# Symbolic Model Checking of Timed Automata using LTSmin

Sybe van Hijum

August 29, 2016

# Contents

| 1 Introduction |      |                                   | 4  |  |  |  |  |  |
|----------------|------|-----------------------------------|----|--|--|--|--|--|
| <b>2</b>       | Prel | Preliminaries 5                   |    |  |  |  |  |  |
|                | 2.1  | Timed Automata                    | 5  |  |  |  |  |  |
|                | 2.2  | Zones                             | 6  |  |  |  |  |  |
|                | 2.3  | Zone subsumption                  | 7  |  |  |  |  |  |
|                | 2.4  | Binary Decision Diagram           | 7  |  |  |  |  |  |
| 3              | Rela | ated Work                         | 8  |  |  |  |  |  |
|                | 3.1  | Methods                           | 8  |  |  |  |  |  |
|                |      | 3.1.1 Clock Difference Diagram    | 8  |  |  |  |  |  |
|                |      | 3.1.2 Difference Decision Diagram | 9  |  |  |  |  |  |
|                |      | 3.1.3 Clock Restriction Diagram   | 9  |  |  |  |  |  |
|                | 3.2  | Constraint Matrix Diagram         | 10 |  |  |  |  |  |
|                |      | 3.2.1 Zone BDD                    | 11 |  |  |  |  |  |
|                |      | 3.2.2 Digitazation                | 11 |  |  |  |  |  |
|                |      | 3.2.3 Orderings                   | 12 |  |  |  |  |  |
|                | 3.3  | LTSmin                            | 12 |  |  |  |  |  |
|                | 3.4  | Difference Decision Diagrams      | 14 |  |  |  |  |  |
|                | 3.5  | List Decision Diagram             | 19 |  |  |  |  |  |
| 4              | Imp  | lementation                       | 20 |  |  |  |  |  |
|                | 4.1  | Flattening DBM                    | 20 |  |  |  |  |  |
|                | 4.2  | Dependency Matrices               | 20 |  |  |  |  |  |
|                | 4.3  | DBM reduction                     | 21 |  |  |  |  |  |
|                | 4.4  | Connecting LDD and DDD            | 23 |  |  |  |  |  |
|                | 4.5  | DDD nodes                         | 23 |  |  |  |  |  |
|                | 4.6  | Creating Nodes                    | 24 |  |  |  |  |  |
|                | 4.7  | Apply                             | 24 |  |  |  |  |  |
|                | 4.8  | Minus                             | 25 |  |  |  |  |  |
|                | 4.9  | Relation                          | 27 |  |  |  |  |  |
|                | 4.10 | BFS                               | 28 |  |  |  |  |  |
|                | 4.11 | State-space count                 | 29 |  |  |  |  |  |
|                | 4.12 | Successor Generator               | 29 |  |  |  |  |  |
|                | 4.13 | Time Extrapolation                | 31 |  |  |  |  |  |
|                | 4.14 | Animo Models                      | 31 |  |  |  |  |  |
|                | 4.15 | Correctness                       | 31 |  |  |  |  |  |
| 5              | Exp  | eriments                          | 34 |  |  |  |  |  |
|                | 5.1  | Viking                            | 34 |  |  |  |  |  |
|                | 5.2  | Fischer                           | 34 |  |  |  |  |  |
|                | 5.3  | CSMA-CD                           | 35 |  |  |  |  |  |

|              | 5.4 Animo                     | 35 |
|--------------|-------------------------------|----|
|              | 5.5 Lynch-Shavit              | 35 |
|              | 5.6 Milner                    | 35 |
|              | 5.7 Other models              | 35 |
|              | 5.8 Benchmark Runs            | 36 |
| 6            | Results                       | 37 |
|              | 6.1 Time                      | 37 |
|              | 6.2 Memory                    | 38 |
| 7            | Different Semantics           | 41 |
|              | 7.1 DBM Translation           | 41 |
|              | 7.2 Minus                     | 43 |
| 8            | Future Work                   | 45 |
|              | 8.1 Canonization              | 45 |
|              | 8.2 Reordering                | 45 |
|              | 8.3 Sparser Dependency Matrix | 46 |
|              | 8.4 Multi-Core                | 47 |
|              | 8.5 Animo Model Compatibility | 47 |
|              | 8.6 Subsumption               | 47 |
|              | 8.7 Checking Properties       | 48 |
|              | 8.8 Skipping Levels           | 48 |
| 9            | Conclusions                   | 49 |
| $\mathbf{A}$ | Experiment Results            | 54 |

## 1 Introduction

Timed automata [2] is a widely used modelling formalism. A recent usage of this formalism is the modelling of biological signalling pathways [29]. ANIMO is a tool that generates these timed automata from biological signalling pathway models. Model checking techniques, like property checking are used on these timed automata. The technique however leads to large state spaces, and sometimes to models that are too large to handle by conventional methods. Therefore better model checking techniques for timed automata, that can handle larger state spaces are needed. We look into symbolic algorithms for timed automata.

BDDs (Binary Decision Diagrams) [1,11] and variations like LDDs (List Decision Diagrams) [10] and MDDs (Multi-valued Decision Diagrams) [30] have proven their worth in model checking algorithms. Due to advances in this field, models with much larger state spaces can be explored on the same machine. This progress has not been translated directly to more efficient methods for timed automata, due to the real clock values that are used. Several methods have been proposed, like CDDs (Clock Difference Diagrams) [20], CMDs (Constraint Matrix Diagrams) [16], CRDs (Clock Restriction Diagrams) [32] and DDDs (Difference Decision Diagrams) [24,27]. All of these methods show some extra difficulties or limitations over BDDs. Also after their introduction they have not been developed further.

LTSmin [9,18] is a language-independent on-the-fly model checker with several algorithmic back-ends. Its symbolic back-end uses BDDs to both represent the state space and the transition relations of models. These BDDs are generated on-the-fly by the search algorithms. LTSmin has a language module for Uppaal [5] through the Opaal [13] lattice model checker. Through this module Uppaal models can be loaded into LTSmin. For this language currently, only the explicit-state multi-core back-end can be used [12]. This explicit-state approach showed efficient enough to compete with the latest version of the Uppaal model checker. It showed significant speedups on multi-core machines, at the cost of some memory increase however. To tackle the memory increase a combination of the opaal front-end and the symbolic back-end could be a solution.

The symbolic back-end of LTSmin provides both a memory reduction by using BDDs and a speedup by using multi-threaded search algorithms and the multi-threaded BDD package Sylvan [31]. Using this together with the Uppaal language front-end will hopefully result in a model checker that can compete both on time and memory consumption with the Uppaal model checker.

We will propose a symbolic reachability for timed automata that is capable of handling the models that are generated by the ANIMO tool.

# 2 Preliminaries

We will first define timed automata and zones, a method used to represent time in timed automata. Also a subsumption check over zones will be defined.

#### 2.1 Timed Automata

Timed automata is a formalism that extends labelled transition systems with one or more clocks. Guards over these clocks, denoted as G(C) can be used for transitions. Also reset actions for clock can be defined for transitions. All clocks in the system will increase at the same rate. As our work continues on [12] we use the same definition of timed automata.

**Definition 1** (Timed Automata). An extended timed automaton is a 6-tuple  $A = \langle L, C, Act, l_0, \rightarrow, I_c \rangle$  where

- L is a finite set of locations, typically denoted by l
- C is a finite set of clocks, typically denoted by c
- Act is a finite set of actions
- $-l_0 \in L$  is the initial location
- $\rightarrow \subseteq L \times G(C) \times Act \times 2^C \times L$  is the (non-deterministic) transition relation. We normally write  $l \stackrel{g,a,r}{\Longrightarrow} l$ ' for a transition., where l is the source location, g is the guard over the clocks, a is the action, and r is the set of clocks reset.
- $I_C: L \to G(C)$  is a function mapping locations to downwards closed clock invariants.

With this definition we can combine a finite number of timed automata to a network of timed automata, which is a parallel composition, to define larger systems.

**Definition 2** (Network of timed automata [12]). Let  $Act = \{ch!, ch? | ch \in Chan\} \cup \{\tau\}$  be a finite set of actions, and let C be a finite set of clocks. Then the parallel composition of extended timed automata  $A_i = \langle L_i, C, Act, L_0^i, \rightarrow_i, I_C^i \rangle$  for all  $1 \leq i \leq n$ , where  $n \in \mathbb{N}$ , is a network of timed automata, denoted  $A = A_1 | |A_2| |... | |A_n$ .

A network of timed automata is a parallel composition that synchronizes on a set of channels Chan [5]. ch! and ch? represent the output and input action on the channel  $ch \in Chan$ .

$$\mathbf{O} \qquad c_1 \qquad c_2 \\
\mathbf{O} \begin{pmatrix} (0, \leq) & (0, \leq) & (0, \leq) \\ c_1 & (5, <) & (0, \leq) & (\infty, \leq) \\ c_2 & (4, \leq) & (\infty, \leq) & (0, \leq) \end{pmatrix}$$

Figure 1: DBM

#### 2.2 Zones

For basic transition systems the state space can grow exponentially for the number of variables in the system. The state space of timed automata is by definition infinite, as clocks have real values. If a state is defined between two points in time, an infinite amount of moments in time can happen during that state. Even when some granularity is used, that defines that clocks will only increase with certain step size the automata can still have infinite state space if a clock is unbounded. To tackle this problem most model checkers use a notion of zones for the representation of time. A zone can be seen as a set of constraints over the clocks C of the form  $c_i \sim x$  and  $c_i - c_j \sim x$  where  $\infty \in \{<, \leq, =, \geq, >\}$  and  $x \in \mathbb{N}$ . To represent these zones several data structures have been developed. One of the most common used structures are Difference Bound Matrices (DBMs) [6,14].

These matrices use both a column and a row for each clock, and on each position (i, j) an upper bound on the difference between the clocks  $c_i$  and  $c_j$  is given in the form  $c_i - c_j \leq x$  where  $\leq \{<, \leq \}$  and  $x \in \mathbb{Z}$ . For the constraints over the single clocks an extra clock  $\mathbf{O}$  with a constant value 0 is added. This way the upper and lower bound of a clock  $c_i$  can be given by  $c_i - \mathbf{O} \leq x$  and  $\mathbf{O} - c_i \leq y$ . The addition of this  $\mathbf{O}$  clock will give the matrix of a timed automaton always size  $(|C| + 1)^2$ . This way convex zones of clock variables can be represented. Each matrix can however only contain a single convex zone. Concave zones and multiple convex zones need multiple matrices to be represented. As a solution often a list of DBMs is used. In figure 1 we give an example of a DBM with two clocks:  $c_1$  and  $c_2$ , representing the zone  $0 \leq c_1 < 5 \land 0 \leq c_2 \leq 4$ . The diagonal only contains  $(0, \leq)$  values as these elements give the difference between a clock and itself, which is clearly always 0.

A number of operations on DBMs has been defined. We will introduce the operations we use. The same notation as [12] is used.

- $D \uparrow$  is called the delay operator. This lets time pass unlimitedly from the zone in D.
- $D \cap D'$  adds additional constraints from D' to D. This is used for transitions that have clock constraints. These constraints can be represented as a DBM.

- D[r] with  $r \subseteq C$ , resets all clocks in r.
- D/B does a maximal bounds extrapolation. In section 4.13 we will go into more detail about this extrapolation.

## 2.3 Zone subsumption

In model checking an important function is to check if a certain state has been visited already earlier. For normal automata this can be done by comparing the newly found state to all states that have already been visited, and check if one of those states is equal to that new state. This is often done by more efficient methods, like hash functions, but the equality check remains. For states with zones this equality check does not suffice. Two zones do not need to be equal, but the newly discovered zone can also be a subset of the earlier discovered zones. In LTSmin this is done by a subsumption check [12] that is performed over the DBMs. This check is delegated to the Uppaal DBM library. The function checks if a new zone is a subset of the zone represented by a DBM.

## 2.4 Binary Decision Diagram

# 3 Related Work

In this related work section we will discuss a number of methods used for model checking timed automata. We will choose a method which we will use for the rest of this project.

#### 3.1 Methods

Already several model checkers for timed automata exist such as Uppaal [5], KRONOS [33], RABBIT [8] and RED [32]. We focus mainly on the Uppaal tool as we use the same input format. Opaal [13], the language module for LTSmin, uses the XML format that is created by the Uppaal tools. This way we can use the Uppaal user interface to create and adapt models. We also use the Uppaal DBM library to represent zones.

The most established method to represent clock zones are DBMs. We gave an introduction to this structure in the preliminaries section. Several diagrams based on BDDs have been developed to represent zones. All of these are similar to DBMs in the sense that they use clock constraints to represent the zones. The structure of these diagrams is BDD-like to represent the zones more efficiently. Below we shortly describe four zone based methods. For each method we give an example, all examples represent  $2 < c_1 - c_2 < 4 \lor 7 \le c_1 - c_2 \le 8$ .

#### 3.1.1 Clock Difference Diagram

CDDs [20] use single nodes for each variable and have multiple edges each containing a disjoint interval of that variable. This results in a node with a larger fanout. The upper and lower bound for each pair of clocks are represented in a single node, as the edges represent intervals. Requiring the disjointness of intervals can lead to a memory inefficient representation, as intervals need to be cut in more smaller parts. All algorithms on CDDs do not maintain disjointness, after every step it needs to be re-established. In Figure 2 we have an example of a CDD.

**Definition 3** (Clock Difference Diagram [20]). A clock difference diaram is defined as a directed, acyclic graph, which has

- a node called the start node from which all nodes of the graph are reachable
- inner nodes written as  $((i, j), (I_1, T_1, ..., (I_q, T_q))$  where (i, j) is the pair of clocks of the constraint, the  $I_n$  are intervals of the real numbers, and the  $T_n$  are CDDs again. We require completeness, i.e.  $\bigcup_{n \in \{1, ..., q\}} I_n = \mathbb{R}$
- end-nodes which are either TRUE or FALSE

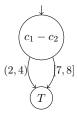


Figure 2: CDD representation

#### 3.1.2 Difference Decision Diagram

DDDs [24, 27] use an upper-bound constraint for a variable pair on each node that can either be true or false. Each node thus has a fixed fanout of two. When a constraint is false, a next node will have another constraint on the same variable. This requires a fixed ordering based on the variables, values and operators. In Figure 3 an example of a DDD is shown.

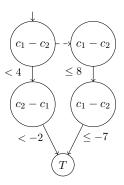


Figure 3: DDD representation

## 3.1.3 Clock Restriction Diagram

CRDs [32] differ mainly from CDDs by not using disjoint intervals but possibly overlapping upper bounds, for a pair of variables on their edges. This diagram will have a larger fanout per node, like CDDs. Several normal forms for this diagram are proposed, with different performance results. It is also shown that CRDs can be combined with BDDs into a single structure to fully symbolically represent the state space. In Figure 4 we give an example of a CRD.

**Definition 4** (Clock Restriction Diagram [32]). Given a set of variables  $V = \{x - x' | x, x' \in X \cup \{0\}\} \cup \{true\}$ , an evaluation index  $\Omega$  over V,

and a timing constant  $C_A$ , a CRD over  $V, \Omega$ , and  $C_A$  is a tuple  $D = (v, (\beta_1, D_1), ..., (\beta_n, D_n))$  with  $n \ge 0$  and  $v \in V$  such that

- v = true iff n = 0
- if  $v \neq true$ , then for all  $1 \leq i \leq n, \beta_i \in B_{C_A}$  and  $D_i$  is a CRD, say  $(v_i, (\beta_{i,1}, D_{i,1}), ..., (\beta_{i,m}, D_{i,m}))$ , over  $V, \Omega$ , and  $C_A$  with  $v \prec_{\Omega} v_i$
- if  $v \neq true$ , then for all  $1 \leq i < j \leq n$ ,  $\beta_i \neq \beta_j$
- if  $v \neq true$  and n = 1, then  $\beta_1 \neq (<, \infty)$

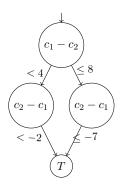


Figure 4: CRD representation

## 3.2 Constraint Matrix Diagram

CMDs [16] combine CDDs, CRDs and DBMs into a single structure. This diagram type differs from the others by having multiple constraints per edge, resulting in a diagram with few nodes. Upper- and lower-bounds of multiple clock pairs can be on a single edge. The diagram can also be used with only single constraints per edge, which gives a structure quite similar to CRDs. CMDs do not have a canonical form so only some reductions are proposed. An example of a CMD is given in Figure 5. This figure contains two examples, the first is a diagram of the constraint we use in this section. To show the difference with other diagrams we also give a diagram representing the same zone as the DBM in Figure 1.

**Definition 5** (Constraint Matrix Diagram [16]). A Constraint Matrix Diagram (CMD) over the set of constraint matrices M is a tuple  $M = (Q, q_0, q_{\perp}, type, E)$  where

- Q is a finite set of nodes
- $q_0 \in Q$  is the root node

- $q_{\top} \in Q$  is the sink
- type:  $Q \to I \cup \{I_{max}+1\}$  is a total function that associates a constraint index to each node
- $E \subseteq Q \times M \times Q$  is an edge relation

Additionally, we require that (1) (Q, E) is a directed acyclic graph with precisely one source node  $q_0$  and one sink node  $q_{\top}$ ; (2)  $type(q_0) = 0$  and  $type(q_{\top}) = I_{max} + 1$ ; (3) for each edge  $(q, m, q') \in E$ ,  $minIdx(m) \ge type(q)$  and maxIdx(m); type(q').

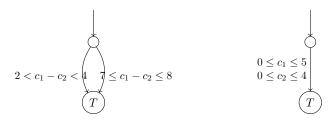


Figure 5: CMD representation

#### 3.2.1 Zone BDD

In [15, 34] a method is proposed purely based on BDDs by translating the constraints directly into BDD nodes. We call this method BDD zones. This results in a unified structure for both the discrete variables and the clock constraints. The method is only a proof of concept and has not been implemented in a model checker and no performance results are known. Subsumption for this method may be difficult. On BDDs only equalities can be checked, and no inequalities. This way inclusion is not trivial to check by normal BDD algorithms.

#### 3.2.2 Digitization

Digitization approximates the continuous values of clocks by using discrete values [7]. The method however only works for closed timed automata, meaning that no strict comparisons on clocks can be made in the model and that clocks only can be compared to integers. This approach is very sensitive to the granularity of the values used and the upper bound of the clock values. When fine granularity or large upper bounds are used, the memory usage will increase too much. An advantage of this approach is that basic model checking approaches can be used and no extra complexity due to zone calculations is added. This method results in a transition system with only discrete variables, so a normal BDD package can be used. In [28]

a similar approach is proposed by using clock tick actions to represent time progress and removing clock variables altogether.

#### 3.2.3 Orderings

A known difficulty in BDDs is the variable ordering. A bad ordering can lead to a BDD of exponential size, where a good ordering can sometimes lead to a significantly smaller diagram. Of the zone diagrams named above, only for CRDs experiments with different orderings have been conducted, the other researches assume a given ordering on the variables and the ordering of the values is fixed. The CRD case shows that full interleaving and having related variables close to each other in the ordering is preferable and gives the best results, both on speed and memory. This is the same result as expected with BDDs. This suggests that similar orderings should be used with these techniques. The techniques using normal BDDs can use standard BDD reorderings.

In Table 1 we compare the different types of diagrams we discussed above.

