{iz}$$

SPINS TENDS TO ALING TO THE FIELD

$T < T_c$

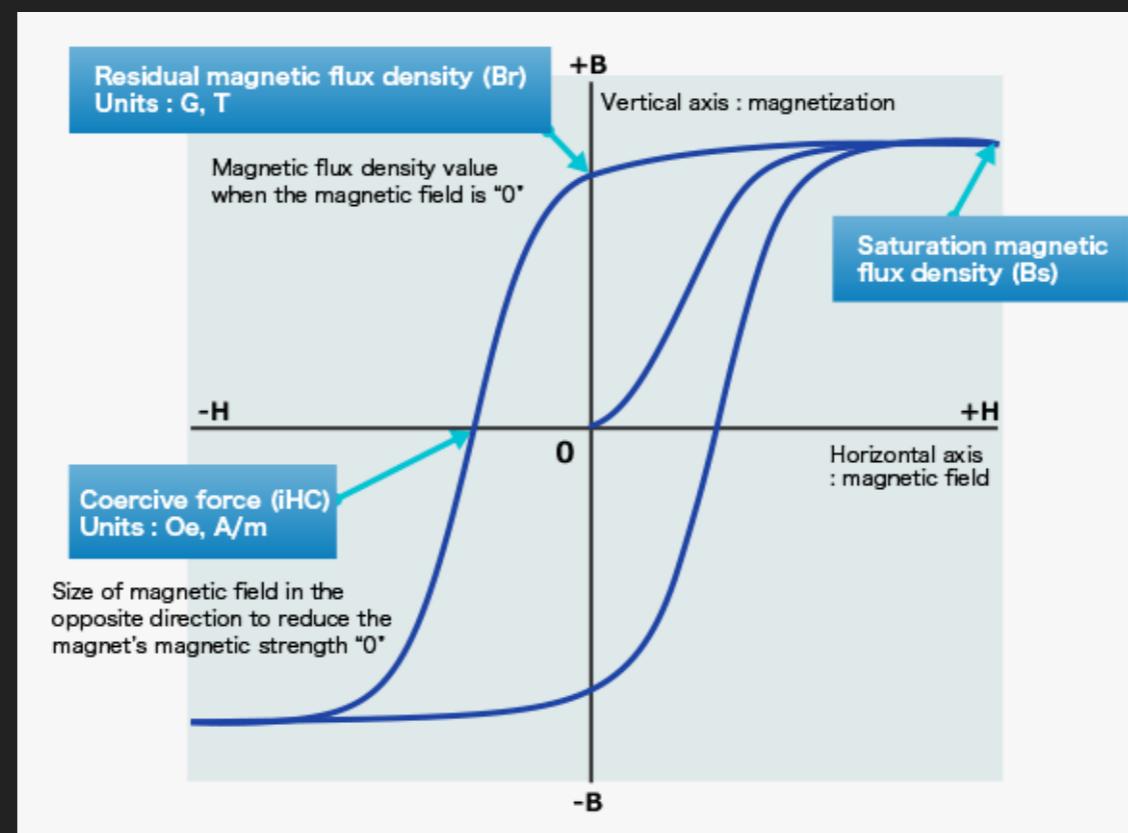


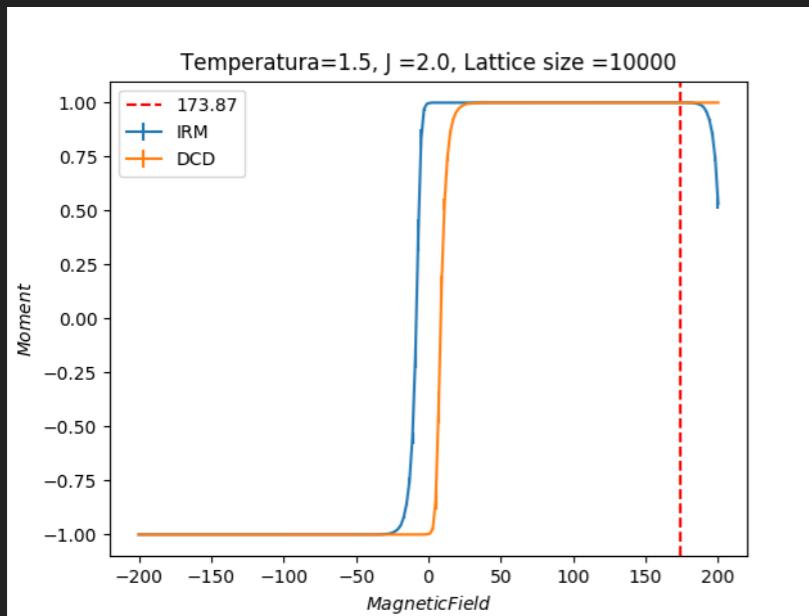
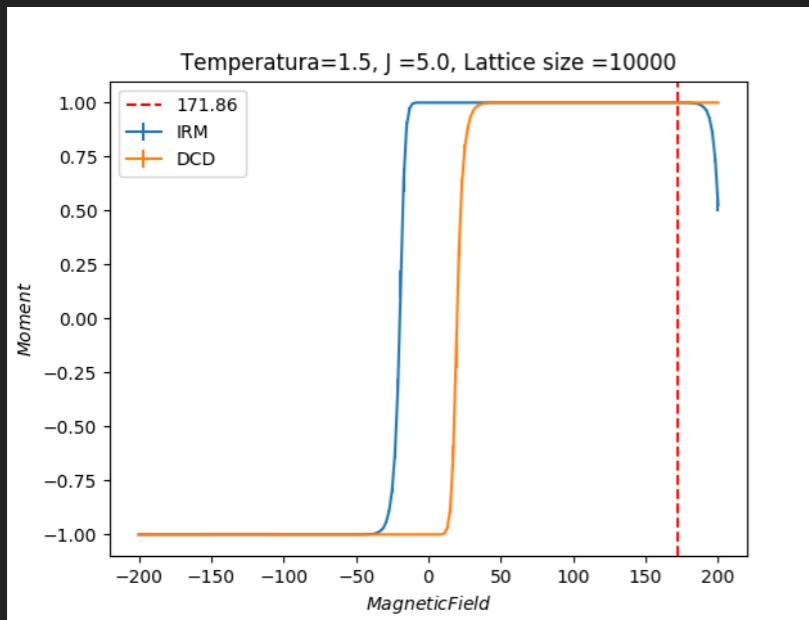
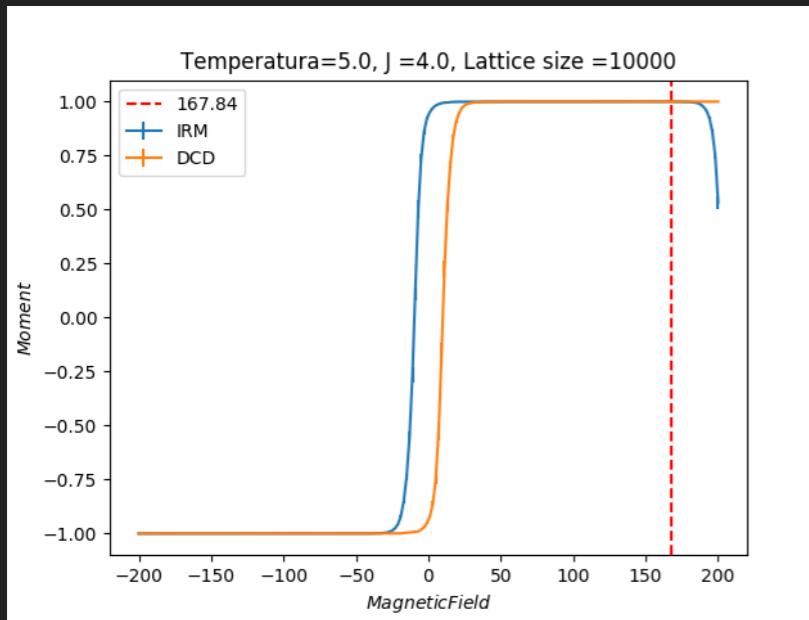
$T > T_c$



# WHAT HAPPEN IF WE VARY THE FIELD, FROM REALLY STRONG IN ONE DIRECTION, TO THE OTHER, AND MEASURE THE MAGNETIZATION?

IT BEHAVES AS THE MAGNET HAS MEMORY. BECAUSE ,WE OBTAIN AN HYSTERESIS LOOP, IN OTHER WORDS IT DOES NOT RETURN BACK AT THE SAME PATH.

