

## lab8, Sydney Ackermann PID A69036053

```
head(mtcars)
```

|                   | mpg  | cyl | disp | hp  | drat | wt    | qsec  | vs | am | gear | carb |
|-------------------|------|-----|------|-----|------|-------|-------|----|----|------|------|
| Mazda RX4         | 21.0 | 6   | 160  | 110 | 3.90 | 2.620 | 16.46 | 0  | 1  | 4    | 4    |
| Mazda RX4 Wag     | 21.0 | 6   | 160  | 110 | 3.90 | 2.875 | 17.02 | 0  | 1  | 4    | 4    |
| Datsun 710        | 22.8 | 4   | 108  | 93  | 3.85 | 2.320 | 18.61 | 1  | 1  | 4    | 1    |
| Hornet 4 Drive    | 21.4 | 6   | 258  | 110 | 3.08 | 3.215 | 19.44 | 1  | 0  | 3    | 1    |
| Hornet Sportabout | 18.7 | 8   | 360  | 175 | 3.15 | 3.440 | 17.02 | 0  | 0  | 3    | 2    |
| Valiant           | 18.1 | 6   | 225  | 105 | 2.76 | 3.460 | 20.22 | 1  | 0  | 3    | 1    |

Let's look at the average mean value of every column.:

```
apply(mtcars, 2, mean) # 2 for col, 1 for rows
```

| mpg       | cyl      | disp       | hp         | drat     | wt       | qsec      |
|-----------|----------|------------|------------|----------|----------|-----------|
| 20.090625 | 6.187500 | 230.721875 | 146.687500 | 3.596563 | 3.217250 | 17.848750 |
| vs        | am       | gear       | carb       |          |          |           |
| 0.437500  | 0.406250 | 3.687500   | 2.812500   |          |          |           |

```
# says average mpg is 20
```

Now let's look at spread in each of these columns. each car (row) is a dimension of the data set.

Let's look at the spread via `sd()`.

```
apply(mtcars, 2, sd)
```



|                   |              |            |             |            |            |
|-------------------|--------------|------------|-------------|------------|------------|
| Valiant           | -0.3302874   | -0.1049878 | -0.04616698 | -0.6080186 | -1.5646078 |
|                   | wt           | qsec       | vs          | am         | gear       |
| Mazda RX4         | -0.610399567 | -0.7771651 | -0.8680278  | 1.1899014  | 0.4235542  |
| Mazda RX4 Wag     | -0.349785269 | -0.4637808 | -0.8680278  | 1.1899014  | 0.4235542  |
| Datsun 710        | -0.917004624 | 0.4260068  | 1.1160357   | 1.1899014  | 0.4235542  |
| Hornet 4 Drive    | -0.002299538 | 0.8904872  | 1.1160357   | -0.8141431 | -0.9318192 |
| Hornet Sportabout | 0.227654255  | -0.4637808 | -0.8680278  | -0.8141431 | -0.9318192 |
| Valiant           | 0.248094592  | 1.3269868  | 1.1160357   | -0.8141431 | -0.9318192 |
|                   | carb         |            |             |            |            |
| Mazda RX4         | 0.7352031    |            |             |            |            |
| Mazda RX4 Wag     | 0.7352031    |            |             |            |            |
| Datsun 710        | -1.1221521   |            |             |            |            |
| Hornet 4 Drive    | -1.1221521   |            |             |            |            |
| Hornet Sportabout | -0.5030337   |            |             |            |            |
| Valiant           | -1.1221521   |            |             |            |            |

What is the mean of each dimension/column in mtscale?

```
round(apply(mtscale, 2, mean), 3) # round to 3 sig figs
```

|     |     |      |    |      |    |      |    |    |      |      |
|-----|-----|------|----|------|----|------|----|----|------|------|
| mpg | cyl | disp | hp | drat | wt | qsec | vs | am | gear | carb |
| 0   | 0   | 0    | 0  | 0    | 0  | 0    | 0  | 0  | 0    | 0    |

#scaling finds the mean center - find the mean of all the data and subtract it from zero

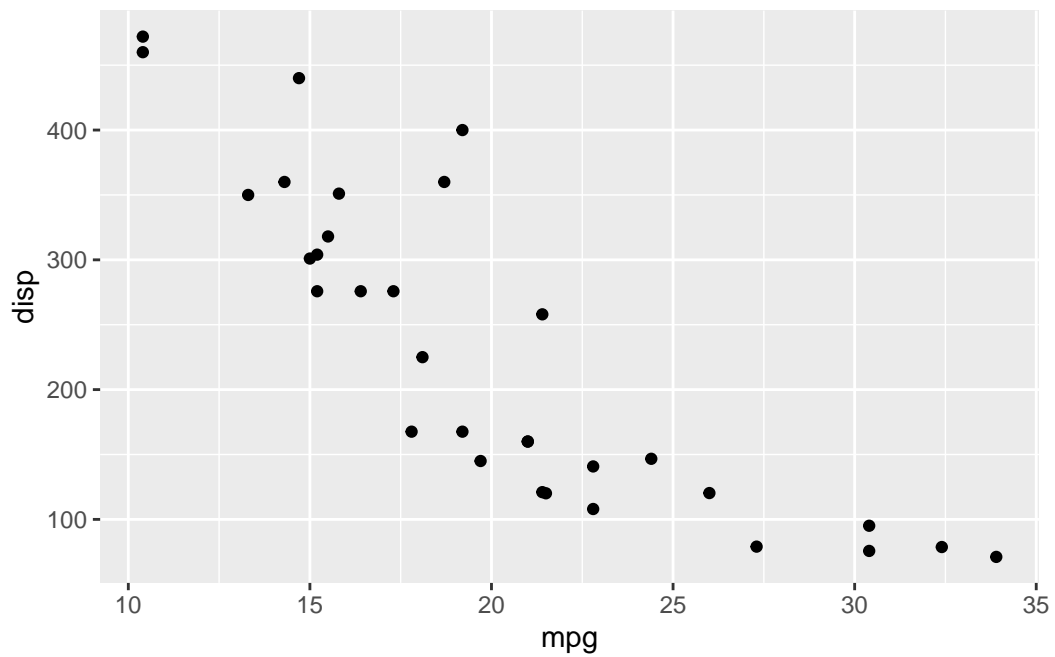
```
round(apply(mtscale, 2, sd), 3)
```

|     |     |      |    |      |    |      |    |    |      |      |
|-----|-----|------|----|------|----|------|----|----|------|------|
| mpg | cyl | disp | hp | drat | wt | qsec | vs | am | gear | carb |
| 1   | 1   | 1    | 1  | 1    | 1  | 1    | 1  | 1  | 1    | 1    |