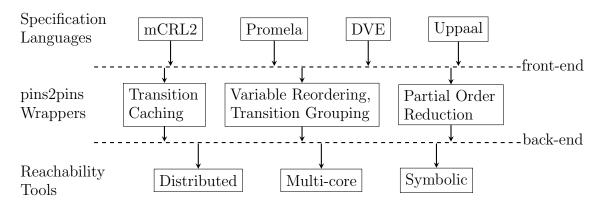


Figure 6: Modular structure of LTSmin

## 3.3 LTSmin

LTSmin [9, 18] is a language independent model checker. It is built in a modular way such that new languages can be added by a PINS (Partitioned Next-State Interface) without too much effort, and new algorithms can be added easily. LTSmin offers four different algorithmic back-ends for model analysis: symbolic, multi-core, sequential and distributed. All of these back-ends support different types of reduction and model checking. Several language modules have already been built for LTSmin such as mCRL2, Promela, DVE and Uppaal. The modular structure of LTSmin is

Table 1: Comparing Diagrams

| Type            | Pro                                                                                                                                                                           | Con                                                                                                                                                                                                        |
|-----------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| DBM             | Canonical form for convex zones Existing library Inclusion check                                                                                                              | Concave zones need multiple DBMs<br>Not memory efficient                                                                                                                                                   |
| DDD             | Structure like LDD Re-ordering of variables possible Apply same efficiency as BDDs Discrete variables also in DDD                                                             | Canonicity hard to obtain  No on the fly canonicity  Expensive normal form computation  Only time performance tested  Only reduction algorithms                                                            |
| CDD             | Structure like MDD Inclusion check (intersection of complement)                                                                                                               | No algorithm to get normal form Only high level algorithms given Methods don't maintain disjointness Expensive normal form computation No implementation results available Disjointness memory inefficient |
| CRD             | Combination with BDD possible Variable reordering shows advantage Library available Some benchmarks exp better than CDD Extensive benchmarks Good performance backwards reach | 3 possible canonical forms No algorithms in paper Some benchmarks linear worse than CDD                                                                                                                    |
| CMD             | Benchmarks against RED and Uppaal                                                                                                                                             | Results differ per case Needs translation from vector to edges Two reduced forms                                                                                                                           |
| BDD<br>discrete | Using existing BDD packages Good performance for small clock values                                                                                                           | Performance decreases fast for large values Not possible with current Opaal PINS Introducing additional 'tick' actions Only for closed timed automata                                                      |
| BDD zones       | Using existing BDD packages All variable reorderings possible Only need direct translation DBM to state vector Easy to implement                                              | Losing zone containment No implementation results                                                                                                                                                          |

shown in Figure 6. The PINS is the core of LTSmin. This interface abstracts as much as possible from the model without losing the structure. It represents states as fixed length integer arrays. The main function of the interface is a (partitioned) next-state function which returns the successor states. With these functions a state space can be generated on the fly. With the use of dependency matrices event locality can be determined statically [22]. With these matrices, more efficient symbolic algorithms can be used, the number of next-state calls can be reduced, efficient variable re-orderings can be used, and transition caching can be used. In the current Uppaal PINS the next-state function is not partitioned and therefore no meaningful dependency matrix is created, and none of these algorithms can be used. Also the DBM variable is only represented by a pointer, which is not a meaningful value for the transition system. LTSmin uses the pointer to a DBM to do the subsumption check as described in section 2.3.

## 3.4 Difference Decision Diagrams

We have discussed several symbolic approaches for representing zones. All of these approaches have benefits and downsides over each other. We chose to develop one of these approaches in LTSmin. We wanted a diagram that can store both discrete states and zones, this can either be done in the diagram, or in a combination of the diagram and BDD or LDD nodes. Also a subsumption check on the diagram should be possible. We chose from the four zone-representing diagrams discussed earlier. The CDD approach was not chosen due to the memory inefficient disjoint intervals and their algorithms not maintaining these disjointness. The CMD approach is too similar to DBMs, on which we already have an approach. The choice between CRD and DDD was between two quite similar diagrams. We have decided to continue on the DDD. It is a diagram form that is closely related to LDDs, for which we already have a library, so we can reuse parts of the LDD library, and it is also quite compatible to the current PINS structure and its next-state function, so no big changes are needed to that.

So DDDs are a diagram type that seems to fit well in the current structure we have, but there is still room for some more research. First we give the definition of a DDD.

**Definition 6** (Difference Decision Diagram [27]). A difference decision diagram (DDD) is a directed acyclic graph (V, E). The vertex set V contains two terminals 0 and 1 with out-degree zero, and a set of non-terminal vertices with out-degree two and the following attributes.

| Attribute       | Type         | Description                                             |
|-----------------|--------------|---------------------------------------------------------|
| pos(v), neg(v)  | Var          | Positive variable $x_i$ , and negative variable $x_j$ . |
| op(v)           | $\{<,\leq\}$ | $Operator < or \le$ .                                   |
| const(v)        | $\mathbb{D}$ | $Constant \ c.$                                         |
| high(v), low(v) | V            | High-branch h, and low-branch l.                        |

The set E contains the edges (v, low(v)) and (v, high(v)), where  $v \in V$  is a non-terminal vertex.

Now we have the definition of the structure. We also give the semantics of this structure.

**Definition 7** (DDD semantics). The semantics of a vertex is defined recursively by the function  $\mathcal{V}: V \to \mathbf{Exp}$ :

- $\mathcal{V}[[0]] \stackrel{\text{def}}{=} false$ ,
- $\mathcal{V}[[1]] \stackrel{\text{def}}{=} true$ ,

$$\bullet \quad \mathcal{V}[[v]] \overset{\text{def}}{=} \begin{cases} (pos(v) - neg(v) < const(v)) \rightarrow \mathcal{V}[[high(v)]], \mathcal{V}[[low(v)]] \text{ if } op(v) = <' \\ (pos(v) - neg(v) \leq const(v)) \rightarrow \mathcal{V}[[high(v)]], \mathcal{V}[[low(v)]] \text{ if } op(v) = ' \leq ' \end{cases}$$

In the semantics we only take the information on the high edges. The implicit information on the low edge is not used. A node can thus only represent an upper-bound which is either true or false, it can not implicitly represent a lower-bound on the same variable pair. This representation also makes it easier to work with the state-vectors of LTSmin.

In [27] a canonical form for DDDs is discussed, also called a fully reduced DDD. Only definitions are given here, no algorithms to reach this form. It is stated that it is difficult to reach this fully reduced form. It is not clear if they managed to make their apply function in such a way that it maintains canonicity, as the function for BDDs does. To reach canonicity, local reductions and ordering are a first step, but it is not enough due to dependencies among the constraints. For BDDs the local reductions and ordering are sufficient to reach a canonical form. First we give some notational shorthands and then we define an ordering and local reductions on DDDs.

$$var(v) = (pos(v), neg(v))$$
  
 $bound(v) = (const(v), op(v))$   
 $cstr(v) = (var(v), bound(v))$ 

To order DDD nodes we use the operator  $\prec$ . This orders variables and variable pairs in a predefined order. It orders bounds by increasing constants, and the < operator before the  $\leq$  operator. So a node v with bound(v) = (0, <) comes before  $bound(u) = (0, \leq)$  which comes before bound(w) = (1, <).

**Definition 8** (Ordered DDD [27]). An ordered DDD (ODDD) is a DDD where each non-terminal vertex v satisfies:

- 1.  $neg(v) \prec pos(v)$ ,
- 2.  $var(v) \prec var(high(v))$ ,
- 3.  $var(v) \prec var(low(v))$  or var(v) = var(low(v)) and  $bound(v) \prec bound(low(v))$ .

After ordering a DDD some local reductions can be defined to reduce the size of a DDD.

**Definition 9** (Locally Reduced DDD [27]). A locally reduced DDD  $(R_LDDD)$  is an ODDD satisfying, for all non-terminals u and v:

- 1.  $\mathbb{D} = \mathbb{Z} \text{ implies } \forall v.op(v) = \leq' \leq',$
- 2. (cstr(u), high(u), low(u)) = (cstr(v), high(v), low(v)) implies u = v,
- 3.  $low(v) \neq high(v)$ ,
- 4. var(v) = var(low(v)) implies  $high(v) \neq high(low(v))$ .

We give an example of the last point in figure 7. Here both diagrams represent the same zone:  $2 < c_1 - c_2 \le 8$ . The node with < 4 on the high edge is redundant in this example and can thus be removed.

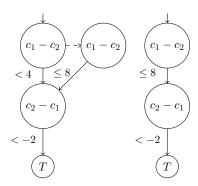


Figure 7: Local reduction

For BDDs these reductions would be enough to have a fully canonical structure. For DDDs this is not the case, due to dependencies between the bounds. In Figure 8 we give an example for this by giving two different locally reduced DDDs representing the same zone. The resulting zone of both these DDDs is drawn in Figure 9, which is the square in which both clock  $c_1$  and  $c_2$  are between 0 and 5.

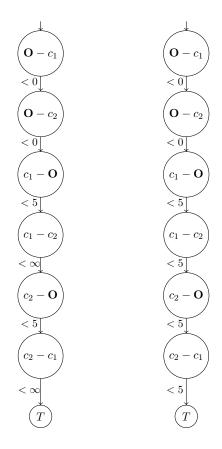


Figure 8: Two DDDs representing the same zone

The  $R_LDDD$  is clearly not canonical. We first define a path in a DDD as the bound on all high edges that are traversed in a single walk from the top node to the true node. A path will only have one bound for each variable pair.

**Definition 10** (Path-reduced DDD [27]). A path-reduced DDD  $(R_PDDD)$  is a locally reduced DDD where all paths are feasible.

This definition ensures that all paths in a DDD actually represent a zone, and that there are no redundant paths in the DDD that just represent an empty set. This usage of paths is compatible to the state vectors used in LTSmin. An  $R_PDDD$  is still not canonical. We need to define tightness, saturation and disjunctive vertices. To define tightness we first need to define dominating constraints.

**Definition 11** (Dominating constraint [27]). A constraint  $x_i - x_j \lesssim c$  is dominating in a path p if all other constraints  $x_i - x_j \lesssim' c'$  on the same pair of variables in p are less restrictive.

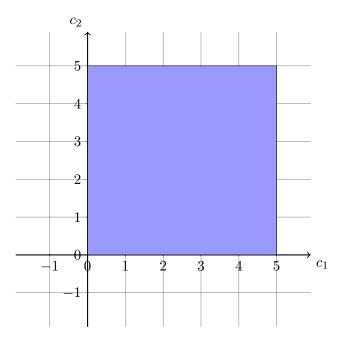


Figure 9: Resulting zone of DDDs in figure 8

**Definition 12** (Tightness [27]). A dominating constraint  $\alpha = x_i - x_j \lesssim c$  is tight in a feasible path  $[p] = [p_1] \land \alpha \land [p_2]$  if for all tighter constraints  $(c', \leq') < (c, \leq)$ , the systems  $[p_1] \land (x_i - x_j \leq' c') \land [p_2]$  and [p] have different solutions. A path p is tight if it is feasible and all dominating constraints on it are tight. An  $R_LDDDu$  is tight if all paths from u are tight.

**Definition 13** (Saturation [27]). A tight path p from an  $R_PDDD$  is saturated if for all constraints  $\alpha$  not on p, if  $\alpha$  is added to p either (1)  $\alpha$  is not dominating and tight, or (2) the constraint system  $[p_1] \wedge \neg \alpha$  is infeasible when [p] is written  $[p] = [p_1] \wedge [p_2]$  with all constraints on  $p_1$  smaller than  $\alpha$  with respect to  $\prec$  and all constraints on  $p_2$  larger than  $\alpha$ . An  $R_PDDD$  u is saturated if all paths from u are saturated.

**Definition 14** (Disjunctive vertex [27]). Let p be a path leading to the vertex u in a DDD, and assume  $\alpha = cstr(u), h = high(u),$  and l = low(u). Then u is disjunctive in p if  $[p] \wedge (\alpha \to h, l)$  and  $[p] \wedge (h \vee l)$  have the same set of solutions.

All of these definitions together lead to the following definition of a fully reduced DDD.

**Definition 15** (Fully reduced DDD [27]). An  $R_pDDD$  u is a fully-reduced DDD  $(R_FDDD)$  if it is tight, saturated and has no disjunctive vertices.

We assume that this fully-reduced DDD is canonical and work from that. It is not ensured that this is actually the case, there is no proof for it. Conjecture 1 (Canonical DDD [27]). If u and v are  $R_FDDDs$  with the same set of solutions then u = v.

DDDs can also be used to represent the discrete variables in automata. This is done by translating the variable into a difference constraint. For example  $x_1 = 3$  will be translated into  $x_1 - 0 \le 3 \land 0 - x_1 \le -3$ , thus resulting into a DDD with two nodes. We will instead connect the DDD to an LDD to represent discrete variables to limit the number of nodes.

So far we only found the results of two benchmark tests of DDDs, Milner's scheduler and Fischer's protocol [25]. Here the DDD approach has been compared with KRONOS and Uppaal which were both slower than the DDD implementation. The results of these benchmarks show no memory usage or number of nodes needed.

## 3.5 List Decision Diagram

We will introduce the LDD structure here. An LDD is used to represent variables with integer values, not only binary values. In contrast to MDDs this is done for one value per node, resulting in nodes with equal size. We will first define the LDD structure.

**Definition 16** (List Decision Diagram). A List Decision Diagram (LDD) is a directed acyclic graph (V, E). The vertex set V contains two terminals 0 and 1 with out-degree zero, and a set of non-terminal vertices with out-degree two and the following attributes.

| Attribute       | Type         | Description                      |
|-----------------|--------------|----------------------------------|
| var(v)          | Var          | Variable x                       |
| const(v)        | $\mathbb{Z}$ | $Constant \ c.$                  |
| high(v), low(v) | V            | High-branch h, and low-branch l. |

The set E contains the edges (v, low(v)) and (v, high(v)), where  $v \in V$  is a non-terminal vertex.

The definition is almost equal to DDDs, Definition 6. The difference is the operator that is not in LDDs. LDDs can be seen as a DDD with not a < or  $\le$  as operator, but a =.

# 4 Implementation

This section will go more into detail about the implementation we made and the design choices that were needed.

## 4.1 Flattening DBM

In the LTSmin implementation that we already have the state vector consists of all discrete variables and an 64 bit pointer to a C++ class containing a DBM [12]. For a symbolic solution this pointer has no meaning, thus we take the actual values from the DBM and put these into the state vector. This increases the length of a state vector, but does not need to increase the memory footprint, as the DBM was already stored. In the DBM library we use a DBM is represented by a one-dimensional array of 32-bit integers. In the integers the complete bound is stored, so both the operator and the constant value. We flattened the DBMs to work with a symbolic solution. We only did this on the edges of the successor function. So this function reads a state with a flattened DBM as input and returns successor states, again with flattened DBMs, internally the original DBM representation is still used. This way the code had to be adapted the least. In this flattening step we removed the diagonal elements of each DBM. By the way DBMs are constructed this will always represent the difference between a clock and itself. This difference is by definition always 0, so it can be removed, and hard coded be set to  $(0, \leq)$  internally. This reduces the number of state variables in the state vector by one for each clock. This flattening of DBMs results into a language module that can be connected to all LTSmin algorithmic back-ends for state-space generation.

## 4.2 Dependency Matrices

To get the best possible result of the regrouping algorithms, the dependency matrices had to be made as sparse as possible. This has been done for both the read matrix and may-write matrix. For even better results, also the must-write matrix is needed. This needs effort when analysing the code, this can be done, but is left out for this thesis. To generate the matrices we parse the Uppaal models. First of all, all C-like code is parsed. Here it is stored per function which variables are read and written, and which other functions are called. Next all transitions are parsed, here some variables are read and written directly. Transitions can also call functions, in such cases the variables that were found in the parsing of these functions are added to the read and may-write variables of the transition. In the third step we need to look at the time extrapolation. This extrapolation is based on the value of the location variable, so it results in a read dependency. In some cases, there is no difference between all possible location values for this

extrapolation, so a location does not need to be read. A final step is that a location variable that can be urgent or committed always has to be read. If this location is in an urgent state, than no other transitions can happen, so all other transitions have to check that they are not in an urgent state. In which only an other transition can take place. The correct filling of the matrices is only for the discrete parts of the states. For the zone part, to optimizations have been created. The matrices for these parts will always be filled. The problem is that changing only one clock can have a much larger impact on a DBM when a normal form is used. The flattened DBMs and the sparser dependency matrices together enable the reordering algorithms in the symbolic back-end of LTSmin to be used.

# 4.3 DBM reduction

We work towards a fully reduced DDD solution. This is already started at the language module side. The next-state function will only return tight and saturated paths. In DBM terms this is a minimal constraint system [6]. As the length of a state-vector cannot be changed on the fly, all removed constraints are set to  $(\infty, <)$ . This means that there is no upper-bound on the variable pair of that position. In Algorithm 2 which uses Algorithm 1 we show the algorithm that determines all bounds that are not needed an can be set to  $(\infty, <)$ . The DBM library cannot use these minimal constraint systems. In the next-state function the incoming DBM is tightened, then all needed operations for the successor generation are conducted and if a successor is returned, its DBM is again turned into a minimal constraint system. This will give algorithmic overhead for each next-state call. The advantage of this procedure is that many bounds will be redundant and turned into  $(\infty, <)$ . In the symbolic back-end these bounds which are the same can be shared in a single node. Thus taking more time in the successor generator, it can also reduce the number of nodes in the algorithmic backend. This reduction is used in the successor generator for the LDD symbolic back-end, and will also be used for the DDD solution.

#### Algorithm 1 Reduce

```
1: procedure Reduce(dbm, dim)

2: for i \in dim do

3: for j \in dim do

4: for k \in dim do

5: if !(dbm[i, k] \lor dbm[k, j] \lor dbm[i, j] on diagonal) then

6: if dbm[i, k] + dbm[k, j] \le dbm[i, j] then

7: dbm[i, j] := \infty
```

# Algorithm 2 Reduce

```
1: procedure ReduceZero(dbm, dim)
       placed[dim] all 0
2:
       red[dim, dim] all 0
3:
        eq[dim, dim] all 0
 4:
       cl := 0
5:
       newDBM[dim, dim] diagonal \infty rest 0
6:
       for i \in dim \ \mathbf{do}
7:
           if placed[i] = 0 then
8:
               for j \in \dim do
9:
                   if dbm[i, j] + dbm[j, i] = 0 then
10:
                       placed[j] := 1
11:
                       eq[cl, j] := 1
12:
               cl + +
13:
       repr[cl]
14:
       for i \in cl do
15:
16:
           for j \in dim \ \mathbf{do}
               if eq[i,j] = 1 then
17:
                   repr[i] := j
18:
                   break
19:
       clg[cl, cl]
20:
21:
       for i \in cl do
           for j \in cl do
22:
               clg[i,j] := dbm[repr[i], repr[j]]
23:
        Reduce(clg, cl)
24:
       for i \in cl do
25:
26:
           for j \in dim \ \mathbf{do}
               if eq[i,j] = 1 then
27:
28:
                   for k \in dim \ \mathbf{do}
                       if eq[i,k] then
29:
                           newDBM[j, k] = dbm[j, k]
30:
            for j \in cl do
31:
               newDBM[repr[i], repr[j]] := clg[i, j]
32:
33:
       return newDBM
```

#### 4.4 Connecting LDD and DDD

To represent the discrete variables in states LDD nodes are used. The structure of these nodes is quite similar to DDD nodes. We decided to not mix the nodes, but to first have all the LDD nodes and then all DDD nodes in the tree. In the state vector the first part exists of all discrete variables, the last part are the DBM variables. The top of the diagram can be seen as a MTLDD(Multi-Terminal List Decision Diagram) with not values on the leaf nodes, but pointers to DDD nodes. The DDD part is not influenced by the LDD part, as a node is only influenced by the nodes below it, it has no information about the nodes above it in the diagram. This strict separation between LDD and DDD nodes makes that the reordering algorithms can not be used. The lack of reordering makes it also possible to reconstruct the DBMs on the DDD side. This is used for the minus function which we discuss later.

#### 4.5 DDD nodes

We used the basis of the LDD package in Sylvan to create our DDD nodes. The nodes are the same as the LDD nodes, only two previously unused bits are now used to store the operator and the type of the node. DDD nodes are stored in 128 bits, represented as a struct of two 64 bit integers. The hashtable that is already used by Sylvan is specifically for 128 bit entries, so the DDD nodes can use the same hashtable. A node is in C code represented as follows:

```
struct dddnode {
     uint64_t a, b;
} * dddnode_t;
```

In this struct the value(32 bits), the true edge(40 bits), the false edge(40 bits) and a type bit, operator bit and flag bit are stored. These values are not specifically named in the struct, all values are stored in the two integers a and b. Figure 10 shows how this is coded in memory. The type, operator and flag bit are stored in the black areas. We do not show them explicitly due to the scale. The type bit indicates if a node is a DDD or an LDD node, if it is set to 0 it should be treated as a normal LDD node. The operator bit shows if the operator is  $\langle$  or  $\leq$ , this can only be used if the type bit is also set to 1(DDD). The flag bit is used in some algorithms to indicate that a certain node has already been visited. All of this is stored compactly in the two 64 bit integers. The total information is 115 bits, so there are still 17 unused bits, all unused bits are set to 0. The depth of the node is not stored, this can be calculated by going down through the structure. This implies that no level can be skipped. Other DDD algorithms and reductions show that some levels are not needed. We solved this by indication a skipped level

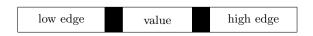


Figure 10: In memory representation of DDD node

by  $(\infty, <)$ , which is true for every upper bound. For such nodes the false edge will always directly lead to the false end node.

## 4.6 Creating Nodes

To create a node a special MK function is used. This function will ensure that a DDD is always locally reduced. This MK function is shown in algorithm 3. This function ensures the correct total structure and puts newly created nodes in the hashtable. The actual creation of a node is done in the MakeNode function that is called inside the MK function. The code for the MakeNode function is not shown here as it is only technical coding, putting all the information in the struct.