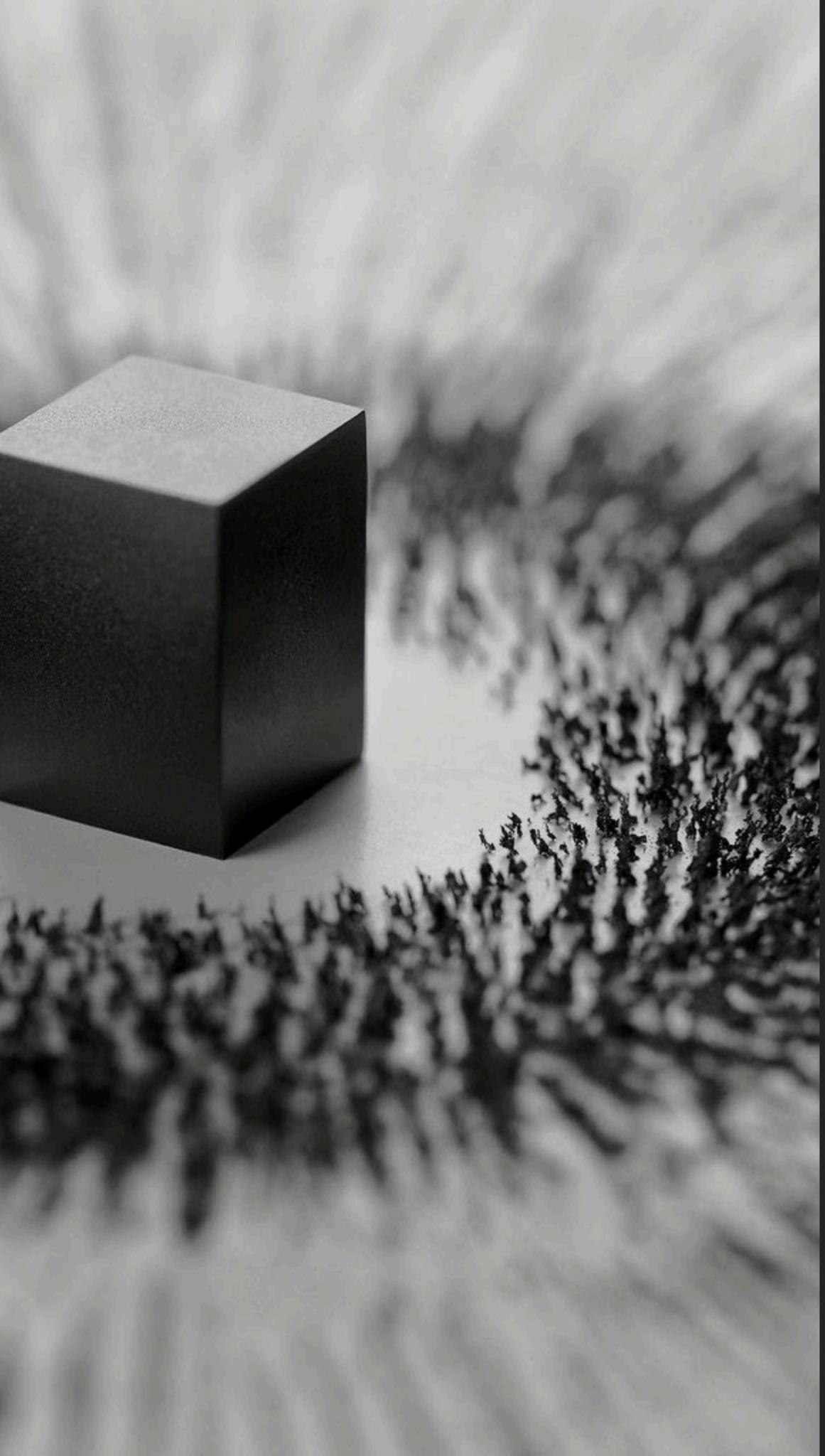




CAN WE REPRODUCE  
THIS BEHAVIOR WITH  
OUR SIMULATION?

---

YES, THE 2D ISING  
MODEL HAS MEMORY.

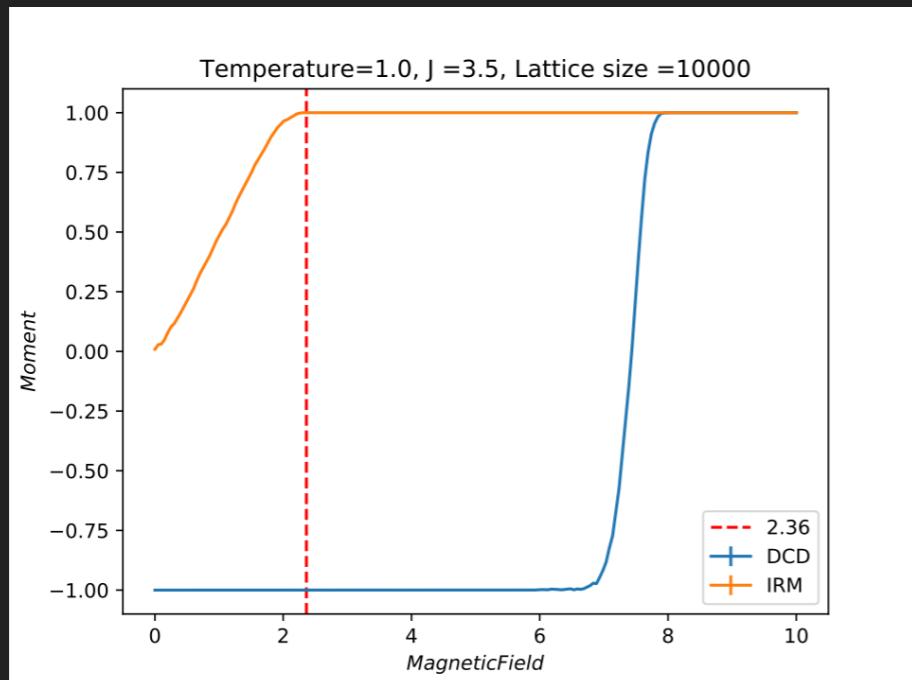


BUT WHAT OTHER  
MEASURES CAN WE  
REPRODUCE WITH THIS  
MODEL AND THE  
METROPOLIS  
ALGORITHM?

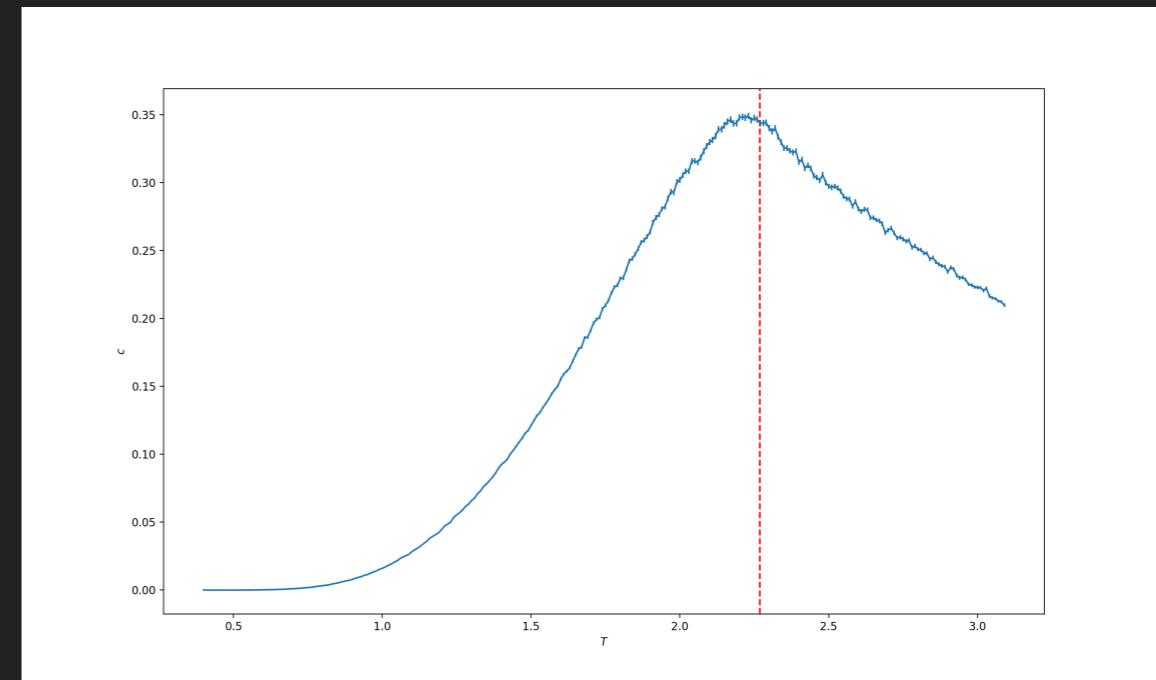
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ISOETHERMAL REMANENT  
MAGNETIZATION  
DIRECT CURRENT DEMAGNETIZATION  
HEAT CAPACITY  
SUSCEPTIBILITY  
ENERGY