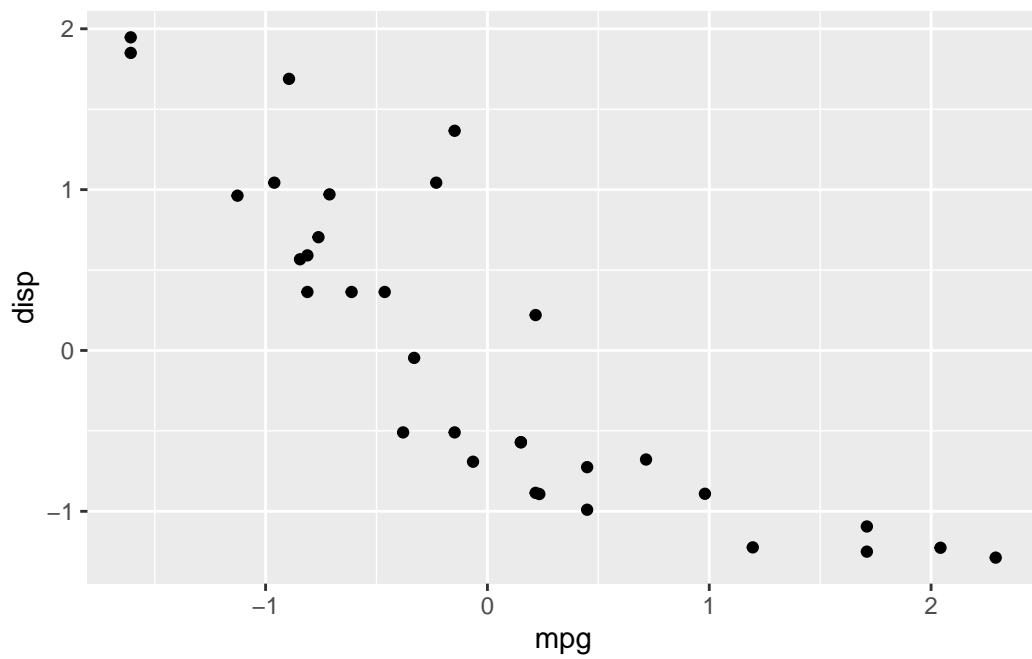
Let's plot mpg vs disp for both mtcars and the scaled version of it (mtscale).

```
library(ggplot2)

ggplot(mtcars) +
  aes(mpg, disp) +
  geom_point()
```

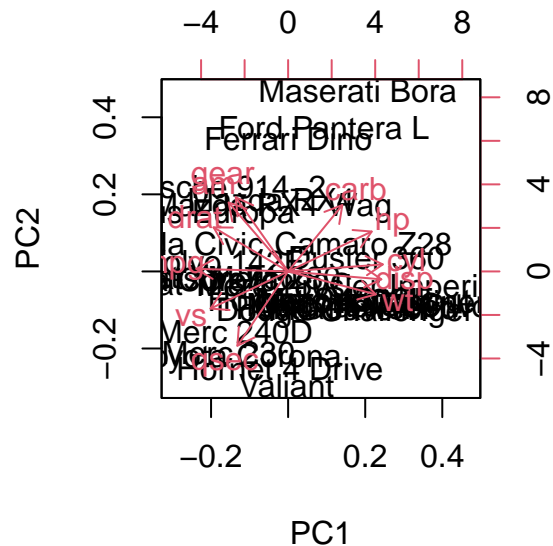


```
ggplot(mtcars) +  
  aes(mpg, disp) +  
  geom_point()
```



The only difference is that it is centered at zero. doesn't change the relationships between the data - it just scales it.

```
pca2 <- prcomp(mtscale)
biplot(pca2)
```



More fair representation of all the cars because its not being dominated by different units.

##Breast Cancer FNA data # were going to do PCA/clustering on this data

```
# first step is to download the csv file and save it in the same directory as your script
fna.data <- "WisconsinCancer.csv"
wisc.df <- read.csv(fna.data, row.names=1) # what does row.names=1 mean? You set the row names
head(wisc.df)
```

|          | diagnosis       | radius_mean      | texture_mean   | perimeter_mean      | area_mean |
|----------|-----------------|------------------|----------------|---------------------|-----------|
| 842302   | M               | 17.99            | 10.38          | 122.80              | 1001.0    |
| 842517   | M               | 20.57            | 17.77          | 132.90              | 1326.0    |
| 84300903 | M               | 19.69            | 21.25          | 130.00              | 1203.0    |
| 84348301 | M               | 11.42            | 20.38          | 77.58               | 386.1     |
| 84358402 | M               | 20.29            | 14.34          | 135.10              | 1297.0    |
| 843786   | M               | 12.45            | 15.70          | 82.57               | 477.1     |
|          | smoothness_mean | compactness_mean | concavity_mean | concave.points_mean |           |

|  |         |          |         |         |         |
|--|---------|----------|---------|---------|---------|
| 842302   | 0.11840 | 0.27760  | 0.3001  | 0.14710 |         |
| 842517   | 0.08474 | 0.07864  | 0.0869  | 0.07017 |         |
| 84300903   | 0.10960 | 0.15990  | 0.1974  | 0.12790 |         |
| 84348301   | 0.14250 | 0.28390  | 0.2414  | 0.10520 |         |
| 84358402   | 0.10030 | 0.13280  | 0.1980  | 0.10430 |         |
| 843786   | 0.12780 | 0.17000  | 0.1578  | 0.08089 |         |
| symmetry_mean fractal_dimension_mean radius_se texture_se perimeter_se |         |          |         |         |         |
| 842302   | 0.2419  | 0.07871  | 1.0950  | 0.9053  | 8.589   |
| 842517   | 0.1812  | 0.05667  | 0.5435  | 0.7339  | 3.398   |
| 84300903   | 0.2069  | 0.05999  | 0.7456  | 0.7869  | 4.585   |
| 84348301   | 0.2597  | 0.09744  | 0.4956  | 1.1560  | 3.445   |
| 84358402   | 0.1809  | 0.05883  | 0.7572  | 0.7813  | 5.438   |
| 843786   | 0.2087  | 0.07613  | 0.3345  | 0.8902  | 2.217   |
| area_se smoothness_se compactness_se concavity_se concave.points_se    |         |          |         |         |         |
| 842302   | 153.40  | 0.006399 | 0.04904 | 0.05373 | 0.01587 |
| 842517   | 74.08   | 0.005225 | 0.01308 | 0.01860 | 0.01340 |
| 84300903   | 94.03   | 0.006150 | 0.04006 | 0.03832 | 0.02058 |
| 84348301   | 27.23   | 0.009110 | 0.07458 | 0.05661 | 0.01867 |
| 84358402   | 94.44   | 0.011490 | 0.02461 | 0.05688 | 0.01885 |
| 843786   | 27.19   | 0.007510 | 0.03345 | 0.03672 | 0.01137 |
| symmetry_se fractal_dimension_se radius_worst texture_worst            |         |          |         |         |         |
| 842302   | 0.03003 | 0.006193 | 25.38   | 17.33   |         |
| 842517   | 0.01389 | 0.003532 | 24.99   | 23.41   |         |
| 84300903   | 0.02250 | 0.004571 | 23.57   | 25.53   |         |
| 84348301   | 0.05963 | 0.009208 | 14.91   | 26.50   |         |
| 84358402   | 0.01756 | 0.005115 | 22.54   | 16.67   |         |
| 843786   | 0.02165 | 0.005082 | 15.47   | 23.75   |         |
| perimeter_worst area_worst smoothness_worst compactness_worst          |         |          |         |         |         |
| 842302   | 184.60  | 2019.0   | 0.1622  | 0.6656  |         |
| 842517   | 158.80  | 1956.0   | 0.1238  | 0.1866  |         |
| 84300903   | 152.50  | 1709.0   | 0.1444  | 0.4245  |         |
| 84348301   | 98.87   | 567.7    | 0.2098  | 0.8663  |         |
| 84358402   | 152.20  | 1575.0   | 0.1374  | 0.2050  |         |
| 843786   | 103.40  | 741.6    | 0.1791  | 0.5249  |         |
| concavity_worst concave.points_worst symmetry_worst                    |         |          |         |         |         |
| 842302   | 0.7119  | 0.2654   | 0.4601  |         |         |
| 842517   | 0.2416  | 0.1860   | 0.2750  |         |         |
| 84300903   | 0.4504  | 0.2430   | 0.3613  |         |         |
| 84348301   | 0.6869  | 0.2575   | 0.6638  |         |         |
| 84358402   | 0.4000  | 0.1625   | 0.2364  |         |         |
| 843786   | 0.5355  | 0.1741   | 0.3985  |         |         |
| fractal_dimension_worst  |         |          |         |         |         |
| 842302   | 0.11890 |          |         |         |         |

|          |         |
|----------|---------|
| 842517   | 0.08902 |
| 84300903 | 0.08758 |
| 84348301 | 0.17300 |
| 84358402 | 0.07678 |
| 843786   | 0.12440 |

