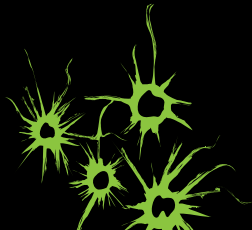
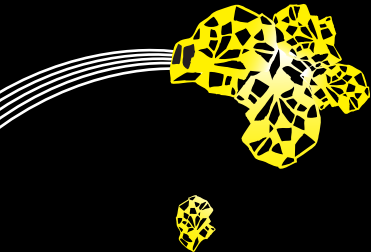


Symbolic Model Checking of Timed Automata using LTSmin

Sybe van Hijum





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Time Zones


LDD solution

DDD Solution

Results

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Modelchecking


- ▶ Models a system, program, protocol, etc...
- ▶ Check if model meets specifications
- ▶ Problem: State space explosion
 - ▶ Grows exponentially with size of model
- ▶ Timed Automata adds time to these models



Research Problems

Problem: Model checkers are designed for discrete variables (integers), clocks have real values.

- ▶ Can we use the LTSmin symbolic model checker for timed automata?
- ▶ Can we optimize the symbolic back end for clocks?



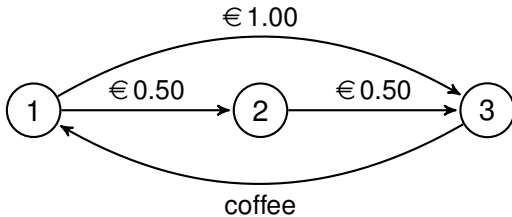
Transition System

1

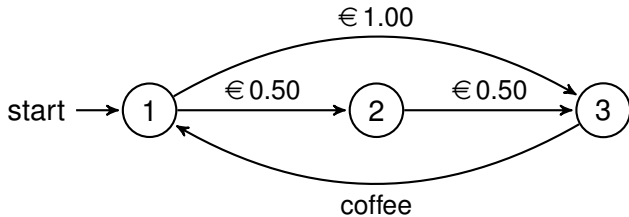
2

3

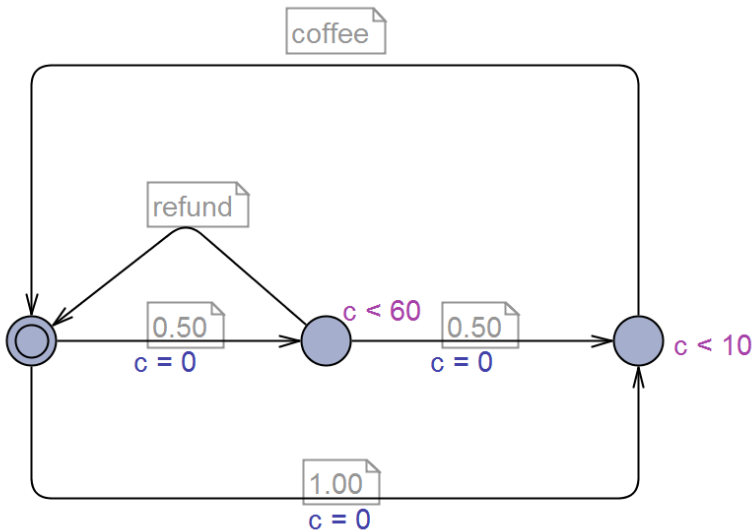
Transition System



Transition System



Timed Automata





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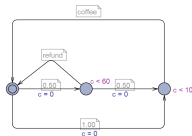
Future Work

Questions?

Time Zones

Time not represented as a variable, but as a zone. Most used structure to represent zones: Different Bound Matrix (DBM)