#### Algorithm 3 MK

```
1: procedure MK(value, h, l, type, op)
2:
       if h = 0 \land type = LDD then
           return l
3:
       if h = 1 \wedge l = 1 then
4:
5:
           return 1
       if h = 0 \wedge l = 0 then
6:
           return 0
7:
       if h = 0 \land l \neq 0 then
8:
           return 1
9:
10:
       if h = high(l) then
           return l
11:
       node = MAKENODE(value, h, l, type, op)
12:
       if node \notin table then
13:
           Put(node)
14:
       return node
15:
```

## 4.7 Apply

One of the core operations on DDDs is the apply operation. This operation takes two DDDs and a binary operator and combines the two DDDs according to the operator. The apply function for DDDs is a generalisation of the function for BDDs. In [27] a general definition of the algorithm is given. We turned this more mathematical definition into an algorithm, we give pseudo-code in Algorithm 4. The algorithm will search down to the

leaf nodes and use the operator on that level. We can optimize this a bit for cases where we see two equal nodes, or only one leaf node. In Algorithm 5 we give the pseudo-code for the apply function with the or operator, or the union function, this way we can increase performance by not going down the entire diagram if we already found a false leaf, or two equal nodes. The apply operator does not ensure path-reducedness, even when both inputs are path reduced.

#### **Algorithm 4** Apply

```
1: procedure Apply (v1, v2, op)
        if v1 \in \{0,1\} \land v2 \in \{0,1\} then
 2:
 3:
             result \leftarrow (v1 \ op \ v2)
         else if var(v1) \prec var(v2) then
 4:
             high \leftarrow Apply(high(v1), v2, op)
 5:
             low \leftarrow Apply(low(v1), v2, op)
 6:
 7:
             result \leftarrow \text{MK}(cstr(v1), high, low)
         else if var(v2) \prec var(v1) then
 8:
             high \leftarrow Apply(high(v2), v1, op)
 9:
             low \leftarrow Apply(low(v2), v1, op)
10:
11:
             result \leftarrow MK(cstr(v2), high, low)
         else if v1 \prec v2 then
12:
             high \leftarrow Apply(high(v1), high(v2), op)
13:
14:
             low \leftarrow Apply(low(v1), v2, op)
             result \leftarrow \text{MK}(cstr(v1), high, low)
15:
16:
         else if v2 \prec v1 then
17:
             high \leftarrow Apply(high(v1), high(v2), op)
             low \leftarrow Apply(v1, low(v2), op)
18:
             result \leftarrow \text{MK}(cstr(v2), high, low)
19:
         else if v1 = v2 then
20:
             high(v1) \leftarrow Apply(high(v1), high(v2), op)
21:
             low(v1) \leftarrow Apply(low(v1), low(v2), op)
22:
23:
             result \leftarrow MK(cstr(v1), high, low)
        return result
24:
```

#### **4.8** Minus

The minus function, used for the reachability, has not been implemented as an DDD functions. This function is different to other functions, as information has to be transferred over different levels. For simple cases, an upper-bound in one of the operands of the minus, can become a lower-bound in the result, and vice-versa. A simple one dimensional example is [0..8]/[0..4), this will result in [4..8]. In this case the 4 is the upper-bound of the subtrahend. It will however become the lower-bound of the difference.

## Algorithm 5 Union

```
1: procedure Union(v1, v2)
        if v1 = v2 then return v1
        else if v1 = false then return v2
 3:
        else if v2 = false then return v1
 4:
        else if var(v1) \prec var(v2) then
5:
             high \leftarrow \text{Union}(high(v1), v2)
6:
 7:
             low \leftarrow Union(low(v1), v2)
             result \leftarrow \text{MK}(cstr(v1), high, low)
8:
9:
        else if var(v2) \prec var(v1) then
10:
             high \leftarrow \text{Union}(high(v2), v1)
             low \leftarrow \text{Union}(low(v2), v1)
11:
12:
             result \leftarrow \text{MK}(cstr(v2), high, low)
        else if v1 \prec v2 then
13:
             high \leftarrow \text{Union}(high(v1), high(v2))
14:
15:
             low \leftarrow Union(low(v1), v2)
             result \leftarrow \text{MK}(cstr(v1), high, low)
16:
        else if v2 \prec v1 then
17:
             high \leftarrow \text{Union}(high(v1), high(v2))
18:
             low \leftarrow Union(v1, low(v2))
19:
             result \leftarrow \text{MK}(cstr(v2), high, low)
20:
        else if v1 = v2 then
21:
             high(v1) \leftarrow \text{Union}(high(v1), high(v2))
22:
             low(v1) \leftarrow UNION(low(v1), low(v2))
23:
24:
             result \leftarrow \text{MK}(cstr(v1), high, low)
        return \ result
25:
```

As lower- and upper-bounds are saved on different levels in DDDs this makes the function different from all other functions, which only look at values on the same level.

In figure 11 we have a two-dimensional example of how the minus function can become more complex for multiple-dimensions. In this case we make a hole in a larger zone. Both the minuend and the subtrahend are represented by a DDD with a single path, as shown in figure 12. For simplicity we removed the diagonals in this example, as they play no role. The difference however becomes a DDD with 4 paths and 10 nodes, figure 13. Again a lot of upper- and lower-bounds are switched. Already for this example we could not find a algorithm that does this in general. For more dimensions, and DDDs with already multiple paths the problem will only get harder. That is why we returned to a DBM function for this.

The DBM function we use is defined in the Uppaal DBM library. The minus function is defined over a federation of DBMs. This federation is a C++ class containing multiple DBMs. This federation is needed as we can do a minus over a collection of zones, multiple paths in the DDD, and the result can contain multiple zones. As already shown in the example of figure 11. For this function we first take the normal LDD minus function over the discrete part. At the first DDD level, representing the zones, the DBM function is called. From this level all possible paths are searched, and for each path a DBM is created and tightened. All these DBMs are put in a federation, on which the library function can be called. The result is again (a possibly empty) federation. If the federation is empty, simply a DDD-false node is returned. Otherwise each DBM is turned into a DDD path and these paths are made into a single structure using the union function.

#### 4.9 Relation

The transition relation we use is stored in an LDD structure. Both bound values and operators are implicitly encoded in a single value, like in the DBM library. When creating new nodes, the nodes are matched against the state space. By checking the type of the node on the current level it can be checked if the relation node should be treated as a normal LDD node with a discrete variable, or as an LDD node which implicitly stores an upper-bound. The choice to not use the DDD type nodes in the relation has been made to have better support for possible future reordering options. If reorderings are used, it would need explicit information for which relation levels contain zone variables, with matching against the states this extra information is not needed.

#### 4.10 BFS

The DBM minus function we use is quite expensive. As it is imported from a library we do not know the exact complexity. To overcome this problem we will use two different versions of the search algorithm. Our second version will not use the minus function. In algorithm 6 we show the standard BFS algorithm, this will be the first algorithm we use. Algorithm 7 shows how we can edit this algorithm. The constraint of the loop is changed from an empty check of the current set, to a check that the total visited set has not been changed. This check is basically the same, the first checks if now new states are found, the second checks that the total state-space has not been changed. This change now shows that the minus is not necessary any more, as shown in algorithm 8. This version uses the same check as the previous one, but now the minus of the current and the visited set has been removed. The implication is that the current set will in some cases be larger than in the previous algorithm. This will have some negative impact on the next-state calls, which will take more time. Not using the expensive minus function might compensate for that. We have implemented these two versions in the bfs-prev algorithm [22]. This is the default search algorithm that is used in LTSmin. In the results section we will show the outcome of both BFS algorithms.

# Algorithm 6 BFS

```
1: procedure BFS(initial)
2: vis := cur := initial
3: while cur \neq \emptyset do
4: cur := next(cur)
5: vis := vis \cup cur
6: cur := cur \setminus vis
```

#### Algorithm 7 BFS

```
1: procedure BFS(initial)
2: vis := cur := initial
3: vis_{prev} := \emptyset
4: while vis \neq vis_{prev} do
5: vis_{prev} := vis
6: cur := next(cur)
7: vis := vis \cup cur
8: cur := cur \setminus vis
```

### Algorithm 8 BFS

```
1: procedure BFS(initial)
2: vis := cur := initial
3: vis_{prev} := \emptyset
4: while vis \neq vis_{prev} do
5: vis_{prev} := vis
6: cur := next(cur)
7: vis := vis \cup cur
```

# 4.11 State-space count

One of the basic outputs that LTSmin gives when calculating a state-space, is the number of states. For timed automata this is not trivial, as a state is not well defined. Systems with digitization will have other states than systems which use zones for representing time. Even for zones no clear definition of a state exists, as DBMs give no canonical representation of zones, when they are not convex. Now our representation with DDDs will again give another result. We decided to take as the state count only the number of discrete states. This number should be equal for each method for analysing timed automata.

#### 4.12 Successor Generator

The language module uses the opaal successor generator for Uppaal models. This generator is written in Python and reads Uppaal XML files. A C++ file is generated from this. These files are compiled to object files which can be dynamically linked to LTSmin. The structure of the next-state function is slightly different from [12]. The new structure can be found in algorithm 9. At line 6, the function iterates over all outgoing transitions from the current location. If it is an internal transition the successor will be generated on lines 9-18. If it is a sending transition, receivers will be searched for on lines 20-32. In the generated C++ code the loops on lines 5 and 21 are unrolled. The algorithm contains several empty checks, on lines 8, 13, 23 and 27. After each addition of constraints the DBM can possibly be empty. If the DBM is at one of these points empty, no point in time exists where the new state can exist, so further exploration of the transition is not needed. After the empty checks on lines 13 and 27 the extrapolation and the reduction are done. These operations can not empty the DBM, the extrapolation can make the zone larger, not smaller. The reduction will not change the zone at all, only its representation. If the DBM is not empty before these operations it can safely be put into the output.

## Algorithm 9 Next-State

```
1: procedure NEXT-STATE(s_{in} = \{l_1, ...l_n, l_{n+1}, ..., l_m\})
          out\_states := \emptyset
          D := \text{CreateDBM}(\{l_{n+1}, ..., l_m\})
 3:
          TIGHTENDBM(D)
 4:
          for l_i \in l_1, ..., l_n do for all l_i \xrightarrow{g,a,r} l'_i do
 5:
 6:
                    D' := D \cap g
 7:
                    if D' \neq \emptyset then
 8:
                          if a = \tau then
 9:
                               D' := D'[r]
10:
                               D' := D' \uparrow
11:
                               D' := D' \cap I_C^i(l_i') \cap \bigcap_{k \neq i} I_C^k(l_k)
12:
                               if D' \neq \emptyset then
13:
                                    D' := D'/B(l_1, ..., l'_i, ..., l_n)
14:
                                    ReduceZero(D')
15:
                                    \{l'_{n+1},...,l'_m\} := \text{FlattenDBM}(D')
16:
                                    s_{out} := \{l_1, ..., l'_i, ..., l_n, l'_{n+1}, ..., l'_m\}
17:
                                    out\_states := out\_states \cup s_{out}
18:
19:
                          else
                               if a = ch! then
20:
                                    for l_j \in l_1, ..., l_n, j \neq i do
21:
                                         for all l_j \xrightarrow{g_j, ch?, r_j} l'_j do
if D''" = D' \cap g_j \neq \emptyset then
22:
23:
                                                    D'' := D''[r][r_j]
24:
                                                    D'' := D'' \uparrow
25:
                                                   D'' := D'' \cap I_C^i(l_i') \cap I_C^j(l_j') \cap \bigcap_{k \neq \{i,j\}} I_C^k(l_k)
26:
                                                   if D'' \neq \emptyset then
27:
                                                         D'' := D''/B(l_1, ..., l'_i, ..., l'_j, ..., l_n)
28:
                                                         ReduceZero(D'')
29:
                                                         \{l'_{n+1}, ..., l'_{m}\} := \text{FLATTENDBM}(D')
30:
31:
     \{l_1,...,l'_i,...,l'_j,...,l_n,l'_{n+1},...,l'_m\}
32:
                                                         out\_states := out\_states \cup s_{out}
33:
          return out_states
```

# 4.13 Time Extrapolation

In the successor generator step a time extrapolation is used. This extrapolation step reduces the number of DBMs created and makes sure that this number is finite. The most coarse abstraction as described in [4] is used. This extrapolation reduces the number of zones that are explored significantly. It also makes that less improvements can be made on the representation of the zones, for some models all states are extrapolated to the same zone, so nothing interesting happens at the timed side of the model any more. In opaal this algorithm is implemented in such a way that all Uppaal locations are always read. The maximum extrapolation is based on the values of these locations. Only if there is no difference between all values for a certain location, it is not needed to read this. This results into an densely populated dependency matrix.

#### 4.14 Animo Models

We started the project with ANIMO models that were not compatible with opaal. As opaal does only support a subset of all options of Uppaal. First of all we changed the model, such that it does not use global variables in in the system declaration. Also some smaller changes to the use of structs had to be made. This resulted in a basic ANIMO model that is compatible. Larger models are still not compatible due to clock guards on input synchronization channels. This is a feature only recently implemented by Uppaal(version 4.1.3). Opaal does not support this feature, and its semantics are not completely clear, as it is not described in the manual. Adding this to opaal can be done, but is not trivial. This improvement of the language module is out of scope of this thesis.

#### 4.15 Correctness

The DDD state space generator needs to be checked for correctness to say anything about the results. We only checked for partial correctness by comparing discrete states. Counting the discrete state-space can be done by counting the number of paths until the first DDD level in the diagram. These numbers were compared to the discrete state space in the LDD solution without reordering, here the discrete state-space can also be determined by counting paths until the first level representing zones. We can not directly compare state-spaces to Uppaal, different representations of the timing part of the state-space can give different numbers.

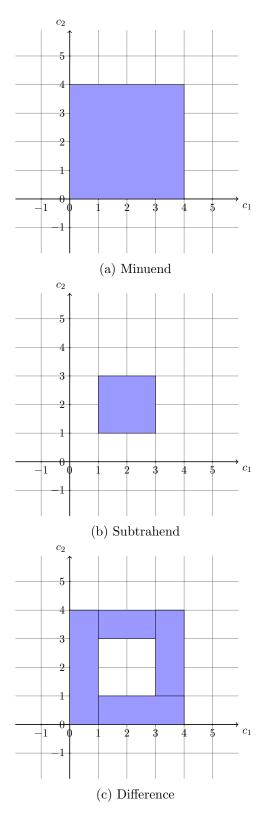


Figure 11: Minus complexity example \$32\$

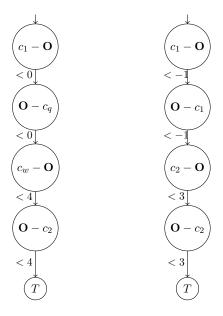


Figure 12: DDD representation of the minuend and subtrahend of figure 11

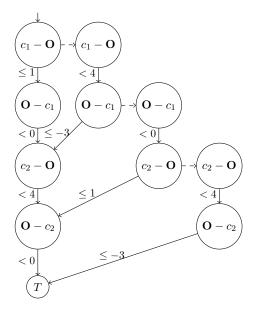


Figure 13: DDD representation of the difference of figure 11

# 5 Experiments

Below we describe the different models we used to run the benchmarks. We tried to find models that scale up for a number of nodes or processes, so that we can also check the behaviour of our approaches for different sizes of the same model. In this section we use the terminology 'locations' and other 'discrete variables'. The definition of timed automata does not have this difference, but we use it to describe models, because the time extrapolation is dependent on locations, and not on the other discrete variables. This dependency fills a large part of the dependency matrices. In this section, a location is a state in the Uppaal transition system editor, the other discrete variables are declared in the C-like syntax that Uppaal uses.

#### 5.1 Viking

The set of Viking tests, models the classical Viking and bridge problem. It models 4 Vikings at a dark bridge, they only carry one torch. The torch is only strong enough to give light for 2 Vikings. All Vikings have different walking speeds, a faster Viking will have to adapt to a slower one, when crossing the bridge together. The walking speed of the Vikings is modelled by time constraints on the action of letting go of the torch. The model has a low number of discrete variables, one per Viking, one for the torch and an indicator for the side of the bridge on which the torch is. It has a global clock and a clock per Viking. The standard version of this problem has 4 Vikings. This can however be generalized to n Vikings.

The model results in a densely filled dependency matrix. The torch and all Viking variables are always read for the time extrapolation. Only the side indicator is not read always. The write matrix is sparser.

The difference between the LDD and DDD representation is quite small for this model. In the extrapolation step all clock zones are set to  $[0..\infty]$  for all states, so in both diagrams the zones are represented by a single path. So the interesting things are only happening in the discrete parts.

#### 5.2 Fischer

Fischers mutual exclusion protocol [19] is modelled for a number of processes. There is no synchronization between processes, only blocking of actions can occur. This model has a slightly higher number of discrete variables compared to the Viking tests. Each process has a location and an id. The model also has 2 global discrete variables. Each process has a local clock, no global clock is used.

The dependency matrix of this model has some sparse rows, as each model has an id, which is a constant and can only be read. Again all the location variables are always read due to the time extrapolation.

#### 5.3 CSMA-CD

The Carrier Sense Multiple Access/Collision Detection [33] is modelled for a number of senders. The model has a few discrete variables. Each sender only has a location and only one global counter is used. Each sender and the bus have a local clock. The model uses a lot of synchronizations between the senders and the bus.

#### 5.4 Animo

We could not use the ANIMO models, only the smallest model with no synchronizations was possible. As we started the project to work on ANIMO models, we still included that single model in the benchmark set. It is a model with only one node, so only one location variable. The model has two clocks, a global clock and a clock for the node. Further it does have quite a large number of discrete variables. Both the global declaration and the node have a portion of c-like code with a number of global variables.

This results in a model with a quite sparse dependency matrix, as only the single location is used for the time extrapolation. We expected this model to have good performance for the LDD method with variable reordering.

### 5.5 Lynch-Shavit

The Lynch-Shavit mutual exclusion protool [21] is modelled for different number of processes. The structure of the model is quite like the Fischer model. It only uses one global variable more than Fischer.

#### 5.6 Milner

Milners scheduler [23] is modelled for a number of nodes. The structure is like that of the CSMA-CD model, except that it does not use a bus. The model has a lot of synchronizations between the nodes, an between the node and a global process. Each node has two clocks, so the zone representation blows up quickly.

#### 5.7 Other models

We also used some models that we could not scale up enough due to memory/time limitations, or that could not scale up due to the nature of the model. We will not describe those models into detail. These models were the critRegion, Critical, bocdp(-fixed) [17], bando and timelock model.

#### 5.8 Benchmark Runs

We ran benchmarks with the different solutions we described to compare them to each other. The DDD solution has been ran with the two BFS-prev algorithms as explained in section 4.10, we also used the bfs algorithm from LTSmin. For the LDD solution we only used the original BFS-prev algorithm. We ran this without reordering and with some of the reordering algorithms that LTSmin provides. We used the options gsa, rb4w, cw, rs,rn, rs,ru. These results are compared to the explicit-state multi-core LTSmin and the original Uppaal. All experiments have been done with and without the DBM reduction. All solutions are ran with one thread. The LDD and explicit-state multi-core solutions can be ran with multiple treads. The DDD solution does not support this, so for comparison reasons all methods are used in single-core mode. We also used the new language module with flattened DBMs in combination with the explicit-state multi-core tool.

### 6 Results

In this section we will only give an overview of all experiment results. The complete tables with all results are added in appendix A. In table 2 and table 3 we have summarized the results for some of the most interesting models. For the DDD, LDD and mc-flattened column, we give the best result that was found in the different experiment setups.

#### 6.1 Time

The timed results show that our symbolic solutions are slower for almost all models, compared to both Uppaal and the explicit state multi-core tool. Only for the small bocdp models we have a symbolic solution that is faster than Uppaal.

One of the reasons we found was the high number of next-state calls. This is much higher than for the explicit-state tool as we partitioned the next-state function. For symbolic solutions this should be and advantage, as locality of transitions can be used. This same advantage should hold for the LDD solution we have, but the dependency matrices are too densely filled to give a real advantage. For the DDD solution we do not even make use of these localities, so there all advantages are lost. To confirm this hypothesis we also ran experiments without the partitioned next-state function. This gave for almost all models much better results. The results differ from a small loss in speed to a speedup of a factor 10. This is still not enough to compete with Uppaal, but makes it possible to explore larger models within a given time-bound.

Another problem seems to be the flattening of the DBM. This is an extra action that has to be executed in each next-state call, compared to the multi-core tool. This flattening is not a really expensive operation, it is only copying values, but it has to be executed a lot of times. For the DDD approach it is also necessary to close each DBM, as the DDD structure does not guarantee this. This is a more expensive operation and will also be executed in each next-state call. We implemented this in the language module, this closing is used for all experiments, so also for the experiments where it is not explicitly needed. This will also explain why the explicit state tool with subsumption is in most cases faster than the explicit state tool with flattened DBMs and without subsumption, even for models where subsumption will not have a real role, like the Viking models.