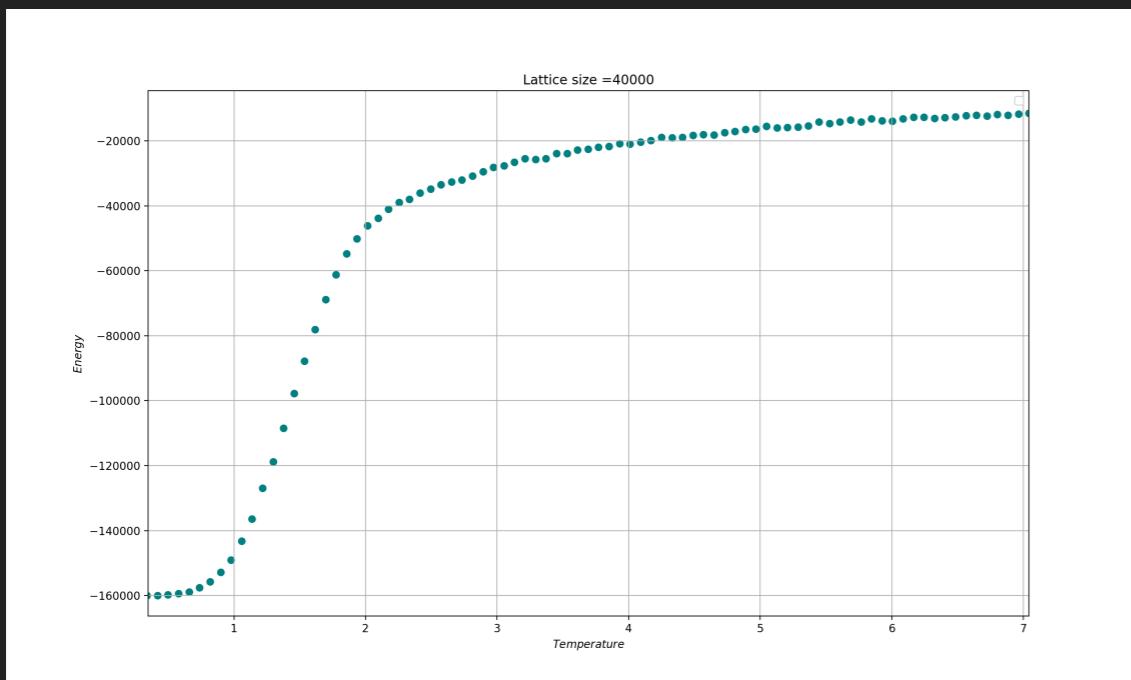
## IRM AND DCD



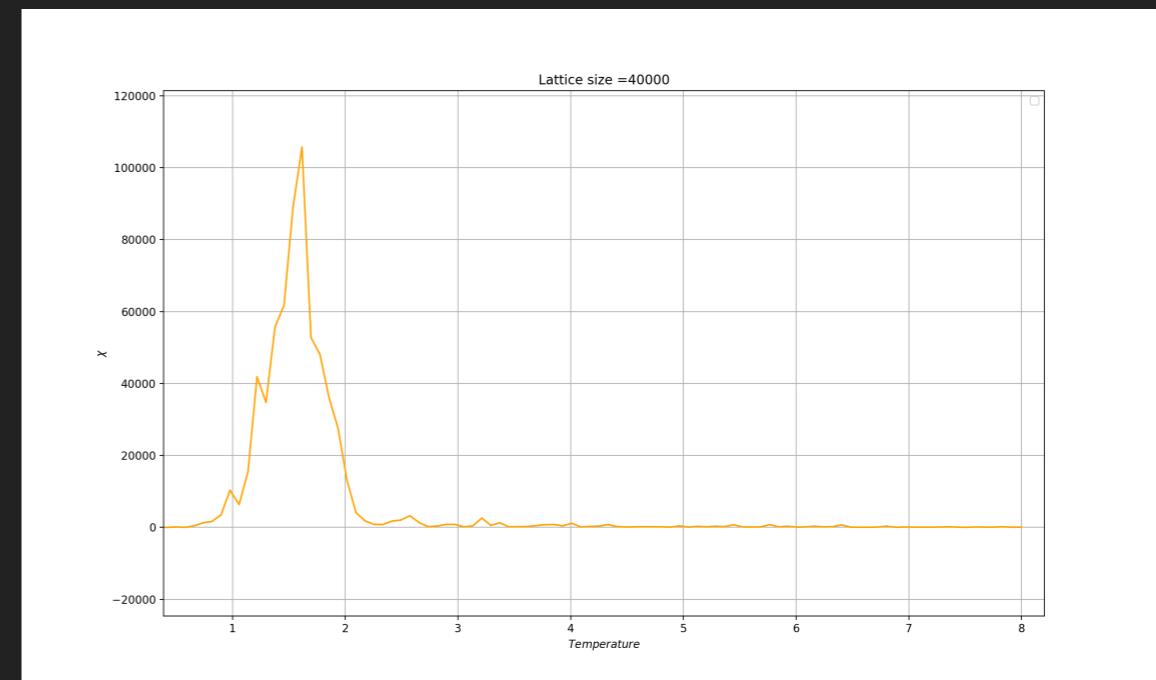
## HEAT CAPACITY AS FUNCTION OF T



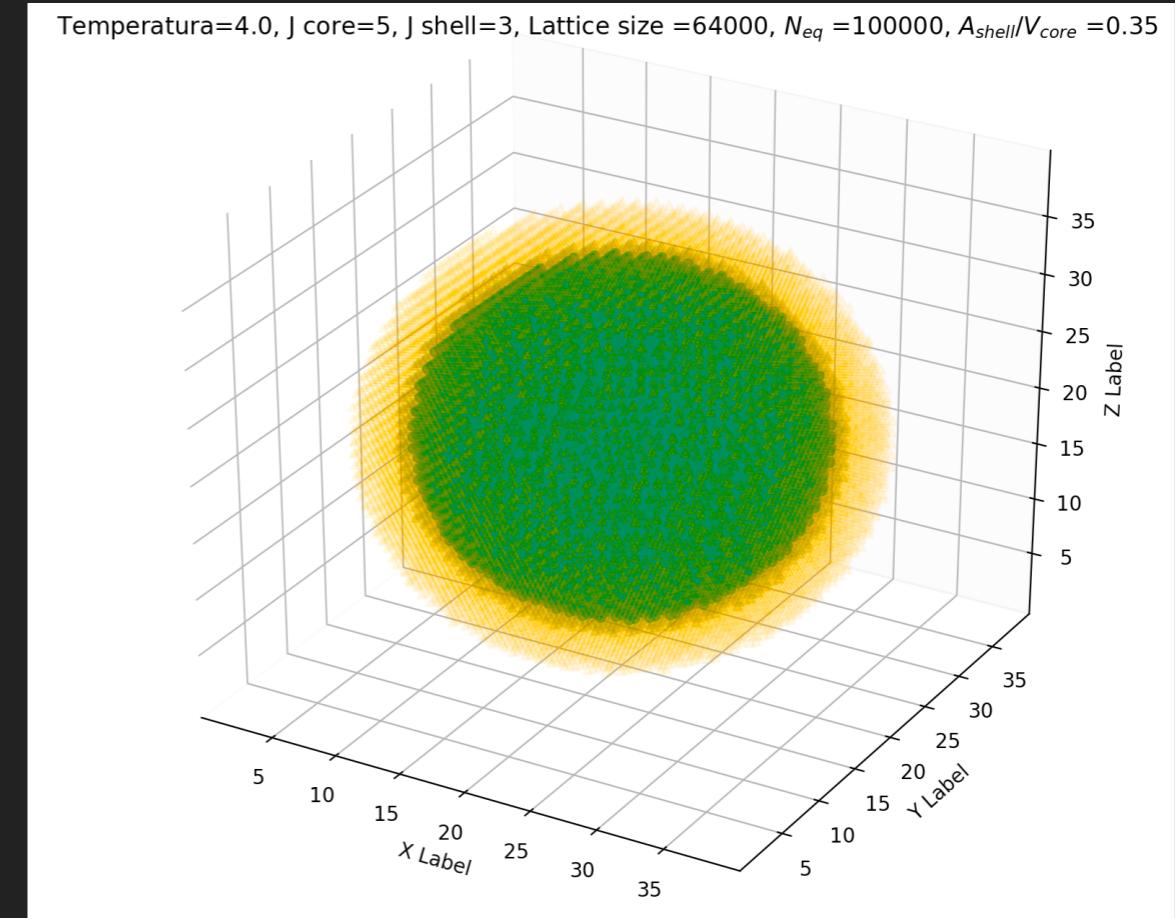
## ENERGY AS FUNCTION OF T



## SUSCEPTIBILITY AS FUNCTION OF T



WE SIMULATE A NANO-PARTICLE AS AN