Remove the first column from the data set

Q1. How many rows/patients/subjust.

```
nrow(wisc.df)
```

```
[1] 569
```

How many malignants are there? "M"

```
table(wisc.df$diagnosis)
```

```

  B    M
357 212

```

Get rid of diagnosis column

```

wisc.data <- wisc.df[,-1] # gets rid of first column
diagnosis <- as.factor(wisc.df$diagnosis) # benign or malignant, save as a factor
head(wisc.data)

```

|          | radius_mean | texture_mean | perimeter_mean | area_mean | smoothness_mean |
|----------|-------------|--------------|----------------|-----------|-----------------|
| 842302   | 17.99       | 10.38        | 122.80         | 1001.0    | 0.11840         |
| 842517   | 20.57       | 17.77        | 132.90         | 1326.0    | 0.08474         |
| 84300903 | 19.69       | 21.25        | 130.00         | 1203.0    | 0.10960         |
| 84348301 | 11.42       | 20.38        | 77.58          | 386.1     | 0.14250         |
| 84358402 | 20.29       | 14.34        | 135.10         | 1297.0    | 0.10030         |
| 843786   | 12.45       | 15.70        | 82.57          | 477.1     | 0.12780         |

|          | compactness_mean | concavity_mean | concave.points_mean | symmetry_mean |
|----------|------------------|----------------|---------------------|---------------|
| 842302   | 0.27760          | 0.3001         | 0.14710             | 0.2419        |
| 842517   | 0.07864          | 0.0869         | 0.07017             | 0.1812        |
| 84300903 | 0.15990          | 0.1974         | 0.12790             | 0.2069        |
| 84348301 | 0.28390          | 0.2414         | 0.10520             | 0.2597        |

|          |                         |                      |                  |                      |
|----------|-------------------------|----------------------|------------------|----------------------|
| 84358402 | 0.13280                 | 0.1980               | 0.10430          | 0.1809               |
| 843786   | 0.17000                 | 0.1578               | 0.08089          | 0.2087               |
|          | fractal_dimension_mean  | radius_se            | texture_se       | perimeter_se area_se |
| 842302   | 0.07871                 | 1.0950               | 0.9053           | 8.589 153.40         |
| 842517   | 0.05667                 | 0.5435               | 0.7339           | 3.398 74.08          |
| 84300903 | 0.05999                 | 0.7456               | 0.7869           | 4.585 94.03          |
| 84348301 | 0.09744                 | 0.4956               | 1.1560           | 3.445 27.23          |
| 84358402 | 0.05883                 | 0.7572               | 0.7813           | 5.438 94.44          |
| 843786   | 0.07613                 | 0.3345               | 0.8902           | 2.217 27.19          |
|          | smoothness_se           | compactness_se       | concavity_se     | concave.points_se    |
| 842302   | 0.006399                | 0.04904              | 0.05373          | 0.01587              |
| 842517   | 0.005225                | 0.01308              | 0.01860          | 0.01340              |
| 84300903 | 0.006150                | 0.04006              | 0.03832          | 0.02058              |
| 84348301 | 0.009110                | 0.07458              | 0.05661          | 0.01867              |
| 84358402 | 0.011490                | 0.02461              | 0.05688          | 0.01885              |
| 843786   | 0.007510                | 0.03345              | 0.03672          | 0.01137              |
|          | symmetry_se             | fractal_dimension_se | radius_worst     | texture_worst        |
| 842302   | 0.03003                 | 0.006193             | 25.38            | 17.33                |
| 842517   | 0.01389                 | 0.003532             | 24.99            | 23.41                |
| 84300903 | 0.02250                 | 0.004571             | 23.57            | 25.53                |
| 84348301 | 0.05963                 | 0.009208             | 14.91            | 26.50                |
| 84358402 | 0.01756                 | 0.005115             | 22.54            | 16.67                |
| 843786   | 0.02165                 | 0.005082             | 15.47            | 23.75                |
|          | perimeter_worst         | area_worst           | smoothness_worst | compactness_worst    |
| 842302   | 184.60                  | 2019.0               | 0.1622           | 0.6656               |
| 842517   | 158.80                  | 1956.0               | 0.1238           | 0.1866               |
| 84300903 | 152.50                  | 1709.0               | 0.1444           | 0.4245               |
| 84348301 | 98.87                   | 567.7                | 0.2098           | 0.8663               |
| 84358402 | 152.20                  | 1575.0               | 0.1374           | 0.2050               |
| 843786   | 103.40                  | 741.6                | 0.1791           | 0.5249               |
|          | concavity_worst         | concave.points_worst | symmetry_worst   |                      |
| 842302   | 0.7119                  | 0.2654               | 0.4601           |                      |
| 842517   | 0.2416                  | 0.1860               | 0.2750           |                      |
| 84300903 | 0.4504                  | 0.2430               | 0.3613           |                      |
| 84348301 | 0.6869                  | 0.2575               | 0.6638           |                      |
| 84358402 | 0.4000                  | 0.1625               | 0.2364           |                      |
| 843786   | 0.5355                  | 0.1741               | 0.3985           |                      |
|          | fractal_dimension_worst |                      |                  |                      |
| 842302   | 0.11890                 |                      |                  |                      |
| 842517   | 0.08902                 |                      |                  |                      |
| 84300903 | 0.08758                 |                      |                  |                      |
| 84348301 | 0.17300                 |                      |                  |                      |
| 84358402 | 0.07678                 |                      |                  |                      |



843786

0.12440

```
# now there is no diagnosis column, because we dont want to include that in our analysis  
#will compare with it at the end
```

Useful functions: `table()`, `grep()` -> finds matching patterns

Q3. How many variables/features (can be called by `colnames()`) in the data are suffixed with `_mean`?

```
#colnames(wisc.data)  
length(grep("_mean", colnames(wisc.data), value="T"))
```

[1] 10

## 2 PCA Principle Component Analysis

We want to scale our data before PCA by setting the `scale=True` argument.

```
wisc.pr <- prcomp(wisc.data, scale=TRUE)
```

How much variance is captured in each Principle component?

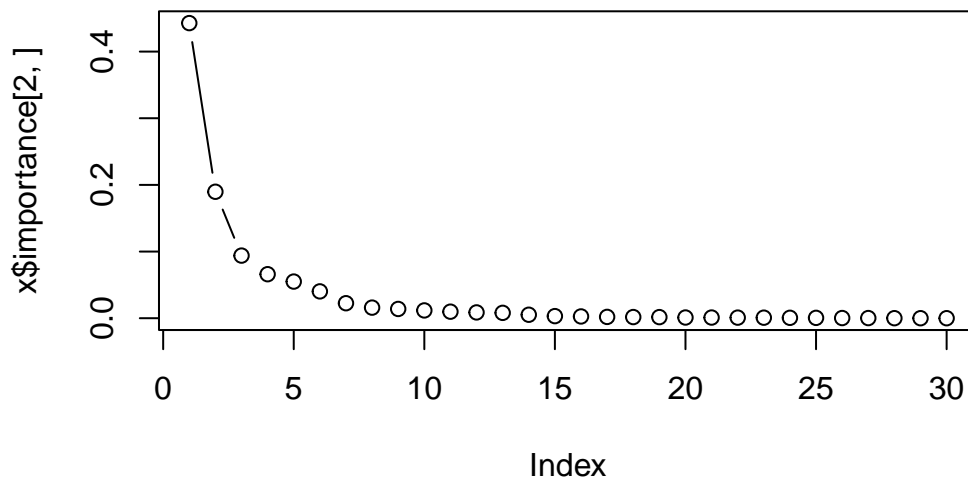
```
x <-summary(wisc.pr)  
x$importance
```