The last problem we see are the large state-vectors. This is mostly due to the quadratic size of the DBMs. For each of these variables a DDD level is created. As we have shown earlier, in some cases a lot of these levels will not have any impact on the zone represented. We can exploit this a little by setting these nodes to  $(\infty, <)$ , but the time-expensive function that does this has too much of an impact on the timing results. The diagram

|                    | DDD   | LDD   | mc-flattened | mc-original | uppaal |
|--------------------|-------|-------|--------------|-------------|--------|
| fischer6           | 481.9 | 48.3  | 19.2         | 0.4         | 0.0    |
| critRegion4        | 56.3  | 39.5  | 24.3         | 0.5         | 0.1    |
| Critical_04-25-50  | ТО    | ТО    | 1.1          | 0.9         | 0.6    |
| CSMACD_08          | 1.9   | 7.3   | 6.9          | 0.5         | 0.1    |
| viking12           | 17.6  | 18.7  | 10.4         | 0.7         | 1.0    |
| Lynch5-16          | 34.2  | 120.0 | 50.0         | 0.3         | 0.0    |
| bocdp              | 0.1   | 0.2   | 0.2          | 0.0         | 0.2    |
| bocdpFIXED         | 0.2   | 0.2   | 0.1          | 0.0         | 0.3    |
| bando              | 0.2   | 0.2   | 0.1          | 0.0         | 0.3    |
| Milner-8Nodes-flat | 0.4   | 1.2   | 1.4          | 0.1         | 0.0    |
| hddi_input_10      | ТО    | 93.3  | 43.1         | 0.0         | 0.0    |

Table 2: Time Results

|                    | DDD   | LDD    |
|--------------------|-------|--------|
| fischer6           | 15156 | 85041  |
| critRegion4        | 55890 | 100006 |
| Critical_03-25-50  | 3291  | 17505  |
| CSMACD_08          | 36098 | 321001 |
| viking12           | 342   | 342    |
| Lynch5-16          | 49430 | 112397 |
| bocdp              | 487   | 355    |
| bocdpFIXED         | 488   | 427    |
| bando              | 488   | 425    |
| Milner-8Nodes-flat | 11012 | 30883  |
| hddi_input_10      | ТО    | 454246 |

Table 3: Node Results

could make much more use of this by skipping levels. This is not possible in our implementation as we only implicitly store the level of each node by its depth.

#### 6.2 Memory

We have not measured memory usage. A good symbolic solution will use a lot of memory for caching when it is available. Comparing this to other solutions which use less caching will not be representative. We do compare the number of nodes between the different solutions.

For most models the best DDD solutions uses less nodes than the best LDD solution. This is what we expected as local reductions on clocks can be made. For the smallest models the LDD sometimes gives less nodes for some reorderings. These models have such low number of clocks that no

reductions can be made yet. The bocdp and bando models are the largest models which have a lower LDD than DDD representation. These models have quite a high number of discrete variables with a low number of clocks. For most larger models the LDD solution without reordering is smaller than with reordering. This is probably due to the densely filled matrices, so no good reorderings can be created from them.

There is a difference between the number of nodes for the normal BFS and the BFS without minus. This is possible because we do not use a canonical form of DDDs. Most results show a higher number of nodes for the runs with the minus. In figure 14 we show an example of how this can happen. We assume all zones in the figures belong to the same set of locations. In figure 14a we have the zone that is already visited. Now a new state with the zone in figure 14b is discovered. If the minus is not used, successors of this state are directly generated from the set of locations and this zone. If the minus is used the first zone will first be subtracted before successors are generated. The result of the subtraction is shown in figure 14c. This is not a convex zone, so a DDD with multiple paths is needed. From this state also other successors can be generated, possibly needing more nodes to be represented. If the newly generated states are then unioned with the visited set the result can again have more nodes than the version without minus. The less fractionated zones in the current set can also have implications on the time results, as less work in the next-state function is needed. On the other hand the next-state function can also need extra time, as some states would otherwise have completely been removed from the current set, and no work for that states would need to be done.

The DBM reduction does not give the results we aimed for. For most models exploration is faster without the reduction. This is due to the expensive algorithm that the reduction is. Also the reduction of the number of nodes is not what we hoped for. Most models get more nodes when the reduction is turned on. The reduction can however still become usefull if we go to a canonical DDD representation.

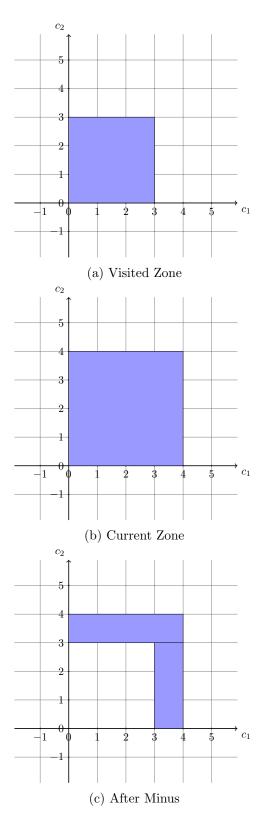


Figure 14: Minus fragmentation 40

## 7 Different Semantics

We chose in our implementation to take no information from the low edges of nodes. A node only represents an upper-bound, a false edge does not implicitly represent a lower bound. This is a design choice we made to be able to switch efficiently from the DBM representation in the language module to the DDD representation. We could however also have used a semantics where the low edges do represent a lower-bound. We did not implement this, but this section will discuss this other semantics.

**Definition 17.** The semantics of a vertex is defined recursively by the function  $\mathcal{V}: V \to \mathbf{Exp}$ :

- $\mathcal{V}[[0]] \stackrel{\text{def}}{=} false$ ,
- $\mathcal{V}[[1]] \stackrel{\text{def}}{=} true$ ,

$$\bullet \ \ \mathcal{V}[[v]] \overset{\text{def}}{=} \begin{cases} (pos(v) - neg(v) < const(v)) \rightarrow \mathcal{V}[[high(v)]], \mathcal{V}[[low(v)]] \textit{if } op(v) = ' < ' \\ (pos(v) - neg(v) \leq const(v)) \rightarrow \mathcal{V}[[high(v)]], \mathcal{V}[[low(v)]] \textit{if } op(v) = ' \leq ' \end{cases}$$

The semantics are almost equal to the one in definition 7, the difference is in the interpretation of the low edge. In this semantics the low edge does not just represent that the upper-bound is higher than the bound of the node, but the actual value of the variable is higher than the bound of the node.

### 7.1 DBM Translation

The translation from a single DBM to a DDD will not change. The translation from multiple DBMs will change neither, as that can be done as a union of DBMs which are individually translated to a DDD. The other way around, from a DDD back to a DBM becomes more complicated. For a DDD with a single path to true nothing will change. For paths that go down some low edges the translation will change. The falsification of an upper-bound, leading to a lower-bound, or a upper-bound of the inverse pair, can overrule the upper-bound of an other node. We give an example in figure 15. In this example all nodes that are not in the path we consider are hidden. The DDD will have more nodes to reach this representation. In figure 16 we have a DBM for both interpretations. In figure 16a we have the DBM as we use the interpretation from our implementation. In figure 16b the DBM of the other interpretation is shown. The difference between the two DBMs is on the position  $c_2 - O$ ). The information from the low edge of the  $O - c_2$  node has overruled the information of the high edge of the  $c_2 - O$  node. Using a canonical form of a DDD can also overcome this problem.

To make the translation from DDD to DBM correctly the relative positions of the upper- and lower-bound of each pair of variables need to be

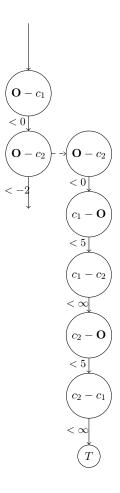


Figure 15: Implicit bound DDD

known. Also a function to determine the stronger bound of a pair needs to be created. Lastly the bounds need to be changed correctly. A < sign changes into a  $\le$  and vice versa, the constant is multiplied by -1. We give an example of this change:

$$c_1 - c_2 \nleq 3$$

$$\updownarrow$$

$$c_1 - c_2 \ge 3$$

$$\updownarrow$$

$$c_2 - c_1 \le -3$$

A similar translation will have to be conducted in the relprod function. This function does not explicitly need the DBMs. The relations that are used are however created in the language module which uses DBMs. In the current implementation, a path in the state space needs to be found that

$$\begin{array}{c} \mathbf{O} & c_1 & c_2 \\ \mathbf{O} & (0, \leq) & (0, <) & (0, <) \\ c_1 & (5, <) & (0, \leq) & (\infty, <) \\ c_2 & (5, <) & (\infty, <) & (0, \leq) \end{array} \\ \text{(a) Original semantics} \\ \mathbf{O} & c_1 & c_2 \\ \mathbf{O} & (0, \leq) & (0, <) & (0, <) \\ c_1 & (5, <) & (0, \leq) & (\infty, <) \\ c_2 & (2, \leq) & (\infty, <) & (0, \leq) \\ \end{array}$$

$$\text{(b) New semantics}$$

Figure 16: DBM's of two different DDD interpretations

has on each level the same high edges as the relation. Which low edges are traversed on the way is not important. Now this information is taken into account some changes will have to be made. A simple path in the relation, might need some false edges in the state-space to get all the correct bounds.

### 7.2 Minus

Implementation of the minus function will become easier in DDDs, no coupling to the DBM library will be needed any more. First of all we will give the complement function. We give the pseudocode for this function in algorithm 10. The algorithm switches all 0 and 1 nodes. This will have a running time of O(n) where n is the number of nodes in the tree. Our current implementation does not skip levels in the DDD towards a 1 node. This can happen in this complement function. This can be solved by filling the gap that is created with nodes with  $(\infty, <)$  as bound. Another solution would be to allow this behaviour, this would need some extra work when creating state-vectors out of a diagram.

### **Algorithm 10** Complement

```
1: procedure Complement(a)
2: if a = 0 then
3: return 1
4: if a = 1 then
5: return 0
6: h := \text{Complement}(high(a))
7: l := \text{Complement}(low(a))
8: return MK(bound(a), h, l)
```

With this function we can create a minus function, as for set theory, minus can be defined as  $A \setminus B = A \cap \overline{B}$ . Now we can build the minus function

from the complement and intersection function as shown in algorithm 11. This algorithm is probably less complex than the DBM minus we currently use. We do not know the exact complexity of the DBM minus algorithm, so we cannot call this certain.

# Algorithm 11 Minus

```
1: procedure Minus(a,b)

2: if a = 0 then

3: return 0

4: if b = 0 then

5: return 1

6: notB = \text{Complement}(b)

7: result = \text{Intersection}(a, notB)

8: return result
```

# 8 Future Work

In this section we discuss improvements that can be made for better results. In the previous section we already discussed the possibility of different semantics. This is also future work, but is written in a separate section.

#### 8.1 Canonization

The DDD package does not use any canonical form. This means that some operations like equality and emptiness become less trivial. They can however still be done. The diagrams are ordered and locally reduced. The resulting state-vectors that the language module produces are also path-reduced. Most operators do not preserve this path-reducedness, so most diagrams will not be path-reduced.

We can implement two types of reduced DDDs. A DDD that is only path-reduced can be called semi-canonical [27]. This means that a tautology and a unsatisfiable expression can only be represented by a true or false node. This will make the checking for an empty DDD trivial, the DDD is only empty if the top node is a false node. We also defined full reducedness as a DDD that is tight and saturated, and has no disjunctive vertices. This fully reduced version is assumed to be canonical. A canonical DDD will change the equality test in a simple pointer comparison of the top nodes. Several algorithms to reach a reduced form are known [26].

The canonical forms are not needed at all times, only for some functions that need the specific form. Therefore we can choose to not have a canonical form at all times. One can choose to canonize the DDD after each operation, or to do this only before operations that actually need this form. The first option will have much canonization calls, where the second option will have less. The first option however, might have a DDD that is in all cases closer to the canonical form, so canonization might take less time, especially when caching is used. The semi-canonical form can also be used for emptiness checks, as the fully reduced diagram is not needed there. To get optimal results we need to find out what is the best option.

#### 8.2 Reordering

The current DDD implementation is not compatible with the reordering algorithms. All algorithms will probably have to be changed somehow. In the current implementation it is assumed that on the top there is a set of LDD nodes, and from a certain level only DDD nodes exist. With reordering this could be mixed, so algorithms can not rely on this any more. A special case will again be the minus function. It is now done by recreating DBMs from the DDD. This can be done, as the nodes are ordered in the same way as the DBM. When reorderings are used this is not trivial any more. It

will need to be explicitly stored which variable is on which level. For the different semantics that we introduced in section 7, a similar problem will occur. We suggested a minus function using the complement. For zones the complement is well defined, as there is a  $\infty$  value representing the most upper- and lower-bounds of possible values. For discrete variables this is not directly clear.

Another option for reordering, which will probably solve some of the problems with the minus function would be reordering, but keeping the discrete and the zone parts separated. The discrete part could use the normal reordering algorithms. As the matrices for the zone variables are completely filled, the reordering algorithms can not do something useful on that level. Here experiments with manual reorderings can be tried. Now the standard ordering of the DBMs is used. It might be that having both bounds on a pair of clocks together gives better results, or maybe even other orderings.

# 8.3 Sparser Dependency Matrix

The dependency matrices are densely filled. We already discussed the problems in section 4.2. There are some solutions that can improve this. Smaller transition groups can be created, maybe even splitting the discrete part and the timed part of a transition. Another option that needs more work, is also filling the may-write matrices. The current code parsing that generates the matrices is not powerful enough to make a difference between may- and must-write variables. On this level also improvements can be made. The parts of the matrices for the zone variables are always filled, as the change of a single clock can have an impact on much of the DBM. We did not check however if an analysis can be done that finds fields which are not changed, or do not need to be read in a transition. A better analysis of the changes in DBMs can lead to sparser matrices on the zone variable side. The final improvement can be made for arrays. If the current implementation sees that a field from an array is read or written, then all fields in the array get a read or write dependency. It should be possible to only have dependencies for the fields that are actually read or written.

Splitting the discrete and timed part of a transition can also result in sparser dependency matrices. This would result in a set of discrete transition groups which only need access to the clock variables on which a bound is calculated. A single transition group will be created to model the continuation of time. This group will also do the time extrapolation. This group will probably need access to all variables as time extrapolation will still be dependent on the locations. Still also some location upperbounds can be present. It will however lead to a matrix that is less densely filled, such that the reordering algorithms and short next-state calls can result in much better performances.

### 8.4 Multi-Core

The DDD library is built in the Sylvan framework which allows for multithreaded decision diagrams. The DDD library is not suited for multithreading however. Most operations are already suited for multi-threading. The biggest problem is in the minus operation. This uses the DBM library. This part is not completely thread-safe. We expect this problem to be in the coupling between the DDD and the DBM library, in the DBM part no objects can be shared between threads. We expect that making the DDD part suitable for multi-threading will give much better time results.

# 8.5 Animo Model Compatibility

The project started to find a solution to model-check ANIMO models. This part has not succeeded. ANIMO models use a Uppaal feature that is not supported by opaal, using clock bounds on input channels. The problem why this can not be fixed directly is in the unrolling of the transitions in the next-state function. Adding the clock constraints on any of the input channels can lead to an empty DBM, in such cases the transition would not be returned. The semantics would however create the transitions, but not synchronize with the location leading to the empty DBM. To ensure that in such cases all possible transitions that can happen will be returned, a unroll of all possible combinations of synchronizing transitions would be needed. This will need a redesign of that part of the successor generator. If this functionality is added to opaal, all ANIMO models should be compatible with opaal, and thus with our symbolic solution.

#### 8.6 Subsumption

The subsumption check that is included in the multi-core explicit-state backend in LTSmin is not implemented in the DDD library. This can be implemented as a DDD operation, with the implication operator and the apply function. A check  $a \subseteq b$  will result in true if  $b \implies a$  returns true. If a canonical form is used as well, the result will be only a true node, or a single path of  $(\infty, <)$  nodes, depending on the possibility of skipping levels. This can limit the number of states added to the current set in the state algorithm, thus reducing the number of next-state calls needed. The most obvious subsumption check would be the check that a newly discovered zone is subsumed by the already visited state-space. It can however also be turned around, check if the visited state-space is subsumed by the newly discovered zone. In such a case the zone in the state space can be replaced by this new zone, such that the union function is not needed, this will not reduce the next-state calls however.

### 8.7 Checking Properties

The model-checker that we have created is only suited for state-space generation. It is not suited for property checking. One extra function is needed to use the LTSmin mu-calculus checker, which can also check CTL\* formulas. The DDD library needs to be extended with a relprev function, which returns the predecessors given a set of states and a relation. This will only result in a discrete model-checker. LTSmin is not suited for timing properties. Some timing properties can be checked by extending the model with an extra automaton.

## 8.8 Skipping Levels

In the original DDD structure it is possible to skip levels. In our implementation this is not possible as the depth of the nodes is only stored explicitly. Skipping levels can be a good option however. In our DBM reduction we already set all unused bounds to  $(\infty, <)$ . In a structure where levels can be skipped, each node containing this value can be removed. This would need a change in the DDD nodes. Two choices can be made here. Nodes can be made of variable size, such that each possible value of depth can be added. One can also choose for a fixed depth field, and thus node-size. This would give a maximum bound to the depth of a diagram. The hashtable that is currently used to store all nodes would also need some changes. The current table is built specifically for nodes of 128 bits.

We ran some small experiments to see on what scale improvements can be achieved. The number of infinity nodes in the final state-spaces of some of our larger models were counted. This was done using the bfs-prev search strategy and with DBM reduction turned on. This showed that 25% to 90% of all nodes were nodes with infinity as bound. In theory all of these can be removed. This will not only reduce the number of nodes, but can also reduce the depth of recursive calls in the DDD. This can result in significant speedups.

## 9 Conclusions

The first goal of this project was to build a symbolic model-checker for timed automata in LTSmin. This has succeeded, we have a model-checker which uses the opaal language front-end for Uppaal models, and the symbolic backend of LTSmin, using either the LDD or the new DDD package. This has all been achieved without changing the PINS structure. We only added one call to it which returns the number of discrete variables a model has.

The experiment results were not what we hoped for. The results are slower than both Uppaal, and the explicit-state tool that was already implemented in LTSmin. We were not able to replicate the results that were achieved earlier [27]. This can be explained by either the different structure of our model-checker or by the improvements that have been made by Uppaal since then [3].

One of the most fundamental problems we see are the densely filled dependency matrices. This makes it much harder to find good reorderings for symbolic structures. From our perspective this is also one of the key factors why partial order reduction for timed automata is a real challenge. Only when sparser dependency matrices can be achieved, the partial order reduction in LTSmin can be used effectively.

We have proposed a number of improvements that can be made to the DDD structure. Or even a complete overhaul of the DDDs by changing the semantics of the diagram. All of these improvements can be built upon the structure we created. With these improvements we hope that a symbolic model-checker can be built that can really compete with Uppaal and other model-checkers for timed automata.

We sticked as much as possible to the LDD design of Sylvan. This to use all of the optimizations that have already been created. On some points we expect better results when we step away from this design. Especially the skipping of levels in a diagram seems to be a serious issue, as this can reduce the size of the diagram significantly. Doing this will require some extra effort, as important parts of Sylvan, as the hashtable storing all nodes, cannot be used directly.

## References

- [1] S. B. Akers. Binary decision diagrams. *IEEE Trans. Comput.*, 27(6):509–516, June 1978.
- [2] Rajeev Alur and David L. Dill. A theory of timed automata. *Theoretical Computer Science*, 126(2):183 235, 1994.
- [3] Gerd Behrmann, Johan Bengtsson, Alexandre David, Kim G. Larsen, Paul Pettersson, and Wang Yi. UPPAAL implementation secrets. In Proc. of 7th International Symposium on Formal Techniques in Real-Time and Fault Tolerant Systems, 2002.
- [4] Gerd Behrmann, Patricia Bouyer, Kim G. Larsen, and Radek Pelánek. Lower and Upper Bounds in Zone Based Abstractions of Timed Automata, pages 312–326. Springer Berlin Heidelberg, Berlin, Heidelberg, 2004.
- [5] Gerd Behrmann, Alexandre David, and Kim G. Larsen. A tutorial on Uppaal. In Marco Bernardo and Flavio Corradini, editors, Formal Methods for the Design of Real-Time Systems, volume 3185 of Lecture Notes in Computer Science, pages 200–236. Springer Berlin Heidelberg, 2004.
- [6] Johan Bengtsson. Clocks, DBMS and States in Timed Systems (Uppsala Dissertations from the Faculty of Science Technology, 39). Uppsala Universitet, 7 2002.
- [7] Dirk Beyer. Efficient reachability analysis and refinement checking of timed automata using BDDs. In T. Margaria and T. F. Melham, editors, Proceedings of the 11th IFIP Advanced Research Working Conference on Correct Hardware Design and Verification Methods (CHARME 2001, Livingston, September 4-7), LNCS 2144, pages 86–91. Springer-Verlag, Heidelberg, 2001.
- [8] Dirk Beyer, Claus Lewerentz, and Andreas Noack. Rabbit: A tool for BDD-based verification of real-time systems. In W. A. Hunt and F. Somenzi, editors, Proceedings of the 15th International Conference on Computer Aided Verification (CAV 2003, Boulder, CO, July 8-12), LNCS 2725, pages 122–125. Springer-Verlag, Heidelberg, 2003.
- [9] S. C. C. Blom, J. C. van de Pol, and M. Weber. LTSmin: Distributed and symbolic reachability. In T. Touili, B. Cook, and P. Jackson, editors, Computer Aided Verification, Edinburgh, volume 6174 of Lecture Notes in Computer Science, pages 354–359, Berlin, July 2010. Springer Verlag.