SPHERICAL ARRAY OF SPINS. WE ALSO COVER A CONFIGURATION CALLED CORE-SHELL

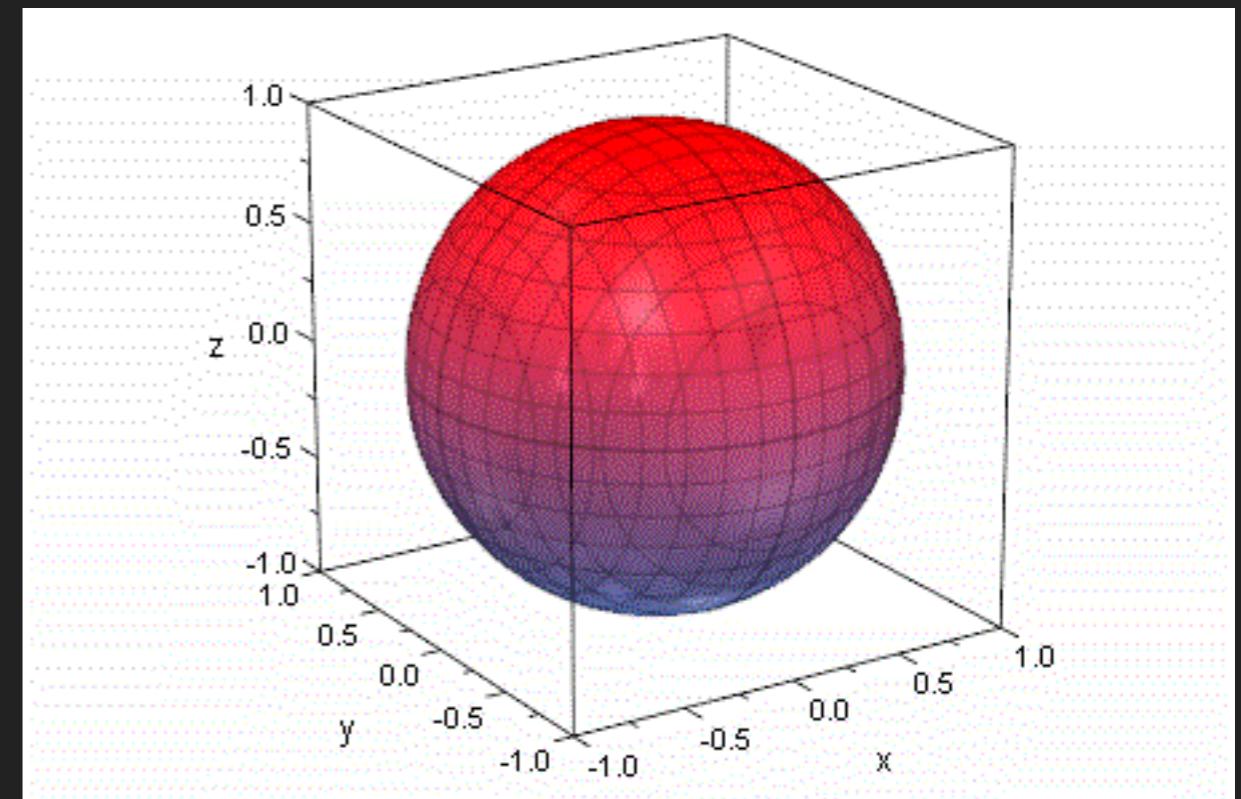
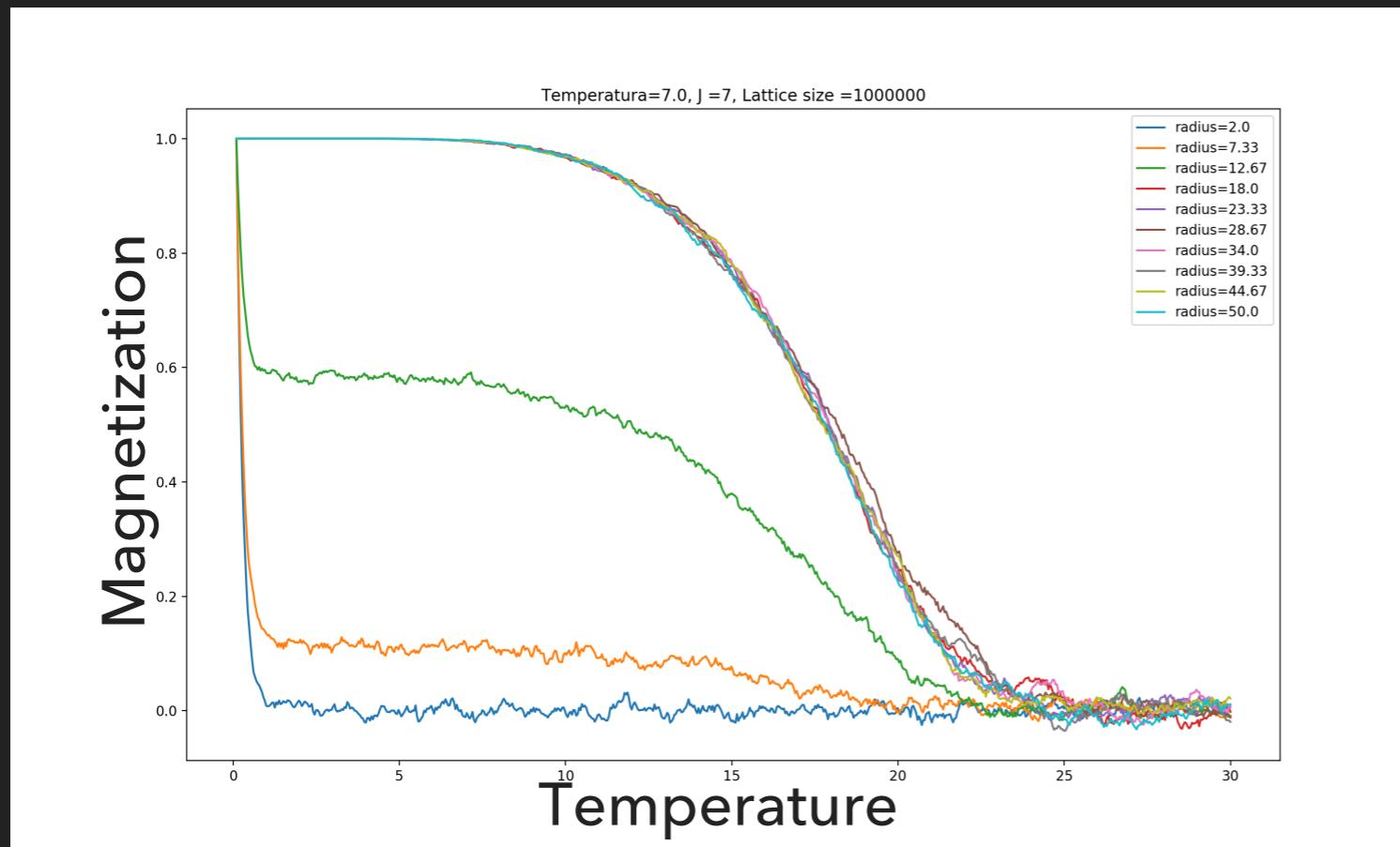


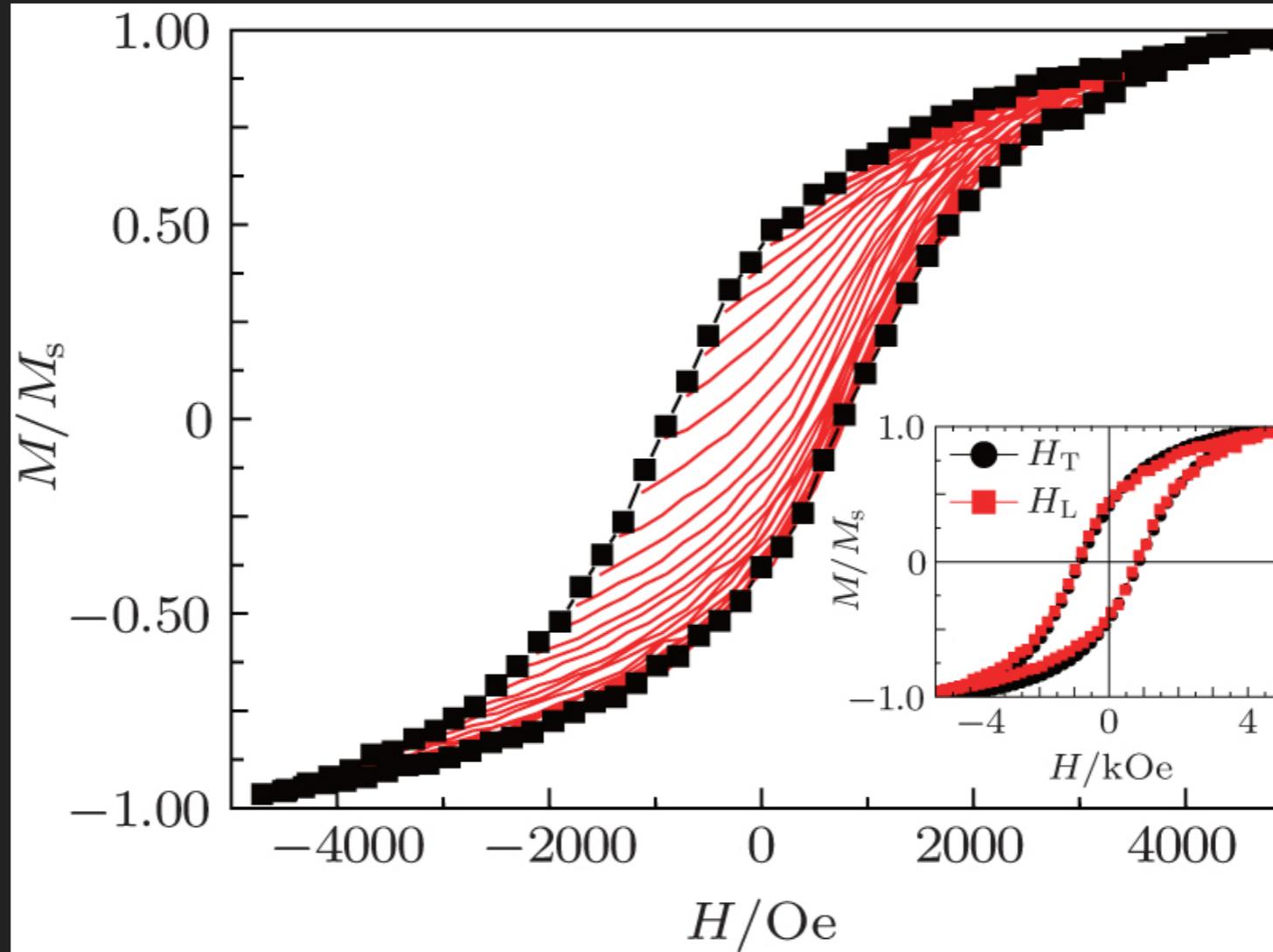
GREEN IS THE CORE, ORANGE THE INTERFACE, EVERY DOMAIN HAS A DIFFERENT COUPLING CONSTANT