|                        | PC1       | PC2       | PC3       | PC4       | PC5       | PC6      |
|------------------------|-----------|-----------|-----------|-----------|-----------|----------|
| Standard deviation     | 3.644394  | 2.385656  | 1.678675  | 1.407352  | 1.284029  | 1.098798 |
| Proportion of Variance | 0.442720  | 0.189710  | 0.093930  | 0.066020  | 0.054960  | 0.040250 |
| Cumulative Proportion  | 0.442720  | 0.632430  | 0.726360  | 0.792390  | 0.847340  | 0.887590 |
|                        | PC7       | PC8       | PC9       | PC10      | PC11      |          |
| Standard deviation     | 0.8217178 | 0.6903746 | 0.6456739 | 0.5921938 | 0.5421399 |          |
| Proportion of Variance | 0.0225100 | 0.0158900 | 0.0139000 | 0.0116900 | 0.0098000 |          |
| Cumulative Proportion  | 0.9101000 | 0.9259800 | 0.9398800 | 0.9515700 | 0.9613700 |          |
|                        | PC12      | PC13      | PC14      | PC15      | PC16      |          |
| Standard deviation     | 0.5110395 | 0.4912815 | 0.3962445 | 0.3068142 | 0.2826001 |          |
| Proportion of Variance | 0.0087100 | 0.0080500 | 0.0052300 | 0.0031400 | 0.0026600 |          |
| Cumulative Proportion  | 0.9700700 | 0.9781200 | 0.9833500 | 0.9864900 | 0.9891500 |          |
|                        | PC17      | PC18      | PC19      | PC20      | PC21      |          |

|                        |            |           |            |            |           |
|------------------------|------------|-----------|------------|------------|-----------|
| Standard deviation     | 0.2437192  | 0.2293878 | 0.2224356  | 0.1765203  | 0.1731268 |
| Proportion of Variance | 0.0019800  | 0.0017500 | 0.0016500  | 0.0010400  | 0.0010000 |
| Cumulative Proportion  | 0.9911300  | 0.9928800 | 0.9945300  | 0.9955700  | 0.9965700 |
|                        | PC22       | PC23      | PC24       | PC25       | PC26      |
| Standard deviation     | 0.1656484  | 0.1560155 | 0.1343689  | 0.1244238  | 0.0904303 |
| Proportion of Variance | 0.0009100  | 0.0008100 | 0.0006000  | 0.0005200  | 0.0002700 |
| Cumulative Proportion  | 0.9974900  | 0.9983000 | 0.9989000  | 0.9994200  | 0.9996900 |
|                        | PC27       | PC28      | PC29       | PC30       |           |
| Standard deviation     | 0.08306903 | 0.0398665 | 0.02736427 | 0.01153451 |           |
| Proportion of Variance | 0.00023000 | 0.0000500 | 0.00002000 | 0.00000000 |           |
| Cumulative Proportion  | 0.99992000 | 0.9999700 | 1.00000000 | 1.00000000 |           |

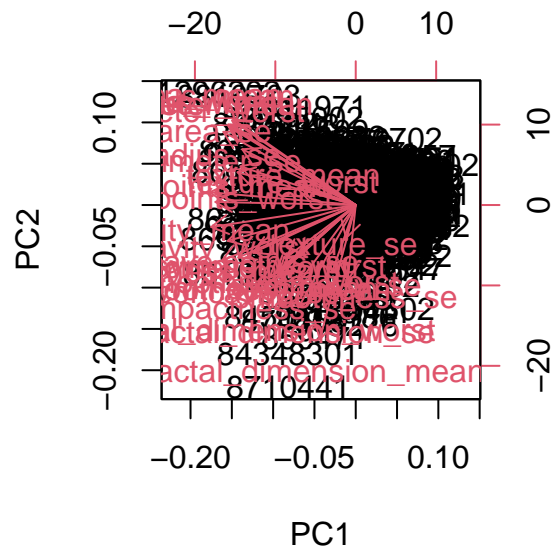
```
# plot variance against PC and look for elbow point
# look here at the summulative proportion numbers
```

```
plot(x$importance[2,], typ="b")
```



Elbow happens around index 3.

```
biplot(wisc.pr) # useless plot
```



```
attributes(wisc.pr)
```

```
$names
```

```
[1] "sdev"      "rotation" "center"    "scale"     "x"
```

```
$class
```

```
[1] "prcomp"
```

x is what we're after

```
head(wisc.pr$x)
```

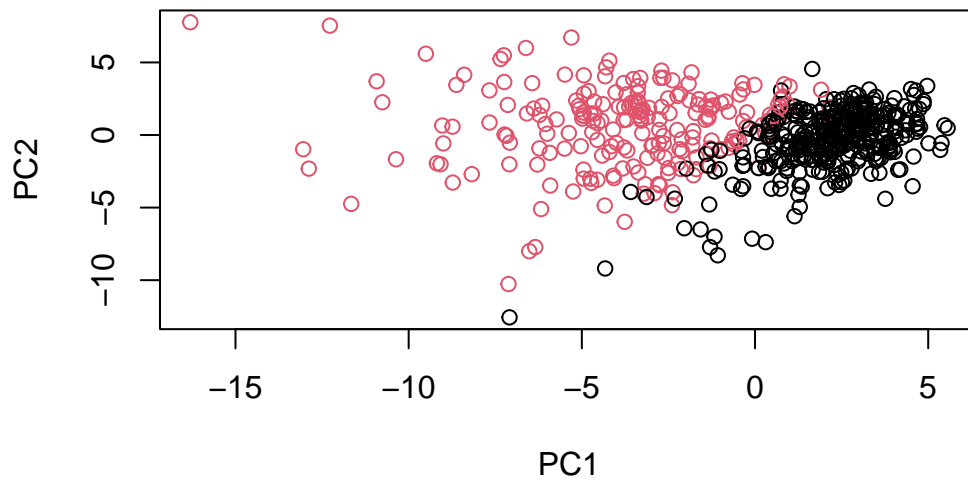
|          | PC1        | PC2        | PC3         | PC4        | PC5        | PC6         |
|----------|------------|------------|-------------|------------|------------|-------------|
| 842302   | -9.184755  | -1.946870  | -1.1221788  | 3.6305364  | 1.1940595  | 1.41018364  |
| 842517   | -2.385703  | 3.764859   | -0.5288274  | 1.1172808  | -0.6212284 | 0.02863116  |
| 84300903 | -5.728855  | 1.074229   | -0.5512625  | 0.9112808  | 0.1769302  | 0.54097615  |
| 84348301 | -7.116691  | -10.266556 | -3.2299475  | 0.1524129  | 2.9582754  | 3.05073750  |
| 84358402 | -3.931842  | 1.946359   | 1.3885450   | 2.9380542  | -0.5462667 | -1.22541641 |
| 843786   | -2.378155  | -3.946456  | -2.9322967  | 0.9402096  | 1.0551135  | -0.45064213 |
|          | PC7        | PC8        | PC9         | PC10       | PC11       | PC12        |
| 842302   | 2.15747152 | 0.39805698 | -0.15698023 | -0.8766305 | -0.2627243 | -0.8582593  |