- [10] Stefan Blom and Jaco van de Pol. Symbolic reachability for process algebras with recursive data types. In J.S. Fitzgerald, A.E. Haxthausen, and H. Yenigun, editors, *Theoretical Aspects of Computing*, volume 5160 of *Lecture Notes in Computer Science*, pages 81–95, Berlin, Germany, August 2008. Springer Verlag.
- [11] R.E. Bryant. Graph-based algorithms for boolean function manipulation. *Computers, IEEE Transactions on*, C-35(8):677–691, Aug 1986.
- [12] A. E. Dalsgaard, A. W. Laarman, K. G. Larsen, M. C. Olesen, and J. C. van de Pol. Multi-core reachability for timed automata. In M. Jurdzinski and D. Nickovic, editors, 10th International Conference on Formal Modeling and Analysis of Timed Systems, FORMATS 2012, London, UK, volume 7595 of Lecture Notes in Computer Science, pages 91–106, London, September 2012. Springer Verlag.
- [13] Andreas Engelbredt Dalsgaard, Ren Rydhof Hansen, Kenneth Yrke Jørgensen, Kim Gulstrand Larsen, Mads Chr. Olesen, Petur Olsen, and Ji Srba. opaal: A lattice model checker. In Mihaela Bobaru, Klaus Havelund, Gerard J. Holzmann, and Rajeev Joshi, editors, NASA Formal Methods, volume 6617 of Lecture Notes in Computer Science, pages 487–493. Springer Berlin Heidelberg, 2011.
- [14] David L. Dill. Timing assumptions and verification of finite-state concurrent systems. In Joseph Sifakis, editor, Automatic Verification Methods for Finite State Systems, volume 407 of Lecture Notes in Computer Science, pages 197–212. Springer Berlin Heidelberg, 1990.
- [15] Junwei Du, Huiping Zhang, Gang Yu, and Xi Wang. A full symbolic compositional reachability analysis of timed automata based on BDD. In *Advanced Computational Intelligence (ICACI)*, 2015 Seventh International Conference on, pages 218–222, March 2015.
- [16] R. Ehlers, D. Fass, M. Gerke, and H.-J. Peter. Fully symbolic timed model checking using constraint matrix diagrams. In *Real-Time Systems Symposium (RTSS)*, 2010 IEEE 31st, pages 360–371, Nov 2010.
- [17] K. Havelund, A. Skou, K. G. Larsen, and K. Lund. Formal modeling and analysis of an audio/video protocol: an industrial case study using UPPAAL. In *Real-Time Systems Symposium*, 1997. Proceedings., The 18th IEEE, pages 2–13, Dec 1997.
- [18] A. W. Laarman, J. C. van de Pol, and M. Weber. Multi-Core LTSmin: Marrying Modularity and Scalability. In M. Bobaru, K. Havelund, G. Holzmann, and R. Joshi, editors, Proceedings of the Third International Symposium on NASA Formal Methods, NFM 2011, Pasadena,

- CA, USA, volume 6617 of Lecture Notes in Computer Science, pages 506–511, Berlin, July 2011. Springer Verlag.
- [19] Leslie Lamport. A fast mutual exclusion algorithm. ACM Trans. Comput. Syst., 5(1):1–11, January 1987.
- [20] Kim Larsen, Carsten Weise, Wang Yi, and Justin Pearson. Clock difference diagrams. *BRICS Report Series*, 5(46), 1998.
- [21] N. Lynch and N. Shavit. Timing based mutual exclusion. In *Proc. of the Annual Real-Time Symposium (RTSS)*, pages 2–11, 1992.
- [22] Jeroen Meijer, Gijs Kant, Stefan Blom, and Jaco van de Pol. Read, write and copy dependencies for symbolic model checking. In Eran Yahav, editor, *Hardware and Software: Verification and Testing*, volume 8855 of *Lecture Notes in Computer Science*, pages 204–219. Springer International Publishing, 2014.
- [23] R. Milner. Communication and Concurrency. Prentice-Hall, Inc., Upper Saddle River, NJ, USA, 1989.
- [24] J. Møller, J. Lichtenberg, H. R. Andersen, and H. Hulgaard. Difference decision diagrams. Technical Report IT-TR-1999-023, Department of Information Technology, Technical University of Denmark, Building 344, DK-2800 Lyngby, Denmark, February 1999.
- [25] Jesper Møller, Henrik Hulgaard, and Henrik Reif Andersen. Symbolic model checking of timed guarded commands using difference decision diagrams. The Journal of Logic and Algebraic Programming, 5253:53 – 77, 2002.
- [26] Jesper Møller and Jakob Lichtenberg. Difference decision diagrams. Master's thesis, Department of Information Technology, Technical University of Denmark, Building 344, DK-2800 Lyngby, Denmark, aug 1998.
- [27] Jesper Møller, Jakob Lichtenberg, HenrikReif Andersen, and Henrik Hulgaard. Difference decision diagrams. In Jörg Flum and Mario Rodriguez-Artalejo, editors, Computer Science Logic, volume 1683 of Lecture Notes in Computer Science, pages 111–125. Springer Berlin Heidelberg, 1999.
- [28] TruongKhanh Nguyen, Jun Sun, Yang Liu, JinSong Dong, and Yan Liu. Improved BDD-based discrete analysis of timed systems. In Dimitra Giannakopoulou and Dominique Méry, editors, FM 2012: Formal Methods, volume 7436 of Lecture Notes in Computer Science, pages 326–340. Springer Berlin Heidelberg, 2012.

- [29] Stefano Schivo, Jetse Scholma, Brend Wanders, Ricardo A. Urquidi Camacho, Paul E. van der Vet, Marcel Karperien, Rom Langerak, Jaco van de Pol, and Janine N. Post. Modelling biological pathway dynamics with timed automata. In 12th IEEE International Conference on Bioinformatics & Bioengineering, BIBE 2012, Larnaca, Cyprus, November 11-13, 2012, pages 447–453, 2012.
- [30] A. Srinivasan, T. Ham, S. Malik, and R.K. Brayton. Algorithms for discrete function manipulation. In Computer-Aided Design, 1990. ICCAD-90. Digest of Technical Papers., 1990 IEEE International Conference on, pages 92–95, Nov 1990.
- [31] Tom van Dijk and Jaco van de Pol. Sylvan: Multi-core decision diagrams. In Christel Baier and Cesare Tinelli, editors, *Tools and Algorithms for the Construction and Analysis of Systems*, volume 9035 of *Lecture Notes in Computer Science*, pages 677–691. Springer Berlin Heidelberg, 2015.
- [32] Farn Wang. Efficient verification of timed automata with BDD-like data-structures. In LenoreD. Zuck, PaulC. Attie, Agostino Cortesi, and Supratik Mukhopadhyay, editors, Verification, Model Checking, and Abstract Interpretation, volume 2575 of Lecture Notes in Computer Science, pages 189–205. Springer Berlin Heidelberg, 2003.
- [33] Sergio Yovine. Kronos: a verification tool for real-time systems. *International Journal on Software Tools for Technology Transfer*, 1(1-2):123–133, 1997.
- [34] Huiping Zhang, Junwei Du, Ling Cao, and Guixin Zhu. A full symbolic reachability analysis algorithm of timed automata based on BDD. In Autonomous Decentralized Systems (ISADS), 2015 IEEE Twelfth International Symposium on, pages 301–304, March 2015.

# A Experiment Results

This appendix contains all experimental results. The tables were too large to fit on a single page, so they have been cut in three parts. The first three tables show the timing results in seconds. The last three tables show the number of nodes in the final state-space for all the symbolic tools. The first five rows show the different options that have been used. The first row gives the state-store, this can be DDD, LDD or explicit-state. The second row gives the search-order, this can be either bfs-prev, bfs or, no-minus which is the altered bfs-prev we created as mentioned in section 4.10. The third row indicates if a partitioned-next state function is used or not. The fourth row indicates which reordering option, if any, is used. The fifth row indicates if the DBM-reduction, as mentioned in section 4.3, is used. The third table also contains a sixth row indicating the representation of the DBM. All options use a flattened DBM, only the explicit-state multi-core tool can use a pointer to the DBM, as this is the only point where this is used, the row is not included in the other tables. A "TO" in any of the tables means that a time-out has occurred. For all experiments this time-out has been set to 600 seconds.

| Sourhender   Sou   | Statestore         | DDD   | DDD   | DDD   | DDD  | DDD   | DDD  | DDD  | DDD  | DDD   | DDD  | DDD  | DDD  |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------|-------|-------|-------|------|-------|------|------|------|-------|------|------|------|
| Particulorid                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |                    | 1     |       |       |      |       |      |      |      |       |      |      |      |
| DBM-reduction                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | Partitioned        | 1 *   | -     |       | -    | +     | -    | +    | -    | +     |      |      |      |
| Sesher   0.2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | Reorder            | -     | -     | -     | -    | -     | -    | -    | -    | -     | -    | -    | -    |
| Secher   10.2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | DBM-reduction      | +     | +     | -     | -    | +     | +    | -    | -    | +     | +    | -    | -    |
| fischers4         0.3         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.2         0.4         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | fischer1           | 0.2   | 0.1   | 0.1   | 0.1  | 0.2   | 0.1  | 0.1  | 0.1  | 0.1   | 0.1  | 0.1  | 0.1  |
| fischerd         0.5         0.3         0.3         0.2         0.4         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.2         0.2         0.2         0.2         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | fischer2           |       |       |       |      | 0.2   |      |      |      |       |      |      |      |
| fischere                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | fischer3           | 0.3   | 0.2   |       |      | 0.3   |      | 0.2  |      |       |      |      |      |
| Secher   TO   TO   TO   TO   TO   TO   TO   T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| cerlBegional critRegional of 1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| certRegion2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2  |                    |       |       |       |      |       |      |      |      |       |      |      |      |
| critRegional 1.9 1.2 0.4 0.3 1.9 1.2 0.4 0.3 0.3 0.9 1.2 0.4 0.3 0.3 1.8 1.2 0.4 0.3 0.3 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| cirklegional TO TO 884 56.3 TO TO 462.9 TO TO TO 471.7 TO (Cirtical.01-25-50 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | 0                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| Critical 02-5-50                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| Critical D2-25-50                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                    |       |       |       |      |       |      |      |      |       |      |      |      |
| CHICHICAL 92-5-50                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| CHIGHALD-425-50 TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                    | I     |       |       |      |       |      |      |      |       |      |      |      |
| CSMACD.01                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| CSMACD-02                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                    |       |       |       |      |       |      |      |      |       |      |      |      |
| CSMACD.03                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| CSMACD.04                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| CSMACD.06                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                    | I     |       |       |      |       |      |      |      |       |      |      |      |
| CSMACD.06  S3.2  1.1  1.0  0.5  0.8  0.4  1.5  0.5  0.3  0.6  0.4  0.5  0.3  0.6  0.4  0.5  0.3  0.6  0.4  0.5  0.3  0.7  CSMACD.08  S3.1  2.3  14.6  1.6  1.9  0.9  1.1  0.7  CSMACD.08  S3.1  2.3  14.6  1.6  1.9  0.1  0.1  0.1  0.1  0.1  0.1  0.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                    | !     |       |       |      |       |      |      |      |       |      |      |      |
| CSMACD.07   13.4   4.8   3.6   1.6   1.9   0.9   1.1   0.7   1.5   0.9   1.1   0.7   CSMACD.08   53.1   22.3   14.6   6.2   5.3   2.5   3.2   1.9   4.2   2.5   3.2   1.9   viking2   0.1   0.1   0.1   0.1   0.1   0.1   0.1   0.1   0.1   0.1   0.1   0.1   viking3   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.1   viking4   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   viking5   0.3   0.4   0.7   0.3   0.5   0.2   0.2   0.2   0.2   0.2   0.2   viking6   0.5   0.3   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.6   2.5   5.2   1.2   0.6   0.5   0.8   0.6   2.5   5.2   1.2   0.6   0.5   0.8   0.6   2.5   5.2   1.2   0.6   0.5   0.8   0.6   2.5   5.2   1.2   0.6   0.5   0.8   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.4   0.7   0.3   0.8   0.6   2.5   5.2   1.2   0.8   0.6   2.5   5.2   1.2   0.8   0.6   2.5   5.2   1.2   0.8   0.6   2.5   5.2   1.2   0.9   0.8   0.4   0.7   0.8   0.8   0.4   0.7   0.8   0.8   0.4   0.7   0.8   0.8   0.8   0.9   0.8   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.8   0.9   0.8   0.9   0.8   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8   0.8   0.9   0.8    |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| viking1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | $CSMACD_07$        | 13.4  | 4.8   | 3.6   | 1.6  | 1.9   | 0.9  | 1.1  | 0.7  | 1.5   | 0.9  | 1.1  | 0.7  |
| viking2 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | CSMACD_08          | 53.1  | 22.3  | 14.6  | 6.2  | 5.3   | 2.5  | 3.2  | 1.9  | 4.2   | 2.5  | 3.2  | 1.9  |
| viking3                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | viking1            | 0.1   | 0.1   | 0.1   | 0.1  | 0.1   | 0.1  | 0.1  | 0.1  | 0.1   | 0.1  | 0.1  | 0.1  |
| viking4                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | viking2            | l     |       |       |      |       | 0.1  |      |      |       |      |      |      |
| viking5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | _                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| viking6                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | _                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| viking7                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | _                  | I     |       |       |      |       |      |      |      |       |      |      |      |
| viking8   2.3   0.9   1.8   0.5   2.4   0.9   1.8   0.5   2.2   0.9   1.8   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0.5   0. | _                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| viking9 6.6 2.5 5.2 1.2 6.6 2.5 5.1 1.2 6.5 2.5 5.1 1.2 6.5 2.5 5.2 1.2 viking10 20.3 7.2 15.1 3.2 20.5 7.2 15.1 3.2 19.0 7.2 15.1 3.2 viking11 62.4 20.4 43.4 8.5 60.6 20.5 43.3 8.5 44.9 20.5 43.4 8.6 viking12 114.6 40.2 109.4 17.7 114.6 40.2 108.9 17.6 115.1 40.2 109.8 17.7 Lynch1-16 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | _                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| viking10                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                    | I     |       |       |      |       |      |      |      |       |      |      |      |
| viking11 62.4 20.4 43.4 8.5 60.6 20.5 43.3 8.5 54.9 20.5 43.4 8.6 viking12 114.6 40.2 109.4 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 40.2 109.8 17.7 114.6 10.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | _                  | I     |       |       |      |       |      |      |      |       |      |      |      |
| viking12         114.6         40.2         109.4         17.7         114.6         40.2         108.9         17.6         115.1         40.2         109.8         17.7           Lynch1-16         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | _                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| Lynch1-16                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | _                  | I     |       |       |      |       |      |      |      |       |      |      |      |
| Lynch2-16         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                    |       |       |       |      |       |      |      |      |       |      |      |      |
| Lynch3-16         0.4         0.2         0.3         0.2         0.4         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.3         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                    | I     |       |       |      |       |      |      |      |       |      |      |      |
| Lynch4-16         5.8         2.6         3.6         1.6         5.2         2.6         3.2         1.5         4.6         2.8         3.4         1.6           Lynch5-16         251.3         110.9         114.8         48.2         143.4         67.4         71.8         34.2         130.9         74.1         75.6         36.7           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | •                  | !     |       |       |      |       |      |      |      |       |      |      |      |
| Lynch5-16         251.3         110.9         114.8         48.2         143.4         67.4         71.8         34.2         130.9         74.1         75.6         36.7           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2 </td <td></td> <td>l</td> <td></td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| bocdpFIXED   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   | Lynch5-16          | 251.3 | 110.9 | 114.8 | 48.2 | 143.4 | 67.4 | 71.8 | 34.2 | 130.9 | 74.1 | 75.6 | 36.7 |
| bando         0.3         0.2         0.2         0.2         0.3         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0 </td <td>bocdp</td> <td>0.2</td> <td>0.2</td> <td>0.2</td> <td>0.2</td> <td>0.2</td> <td>0.1</td> <td>0.2</td> <td>0.2</td> <td>0.2</td> <td>0.2</td> <td>0.2</td> <td>0.2</td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | bocdp              | 0.2   | 0.2   | 0.2   | 0.2  | 0.2   | 0.1  | 0.2  | 0.2  | 0.2   | 0.2  | 0.2  | 0.2  |
| timelock         0.2         0.1         0.0         0.0         0.2         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | bocdpFIXED         | 0.2   | 0.2   | 0.2   | 0.2  | 0.2   | 0.2  | 0.2  | 0.2  | 0.2   | 0.2  | 0.2  | 0.2  |
| Milner-2Nodes-flat   0.3   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.4   0.3   0.3   0.3   0.3   0.4   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3   0.3 | bando              | 0.3   | 0.2   | 0.2   | 0.2  | 0.3   | 0.2  | 0.2  | 0.2  | 0.2   | 0.2  | 0.2  | 0.2  |
| Milner-3Nodes-flat         0.3         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | timelock           | 0.2   | 0.1   | 0.0   | 0.0  | 0.2   | 0.0  | 0.0  |      |       |      | 0.0  | 0.0  |
| Milner-4Nodes-flat         0.4         0.2         0.2         0.2         0.3         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.2         0.4         0.4                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Milner-2Nodes-flat | 0.3   |       |       |      |       |      |      |      |       |      |      |      |
| Milner-5Nodes-flat         0.4         0.3         0.3         0.2         0.4         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.3         0.4         0.4         0.3         Milner-7Nodes-flat         0.2         0.5         0.5         0.5         0.6         0.7         0.4         0.8         0.5         0.6         0.4         0.3         Milner-8Nodes-flat         1.2         0.7         0.5         1.2         0.6         0.7         0.4         0.8         0.5         0.6         0.4         0.4         0.2         0.6         0.4         0.2         0.1         0.1<                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| Milner-6Nodes-flat         0.6         0.3         0.3         0.3         0.6         0.3         0.3         0.4         0.3         0.3         0.3           Milner-7Nodes-flat         0.8         0.5         0.5         0.3         0.8         0.4         0.5         0.3         0.5         0.4         0.4         0.3           Milner-8Nodes-flat         1.2         0.7         0.7         0.5         1.2         0.6         0.7         0.4         0.8         0.5         0.6         0.4           hddi.input_1         0.2         0.2         0.2         0.2         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.2         0.1         0.2         0.1         0.2         0.1         0.2         0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                    | 1     |       |       |      |       |      |      |      |       |      |      |      |
| Milner-7Nodes-flat         0.8         0.5         0.5         0.3         0.8         0.4         0.5         0.3         0.5         0.4         0.4         0.3           Milner-8Nodes-flat         1.2         0.7         0.7         0.5         1.2         0.6         0.7         0.4         0.8         0.5         0.6         0.4           hddi.input_1         0.2         0.2         0.2         0.2         0.2         0.2         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.2         0.1         0.2         0.1         0.2         0.1         0.2         0.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                    | 1     |       |       |      |       |      |      |      |       |      |      |      |
| Milner-8Nodes-flat         1.2         0.7         0.7         0.5         1.2         0.6         0.7         0.4         0.8         0.5         0.6         0.4           hddi.input_1         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2 <td></td> <td>1</td> <td></td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                    | 1     |       |       |      |       |      |      |      |       |      |      |      |
| hddi.input.1         0.2         0.2         0.2         0.2         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.1         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         0.2         0.3 <t< td=""><td></td><td>l</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| hddi.input_2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.1         0.2         0.1         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2 <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                    |       |       |       |      |       |      |      |      |       |      |      |      |
| hddi.input_3       104.2       104.2       18.2       17.9       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2       0.2 </td <td></td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |                    |       |       |       |      |       |      |      |      |       |      |      |      |
| hddi.input.4         TO         TO         TO         TO         0.3         0.2         0.3         0.2         0.3         0.2           hddi.input.5         TO         TO         TO         TO         1.1         0.5         0.3         0.2         1.1         0.5         0.3         0.2           hddi.input.6         TO         T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |                    |       |       |       |      |       |      |      |      |       |      |      |      |
| hddi.input_5         TO         TO         TO         TO         TO         TO         1.1         0.5         0.3         0.2         1.1         0.5         0.3         0.2           hddi.input_6         TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | *                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| hddi.input_6         TO         TO         TO         TO         TO         307.2         22.3         305.2         18.3         308.2         22.2         304.8         18.3           hddi.input_7         TO         TO </td <td>*</td> <td>l</td> <td></td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | *                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| hddi.input_7         TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | *                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| hddi.input_8         TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | *                  | l     |       |       |      |       |      |      |      |       |      |      |      |
| hddi_input_9                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |                    | l     |       |       |      |       |      |      |      |       |      |      |      |
| hddi_input_10 TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                    | I     |       |       |      |       |      |      |      |       |      |      |      |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | hddi_input_10      |       |       |       |      |       |      |      |      |       |      |      |      |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | *                  |       |       |       |      |       |      |      |      |       |      |      |      |