# 3D MODEL.



**WHIT THIS NEW MODEL  
WE DISCOVER THAT:**

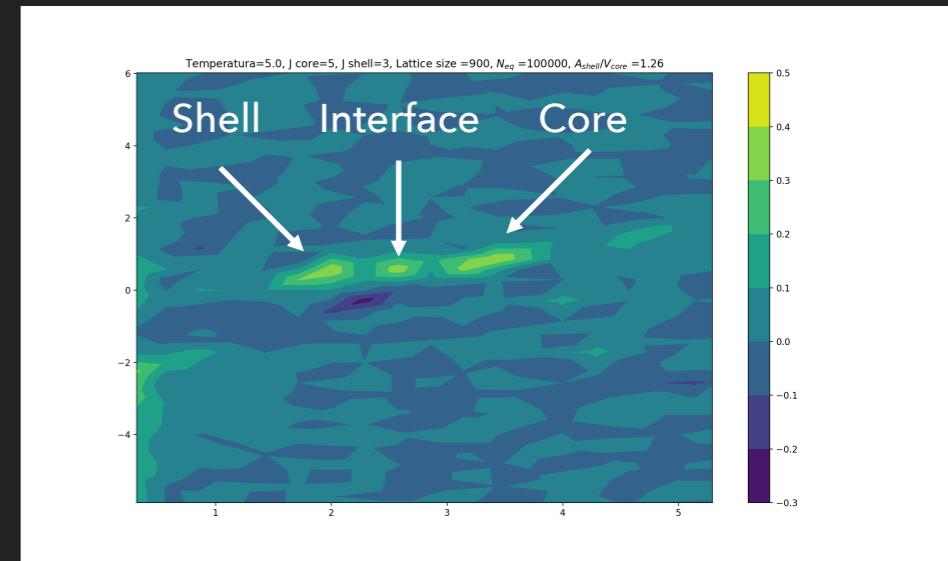
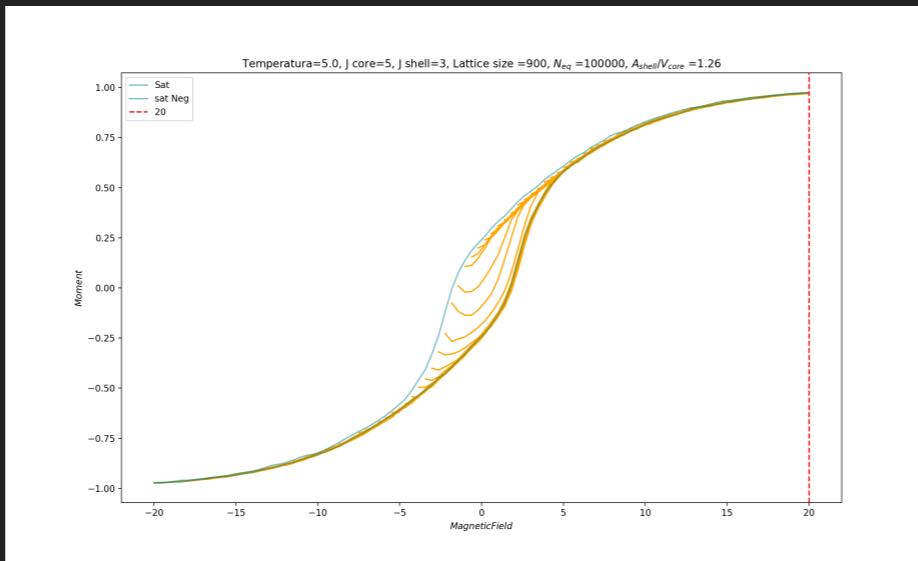
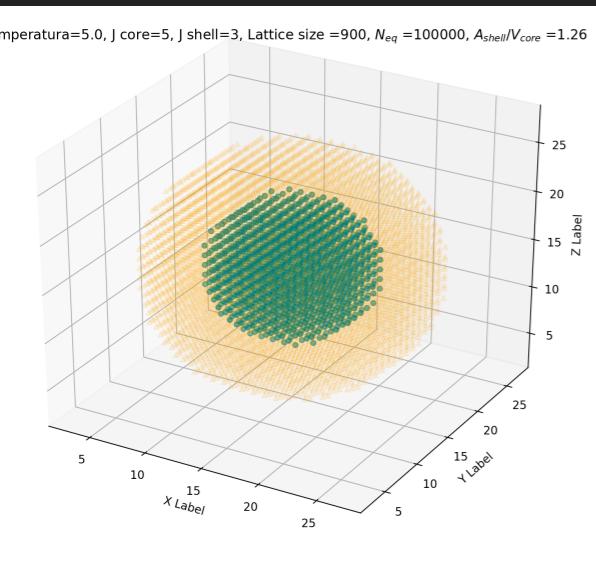
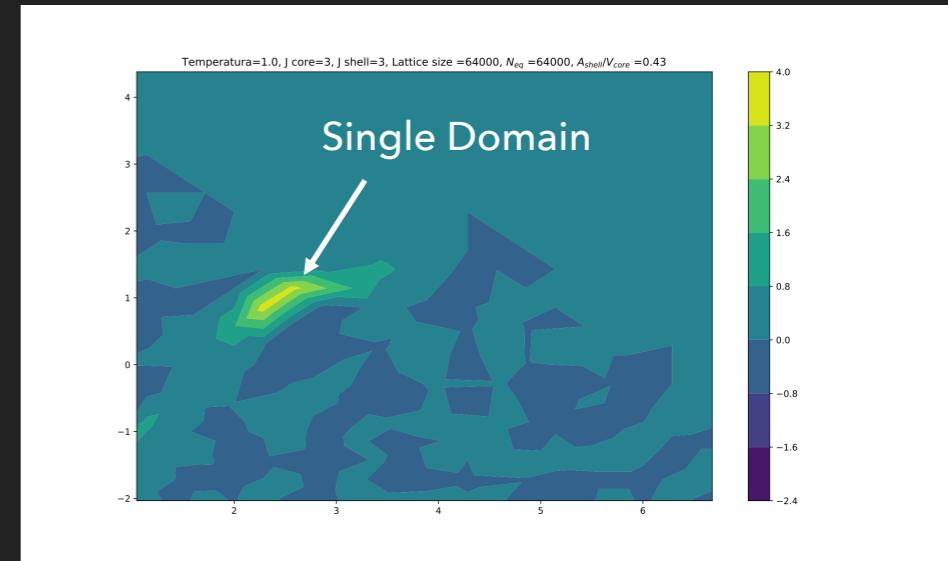
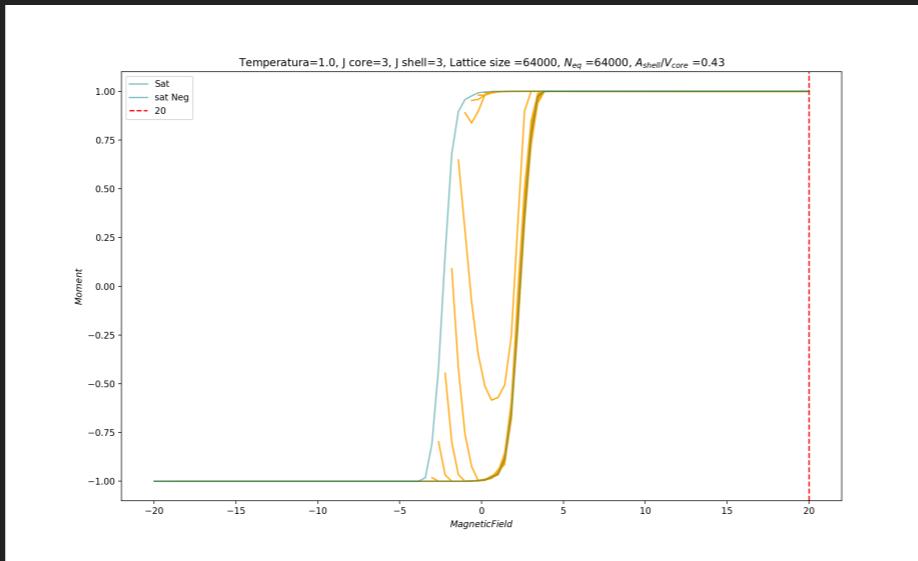
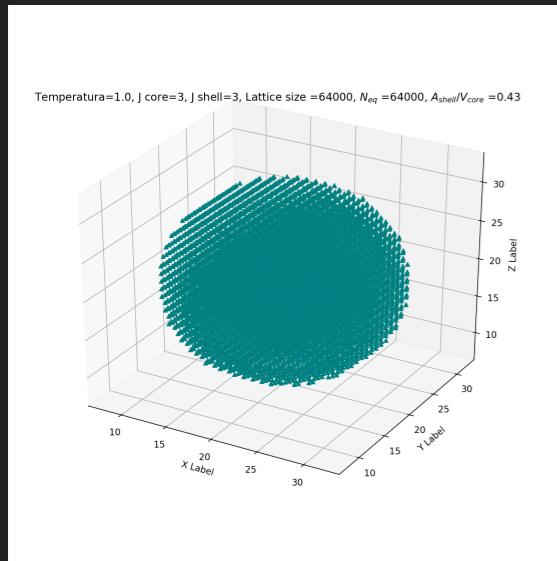