- Only convex zones
- Memory inefficient



$$0 \leq c < 60$$

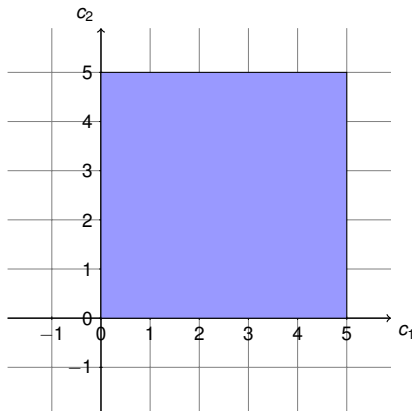
$$\Downarrow$$

$$\begin{aligned} c - 0 &< 60 \\ 0 - c &\leq 0 \end{aligned}$$

$$\begin{matrix} & 0 & c \\ \begin{matrix} 0 \\ c \end{matrix} & \begin{pmatrix} (0, \leq) & (0, \leq) \\ (60, <) & (0, \leq) \end{pmatrix} \end{matrix}$$



	O	c_1	c_2
O	$(0, \leq)$	$(0, \leq)$	$(0, \leq)$
c_1	$(5, <)$	$(0, \leq)$	$(5, <)$
c_2	$(5, <)$	$(5, <)$	$(0, \leq)$





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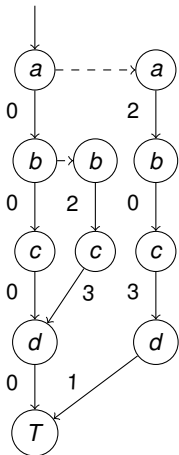
DDD Solution

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Questions?

List Decision Diagram



- Diagram to represent integer variables
- Each node has high and low edge
- Each level represents a variable
- Order of variables important

DBM into state vector

$$\begin{array}{c} \mathbf{O} \quad c_1 \quad c_2 \\ \mathbf{O} \left(\begin{array}{ccc} (0, \leq) & (0, \leq) & (0, \leq) \\ (5, <) & (0, \leq) & (5, <) \\ (5, <) & (5, <) & (0, \leq) \end{array} \right) \\ c_1 \\ c_2 \end{array}$$

- ▶ Old situation
 - ▶ $\{l_0, \dots, l_n, ptr\}$
- ▶ New situation
 - ▶ $\{l_0, \dots, l_n, (0, \leq), (0, \leq), (5, <), (5, <), (5, <), (5, <)\}$



LDD solution

- ▶ Correct, working solution
- ▶ Variable reordering possible
- ▶ All variables seen as discrete values
- ▶ No optimizations based on time



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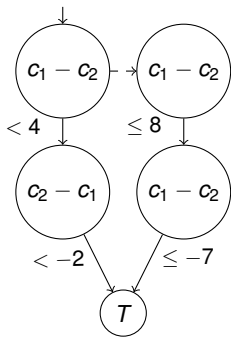
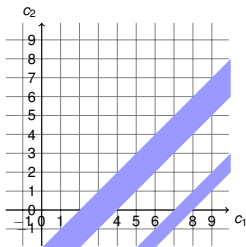
LDD solution

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Difference Decision Diagram

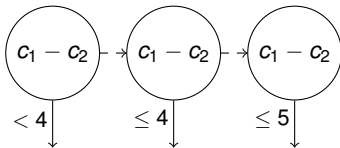
- Structure like LDD
- Added difference operator to each node
- Operator $<$ or \leq

Ordering

Definition (Ordered DDD)

An ordered DDD (ODDD) is a DDD where each non-terminal vertex v satisfies:

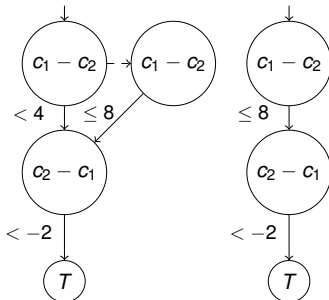
1. $neg(v) \prec pos(v)$,
2. $var(v) \prec var(high(v))$,
3. $var(v) \prec var(low(v))$ or
 $var(v) = var(low(v))$ and $bound(v) \prec bound(low(v))$.



Definition (Locally Reduced DDD)

A locally reduced DDD (R_L DDD) is an ODDD satisfying, for all non-terminals u and v :

1. $\mathbb{D} = \mathbb{Z}$ implies $\forall v. op(v) = '\leq'$,
2. $(cstr(u), high(u), low(u)) = (cstr(v), high(v), low(v))$ implies $u = v$,
3. $low(v) \neq high(v)$,
4. $var(v) = var(low(v))$ implies $high(v) \neq high(low(v))$.