| Statestore                                   | LDD                   | LDD      | LDD      | LDD       | LDD      | LDD      | LDD            | LDD            | LDD      | LDD      |
|----------------------------------------------|-----------------------|----------|----------|-----------|----------|----------|----------------|----------------|----------|----------|
| Search-order                                 | bfs-prev              | bfs-prev | bfs-prev | bfs-prev  | bfs-prev | bfs-prev | bfs-prev       | bfs-prev       | bfs-prev | bfs-prev |
| Partitioned                                  | +                     | -        | +        | -         | +        | -        | +              | -              | +        | -        |
| Reorder                                      | gsa                   | gsa      | rb4w     | rb4w      | cw       | cw       | $_{\rm rs,rn}$ | $_{\rm rs,rn}$ | rs,ru    | rs,ru    |
| DBM-reduction                                | +                     | -        | +        | -         | +        | -        | +              | -              | +        | -        |
| fischer1                                     | 0.4                   | 0.3      | 0.2      | 0.1       | 0.2      | 0.1      | 0.2            | 0.1            | 0.2      | 0.1      |
| fischer2                                     | 0.8                   | 0.6      | 0.2      | 0.1       | 0.2      | 0.1      | 0.2            | 0.1            | 0.2      | 0.1      |
| fischer3                                     | 1.3                   | 1.0      | 0.2      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| fischer4                                     | 2.0                   | 1.5      | 0.5      | 0.3       | 0.5      | 0.3      | 0.4            | 0.3            | 0.4      | 0.3      |
| fischer5                                     | 6.3                   | 4.8      | 4.6      | 3.5       | 4.0      | 3.0      | 3.7            | 2.7            | 3.5      | 2.6      |
| fischer6                                     | 82.2                  | 66.0     | 91.4     | 68.0      | 78.9     | 64.9     | 67.4           | 57.3           | 63.4     | 55.9     |
| critRegion1                                  | 0.4                   | 0.4      | 0.1      | 0.1       | 0.1      | 0.1      | 0.1            | 0.1            | 0.1      | 0.1      |
| critRegion2                                  | 0.6                   | 0.6      | 0.2      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| critRegion3                                  | 1.3                   | 1.8      | 0.8      | 1.2       | 0.7      | 1.1      | 0.6            | 1.0            | 0.9      | 1.5      |
| critRegion4                                  | 46.5                  | 131.3    | 49.6     | 143.6     | 43.7     | 123.7    | 39.5           | 114.3          | 73.5     | 201.7    |
| Critical_01-25-50                            | 0.4                   | 0.4      | 0.1      | 0.1       | 0.1      | 0.1      | 0.1            | 0.1            | 0.1      | 0.1      |
| Critical_02-25-50                            | 0.6                   | 0.6      | 0.2      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| Critical_03-25-50                            | 6.3                   | 5.4      | 6.0      | 5.1       | 4.6      | 3.8      | 3.9            | 3.5            | 7.1      | 6.3      |
| Critical_04-25-50                            | TO                    | TO       | TO       | TO        | TO       | TO       | TO             | TO             | TO       | TO       |
| CSMACD_01                                    | 0.3                   | 0.2      | 0.2      | 0.1       | 0.2      | 0.1      | 0.2            | 0.1            | 0.1      | 0.1      |
| CSMACD_02                                    | 0.6                   | 0.4      | 0.2      | 0.1       | 0.2      | 0.1      | 0.3            | 0.1            | 0.3      | 0.1      |
| CSMACD_03                                    | 0.8                   | 0.5      | 0.3      | 0.1       | 0.2      | 0.1      | 0.3            | 0.1            | 0.2      | 0.1      |
| CSMACD_04                                    | 0.7                   | 0.6      | 0.3      | 0.2       | 0.3      | 0.2      | 0.3            | 0.2            | 0.3      | 0.2      |
| CSMACD_05                                    | 1.1                   | 0.8      | 0.4      | 0.3       | 0.4      | 0.3      | 0.4            | 0.3            | 0.4      | 0.3      |
| CSMACD_06                                    | 1.8                   | 1.4      | 1.4      | 0.9       | 1.2      | 0.9      | 1.1            | 0.8            | 1.2      | 0.8      |
| CSMACD_07                                    | 4.6                   | 3.7      | 4.4      | 3.4       | 4.8      | 3.4      | 4.0            | 2.9            | 3.8      | 2.8      |
| CSMACD_08                                    | 16.2                  | 13.4     | 16.2     | 14.7      | 16.0     | 14.7     | 13.0           | 12.4           | 12.3     | 11.9     |
| viking1                                      | 0.3                   | 0.3      | 0.1      | 0.1       | 0.1      | 0.1      | 0.1            | 0.1            | 0.1      | 0.1      |
| viking2                                      | 0.4                   | 0.4      | 0.1      | 0.1       | 0.1      | 0.1      | 0.1            | 0.1            | 0.1      | 0.1      |
| viking3                                      | 0.5                   | 0.5      | 0.1      | 0.1       | 0.2      | 0.1      | 0.1            | 0.1            | 0.1      | 0.1      |
| viking4                                      | 0.7                   | 0.7      | 0.2      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| viking5                                      | 0.8                   | 0.8      | 0.2      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| viking6                                      | 1.4                   | 1.3      | 0.7      | 0.6       | 0.7      | 0.6      | 0.6            | 0.5            | 0.5      | 0.4      |
| viking7                                      | 1.7                   | 1.6      | 1.0      | 0.8       | 1.0      | 0.8      | 0.8            | 0.7            | 0.7      | 0.6      |
| viking8                                      | 3.5                   | 2.9      | 2.9      | 2.4       | 3.0      | 2.4      | 2.4            | 1.8            | 2.0      | 1.5      |
| viking9                                      | 8.3                   | 6.7      | 9.1      | 7.5       | 9.3      | 7.5      | 7.2            | 5.4            | 6.1      | 4.4      |
| viking10                                     | 23.3                  | 17.7     | 29.8     | 22.9      | 29.5     | 22.9     | 22.8           | 16.2           | 18.2     | 12.8     |
| viking11                                     | 69.9                  | 49.3     | 90.4     | 68.7      | 85.7     | 68.8     | 63.6           | 47.7           | 49.6     | 37.1     |
| viking12                                     | 124.1                 | 100.9    | 164.1    | 141.5     | 164.1    | 141.8    | 122.2          | 100.1          | 100.7    | 78.5     |
| Lynch1-16                                    | 0.5                   | 0.5      | 0.1      | 0.1       | 0.1      | 0.1      | 0.1            | 0.1            | 0.1      | 0.1      |
| Lynch2-16                                    | 1.0                   | 1.1      | 0.2      | 0.2       | 0.1      | 0.1      | 0.2            | 0.1            | 0.2      | 0.2      |
| Lynch3-16                                    | 2.2                   | 1.8      | 0.5      | 0.3       | 0.5      | 0.3      | 0.4            | 0.3            | 0.4      | 0.3      |
| Lynch4-16                                    | 7.9                   | 6.2      | 6.6      | 5.1       | 5.6      | 4.2      | 5.2            | 3.9            | 4.9      | 3.7      |
| Lynch5-16                                    | 149.8                 | 134.1    | 191.8    | 162.6     | 162.5    | 137.9    | 147.5          | 126.3          | 142.8    | 123.1    |
| bocdp                                        | 9.9                   | 9.9      | 0.2      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| bocdpFIXED                                   | 9.8                   | 9.7      | 0.2      | 0.2       | 0.2      | 0.2      | 0.3            | 0.2            | 0.3      | 0.2      |
| bando                                        | 11.6                  | 9.8      | 0.3      | 0.2       | 0.3      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| timelock                                     | 0.2                   | 0.1      | 0.2      | 0.1       | 0.1      | 0.1      | 0.1            | 0.0            | 0.1      | 0.0      |
| Milner-2Nodes-flat                           | 0.5                   | 0.4      | 0.3      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| Milner-3Nodes-flat                           | 0.8                   | 0.6      | 0.3      | 0.2       | 0.3      | 0.2      | 0.3            | 0.2            | 0.3      | 0.2      |
| Milner-4Nodes-flat                           | 1.5                   | 0.9      | 0.7      | 0.4       | 0.7      | 0.4      | 0.7            | 0.4            | 0.7      | 0.4      |
| Milner-5Nodes-flat                           | 1.8                   | 1.2      | 1.1      | 0.7       | 1.1      | 0.7      | 1.0            | 0.6            | 1.0      | 0.6      |
| Milner-6Nodes-flat                           | 2.6                   | 1.7      | 1.7      | 1.1       | 1.6      | 1.1      | 1.5            | 0.9            | 1.5      | 0.9      |
| Milner-7Nodes-flat                           | 3.6                   | 2.4      | 2.6      | 1.7       | 2.7      | 1.7      | 2.4            | 1.5            | 2.2      | 1.3      |
| Milner-8Nodes-flat                           | 5.1                   | 3.4      | 4.1      | 2.8       | 4.1      | 2.8      | 3.5            | 2.2            | 3.4      | 1.9      |
| hddi_input_1                                 | 0.2                   | 0.3      | 0.1      | 0.1       | 0.1      | 0.1      | 0.1            | 0.1            | 0.1      | 0.1      |
| hddi_input_2                                 | 0.3                   | 0.3      | 0.2      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| hddi_input_3                                 | 0.4                   | 0.4      | 0.2      | 0.2       | 0.2      | 0.2      | 0.2            | 0.2            | 0.2      | 0.2      |
| hddi_input_4                                 | 0.7                   | 0.8      | 0.6      | 0.6       | 0.6      | 0.6      | 0.5            | 0.5            | 0.5      | 0.5      |
| hddi_input_5                                 | 1.7                   | 1.8      | 1.5      | 1.6       | 1.6      | 1.6      | 1.3            | 1.3            | 1.2      | 1.3      |
| hddi_input_6                                 | 5.9                   | 6.8      | 7.4      | 8.4       | 7.5      | 8.5      | 5.5            | 6.4            | 5.5      | 6.3      |
| hddi_input_7                                 | 18.9                  | 22.7     | 27.5     | 32.1      | 27.6     | 32.3     | 18.9           | 22.6           | 18.9     | 22.6     |
| hddi_input_8                                 | 64.1                  | 78.9     | 95.2     | 113.7     | 95.1     | 114.2    | 64.1           | 78.9           | 64.1     | 79.0     |
|                                              | 1446                  | 170.9    | 206.6    | 240.5     | 207.0    | 241.5    | 146.1          | 171.7          | 144.0    | 172.8    |
| hddi_input_9                                 | 144.6                 | 172.3    |          |           |          |          |                |                |          |          |
| hddi_input_9<br>hddi_input_10<br>ANIMO_small | 144.6<br>429.6<br>0.7 | 521.4    | TO 0.2   | TO<br>0.2 | TO 0.2   | TO 0.2   | 428.4          | 519.9          | 429.5    | 520.3    |