|          |               |              |               |              |             |            |
|----------|---------------|--------------|---------------|--------------|-------------|------------|
| 842517   | 0.01334635    | -0.24077660  | -0.71127897   | 1.1060218    | -0.8124048  | 0.1577838  |
| 84300903 | -0.66757908   | -0.09728813  | 0.02404449    | 0.4538760    | 0.6050715   | 0.1242777  |
| 84348301 | 1.42865363    | -1.05863376  | -1.40420412   | -1.1159933   | 1.1505012   | 1.0104267  |
| 84358402 | -0.93538950   | -0.63581661  | -0.26357355   | 0.3773724    | -0.6507870  | -0.1104183 |
| 843786   | 0.49001396    | 0.16529843   | -0.13335576   | -0.5299649   | -0.1096698  | 0.0813699  |
|          | PC13          | PC14         | PC15          | PC16         | PC17        |            |
| 842302   | 0.10329677    | -0.690196797 | 0.601264078   | 0.74446075   | -0.26523740 |            |
| 842517   | -0.94269981   | -0.652900844 | -0.008966977  | -0.64823831  | -0.01719707 |            |
| 84300903 | -0.41026561   | 0.016665095  | -0.482994760  | 0.32482472   | 0.19075064  |            |
| 84348301 | -0.93245070   | -0.486988399 | 0.168699395   | 0.05132509   | 0.48220960  |            |
| 84358402 | 0.38760691    | -0.538706543 | -0.310046684  | -0.15247165  | 0.13302526  |            |
| 843786   | -0.02625135   | 0.003133944  | -0.178447576  | -0.01270566  | 0.19671335  |            |
|          | PC18          | PC19         | PC20          | PC21         | PC22        |            |
| 842302   | -0.54907956   | 0.1336499    | 0.34526111    | 0.096430045  | -0.06878939 |            |
| 842517   | 0.31801756    | -0.2473470   | -0.11403274   | -0.077259494 | 0.09449530  |            |
| 84300903 | -0.08789759   | -0.3922812   | -0.20435242   | 0.310793246  | 0.06025601  |            |
| 84348301 | -0.03584323   | -0.0267241   | -0.46432511   | 0.433811661  | 0.20308706  |            |
| 84358402 | -0.01869779   | 0.4610302    | 0.06543782    | -0.116442469 | 0.01763433  |            |
| 843786   | -0.29727706   | -0.1297265   | -0.07117453   | -0.002400178 | 0.10108043  |            |
|          | PC23          | PC24         | PC25          | PC26         | PC27        |            |
| 842302   | 0.08444429    | 0.175102213  | 0.150887294   | -0.201326305 | -0.25236294 |            |
| 842517   | -0.21752666   | -0.011280193 | 0.170360355   | -0.041092627 | 0.18111081  |            |
| 84300903 | -0.07422581   | -0.102671419 | -0.171007656  | 0.004731249  | 0.04952586  |            |
| 84348301 | -0.12399554   | -0.153294780 | -0.077427574  | -0.274982822 | 0.18330078  |            |
| 84358402 | 0.13933105    | 0.005327110  | -0.003059371  | 0.039219780  | 0.03213957  |            |
| 843786   | 0.03344819    | -0.002837749 | -0.122282765  | -0.030272333 | -0.08438081 |            |
|          | PC28          | PC29         | PC30          |              |             |            |
| 842302   | -0.0338846387 | 0.045607590  | 0.0471277407  |              |             |            |
| 842517   | 0.0325955021  | -0.005682424 | 0.0018662342  |              |             |            |
| 84300903 | 0.0469844833  | 0.003143131  | -0.0007498749 |              |             |            |
| 84348301 | 0.0424469831  | -0.069233868 | 0.0199198881  |              |             |            |
| 84358402 | -0.0347556386 | 0.005033481  | -0.0211951203 |              |             |            |
| 843786   | 0.0007296587  | -0.019703996 | -0.0034564331 |              |             |            |

These are the coordinates of the patients on the new axis main pca plot could plot whatever biplot of pcx vs pcy that you want

My main PC result figure (coordination plot)

```
plot(wisc.pr$x, col=diagnosis) # will plot pc1 vs pc2, first two columns
```



```
# colour red for malignant, benign for black
```

Still don't understand PC -> what is PC1? made up of many factors the point is to reduce the dimensionality of the data, to figure out which key factors make up PC1 i.e. explain most of the variation

Each point represents a patient.

Points with little influence are closer to 0.

```
# create a data frame to plot

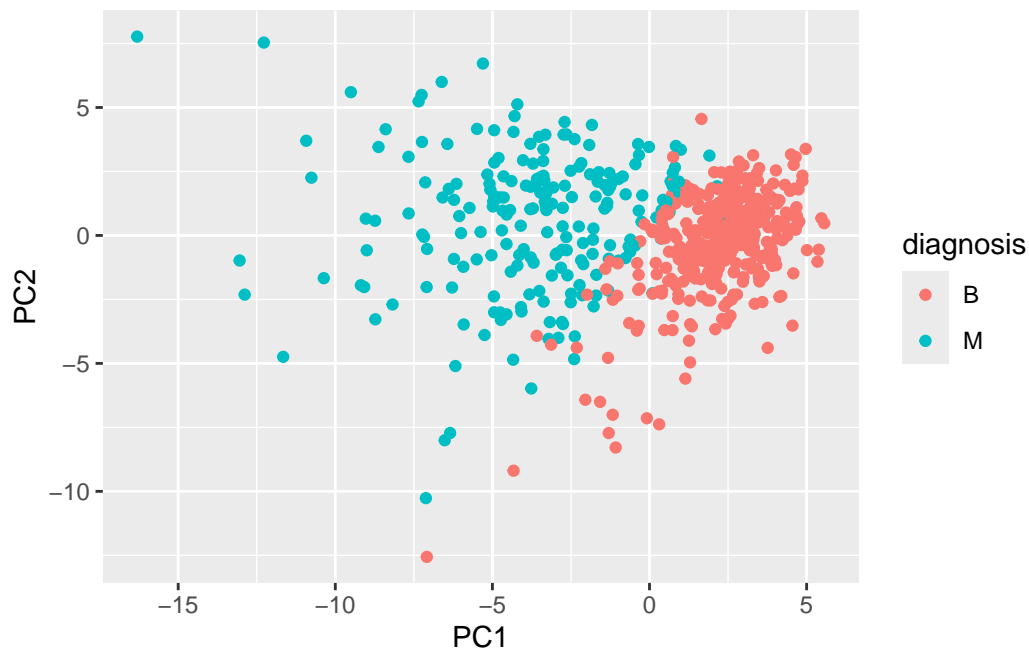
df <- as.data.frame(wisc.pr$x) # just the x column
df$diagnosis <- diagnosis

library(ggplot2)

# Make a scatter plot and colour by diagnosis

# just want coordinates and diagnosis so that's why we are creating our own new data frame.

ggplot(df)+
  aes(PC1, PC2, col=diagnosis)+
  geom_point()
```



```
head(df)
```

|          | PC1         | PC2          | PC3          | PC4         | PC5         | PC6         |
|----------|-------------|--------------|--------------|-------------|-------------|-------------|
| 842302   | -9.184755   | -1.946870    | -1.1221788   | 3.6305364   | 1.1940595   | 1.41018364  |
| 842517   | -2.385703   | 3.764859     | -0.5288274   | 1.1172808   | -0.6212284  | 0.02863116  |
| 84300903 | -5.728855   | 1.074229     | -0.5512625   | 0.9112808   | 0.1769302   | 0.54097615  |
| 84348301 | -7.116691   | -10.266556   | -3.2299475   | 0.1524129   | 2.9582754   | 3.05073750  |
| 84358402 | -3.931842   | 1.946359     | 1.3885450    | 2.9380542   | -0.5462667  | -1.22541641 |
| 843786   | -2.378155   | -3.946456    | -2.9322967   | 0.9402096   | 1.0551135   | -0.45064213 |
|          | PC7         | PC8          | PC9          | PC10        | PC11        | PC12        |
| 842302   | 2.15747152  | 0.39805698   | -0.15698023  | -0.8766305  | -0.2627243  | -0.8582593  |
| 842517   | 0.01334635  | -0.24077660  | -0.71127897  | 1.1060218   | -0.8124048  | 0.1577838   |
| 84300903 | -0.66757908 | -0.09728813  | 0.02404449   | 0.4538760   | 0.6050715   | 0.1242777   |
| 84348301 | 1.42865363  | -1.05863376  | -1.40420412  | -1.1159933  | 1.1505012   | 1.0104267   |
| 84358402 | -0.93538950 | -0.63581661  | -0.26357355  | 0.3773724   | -0.6507870  | -0.1104183  |
| 843786   | 0.49001396  | 0.16529843   | -0.13335576  | -0.5299649  | -0.1096698  | 0.0813699   |
|          | PC13        | PC14         | PC15         | PC16        | PC17        |             |
| 842302   | 0.10329677  | -0.690196797 | 0.601264078  | 0.74446075  | -0.26523740 |             |
| 842517   | -0.94269981 | -0.652900844 | -0.008966977 | -0.64823831 | -0.01719707 |             |
| 84300903 | -0.41026561 | 0.016665095  | -0.482994760 | 0.32482472  | 0.19075064  |             |
| 84348301 | -0.93245070 | -0.486988399 | 0.168699395  | 0.05132509  | 0.48220960  |             |
| 84358402 | 0.38760691  | -0.538706543 | -0.310046684 | -0.15247165 | 0.13302526  |             |