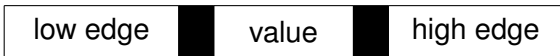


DDD Nodes

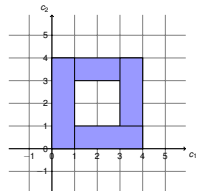
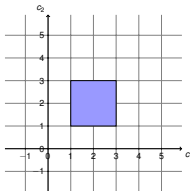
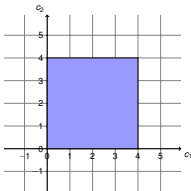
A node contains two 40 bit pointers, 32 bit value, type, operator and flag bit

Node is stored as a 128 bit struct, two 64 bit integers

Total information is 115 bit, 13 unused bits, all set to 0

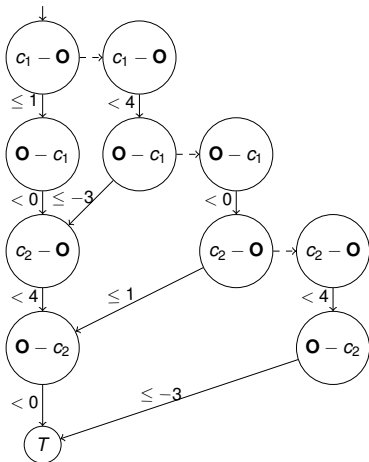
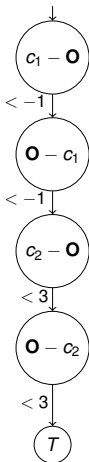
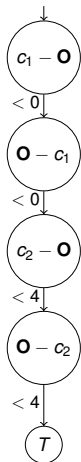


Minus



Difference of two convex zones not always convex

Minus





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Experiments

- ▶ LDD vs. DDD
- ▶ Different search strategies
- ▶ Reorderings for LDD
- ▶ Explicit state with flattened DBM
- ▶ Explicit state with pointer to DBM
- ▶ Uppaal

Results (Nodes)

Model	Discrete states	DDD	LDD
fischer6	16320	15156	85041
critRegion4	6629	55890	100006
Critical4	-	-	-
CSMACD8	10515	96098	321001
Viking12	241662	342	342
Lynch5	228579	49430	112397
bocdp	33	487	355
bocdpFIXED	33	488	427
bando	33	488	425
Milner8	128	11012	30887
hddi10	86	-	454246

Results (Time)

Model	DDD	LDD	mc-flattened	mc-original	Uppaal
fischer6	481.9	48.3	19.2	0.4	0.0
critRegion4	46.3	39.5	24.3	0.5	0.1
Critical4	TO	TO	1.1	0.5	0.6
CSMACD8	1.9	7.3	6.9	0.5	0.1
Viking12	17.6	18.7	10.4	0.7	1.0
Lynch5	34.2	120.0	50.0	0.3	0.0
bocdp	0.1	0.2	0.2	0.0	0.2
bocdpFIXED	0.2	0.2	0.1	0.0	0.3
bando	0.2	0.2	0.1	0.0	0.3
Milner8	0.4	1.2	1.4	0.1	0.0
hddi10	TO	93.3	43.1	0.0	0.0



Results

- ▶ DDD uses less nodes than LDD
- ▶ LDD reorderings not efficient
- ▶ No clearly faster symbolic solution
- ▶ All new options significantly slower than Uppaal
- ▶ Flattening DBM time expensive



Problems

- ▶ Too many function calls
- ▶ Dependency matrices densely filled
- ▶ Large state vectors



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Future work

- ▶ DDD reordering
 - ▶ Needs mapping of positions and types
- ▶ Sparser matrix
 - ▶ Split timed and discrete transition
 - ▶ Must-write matrix
 - ▶ Better insight in timing dependencies



Future work

- ▶ Multi threading
 - ▶ DDD is already thread save
 - ▶ Coupling to DBM not threadsafe
- ▶ Subsumption
- ▶ Skipping levels
 - ▶ All nodes with $(<, \infty)$ left out
 - ▶ Need explicit level of each node
 - ▶ Node reduction up to 90%



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