



# AUTUMN END SEMESTER EXAMINATION-2018

..... Semester B.Tech & B.Tech Dual Degree

DISCRETE MATHEMATICAL STRUCTURES

**MA 302**

(-.....Admitted Batch & Back)

Time: 3 Hours

Full Marks: 60

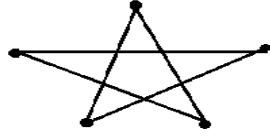
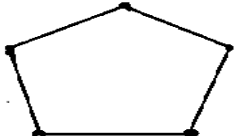
*Answer any SIX questions including question No.1 which is compulsory.*

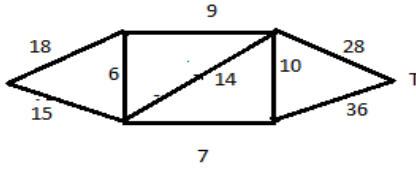
*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words as far as practicable and all parts of a question should be answered at one place only.*

1.			[2 × 10]
	(a)	Find the negation of the statement: $2 + 4 = 6 \Rightarrow 5 + 2 = 7.$	
	(b)	Using truth table prove that $\sim(p \vee q) \equiv \sim p \wedge \sim q.$	
	(c)	Determine the truth value of each of the following statements if the domain consists of all integers. (i) $\forall n(n + 1 > n)$ (ii) $\exists n(2n = 3n)$	
	(d)	Find the equivalence relation corresponding to the partition set $P = \{\{a,b\}, \{c\}, \{d,e\}\}$ of the set $A = \{a, b, c, d, e\}.$	
	(e)	Find the number of positive integers not exceeding 100 that are divisible by either 4 or 9.	
	(f)	Find generating functions corresponding to the numeric function $a_n = n^2; \quad n \geq 1.$	
	(g)	Find the values of the Boolean function represented by $F(x, y, z) = \overline{xy} + z.$	
	(h)	Give example of a zero-divisors in a ring.	

	(i)	Define the following terms: (i) Spanning tree. (ii) Bipartite graph	
	(j)	Find the greatest lower bound and least upper bound of the subset $\{8, 10, 12\}$ , in the poset $(\cdot)$ .	
2.			$[2 \times 4]$
	(a)	Show that $(p \wedge q) \rightarrow (p \vee q)$ is a tautology	
	(b)	Show that the argument form with premises $(p \wedge t) \rightarrow (r \vee s)$ , $q \rightarrow (u \wedge t)$ , $u \rightarrow p$ , and $\sim s$ and conclusion $q \rightarrow r$ is valid.	
3.			$[2 \times 4]$
	(a)	Use mathematical induction to prove that $n^3 - n$ is divisible by 3 whenever $n$ is a positive integer.	
	(b)	Let $R = \{(a_1, a_1), (a_1, a_2), (a_1, a_4), (a_2, a_3), (a_3, a_3), (a_3, a_5), (a_4, a_4), (a_5, a_2)\}$ be a relation on the set $A = \{a_1, a_2, a_3, a_4, a_5\}$ Find the transitive closure of $R$ using Warshall's algorithm.	
4.			$[2 \times 4]$
	(a)	Let $R$ be a reflexive relation on a set $A$ such that $(a, b) \in R, (a, c) \in R \Rightarrow (b, c) \in R$ . Show that $R$ is an equivalence relation.	
	(b)	Let $S = \{a, b, c\}$ . Show that $(P(S), \supseteq)$ is a complemented lattice? Draw its Hasse diagram.	
5.			$[2 \times 4]$
	(a)	Find the numeric solution of the recurrence relation $a_n - a_{n-1} = n$ ; $n \geq 1$ with $a_0 = 0$ using generating function.	

	(b)	Find the numeric solution the recurrence relation $a_r - 4a_{r-1} = 8^r$ ; for $r \geq 1$ , with $a_0 = 1$ .	
6.			$[2 \times 4]$
	(a)	Find the sum-of-products expansion for the Boolean function $F(x, y, z) = (\bar{x} + y)z$ .	
	(b)	For any Boolean algebra $B$ , prove that $(a + b)(b + c)(c + a) = ab + bc + ca$ .	
7.			$[2 \times 4]$
	(a)	Let $G$ be a group and $a, b, c \in G$ . Then show that (i) $ab = ac \Rightarrow b = c$ , (ii) $(ab)^{-1} = b^{-1}a^{-1}$ .	
	(b)	Let $G$ be the set of all nonzero real numbers and $a * b = \frac{ab}{2}$ . Show that $(G, *)$ is an abelian group.	
8.			$[2 \times 4]$
	(a)	Are these following graphs Isomorphic? Justify your answer.  <div style="display: flex; justify-content: space-around; align-items: center;">   </div>	
	(b)	Using Dijkstra's algorithm find the shortest path from vertex $a$ to $z$ from the following weighted graph.	

			
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