|          |               |              |               |              |             |
|----------|---------------|--------------|---------------|--------------|-------------|
| 843786   | -0.02625135   | 0.003133944  | -0.178447576  | -0.01270566  | 0.19671335  |
|          | PC18          | PC19         | PC20          | PC21         | PC22        |
| 842302   | -0.54907956   | 0.1336499    | 0.34526111    | 0.096430045  | -0.06878939 |
| 842517   | 0.31801756    | -0.2473470   | -0.11403274   | -0.077259494 | 0.09449530  |
| 84300903 | -0.08789759   | -0.3922812   | -0.20435242   | 0.310793246  | 0.06025601  |
| 84348301 | -0.03584323   | -0.0267241   | -0.46432511   | 0.433811661  | 0.20308706  |
| 84358402 | -0.01869779   | 0.4610302    | 0.06543782    | -0.116442469 | 0.01763433  |
| 843786   | -0.29727706   | -0.1297265   | -0.07117453   | -0.002400178 | 0.10108043  |
|          | PC23          | PC24         | PC25          | PC26         | PC27        |
| 842302   | 0.08444429    | 0.175102213  | 0.150887294   | -0.201326305 | -0.25236294 |
| 842517   | -0.21752666   | -0.011280193 | 0.170360355   | -0.041092627 | 0.18111081  |
| 84300903 | -0.07422581   | -0.102671419 | -0.171007656  | 0.004731249  | 0.04952586  |
| 84348301 | -0.12399554   | -0.153294780 | -0.077427574  | -0.274982822 | 0.18330078  |
| 84358402 | 0.13933105    | 0.005327110  | -0.003059371  | 0.039219780  | 0.03213957  |
| 843786   | 0.03344819    | -0.002837749 | -0.122282765  | -0.030272333 | -0.08438081 |
|          | PC28          | PC29         | PC30          | diagnosis    |             |
| 842302   | -0.0338846387 | 0.045607590  | 0.0471277407  |              | M           |
| 842517   | 0.0325955021  | -0.005682424 | 0.0018662342  |              | M           |
| 84300903 | 0.0469844833  | 0.003143131  | -0.0007498749 |              | M           |
| 84348301 | 0.0424469831  | -0.069233868 | 0.0199198881  |              | M           |
| 84358402 | -0.0347556386 | 0.005033481  | -0.0211951203 |              | M           |
| 843786   | 0.0007296587  | -0.019703996 | -0.0034564331 |              | M           |

## Variance explained

```
# calculate the variance of each principle component

pr.var <- wisc.pr$sdev^2 # what is wisc.pr again? a table of the PC's and their standard dev.
head(pr.var)
```

```
[1] 13.281608  5.691355  2.817949  1.980640  1.648731  1.207357
```

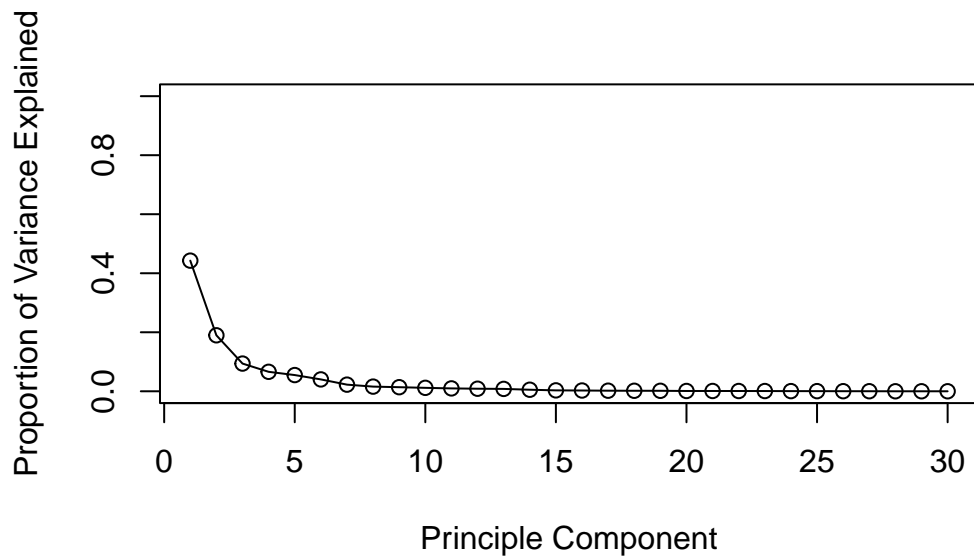
Now we will calculate the variance explained by each PC by dividing by the total variance explained by all PCs

```
pve <- (pr.var)/(sum(pr.var))
pve
```

```
[1] 4.427203e-01 1.897118e-01 9.393163e-02 6.602135e-02 5.495768e-02
```

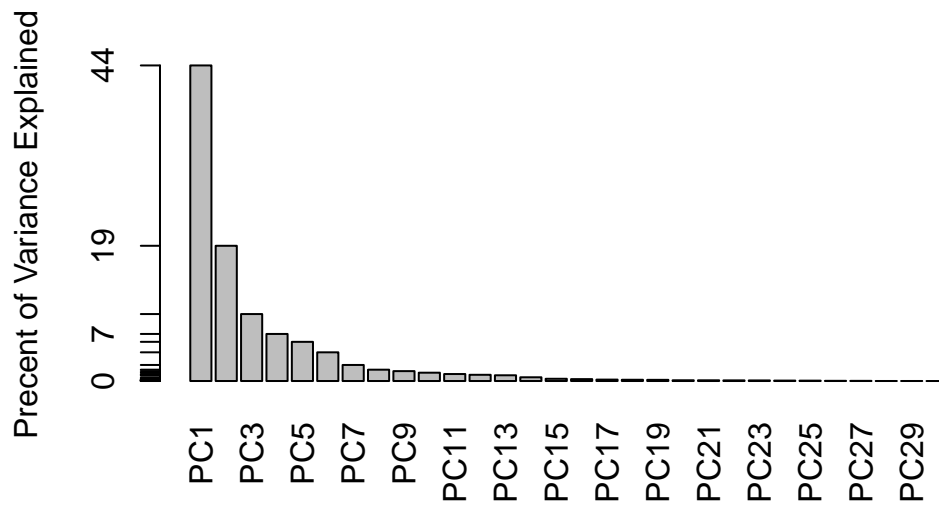
```
[6] 4.024522e-02 2.250734e-02 1.588724e-02 1.389649e-02 1.168978e-02
[11] 9.797190e-03 8.705379e-03 8.045250e-03 5.233657e-03 3.137832e-03
[16] 2.662093e-03 1.979968e-03 1.753959e-03 1.649253e-03 1.038647e-03
[21] 9.990965e-04 9.146468e-04 8.113613e-04 6.018336e-04 5.160424e-04
[26] 2.725880e-04 2.300155e-04 5.297793e-05 2.496010e-05 4.434827e-06
```

```
# now plot the variance explained by each pc: pve
plot(pve, xlab="Principle Component", ylab = "Proportion of Variance Explained", ylim = c(0,
```



```
# Alternative scree plot of the same data, note data driven y-axis
barplot(pve, ylab = "Precent of Variance Explained",
        names.arg=paste0("PC",1:length(pve)), las=2, axes = FALSE)
axis(2, at=pve, labels=round(pve,2)*100 )
```