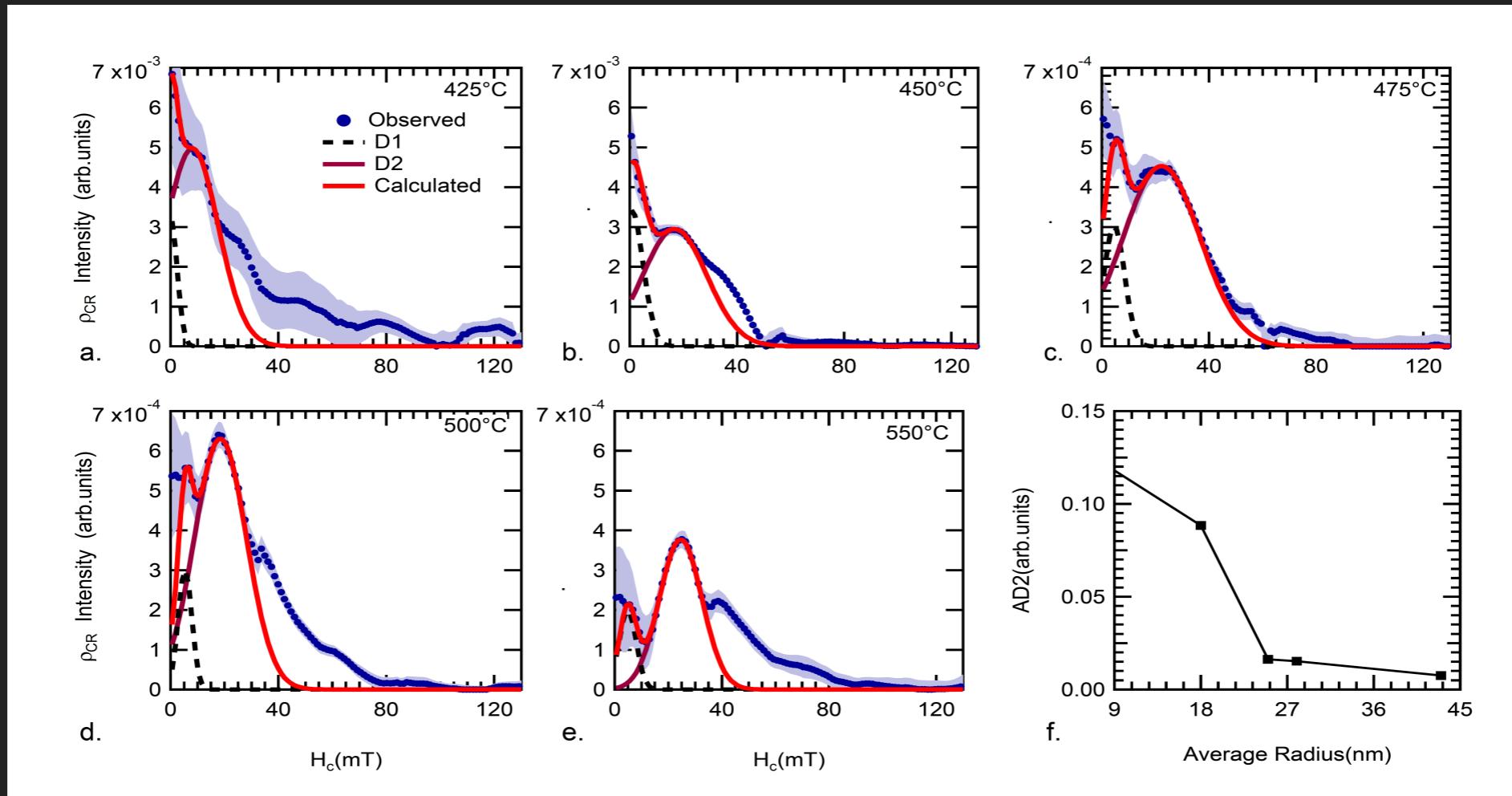


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# FORC

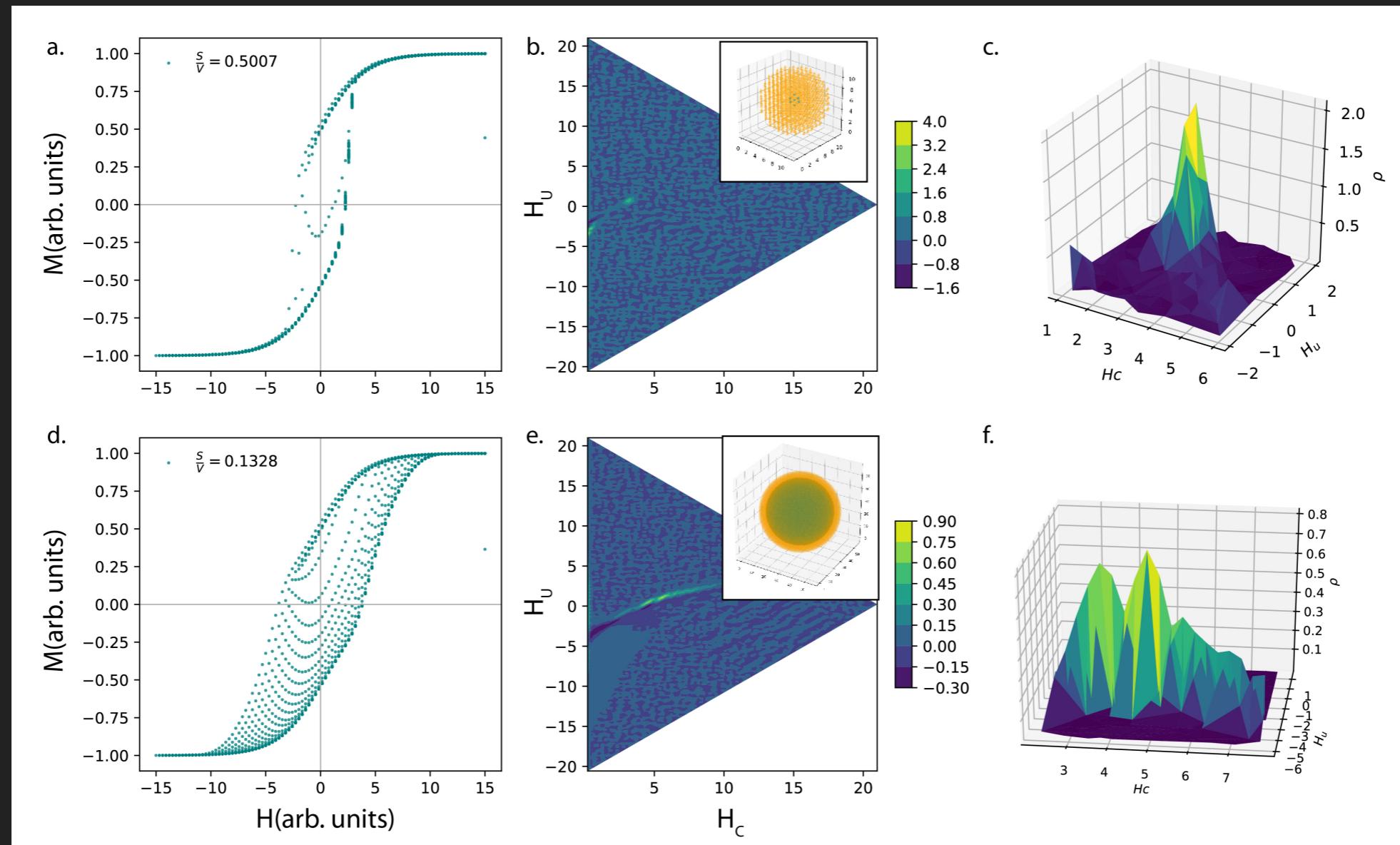
CITE: Fabrication of CoFe<sub>2</sub>O<sub>4</sub> ferrite nanowire arrays in porous silicon template and their local magnetic properties