| Search-order                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | Statestore        | LDD   | LDD   | LDD   | LDD   | Explicit | Explicit | Explicit | Uppaal |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------|-------|-------|-------|-------|----------|----------|----------|--------|
| Partitioned                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |                   |       |       |       |       | -        | -        | -        | Орраат |
| Recorder                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |                   |       | -     | -     | -     |          |          |          |        |
| DBM                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | l .               |       | _     |       | _     | _        |          |          |        |
| BBM                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                   |       | _     |       |       | _        | _        |          |        |
| Secher                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 1                 | Į.    | flat  |       | flat  | pointer  | flat     |          |        |
| Secher2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | fischer1          |       |       |       |       | *        |          |          | 0.0    |
| fischer3         0.2         0.2         0.2         0.2         0.1         0.9         0.9         0.0           fischer5         3.7         2.4         2.7         2.0         0.1         0.9         0.9         0.0           fischer5         3.7         2.4         2.7         2.0         0.2         2.2         3.2         0.0           fischer6         66.4         57.4         57.4         57.4         48.3         0.4         19.2         26.2         0.0           critRegion1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           critRegion3         0.7         0.6         1.1         1.0         0.2         2.4         2.1         0.0           critteal01-25-50         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           Critical01-25-50         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.1         0.1         0.0         0.0         0.0           Critical01-25-50         0.7<                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |                   | 1     |       |       |       |          |          |          |        |
| fscher6         3.7         2.4         2.7         2.0         0.2         2.9         3.2         0.0           fscher6         66.4         57.4         57.4         48.3         0.4         19.2         26.2         0.0           critRegion1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0         0.0           critRegion3         0.7         0.6         1.1         1.0         0.2         2.4         2.1         0.0           critRegion4         44.0         44.5         122.5         136.3         0.5         58.5         24.3         0.1           Critical0-225-50         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.0         0.0         0.0           Critical0-25-50         0.7         0.7         TO         TO         TO         TO         0.0         1.1         1.7         0.6           CSMACD.01         0.2         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           CSMACD.02         0.2         0.1         0.1         0.1         0.0         0.0 <td>fischer3</td> <td>0.2</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | fischer3          | 0.2   |       |       |       |          |          |          |        |
| Ischer6                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | fischer4          | 0.5   | 0.3   | 0.3   | 0.2   | 0.1      | 0.9      | 0.9      | 0.0    |
| critRegion2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | fischer5          | 3.7   | 2.4   | 2.7   | 2.0   | 0.2      | 2.9      | 3.2      | 0.0    |
| critRegion2         0.2         0.2         0.2         0.2         0.2         0.2         0.0         critRegion3         0.7         0.6         1.1         1.0         0.2         2.4         2.1         0.0           critRegion4         45.0         44.5         122.5         136.3         0.5         58.5         24.3         0.1           Critical.02-25-50         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0         0.0           Critical.04-25-50         4.1         4.8         3.7         4.5         0.3         1.0         1.7         0.0           CSMACD.01         0.2         0.1         0.1         0.1         0.0         0.0         0.0         0.0         0.0           CSMACD.03         0.3         0.2         0.1         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | fischer6          | 66.4  | 57.4  | 57.4  | 48.3  | 0.4      | 19.2     | 26.2     | 0.0    |
| critRegion4                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | critRegion1       | 0.1   | 0.1   | 0.1   | 0.1   | 0.0      | 0.0      | 0.0      | 0.0    |
| critRegion4         4.50         44.5         122.5         136.3         0.5         58.5         24.3         0.1           Critical.01-25-50         0.1         0.1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | critRegion2       | 0.2   | 0.2   | 0.2   | 0.2   | 0.1      | 0.2      | 0.2      | 0.0    |
| Critical_0125-50                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | critRegion3       | 0.7   |       | 1.1   | 1.0   | 0.2      | 2.4      | 2.1      |        |
| Critical_03-25-50                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | critRegion4       |       |       |       |       |          |          |          |        |
| Critical_03-25-50                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Critical_01-25-50 |       |       |       |       |          |          |          |        |
| Critical.04-25-50   TO   TO   TO   TO   0.9   1.1   1.7   0.6   CSMACD.01   0.2   0.1   0.1   0.1   0.0   0.0   0.0   0.0   0.0   0.0   CSMACD.03   0.3   0.2   0.1   0.1   0.1   0.0   0.0   0.0   0.0   0.0   CSMACD.03   0.3   0.2   0.1   0.1   0.1   0.0   0.0   0.1   0.1   0.0   CSMACD.04   0.3   0.2   0.2   0.2   0.2   0.2   0.8   0.8   0.0   CSMACD.05   0.5   0.2   0.3   0.2   0.2   0.2   0.8   0.8   0.0   CSMACD.06   1.3   0.6   0.9   0.5   0.3   1.6   1.6   0.0   CSMACD.07   4.6   1.9   3.3   1.7   0.3   3.0   3.4   0.0   CSMACD.08   15.1   7.9   14.3   7.3   0.5   6.9   8.1   0.1   viking    0.1   0.1   0.1   0.1   0.1   0.0   0.0   0.0   0.0   0.0   viking3   0.2   0.1   0.1   0.1   0.1   0.1   0.0   0.0   0.0   0.0   0.0   viking4   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.3   0.0   viking5   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.2   0.5   0.5   0.5   0.0   viking6   0.7   0.3   0.6   0.2   0.3   0.3   1.4   1.5   0.0   viking8   3.0   0.9   2.4   0.5   0.4   2.1   2.4   0.0   viking9   3.7   2.6   7.4   1.3   0.5   2.6   3.8   0.1   viking1   86.6   20.9   67.7   9.0   1.0   6.0   18.0   0.5   viking1   86.6   20.9   67.7   9.0   1.0   6.0   18.0   0.5   viking1   1.0   0.1   0.1   0.1   0.0   0.0   0.0   0.0   viking11   86.6   20.9   67.7   9.0   1.0   6.0   18.0   0.5   viking12   162.9   41.2   410.7   18.7   0.7   10.4   32.9   1.0   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5   1.5 | Critical_02-25-50 | 1     |       |       |       |          |          |          |        |
| CSMACD.01                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                   | 1     |       |       |       |          |          |          |        |
| CSMACD.02                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                   |       |       |       |       |          |          |          |        |
| CSMACD.03                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                   | 1     |       |       |       |          |          |          |        |
| CSMACD.04                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                   |       |       |       |       |          |          |          |        |
| CSMACD_06                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                   | Į.    |       |       |       |          |          |          |        |
| CSMACD_06                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                   |       |       |       |       |          |          |          |        |
| CSMACD_07         4.6         1.9         3.3         1.7         0.3         3.0         3.4         0.0           CSMACD_08         15.1         7.9         14.3         7.3         0.5         6.9         8.1         0.1           viking1         0.1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                   | Į.    |       |       |       |          |          |          |        |
| CSMACD_08         15.1         7.9         14.3         7.3         0.5         6.9         8.1         0.1           viking1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           viking3         0.2         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           viking4         0.2         0.2         0.2         0.2         0.1         0.1         0.0         0.1         0.1         0.0           viking5         0.2         0.2         0.2         0.2         0.2         0.5         0.5         0.0           viking6         0.7         0.3         0.6         0.2         0.3         0.9         1.0         0.0           viking6         0.7         0.3         0.6         0.2         0.3         0.9         1.0         0.0           viking8         3.0         0.9         2.4         0.5         0.4         2.1         1.5         0.0           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         <                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                   | 1     |       |       |       |          |          |          |        |
| viking1         0.1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           viking2         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0         0.0           viking3         0.2         0.1         0.1         0.1         0.0         0.0         0.1         0.1         0.0           viking4         0.2         0.2         0.2         0.2         0.2         0.2         0.3         0.0           viking6         0.7         0.3         0.6         0.2         0.3         0.9         1.0         0.0           viking7         1.0         0.4         0.8         0.3         0.3         1.4         1.5         0.0           viking9         9.7         2.6         7.4         1.3         0.5         2.6         3.8         0.1           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         20.9         67.7         9.0         1.0         6.0         18.0         0.5           viking11         86.6                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                   | l .   |       |       |       |          |          |          |        |
| viking2         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           viking3         0.2         0.1         0.1         0.1         0.0         0.1         0.1         0.0           viking4         0.2         0.2         0.2         0.2         0.2         0.1         0.2         0.3         0.0           viking6         0.7         0.3         0.6         0.2         0.2         0.2         0.5         0.5         0.0           viking6         0.7         0.3         0.6         0.2         0.3         0.9         1.0         0.0           viking8         3.0         0.9         2.4         0.5         0.4         2.1         2.4         0.0           viking9         9.7         2.6         7.4         1.3         0.5         2.6         3.8         0.1           viking10         30.3         7.4         22.6         7.7         9.0         1.0         6.0         18.0         0.5           viking11         16c.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch-1-16         0.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 |                   |       |       |       |       |          |          |          |        |
| viking3         0.2         0.1         0.1         0.1         0.0         0.1         0.1         0.0           viking4         0.2         0.2         0.2         0.2         0.1         0.2         0.3         0.0           viking6         0.7         0.3         0.6         0.2         0.3         0.9         1.0         0.0           viking7         1.0         0.4         0.8         0.3         0.3         1.4         1.5         0.0           viking8         3.0         0.9         2.4         0.5         0.4         2.1         2.4         0.0           viking9         9.7         2.6         7.4         1.3         0.5         2.6         2.6         3.8         0.1           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         20.9         67.7         9.0         1.0         6.0         18.0         0.5           viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch-1-16         0.1         0.1         0.1 <td>  "</td> <td>1</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | "                 | 1     |       |       |       |          |          |          |        |
| viking4         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.5         0.5         0.0           viking6         0.7         0.3         0.6         0.2         0.3         0.9         1.0         0.0           viking7         1.0         0.4         0.8         0.3         0.3         1.4         1.5         0.0           viking8         3.0         0.9         2.4         0.5         0.4         2.1         2.4         0.0           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         20.9         67.7         9.0         1.0         6.0         18.0         0.5           viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch1-16         0.1         0.1         0.2         0.2         0.0         0.0         0.0         0.0         0.0           Lynch3-16         0.5         0.3         0.3         0.3         0.3         0.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                   | I .   |       |       |       |          |          |          |        |
| viking5         0.2         0.2         0.2         0.2         0.2         0.5         0.5         0.0           viking6         0.7         0.3         0.6         0.2         0.3         0.9         1.0         0.0           viking7         1.0         0.4         0.8         0.3         0.3         0.9         1.0         0.0           viking8         3.0         0.9         2.4         0.5         0.4         2.1         2.4         0.0           viking9         9.7         2.6         7.4         1.3         0.5         2.6         3.8         0.1           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch1-16         0.1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           Lynch2-16         0.2         0.1         0.2         0.2         0.0         0.2         0.2         0.0           Lynch3-16         16.4         138.0         129.6<                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | "                 | 1     |       |       |       |          |          |          |        |
| viking6         0.7         0.3         0.6         0.2         0.3         0.9         1.0         0.0           viking7         1.0         0.4         0.8         0.3         0.3         1.4         1.5         0.0           viking8         3.0         0.9         2.4         0.5         0.4         2.1         2.4         0.0           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         20.9         67.7         9.0         1.0         6.0         18.0         0.5           viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch1-16         0.1         0.1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           Lynch2-16         0.2         0.1         0.2         0.2         0.2         0.0         0.2         0.2         0.2         0.0           Lynch3-16         0.5         0.3         0.3         0.3         0.3         0.3         0.1         1.2         1.2         0.0 <td></td> <td>l .</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                   | l .   |       |       |       |          |          |          |        |
| viking7         1.0         0.4         0.8         0.3         0.3         1.4         1.5         0.0           viking8         3.0         0.9         2.4         0.5         0.4         2.1         2.4         0.0           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         20.9         67.7         9.0         1.0         6.0         18.0         0.5           viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch1-16         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           Lynch2-16         0.2         0.1         0.2         0.2         0.0         0.2         0.2         0.2         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | _                 | 1     |       |       |       |          |          |          |        |
| viking8         3.0         0.9         2.4         0.5         0.4         2.1         2.4         0.0           viking9         9.7         2.6         7.4         1.3         0.5         2.6         3.8         0.1           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         20.9         67.7         9.0         1.0         6.0         18.0         0.5           viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch1-16         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           Lynch2-16         0.2         0.1         0.2         0.2         0.0         0.2         0.2         0.2         0.0           Lynch5-16         164.4         138.0         129.6         120.0         0.3         50.0         68.4         0.0           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2 <t< td=""><td></td><td>l .</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                   | l .   |       |       |       |          |          |          |        |
| viking9         9.7         2.6         7.4         1.3         0.5         2.6         3.8         0.1           viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         20.9         67.7         9.0         1.0         6.0         18.0         0.5           viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch2-16         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           Lynch3-16         0.5         0.3         0.3         0.3         0.1         1.2         1.2         0.0           Lynch5-16         164.4         138.0         129.6         120.0         0.3         50.0         68.4         0.0           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | "                 | Į.    |       |       |       |          |          |          |        |
| viking10         30.3         7.4         22.6         3.3         0.7         3.5         7.6         0.2           viking11         86.6         20.9         67.7         9.0         1.0         6.0         18.0         0.5           viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch1-16         0.1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           Lynch2-16         0.2         0.1         0.2         0.2         0.0         0.2         0.2         0.0           Lynch3-16         0.5         0.3         0.3         0.3         0.1         1.2         1.2         0.0           Lynch4-16         5.3         3.8         4.0         3.5         0.2         3.4         3.8         0.0           Lynch5-16         164.4         138.0         129.6         120.0         0.3         50.0         68.4         0.0           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2           bocdp         0.3         0.2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            |                   | I     |       |       |       |          |          |          |        |
| viking12         162.9         41.2         140.7         18.7         0.7         10.4         32.9         1.0           Lynch1-16         0.1         0.1         0.1         0.1         0.1         0.0         0.0         0.0         0.0           Lynch2-16         0.2         0.1         0.2         0.2         0.0         0.2         0.2         0.0           Lynch3-16         0.5         0.3         0.3         0.3         0.1         1.2         1.2         0.0           Lynch4-16         5.3         3.8         4.0         3.5         0.2         3.4         3.8         0.0           Lynch5-16         164.4         138.0         129.6         120.0         0.3         50.0         68.4         0.0           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         timeleck         0.0         0.0         0.0         0.0         0.0         0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | _                 | Į.    |       |       |       |          |          |          |        |
| Lynch -16                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | "                 | I     | 20.9  |       |       |          |          |          |        |
| Lynch2-16         0.2         0.1         0.2         0.2         0.0         0.2         0.2         0.0           Lynch3-16         0.5         0.3         0.3         0.3         0.1         1.2         1.2         0.0           Lynch4-16         5.3         3.8         4.0         3.5         0.2         3.4         3.8         0.0           Lynch5-16         164.4         138.0         129.6         120.0         0.3         50.0         68.4         0.0           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         base         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0 <td< td=""><td>viking12</td><td>162.9</td><td>41.2</td><td>140.7</td><td>18.7</td><td>0.7</td><td>10.4</td><td>32.9</td><td>1.0</td></td<>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | viking12          | 162.9 | 41.2  | 140.7 | 18.7  | 0.7      | 10.4     | 32.9     | 1.0    |
| Lynch3-16         0.5         0.3         0.3         0.3         0.1         1.2         1.2         0.0           Lynch4-16         5.3         3.8         4.0         3.5         0.2         3.4         3.8         0.0           Lynch5-16         164.4         138.0         129.6         120.0         0.3         50.0         68.4         0.0           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         bando         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3         bando         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3         timelock         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | Lynch1-16         | 0.1   | 0.1   | 0.1   | 0.1   | 0.0      | 0.0      | 0.0      | 0.0    |
| Lynch4-16         5.3         3.8         4.0         3.5         0.2         3.4         3.8         0.0           Lynch5-16         164.4         138.0         129.6         120.0         0.3         50.0         68.4         0.0           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         bando         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3         bando         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3         bando         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3         bando         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | Lynch2-16         | 0.2   | 0.1   | 0.2   | 0.2   | 0.0      | 0.2      | 0.2      | 0.0    |
| Lynch5-16         164.4         138.0         129.6         120.0         0.3         50.0         68.4         0.0           bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         bando         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3         timelock         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0 </td <td>Lynch3-16</td> <td>0.5</td> <td>0.3</td> <td>0.3</td> <td>0.3</td> <td>0.1</td> <td>1.2</td> <td>1.2</td> <td>0.0</td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | Lynch3-16         | 0.5   | 0.3   | 0.3   | 0.3   | 0.1      | 1.2      | 1.2      | 0.0    |
| bocdp         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.2         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3           bando         0.3         0.2         0.2         0.2         0.2         0.0         0.1         0.2         0.3           timelock         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0           Milner-SNodes-flat         0.2         0.2         0.2         0.2         0.0         0.1         0.1         0.0           Milner-SNodes-flat         1.0         0.6         0.7         0.5         0.1         0.9         1.0         0.0           Milner-FNodes-flat         1.6         0.9         1.1         0.6         0.1         1.1         1.3         0.0           Milner-SNodes-flat         2.6         1.3         1.7         0.9         0.1         1.2         1.6         0.0           Milner-SNodes-flat         4.1         1.9         2.7                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | Lynch4-16         | 5.3   | 3.8   | 4.0   | 3.5   | 0.2      | 3.4      | 3.8      | 0.0    |
| bocdpFIXED         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3           bando         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3           timelock         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0           Milner-2Nodes-flat         0.2         0.2         0.2         0.2         0.0         0.1         0.1         0.0           Milner-3Nodes-flat         0.3         0.2         0.2         0.2         0.0         0.4         0.4         0.0           Milner-4Nodes-flat         0.7         0.4         0.4         0.3         0.1         0.8         0.8         0.0           Milner-5Nodes-flat         1.6         0.9         1.1         0.6         0.7         0.5         0.1         0.9         1.0         0.0           Milner-7Nodes-flat         1.6         0.9         1.1         0.6         0.1         1.1         1.3         0.0           hddi.input_1         0.1         0.1         0.1         0.2         0.1         1.4         2.1         0.0           hddi.input_                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | Lynch5-16         | 164.4 | 138.0 | 129.6 | 120.0 | 0.3      | 50.0     | 68.4     | 0.0    |
| bando         0.3         0.2         0.2         0.2         0.0         0.1         0.2         0.3           timelock         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | bocdp             | 1     |       | 0.2   | 0.2   |          | 0.2      |          |        |
| timelock         0.1         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.0         0.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |                   | I     |       |       |       |          |          |          |        |
| Milner-2Nodes-flat         0.2         0.2         0.2         0.2         0.0         0.1         0.1         0.0           Milner-3Nodes-flat         0.3         0.2         0.2         0.2         0.0         0.4         0.4         0.0           Milner-4Nodes-flat         0.7         0.4         0.4         0.3         0.1         0.8         0.8         0.0           Milner-5Nodes-flat         1.0         0.6         0.7         0.5         0.1         0.9         1.0         0.0           Milner-6Nodes-flat         1.6         0.9         1.1         0.6         0.1         1.1         1.3         0.0           Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           hddi.input_1         0.1         0.1         0.1         0.2         0.0         0.0         0.0         0.0           hddi.input_2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 1                 | !     |       |       |       |          |          |          |        |
| Milner-3Nodes-flat         0.3         0.2         0.2         0.2         0.0         0.4         0.4         0.0           Milner-4Nodes-flat         0.7         0.4         0.4         0.3         0.1         0.8         0.8         0.0           Milner-5Nodes-flat         1.0         0.6         0.7         0.5         0.1         0.9         1.0         0.0           Milner-6Nodes-flat         1.6         0.9         1.1         0.6         0.1         1.1         1.3         0.0           Milner-8Nodes-flat         2.6         1.3         1.7         0.9         0.1         1.2         1.6         0.0           Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           hddi.input.1         0.1         0.1         0.1         0.1         0.2         0.0         0.0         0.0         0.0           hddi.input.2         0.2         0.2         0.2         0.2         0.2         0.0         0.0         0.0         0.0           hddi.input.3         0.2         0.2         0.2         0.2         0.0         0.0         0.4         0.3         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              |                   |       |       |       |       |          |          |          |        |
| Milner-4Nodes-flat         0.7         0.4         0.4         0.3         0.1         0.8         0.8         0.0           Milner-5Nodes-flat         1.0         0.6         0.7         0.5         0.1         0.9         1.0         0.0           Milner-6Nodes-flat         1.6         0.9         1.1         0.6         0.1         1.1         1.3         0.0           Milner-Nodes-flat         2.6         1.3         1.7         0.9         0.1         1.2         1.6         0.0           Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           hddi.input.1         0.1         0.1         0.1         0.2         0.0         0.0         0.0         0.0           hddi.input.2         0.2         0.2         0.2         0.2         0.0         0.0         0.0         0.0           hddi.input.3         0.2         0.2         0.2         0.2         0.0         0.4         0.3         0.0           hddi.input.4         0.5         0.3         0.6         0.3         0.0         0.6         0.6         0.6           hddi.input.5         1.5                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      |                   |       |       |       |       |          |          |          |        |
| Milner-5Nodes-flat         1.0         0.6         0.7         0.5         0.1         0.9         1.0         0.0           Milner-6Nodes-flat         1.6         0.9         1.1         0.6         0.1         1.1         1.3         0.0           Milner-7Nodes-flat         2.6         1.3         1.7         0.9         0.1         1.2         1.6         0.0           Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           hddi.input_1         0.1         0.1         0.1         0.2         0.0         0.0         0.0         0.0           hddi.input_2         0.2         0.2         0.2         0.2         0.2         0.0         0.0         0.0         0.0           hddi.input_3         0.2         0.2         0.2         0.2         0.0         0.4         0.3         0.0           hddi.input_4         0.5         0.3         0.6         0.3         0.0         0.6         0.6         0.0           hddi.input_5         1.5         0.6         1.6         0.5         0.0         0.8         0.8         0.0           hddi.input_6                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                   |       |       |       |       |          |          |          |        |
| Milner-6Nodes-flat         1.6         0.9         1.1         0.6         0.1         1.1         1.3         0.0           Milner-7Nodes-flat         2.6         1.3         1.7         0.9         0.1         1.2         1.6         0.0           Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           hddi_input_1         0.1         0.1         0.1         0.2         0.0         0.0         0.0         0.0           hddi_input_2         0.2         0.2         0.2         0.2         0.2         0.1         0.0           hddi_input_3         0.2         0.2         0.2         0.2         0.2         0.2         0.0         0.4         0.3         0.0           hddi_input_4         0.5         0.3         0.6         0.3         0.0         0.6         0.6         0.0           hddi_input_5         1.5         0.6         1.6         0.5         0.0         0.8         0.8         0.0           hddi_input_6         7.4         1.9         8.4         1.6         0.0         1.7         2.1         0.0           hddi_input_8         9                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                   |       |       |       |       |          |          |          |        |
| Milner-7Nodes-flat         2.6         1.3         1.7         0.9         0.1         1.2         1.6         0.0           Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           hddi_input_1         0.1         0.1         0.1         0.2         0.0         0.0         0.0         0.0           hddi_input_2         0.2         0.2         0.2         0.2         0.2         0.1         0.0           hddi_input_3         0.2         0.2         0.2         0.2         0.2         0.0         0.4         0.3         0.0           hddi_input_4         0.5         0.3         0.6         0.3         0.0         0.6         0.6         0.0           hddi_input_5         1.5         0.6         1.6         0.5         0.0         0.8         0.8         0.0           hddi_input_6         7.4         1.9         8.4         1.6         0.0         1.7         2.1         0.0           hddi_input_7         27.4         5.8         32.1         5.1         0.2         8.1         12.5         0.1           hddi_input_9         206.9         38                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                   | Į.    |       |       |       |          |          |          |        |
| Milner-8Nodes-flat         4.1         1.9         2.7         1.2         0.1         1.4         2.1         0.0           hddi_input_1         0.1         0.1         0.1         0.2         0.0         0.0         0.0         0.0           hddi_input_2         0.2         0.2         0.2         0.2         0.2         0.1         0.0           hddi_input_3         0.2         0.2         0.2         0.2         0.0         0.4         0.3         0.0           hddi_input_4         0.5         0.3         0.6         0.3         0.0         0.6         0.6         0.0           hddi_input_5         1.5         0.6         1.6         0.5         0.0         0.8         0.8         0.0           hddi_input_6         7.4         1.9         8.4         1.6         0.0         1.7         2.1         0.0           hddi_input_7         27.4         5.8         32.1         5.1         0.2         3.5         4.9         0.0           hddi_input_8         94.6         17.2         114.0         15.1         0.2         8.1         12.5         0.1           hddi_input_10         TO         104.6         TO<                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                   | I     |       |       |       |          |          |          |        |
| hddi_input_1         0.1         0.1         0.1         0.2         0.0         0.0         0.0         0.0           hddi_input_2         0.2         0.2         0.2         0.2         0.2         0.1         0.0           hddi_input_3         0.2         0.2         0.2         0.2         0.0         0.4         0.3         0.0           hddi_input_4         0.5         0.3         0.6         0.3         0.0         0.6         0.6         0.0           hddi_input_5         1.5         0.6         1.6         0.5         0.0         0.8         0.8         0.0           hddi_input_6         7.4         1.9         8.4         1.6         0.0         1.7         2.1         0.0           hddi_input_7         27.4         5.8         32.1         5.1         0.2         3.5         4.9         0.0           hddi_input_8         94.6         17.2         114.0         15.1         0.2         8.1         12.5         0.1           hddi_input_9         206.9         38.8         240.7         34.4         0.1         17.1         25.7         0.0           hddi_input_10         TO         104.6         T                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |                   | Į.    |       |       |       |          |          |          |        |
| hddi.input.2         0.2         0.2         0.2         0.2         0.1         0.0           hddi.input.3         0.2         0.2         0.2         0.2         0.0         0.4         0.3         0.0           hddi.input.4         0.5         0.3         0.6         0.3         0.0         0.6         0.6         0.0           hddi.input.5         1.5         0.6         1.6         0.5         0.0         0.8         0.8         0.0           hddi.input.6         7.4         1.9         8.4         1.6         0.0         1.7         2.1         0.0           hddi.input.7         27.4         5.8         32.1         5.1         0.2         3.5         4.9         0.0           hddi.input.8         94.6         17.2         114.0         15.1         0.2         8.1         12.5         0.1           hddi.input.9         206.9         38.8         240.7         34.4         0.1         17.1         25.7         0.0           hddi.input.10         TO         104.6         TO         93.3         0.0         43.1         68.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                   |       |       |       |       |          |          |          |        |
| hddi_input_3         0.2         0.2         0.2         0.2         0.0         0.4         0.3         0.0           hddi_input_4         0.5         0.3         0.6         0.3         0.0         0.6         0.6         0.0           hddi_input_5         1.5         0.6         1.6         0.5         0.0         0.8         0.8         0.0           hddi_input_6         7.4         1.9         8.4         1.6         0.0         1.7         2.1         0.0           hddi_input_7         27.4         5.8         32.1         5.1         0.2         3.5         4.9         0.0           hddi_input_8         94.6         17.2         114.0         15.1         0.2         8.1         12.5         0.1           hddi_input_9         206.9         38.8         240.7         34.4         0.1         17.1         25.7         0.0           hddi_input_10         TO         104.6         TO         93.3         0.0         43.1         68.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                   |       |       |       |       |          |          |          |        |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                   |       |       |       |       |          |          |          |        |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                   | Į.    |       |       |       |          |          |          |        |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                   | l .   |       |       |       |          |          |          |        |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                   |       |       |       |       |          |          |          |        |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     |                   |       |       |       |       |          |          |          |        |
| hddi_input_9         206.9         38.8         240.7         34.4         0.1         17.1         25.7         0.0           hddi_input_10         TO         104.6         TO         93.3         0.0         43.1         68.0         0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                   | Į.    |       |       |       |          |          |          |        |
| hddi_input_10 TO 104.6 TO 93.3 0.0 43.1 68.0 0.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                   | 1     |       |       |       |          |          |          |        |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | _                 | Į.    |       |       |       |          |          |          |        |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |                   | 0.2   |       | 0.2   |       | 0.2      | 0.4      |          | 0.0    |