Q9. For the first principal component, what is the component of the loading vector (i.e. `wisc.pr$rotation[,1]`) for the feature `concave.points_mean`? This tells us how much this original feature contributes to the first PC.

```
wisc.pr$rotation[,1]["concave.points_mean"]
```

```
concave.points_mean
-0.2608538
```

## Hierarchical Clustering

We are going to do hierarchical clustering of the original data. This kind of analysis doesn't require us to know how many clusters there should be in advance - unlike kmeans clustering.

First scale the `wisc.data` data and assign the result to `data.scaled`

```
head(wisc.data)
```

|          | radius_mean | texture_mean | perimeter_mean | area_mean | smoothness_mean |
|----------|-------------|--------------|----------------|-----------|-----------------|
| 842302   | 17.99       | 10.38        | 122.80         | 1001.0    | 0.11840         |
| 842517   | 20.57       | 17.77        | 132.90         | 1326.0    | 0.08474         |
| 84300903 | 19.69       | 21.25        | 130.00         | 1203.0    | 0.10960         |

|          |                        |                      |                     |                   |         |
|----------|------------------------|----------------------|---------------------|-------------------|---------|
| 84348301 | 11.42                  | 20.38                | 77.58               | 386.1             | 0.14250 |
| 84358402 | 20.29                  | 14.34                | 135.10              | 1297.0            | 0.10030 |
| 843786   | 12.45                  | 15.70                | 82.57               | 477.1             | 0.12780 |
|          | compactness_mean       | concavity_mean       | concave.points_mean | symmetry_mean     |         |
| 842302   | 0.27760                | 0.3001               | 0.14710             | 0.2419            |         |
| 842517   | 0.07864                | 0.0869               | 0.07017             | 0.1812            |         |
| 84300903 | 0.15990                | 0.1974               | 0.12790             | 0.2069            |         |
| 84348301 | 0.28390                | 0.2414               | 0.10520             | 0.2597            |         |
| 84358402 | 0.13280                | 0.1980               | 0.10430             | 0.1809            |         |
| 843786   | 0.17000                | 0.1578               | 0.08089             | 0.2087            |         |
|          | fractal_dimension_mean | radius_se            | texture_se          | perimeter_se      | area_se |
| 842302   | 0.07871                | 1.0950               | 0.9053              | 8.589             | 153.40  |
| 842517   | 0.05667                | 0.5435               | 0.7339              | 3.398             | 74.08   |
| 84300903 | 0.05999                | 0.7456               | 0.7869              | 4.585             | 94.03   |
| 84348301 | 0.09744                | 0.4956               | 1.1560              | 3.445             | 27.23   |
| 84358402 | 0.05883                | 0.7572               | 0.7813              | 5.438             | 94.44   |
| 843786   | 0.07613                | 0.3345               | 0.8902              | 2.217             | 27.19   |
|          | smoothness_se          | compactness_se       | concavity_se        | concave.points_se |         |
| 842302   | 0.006399               | 0.04904              | 0.05373             | 0.01587           |         |
| 842517   | 0.005225               | 0.01308              | 0.01860             | 0.01340           |         |
| 84300903 | 0.006150               | 0.04006              | 0.03832             | 0.02058           |         |
| 84348301 | 0.009110               | 0.07458              | 0.05661             | 0.01867           |         |
| 84358402 | 0.011490               | 0.02461              | 0.05688             | 0.01885           |         |
| 843786   | 0.007510               | 0.03345              | 0.03672             | 0.01137           |         |
|          | symmetry_se            | fractal_dimension_se | radius_worst        | texture_worst     |         |
| 842302   | 0.03003                | 0.006193             | 25.38               | 17.33             |         |
| 842517   | 0.01389                | 0.003532             | 24.99               | 23.41             |         |
| 84300903 | 0.02250                | 0.004571             | 23.57               | 25.53             |         |
| 84348301 | 0.05963                | 0.009208             | 14.91               | 26.50             |         |
| 84358402 | 0.01756                | 0.005115             | 22.54               | 16.67             |         |
| 843786   | 0.02165                | 0.005082             | 15.47               | 23.75             |         |
|          | perimeter_worst        | area_worst           | smoothness_worst    | compactness_worst |         |
| 842302   | 184.60                 | 2019.0               | 0.1622              | 0.6656            |         |
| 842517   | 158.80                 | 1956.0               | 0.1238              | 0.1866            |         |
| 84300903 | 152.50                 | 1709.0               | 0.1444              | 0.4245            |         |
| 84348301 | 98.87                  | 567.7                | 0.2098              | 0.8663            |         |
| 84358402 | 152.20                 | 1575.0               | 0.1374              | 0.2050            |         |
| 843786   | 103.40                 | 741.6                | 0.1791              | 0.5249            |         |
|          | concavity_worst        | concave.points_worst | symmetry_worst      |                   |         |
| 842302   | 0.7119                 | 0.2654               | 0.4601              |                   |         |
| 842517   | 0.2416                 | 0.1860               | 0.2750              |                   |         |
| 84300903 | 0.4504                 | 0.2430               | 0.3613              |                   |         |
| 84348301 | 0.6869                 | 0.2575               | 0.6638              |                   |         |

|          |                         |        |        |
|----------|-------------------------|--------|--------|
| 84358402 | 0.4000                  | 0.1625 | 0.2364 |
| 843786   | 0.5355                  | 0.1741 | 0.3985 |
|          | fractal_dimension_worst |        |        |
| 842302   | 0.11890                 |        |        |
| 842517   | 0.08902                 |        |        |
| 84300903 | 0.08758                 |        |        |
| 84348301 | 0.17300                 |        |        |
| 84358402 | 0.07678                 |        |        |
| 843786   | 0.12440                 |        |        |

Try to cluster the wisc.data

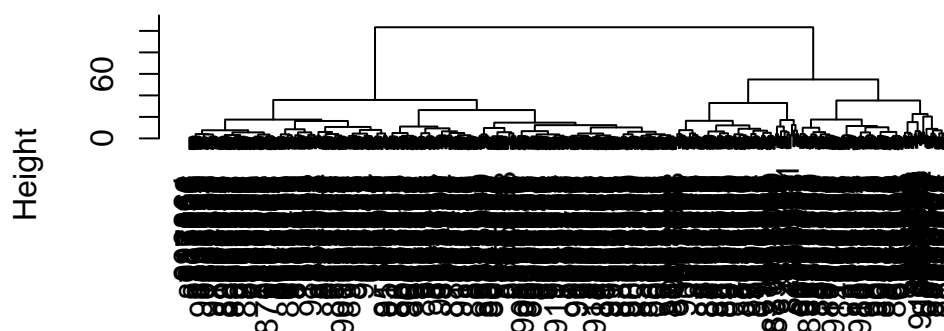
```
km <- kmeans(wisc.data, centers = 2)
table(km$cluster)
```

```
  1   2
438 131
```

In other words use my PCA results as a basis of clustering. PCA is giving some signal. now we will cluster based on that signal

```
d <- dist(wisc.pr$x[,1:3])
hc <- hclust(d, method="ward.D2")
plot(hc)
```

## Cluster Dendrogram



d  
hclust (\*, "ward.D2")

#use these moved variables , pc1, pc2, pc3 as input to cluster rather than the original data

Cut this tree to yeild s groups/clusters

```
grps <- cutree(hc, k=2)
table(grps)
```

```
grps
  1  2
203 366
```

Compare to my expert M and B diagnosis

```
table(diagnosis)
```

```
diagnosis
  B  M
357 212
```

Cross table

```
table(diagnosis, grps)
```

```
      grps  
diagnosis  1   2  
  B    24 333  
  M   179  33
```

$179+33 = 212$  and the vast majority are cluster 1 this table shows how the clustering and expert diagnosis correspond.