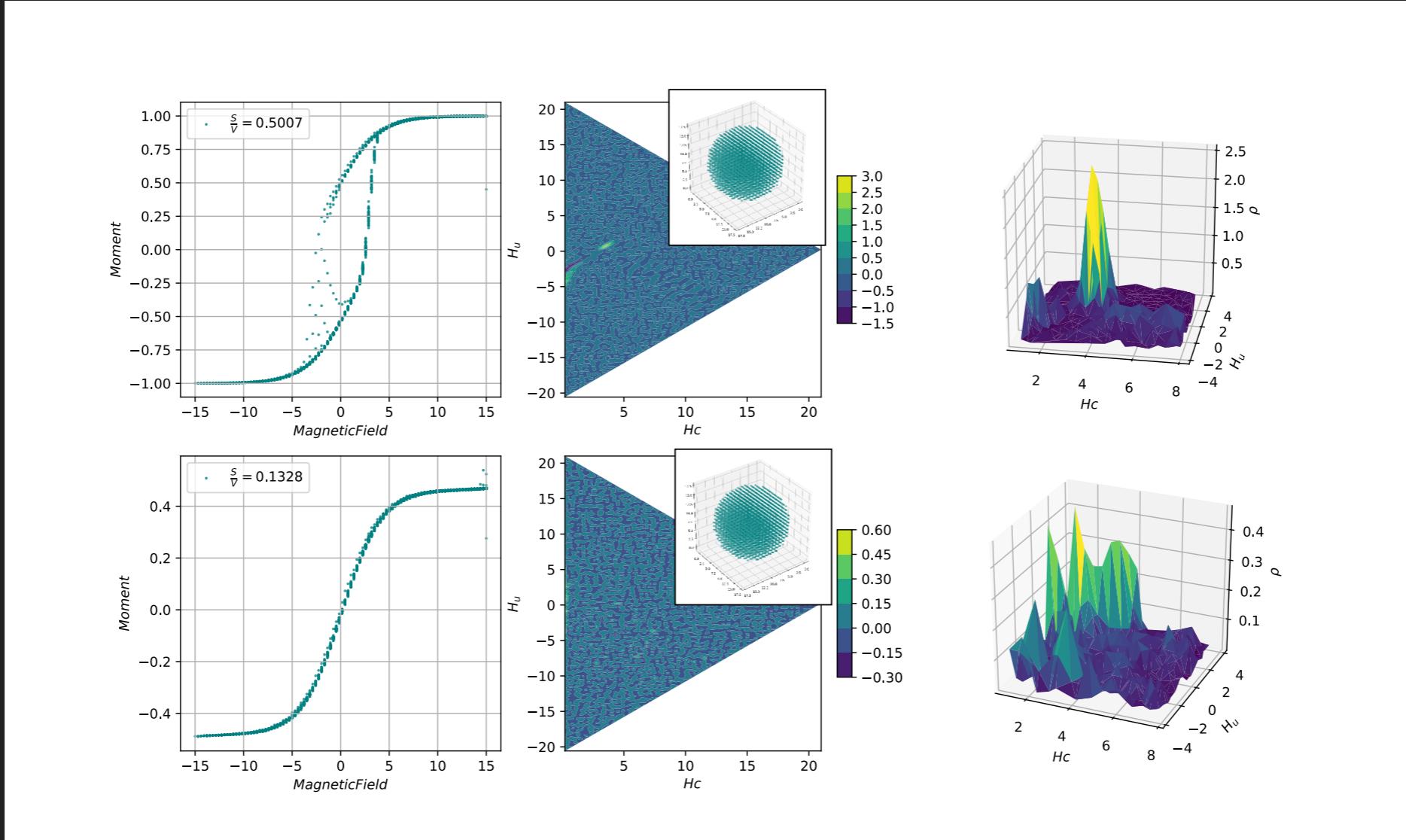


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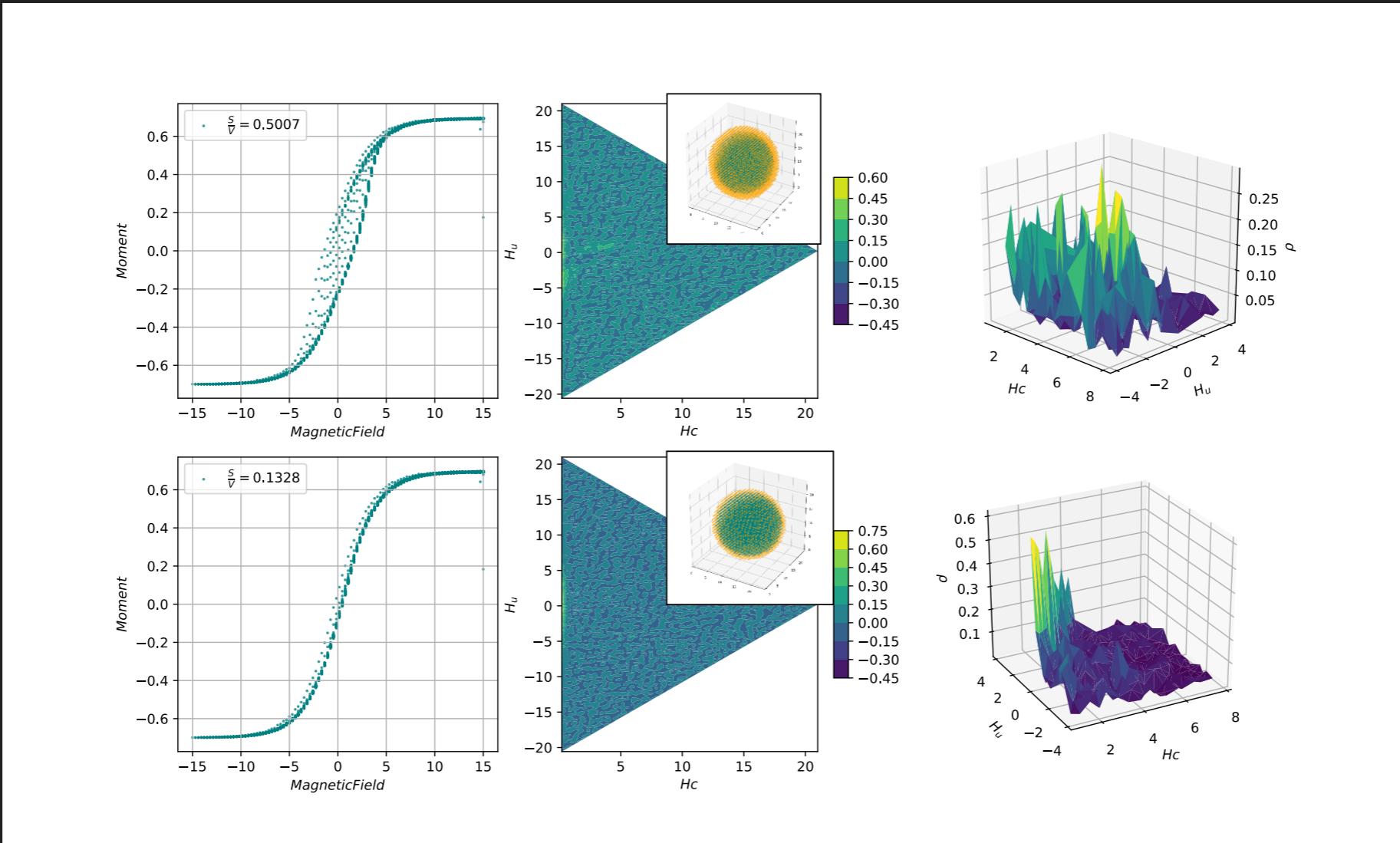
# LAB DATA MEASURED BY ALEXANDER CARDONA



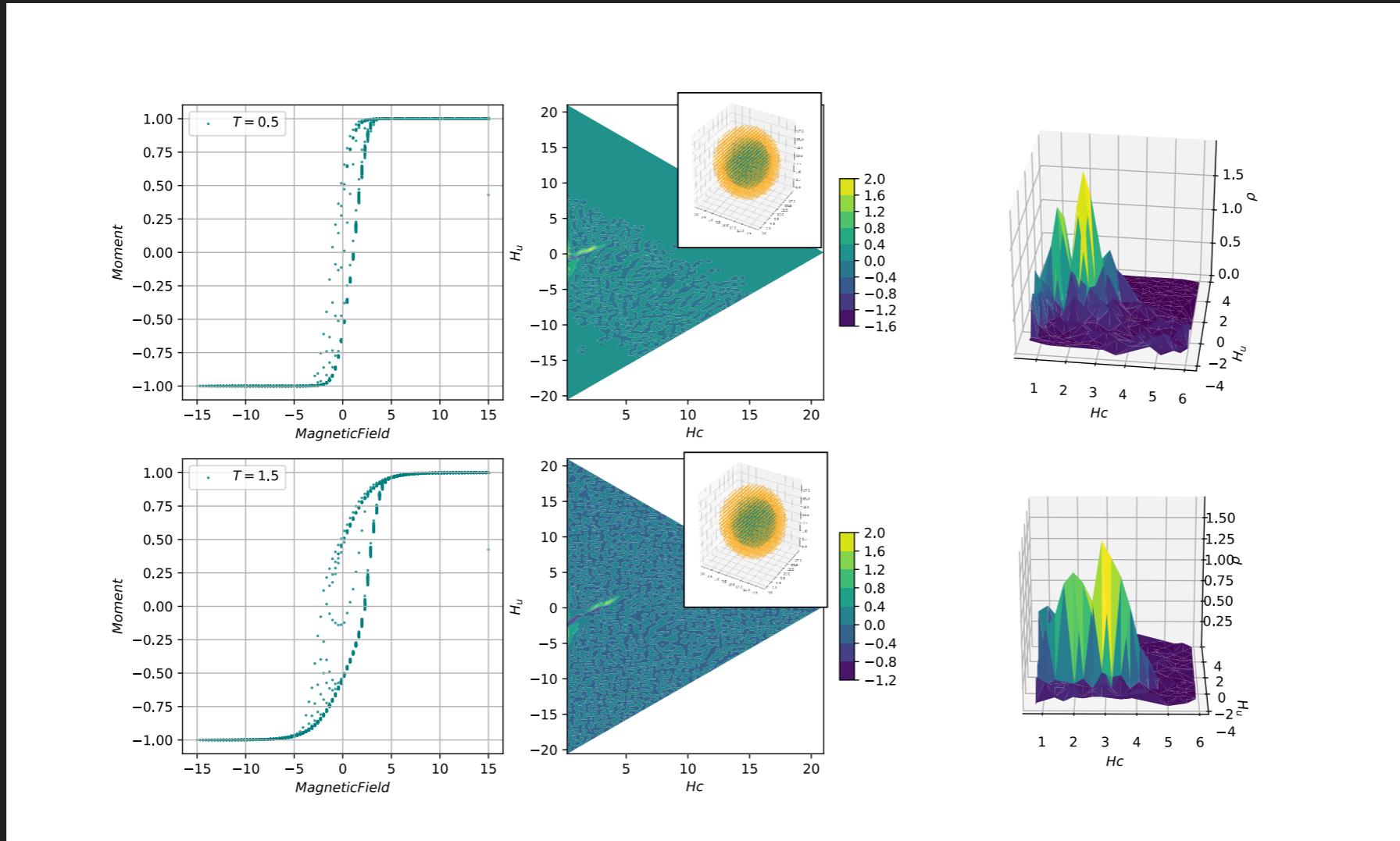
# TAKE TWO CASES, DIFFERENT RELATIONS OF S/V