| Statestore DDD DDD DDD DDD DDD                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | DDD          | DDD      | DDD          |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------|----------|--------------|
| Search-order bfs-prev bfs-prev bfs-prev bfs                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | bfs          | bfs      | bfs          |
| Partitioned + - + - +                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | -            | +        | -            |
| Reorder                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | _            |          | _            |
| DBM-reduction + + +                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | +            | _        |              |
| fischer1 14 14 14 14 14 14                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 14           | 14       | 14           |
| fischer2   66   66   66   66   66   66                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 66           | 66       | 66           |
| fischer3 509 509 468 468 288                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | 288          | 250      | 250          |
| fischer4 5025 5025 4631 4631 1300                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | 1300         | 987      | 987          |
| fischer5 49634 49634 46879 46879 5535                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 5535         | 3920     | 3920         |
| fischer6 TO TO TO 444745 TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | ТО           | TO       | TO           |
| critRegion1   24   24   24   24   24   24                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 24           | 24       | 24           |
| critRegion2 251 251 227 227 190                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 190          | 140      | 140          |
| critRegion3 4643 4643 3042 3042 3836                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 3836         | 1683     | 1683         |
| critRegion4 TO TO 83145 83145 TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | ТО           | 56222    | ТО           |
| Critical_01-25-50 25 25 25 25                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | 25           | 25       | 25           |
| Critical_02-25-50 313 313 253 253 262                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 262          | 158      | 158          |
| Critical_03-25-50   12322   12322   5265   5265   10898                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 10898        | 3291     | 3291         |
| Critical_04-25-50 TO TO TO TO TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | TO           | TO       | TO           |
| CSMACD_01 17 17 17 17 17                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 17           | 17       | 17           |
| CSMACD_02   112   112   107   107   108                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 108          | 108      | 108          |
| CSMACD_03 686 686 525 525 458                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | 458          | 435      | 435          |
| CSMACD_04 3305 3305 2210 2210 1356                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 1356         | 1357     | 1357         |
| CSMACD_05   13867   13867   8320   8320   3478                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 3478         | 3790     | 3790         |
| CSMACD_06 51633 51633 28838 28838 7925                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 7925         | 10099    | 10099        |
| CSMACD_07   176965 176965 93717 93717 17069                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 17069        | 26381    | 26381        |
| CSMACD_08   569760                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 36098        | 68197    | 68197        |
| viking1 12 12 12 15                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | 15           | 15       | 15           |
| viking2   37   37   37   37   37                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 37           | 37       | 37           |
| viking3 86 86 86 86 86                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 86           | 86       | 86           |
| viking4   105   105   105   105   105                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 105          | 105      | 105          |
| viking5   124   124   124   124   124                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 124          | 124      | 124          |
| viking6 233 233 233 233                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 233          | 233      | 233          |
| viking7 190 190 190 190 190                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 190          | 190      | 190          |
| viking8 224 224 224 224 224                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 224          | 224      | 224          |
| viking9 263 263 263 263                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 263          | 263      | 263          |
| viking10 304 304 304 304 304                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | 304          | 304      | 304          |
| viking11 347 347 347 347 347                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             | 347          | 347      | 347          |
| viking12 342 342 342 342 342 342                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 342          | 342      | 342          |
| Lynch1-16 24 24 24 24 24 24 160 160 160 160 160 160 160 160 160 160                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | 24           | 24       | 24           |
| Lynch2-16 162 162 149 149 162                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | 162          | 149      | 149          |
| Lynch3-16 1175 1175 915 915 922                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 922<br>8246  | 721      | 721          |
| Lynch4-16         14280         14280         9795         9795         8246           Lynch5-16         210433         210433         107391         107391         95362                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               |              | 5750     | 5750         |
| v .                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | 95362<br>541 | 49430    | 49430<br>487 |
| bocdp         541         541         487         487         541           bocdpFIXED         542         542         488         488         542                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 541 $542$    | 487      | 487          |
| bando 542 542 488 488 542 542 542 542 542 542 542 542 542 542                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | 542          | 488      | 488<br>488   |
| timelock 4 4 4 4 4                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 4            | 400      | 400          |
| Milner-2Nodes-flat 442 442 432 432 245                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 245          | 133      | 133          |
| Milner-3Nodes-flat 2709 2709 2671 2671 918                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 918          | 528      | 528          |
| Milner-4Nodes-flat 4999 4999 4809 4809 2968                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 2968         | 1776     | 1776         |
| Milner-5Nodes-flat 9106 9106 8856 8856 5293                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 5293         | 3146     | 3146         |
| Milner-6Nodes-flat   17008   17008   16030   16030   7755                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 7755         | 5078     | 5078         |
| Milner-7Nodes-flat   25493   25493   24347   24347   12188                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 12188        | 7668     | 7668         |
| Milner-8Nodes-flat   39887   39887   37433   37433   16324                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 16324        | 11012    | 11012        |
| hddi_input_1 221 221 217 217 119                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 119          | 136      | 136          |
| hddi_input_2 2735 2735 2457 2457 693                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 693          | 710      | 710          |
| hddi_input_3 20485 20485 18508 18508 2013                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 2013         | 2338     | 2338         |
| hddi_input_4 TO TO TO TO 4495                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            | 4495         | 5377     | 5377         |
| hddi_input_5 TO TO TO 13824                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 13824        | 10331    | 10331        |
| hddi_input_6 TO TO TO TO 14175                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 14175        | 18682    | 18682        |
| hddi_input_7 TO TO TO TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | ТО           | ТО       | ТО           |
| hddi.input.8 TO TO TO TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | TO           | TO       | TO           |
| 1.41: :                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  |              |          |              |
| hddi_input_9 TO TO TO TO TO                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | TO           | TO       | ТО           |
| hddi.input_9         TO         TO | $_{ m TO}$   | TO<br>TO | TO<br>TO     |

| Statestore         | DDD      | DDD      | DDD      | DDD      | LDD      | LDD      | LDD      | LDD     |
|--------------------|----------|----------|----------|----------|----------|----------|----------|---------|
| Search-order       | no-minus | no-minus | no-minus | no-minus | bfs-prev | bfs-prev | bfs-prev | bfs-pre |
| Partitioned        | +        | -        | +        | -        | +        | -        | +        | -       |
| Reorder            | -        | -        | -        | -        | gsa      | gsa      | rb4w     | rb4w    |
| DBM-reduction      | +        | +        | -        | -        | +        | -        | +        | -       |
| fischer1           | 14       | 14       | 14       | 14       | 13       | 13       | 14       | 14      |
| fischer2           | 66       | 66       | 66       | 66       | 65       | 64       | 63       | 61      |
| fischer3           | 288      | 288      | 250      | 250      | 505      | 502      | 433      | 413     |
| fischer4           | 1300     | 1300     | 987      | 987      | 3905     | 3757     | 3190     | 2877    |
| fischer5           | 5535     | 5535     | 3920     | 3920     | 30665    | 26533    | 26004    | 20436   |
| fischer6           | TO       | 22060    | ТО       | 15156    | 240846   | 177329   | 215066   | 140947  |
| critRegion1        | 24       | 24       | 24       | 24       | 24       | 24       | 20       | 20      |
| critRegion2        | 190      | 190      | 140      | 140      | 358      | 399      | 296      | 362     |
| critRegion3        | 3825     | 3825     | 1701     | 1701     | 5798     | 11387    | 5506     | 11296   |
| critRegion4        | ТО       | ТО       | 55890    | 146808   | 146808   | 451815   | 140144   | 459489  |
| Critical_01-25-50  | 25       | 25       | 25       | 25       | 24       | 24       | 23       | 23      |
| Critical_02-25-50  | 262      | 262      | 158      | 158      | 499      | 542      | 427      | 489     |
| Critical_03-25-50  | 11183    | 11183    | 3375     | 3375     | 29517    | 34331    | 28443    | 34754   |
| Critical_04-25-50  | ТО       | ТО      |
| CSMACD_01          | 17       | 17       | 17       | 17       | 17       | 17       | 17       | 17      |
| CSMACD_02          | 108      | 108      | 108      | 108      | 101      | 111      | 101      | 111     |
| CSMACD_03          | 458      | 458      | 435      | 435      | 553      | 578      | 551      | 619     |
| CSMACD_04          | 1356     | 1356     | 1357     | 1357     | 2528     | 2737     | 2520     | 2729    |
| $CSMACD_05$        | 3478     | 3478     | 3790     | 3790     | 8819     | 9422     | 10127    | 10473   |
| CSMACD_06          | 7925     | 7925     | 10099    | 10099    | 37022    | 36646    | 36938    | 36562   |
| CSMACD_07          | 17069    | 17069    | 26381    | 26381    | 104287   | 119267   | 125019   | 119022  |
| CSMACD_08          | 36098    | 36098    | 68197    | 68197    | 399577   | 325031   | 398899   | 367047  |
| viking1            | 15       | 15       | 15       | 15       | 15       | 15       | 24       | 24      |
| viking2            | 37       | 37       | 37       | 37       | 37       | 37       | 66       | 66      |
| viking3            | 86       | 86       | 86       | 86       | 91       | 91       | 176      | 176     |
| viking4            | 105      | 105      | 105      | 105      | 111      | 111      | 196      | 196     |
| viking5            | 124      | 124      | 124      | 124      | 131      | 131      | 216      | 216     |
| viking6            | 233      | 233      | 233      | 233      | 241      | 239      | 504      | 504     |
| viking7            | 190      | 190      | 190      | 190      | 197      | 200      | 342      | 342     |
| viking8            | 224      | 224      | 224      | 224      | 235      | 234      | 415      | 415     |
| viking9            | 263      | 263      | 263      | 263      | 275      | 274      | 495      | 495     |
| viking10           | 304      | 304      | 304      | 304      | 317      | 317      | 581      | 581     |
| viking11           | 347      | 347      | 347      | 347      | 359      | 359      | 671      | 671     |
| viking12           | 342      | 342      | 342      | 342      | 356      | 356      | 621      | 621     |
| Lynch1-16          | 24       | 24       | 24       | 24       | 22       | 22       | 27       | 27      |
| Lynch2-16          | 162      | 162      | 149      | 149      | 185      | 173      | 217      | 210     |
| Lynch3-16          | 922      | 922      | 721      | 721      | 1757     | 1738     | 2600     | 2531    |
| Lynch4-16          | 8246     | 8246     | 6131     | 6131     | 22033    | 23182    | 32144    | 31516   |
| Lynch5-16          | 95782    | 95782    | 51698    | 51698    | 236029   | 265223   | 406904   | 400277  |
| bocdp              | 541      | 541      | 487      | 487      | 355      | 379      | 435      | 434     |
| bocdpFIXED         | 542      | 542      | 488      | 488      | 427      | 487      | 448      | 457     |
| bando              | 542      | 542      | 488      | 488      | 425      | 491      | 448      | 457     |
| timelock           | 4        | 4        | 4        | 4        | 4        | 4        | 4        | 4       |
| Milner-2Nodes-flat | 245      | 245      | 133      | 133      | 327      | 532      | 394      | 586     |
| Milner-3Nodes-flat | 918      | 918      | 528      | 528      | 1571     | 2591     | 1702     | 2732    |
| Milner-4Nodes-flat | 2968     | 2968     | 1776     | 1776     | 4789     | 14916    | 4997     | 15423   |
| Milner-5Nodes-flat | 5293     | 5293     | 3146     | 3146     | 8596     | 27351    | 8946     | 28078   |
| Milner-6Nodes-flat | 7755     | 7755     | 5078     | 5078     | 14026    | 45279    | 14551    | 46271   |
| Milner-7Nodes-flat | 12188    | 12188    | 7668     | 7668     | 21348    | 69708    | 22098    | 71000   |
| Milner-8Nodes-flat | 16324    | 16324    | 11012    | 11012    | 30883    | 101633   | 31874    | 103272  |
| hddi_input_1       | 119      | 119      | 136      | 136      | 134      | 142      | 134      | 148     |
| hddi_input_2       | 693      | 693      | 710      | 710      | 1025     | 999      | 1090     | 1051    |
| hddi_input_3       | 2013     | 2013     | 2338     | 2338     | 3675     | 4815     | 3971     | 5033    |
| hddi_input_4       | 4495     | 4495     | 5377     | 5377     | 11493    | 16680    | 12572    | 17468   |
| hddi_input_5       | 13824    | 13824    | 10331    | 10331    | 19470    | 40262    | 21584    | 43436   |
| hddi_input_6       | 14175    | 14175    | 18682    | 18682    | 57930    | 112878   | 64959    | 118653  |
| hddi_input_7       | TO       | TO       | TO       | TO       | 122999   | 255603   | 122999   | 255603  |
| hddi_input_8       | TO       | TO       | TO       | TO       | 218050   | 503802   | 218050   | 503802  |
| hddi_input_9       | TO       | TO       | TO       | TO       | 307943   | 911847   | 307943   | 911847  |
|                    |          | - U      | 10       | - U      | 301340   | 011011   | 301340   | 011041  |
| hddi_input_10      | ТО       | TO       | TO       | TO       | 508598   | 1621272  | TO       | TO      |

| Statestore         | LDD      | LDD        | LDD            | LDD            | LDD            | LDD            | LDD       | LDD       | LDD       | LDD       |
|--------------------|----------|------------|----------------|----------------|----------------|----------------|-----------|-----------|-----------|-----------|
| Search-order       | bfs-prev | bfs-prev   | bfs-prev       | bfs-prev       | bfs-prev       | bfs-prev       | bfs-prev  | bfs-prev  | bfs-prev  | bfs-prev  |
| Partitioned        | +        | -          | +              | -              | +              | -              | +         | -         | +         | -         |
| Reorder            | cw       | cw         | $_{\rm rs,rn}$ | $_{\rm rs,rn}$ | $_{\rm rs,ru}$ | $_{\rm rs,ru}$ | -         | -         | -         | -         |
| DBM-reduction      | +        | -          | +              | -              | +              | -              | +         | -         | +         | -         |
| fischer1           | 13       | 13         | 14             | 14             | 14             | 14             | 14        | 14        | 14        | 14        |
| fischer2           | 66       | 66         | 66             | 66             | 66             | 66             | 66        | 66        | 66        | 66        |
| fischer3           | 532      | 552        | 409            | 420            | 409            | 420            | 409       | 409       | 420       | 420       |
| fischer4           | 4184     | 4112       | 2541           | 2486           | 2541           | 2486           | 2541      | 2541      | 2486      | 2486      |
| fischer5           | 32446    | 27909      | 17131          | 14526          | 17131          | 14526          | 17131     | 17131     | 14526     | 14526     |
| fischer6           | 247845   | 179025     | 121944         | 85041          | 121944         | 85041          | 121944    | 121944    | 85041     | 85041     |
| critRegion1        | 26       | 26         | 24             | 24             | 24             | 24             | 24        | 24        | 24        | 24        |
| critRegion2        | 242      | 321        | 243            | 326            | 243            | 326            | 243       | 243       | 326       | 326       |
| critRegion3        | 4627     | 11234      | 3743           | 9385           | 3743           | 9385           | 3743      | 3743      | 9385      | 9385      |
| critRegion4        | 116312   | 428689     | 100006         | 369121         | 100006         | 369121         | 100006    | 100006    | 369121    | 369121    |
| Critical_01-25-50  | 29       | 29         | 25             | 25             | 25             | 25             | 25        | 25        | 25        | 25        |
| Critical_02-25-50  | 370      | 404        | 316            | 345            | 316            | 345            | 316       | 316       | 345       | 345       |
| Critical_03-25-50  | 20293    | 27533      | 17505          | 23083          | 17505          | 23083          | 17505     | 17505     | 23083     | 23083     |
| Critical_04-25-50  | ТО       | ТО         | ТО             | ТО             | ТО             | ТО             | ТО        | ТО        | TO        | TO        |
| CSMACD_01          | 17       | 17         | 17             | 17             | 17             | 17             | 17        | 17        | 17        | 17        |
| CSMACD_02          | 101      | 111        | 99             | 109            | 99             | 109            | 99        | 99        | 109       | 109       |
| CSMACD_03          | 551      | 619        | 500            | 558            | 500            | 558            | 500       | 500       | 558       | 558       |
| CSMACD_04          | 2520     | 2729       | 2205           | 2401           | 2205           | 2401           | 2205      | 2205      | 2401      | 2401      |
| CSMACD_05          | 10127    | 10473      | 8634           | 9158           | 8634           | 9158           | 8634      | 8634      | 9158      | 9158      |
| CSMACD_06          | 36938    | 36562      | 30862          | 31948          | 30862          | 31948          | 30862     | 30862     | 31948     | 31948     |
| CSMACD_07          | 125019   | 119022     | 102821         | 104048         | 102821         | 104048         | 102821    | 102821    | 104048    | 104048    |
| CSMACD_08          | 398899   | 367047     | 324047         | 321001         | 324047         | 321001         | 324047    | 324047    | 321001    | 321001    |
| viking1            | 24<br>66 | 24         | 15             | 15             | 15<br>37       | 15<br>37       | 15<br>37  | 15<br>37  | 15        | 15        |
| viking2            | 176      | 66         | 37<br>86       | 37<br>86       | 86             | 86             | 86        | 86        | 37<br>86  | 37<br>86  |
| viking3            | 196      | 176<br>196 | 80<br>105      | 80<br>105      | 80<br>105      | 80<br>105      | 80<br>105 | 80<br>105 | 80<br>105 | 80<br>105 |
| viking4<br>viking5 | 216      | 216        | 103            | 124            | 103            | 103            | 103       | 105       | 103       | 103       |
| viking6            | 504      | 504        | 233            | 233            | 233            | 233            | 233       | 233       | 233       | 233       |
| viking7            | 342      | 342        | 190            | 190            | 190            | 190            | 190       | 190       | 190       | 190       |
| viking8            | 415      | 415        | 224            | 224            | 224            | 224            | 224       | 224       | 224       | 224       |
| viking9            | 495      | 495        | 263            | 263            | 263            | 263            | 263       | 263       | 263       | 263       |
| viking10           | 581      | 581        | 304            | 304            | 304            | 304            | 304       | 304       | 304       | 304       |
| viking11           | 671      | 671        | 347            | 347            | 347            | 347            | 347       | 347       | 347       | 347       |
| viking12           | 621      | 621        | 342            | 342            | 342            | 342            | 342       | 342       | 342       | 342       |
| Lynch1-16          | 21       | 21         | 24             | 24             | 24             | 24             | 24        | 24        | 24        | 24        |
| Lynch2-16          | 187      | 185        | 173            | 180            | 173            | 180            | 173       | 173       | 180       | 180       |
| Lynch3-16          | 1649     | 1924       | 1277           | 1485           | 1277           | 1485           | 1277      | 1277      | 1485      | 1485      |
| Lynch4-16          | 17146    | 22181      | 11113          | 14968          | 11113          | 14968          | 11113     | 11113     | 14968     | 14968     |
| Lynch5-16          | 177187   | 231890     | 112397         | 159146         | 112397         | 159146         | 112397    | 112397    | 159146    | 159146    |
| bocdp              | 517      | 532        | 572            | 587            | 572            | 587            | 572       | 572       | 587       | 587       |
| bocdpFIXED         | 514      | 529        | 572            | 587            | 572            | 587            | 572       | 572       | 587       | 587       |
| bando              | 514      | 529        | 572            | 587            | 572            | 587            | 572       | 572       | 587       | 587       |
| timelock           | 4        | 4          | 4              | 4              | 4              | 4              | 4         | 4         | 4         | 4         |
| Milner-2Nodes-flat | 338      | 543        | 338            | 543            | 338            | 543            | 338       | 338       | 543       | 543       |
| Milner-3Nodes-flat | 1602     | 2622       | 1602           | 2622           | 1602           | 2622           | 1602      | 1602      | 2622      | 2622      |
| Milner-4Nodes-flat | 4834     | 14965      | 4834           | 14965          | 4834           | 14965          | 4834      | 4834      | 14965     | 14965     |
| Milner-5Nodes-flat | 8653     | 27410      | 8653           | 27410          | 8653           | 27410          | 8653      | 8653      | 27410     | 27410     |
| Milner-6Nodes-flat | 14100    | 45357      | 14100          | 45357          | 14100          | 45357          | 14100     | 14100     | 45357     | 45357     |
| Milner-7Nodes-flat | 21455    | 69806      | 21455          | 69806          | 21455          | 69806          | 21455     | 21455     | 69806     | 69806     |
| Milner-8Nodes-flat | 31008    | 101767     | 31008          | 101767         | 31008          | 101767         | 31008     | 31008     | 101767    | 101767    |
| hddi_input_1       | 134      | 142        | 130            | 138            | 130            | 138            | 130       | 130       | 138       | 138       |
| hddi_input_2       | 1023     | 997        | 1021           | 995            | 1021           | 995            | 1021      | 1021      | 995       | 995       |
| hddi_input_3       | 3675     | 4815       | 3675           | 4815           | 3675           | 4815           | 3675      | 3675      | 4815      | 4815      |
| hddi_input_4       | 11499    | 16686      | 11501          | 16688          | 11501          | 16688          | 11501     | 11501     | 16688     | 16688     |
| hddi_input_5       | 19473    | 40265      | 19477          | 40269          | 19477          | 40269          | 19477     | 19477     | 40269     | 40269     |
| hddi_input_6       | 57960    | 112908     | 57966          | 112914         | 57966          | 112914         | 57966     | 57966     | 112914    | 112914    |
| hddi_input_7       | 108366   | 243123     | 108374         | 243131         | 108374         | 243131         | 108374    | 108374    | 243131    | 243131    |
| hddi_input_8       | 189156   | 479334     | 189166         | 479344         | 189166         | 479344         | 189166    | 189166    | 479344    | 479344    |
| hddi_input_9       | 275980   | 802694     | 275992         | 802706         | 275992         | 802706         | 275992    | 275992    | 802706    | 802706    |
| hddi_input_10      | ТО       | ТО         | 454246         | 1412675        | 454246         | 1412675        | ТО        | 454246    | ТО        | 1412675   |
| ANIMO_small        | 185      | 187        | 197            | 199            | 197            | 199            | 197       | 235       | 199       | 237       |