Getting 179 correct, and 33 not correct - figuring out the false positives ideally want to get all M's into cluster 1 so you are 100% good at catching all M's

Trade-off between sensitivity and specificity.

do up to Q12

### 3 Hierarchical Clustering

First scale the wisc.data

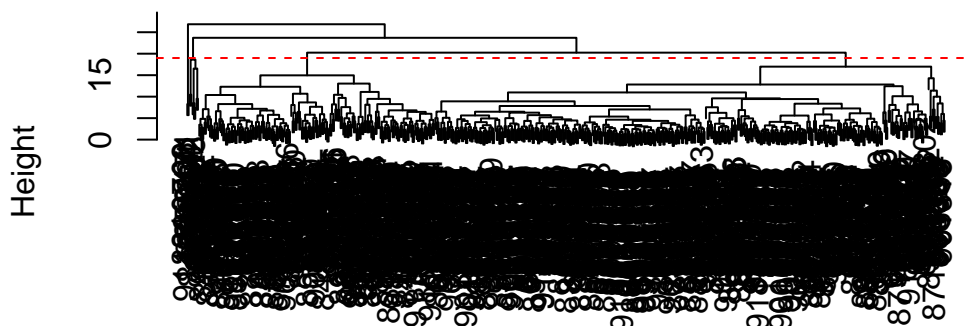
```
data.scaled <- scale(wisc.data)  
  
# now calculate the distance between all pairs in the scaled version  
data.dist <- dist(data.scaled, method = "euclidean")  
  
# create a hierarchical clustering model  
  
wisc.hclust <- hclust(data.dist)
```

### Results of hierarchical clustering

10 What is the height at which the clustering model has 4 clusters

```
plot(wisc.hclust)  
abline(19, 0, col="red", lty=2)
```

## Cluster Dendrogram



```
data.dist  
hclust (*, "complete")
```

It happens at height 19

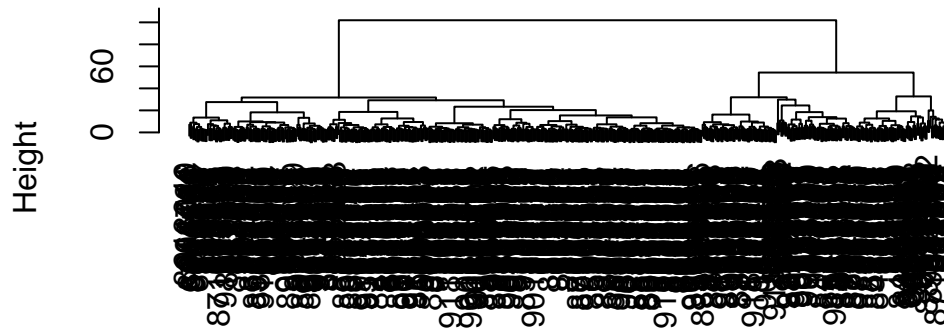
### Using different methods

As we discussed in our last class videos there are number of different “methods” we can use to combine points during the hierarchical clustering procedure. These include “single”, “complete”, “average” and (my favorite) “ward.D2” >Q12 Which method gives your favorite results for the same data.dist dataset? Explain your reasoning.

“Complete” and “ward.D2” are my favourites because they produce the trees that are the easiest to read.

```
wisc.hclust <- hclust(data.dist, method="ward.D2")  
plot(wisc.hclust)
```

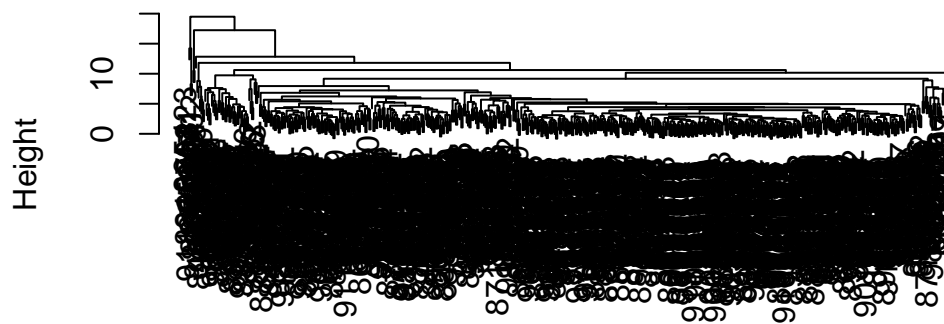
## Cluster Dendrogram



```
data.dist  
hclust (*, "ward.D2")
```

```
wisc.hclust <- hclust(data.dist, method="average")  
plot(wisc.hclust)
```

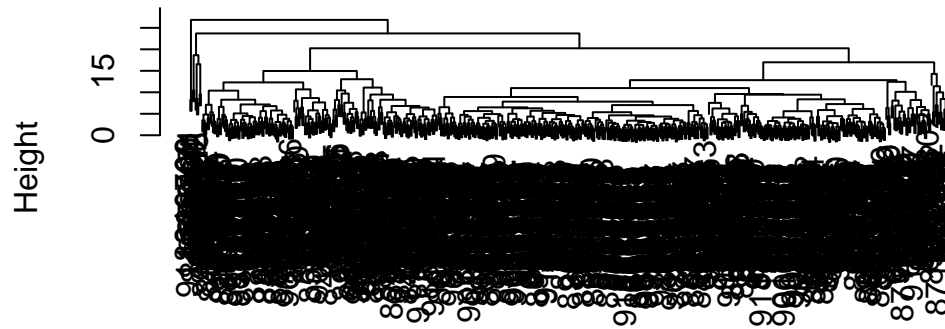
## Cluster Dendrogram



```
data.dist  
hclust (*, "average")
```

```
wisc.hclust <- hclust(data.dist, method="complete")  
plot(wisc.hclust)
```

## Cluster Dendrogram

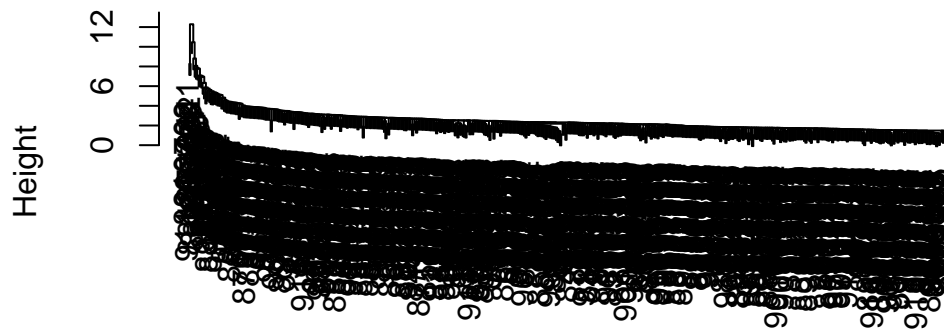


data.dist  
hclust (\*, "complete")

```
wisc.hclust <- hclust(data.dist, method="single")  
plot(wisc.hclust)
```



## Cluster Dendrogram



```
data.dist  
hclust (*, "single")
```

stop at ## 4 combining methods