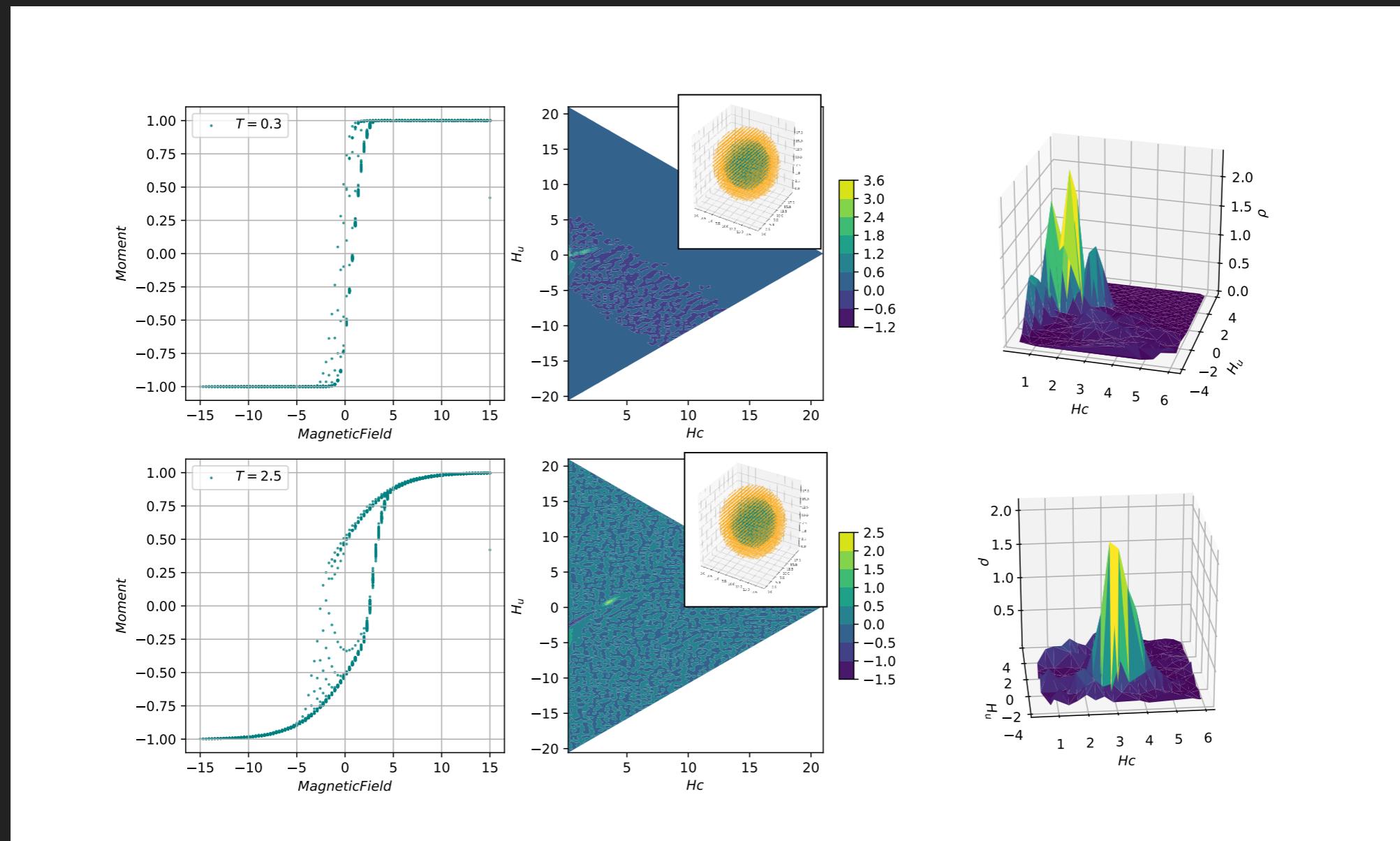
# FERRO-ANTIFERRO SINGLE DOMAIN



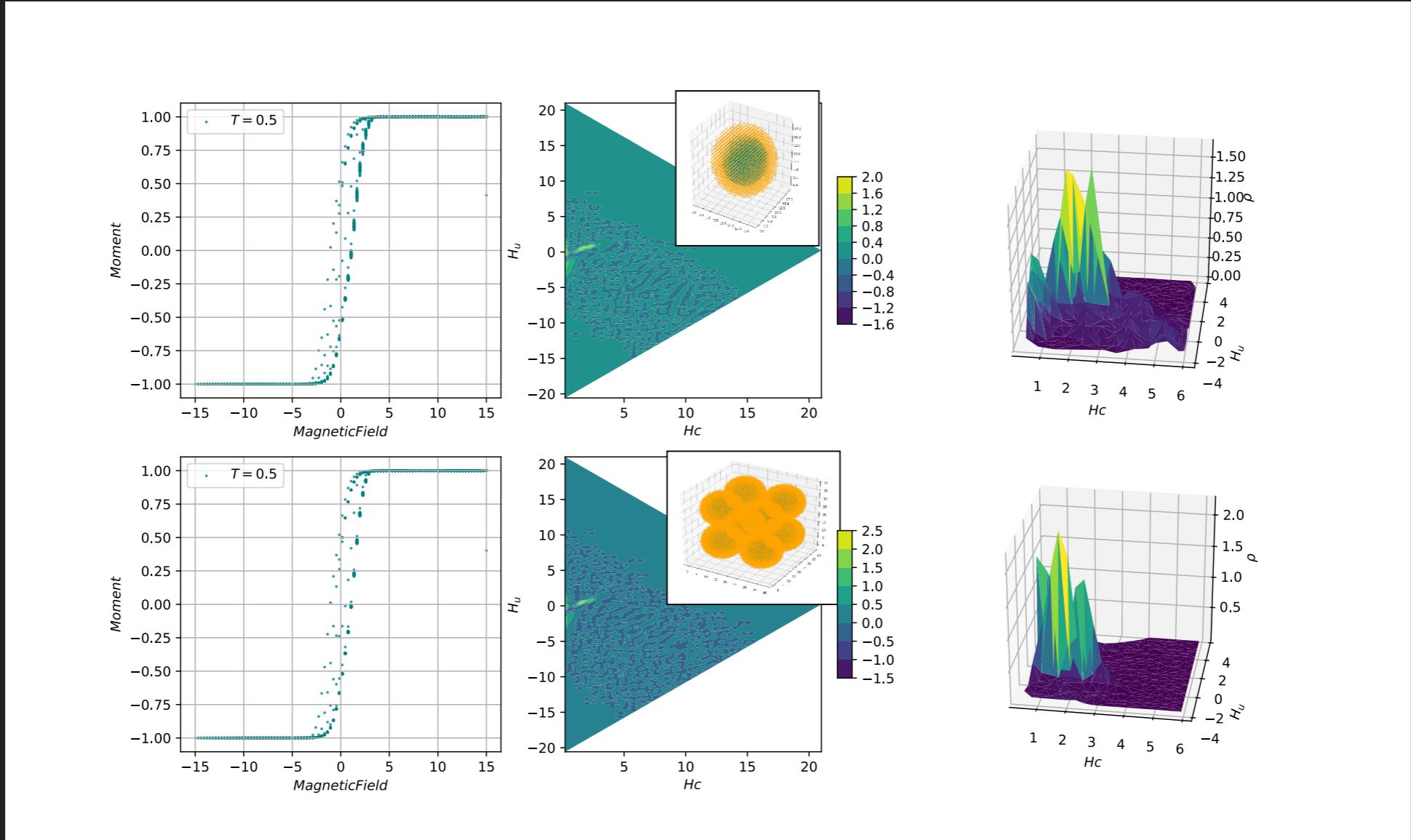
# BIG CORE ANTIFERRO



# POLES SEPARATION TEMPERATURE



# POLES SEPARATION TEMPERATURE



# INCREASING THE NUMBER OF PARTICLES

- ▶ Metropolis algorithm is an useful tool for optimization of non-convex problems, as it's the minimization of the energy of a system in the canonical ensemble
- ▶ The Ising model makes an important contribution to the explanation of the physical phenomena that involves magnetic materials.
- ▶ FORC diagrams shows the core, shell and interface domains.
- ▶ There is a limit on the size of the particles, at which the magnetic properties depends on the size.
- ▶ Temperature is a key feature for being able to see domains.

- 1. INITIALIZATION:** CHOOSE INITIAL POINT  $x_0$  AND AN ACCEPTANCE PROBABILITY DISTRIBUTION  $g(x_i|x_{i-1})$ .
- 2. GENERATE:** A CANDIDATE FOR THE NEXT SAMPLE  $g(x_i|x_{i-1}) \rightarrow x_i'$
- 3. CALCULATE:** THE ACCEPTANCE RATIO  $\alpha = \frac{f(x_i')}{f(x_{i-1})}$
- 4. ACCEPT OR REJECT:** GENERATE A RANDOM NUMBER  $u \sim [0,1]$ . IF  $u \leq \alpha \Rightarrow x' = x_i$   
ELIF  $u > \alpha \Rightarrow x' = x_{i-1}$
- 5. REPEAT :** 2-3 UNTIL ACCOMPLISH CONDITION

**1. INITIALIZATION:** CREATE THE SYSTEM IN A RANDOM MICRO-STATE

**2. GENERATE:** CHOOSE A RANDOM ELEMENT OF THE SYSTEM WITH AN UNIFORM DISTRIBUTION  $S$

**3. CALCULATE:** CHANGE THE STATE OF THE ELEMENT  $S$ , COMPUTE THE ENERGY AND CALCULATE  $p_x = \frac{1}{Z} e^{-\frac{E_S}{K_b T}}$

**4. ACCEPT OR REJECT:** IF  $S$  REDUCE THE ENERGY ACCEPT THE NEW MICRO STATE. ELSE IF  $u \sim [0,1]$ .  $u \leq p_x \Rightarrow \text{ACCEPT}$ . ELSE REJECT.

**5. REPEAT 2-3 UNTIL ENERGY CONVERGES.**

- ▶ To Edwin Ramos and Alexander Cardona for the guidance on the direction of the simulation, and the potential that it can have on the description of the physical phenomena.
- ▶ To Juan Gabriel Ramirez, for taking time to help me be prepare for this talk and being exigent in order to be a better physicist
- ▶ To the nano-magnetism lab for the disposal of all the resources needed for the develop of this work

- ▶ 1. N. Metropolis; A.W. Rosenbluth; M.N. Rosenbluth; A.H. Teller & E. Teller (1953). "Equation of State Calculations by Fast Computing Machines". *Journal of Chemical Physics*. 21 (6): 1087-1092. [Bibcode:1953JChPh..21.1087M](#).
- ▶ 2. W. K. Hastings, Monte Carlo sampling methods using Markov chains and their applications, *Biometrika*, Volume 57, Issue 1, April 1970, Pages 97-109, <https://doi.org/10.1093/biomet/57.1.97>
- ▶ 3. [Ernst Ising, Contribution to the Theory of Ferromagnetism.](http://www.h-s-augsburg.de/~harsch/anglica/Chronology/20thC/Ising/isi_fm00.html) [http://www.h-s-augsburg.de/~harsch/anglica/Chronology/20thC/Ising/isi\\_fm00.html](http://www.h-s-augsburg.de/~harsch/anglica/Chronology/20thC/Ising/isi_fm00.html)
- ▶ 4. Heslop, D., Dekkers, M. J., Kruiver, P. P., & Van Oorschot, I. H. M. (2002). Analysis of isothermal remanent magnetization acquisition curves using the expectation-maximization algorithm. *Geophysical Journal International*, 148(1), 58-64.
- ▶ 5. Soares, J. M., Cabral, F. A. O., de Araújo, J. H., & Machado, F. L. A. (2011). Exchange-spring behavior in nanopowders of CoFe<sub>2</sub>O<sub>4</sub>-CoFe<sub>2</sub>. *Applied Physics Letters*, 98(7), 072502.