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Question 4.1: Solution:

Given likelihoods:

	pos	neg
I	0.09	0.16
always	0.07	0.06
like	0.29	0.06
foreign	0.04	0.15
films	0.08	0.11

Prior Probabilities (equal):

$$P(\text{pos}) = P(\text{neg}) = 0.5$$

$$\begin{aligned} P(\text{pos} | \text{'I always like foreign films'}) = & \\ & P(\text{pos}) \times P(\text{'I' | pos}) \times P(\text{'always' | pos}) \\ & \times P(\text{'like' | pos}) \times P(\text{'foreign' | pos}) \times \\ & P(\text{'films' | pos}) \end{aligned}$$

$$\begin{aligned} \Rightarrow P(\text{pos} | \text{'I always like foreign films'}) & \\ = 0.5 \times 0.07 \times 0.29 \times 0.04 \times 0.08 & \end{aligned}$$

$$\begin{aligned} \Rightarrow P(\text{pos} | \text{'I always like foreign films'}) & \\ = 0.00003248 & \end{aligned}$$

$$P(\text{neg} | \text{'I always like foreign films'}) = 0.5 \times 0.16 \times 0.06 \times 0.06 \times 0.15 \times 0.11$$

$$\Rightarrow P(\text{neg} | \text{'I always like foreign films'}) = 0.0000297$$

$$\therefore P(\text{pos} | \text{'I always like foreign films'}) > P(\text{neg} | \text{'I always like foreign films'})$$

\therefore Naive Bayes would classify the sentence 'I always like foreign films' as positive.

Question 4.2: Solution:

Step 1: Computing Prior Probabilities:

$$P(\text{Comedy}) = \frac{2}{5} = 0.4$$

$$P(\text{action}) = \frac{3}{5} = 0.6$$

Comedy Class:

words	Count
fun	3

Couple	2
love	2
fly	1
fast	1
Total words in comedy class: 9	
Vocabulary (unique words) size:	

Action class:

words	Count
fast	2
furios	2
Shoot	4
fun	1
fly	1
love	1

Total words in action class: 11

Vocabulary: { fun, Couple, love, fly, fast, furios, Shoot }

(words in both classes / total words)

Vocabulary size: 7

Likelihoods with Add-1 Smoothing:

$$P(\text{word} | \text{Class}) = \frac{\text{Count}(\text{word in Class}) + 1}{\text{total words in Class} + \text{Vocabulary size}}$$

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Comedy Class likelihoods:

$$P(\text{fast} | \text{Comedy}) = \frac{1+1}{9+7} = \frac{2}{16} = 0.125$$

$$P(\text{Couple} | \text{Comedy}) = \frac{2+1}{9+7} = \frac{3}{16} = 0.1875$$

$$P(\text{Shoot} | \text{Comedy}) = \frac{0+1}{9+7} = \frac{1}{16} = 0.0625$$

$$P(\text{fly} | \text{Comedy}) = \frac{1+1}{9+7} = \frac{2}{16} = 0.125$$

Action Class likelihoods:

$$P(\text{fast} | \text{action}) = \frac{2+1}{11+7} = \frac{3}{18} = 0.166$$

$$P(\text{Couple} | \text{action}) = \frac{0+1}{11+7} = \frac{1}{18} = 0.055$$

$$P(\text{Shoot} | \text{action}) = \frac{4+11}{11+7} = \frac{15}{18} = 0.833$$

$$P(\text{fly} | \text{action}) = \frac{1+1}{1.1+7} = \frac{2}{18} = 0.11$$

Compute Posterior probabilities:

$$P(\text{Comedy} | D) = P(\text{Comedy}) \times P(\text{fust} | \text{Comedy}) \times P(\text{Couple} | \text{Comedy}) \times P(\text{Shoot} | \text{Comedy}) \times P(\text{fly} | \text{Comedy})$$

document

$$= 0.4 \times 0.125 \times 0.1875 \times 0.0625 \times 0.125$$

$$= \boxed{0.000073}$$

$$P(\text{action} | D) = 0.6 \times 0.166 \times 0.055 \times 0.833$$

$$= \boxed{0.00456}$$

$$\therefore P(\text{action} | D) > P(\text{Comedy} | D)$$

\therefore The most likely class for document D is action.

Question 4.3: Solution:

Given document data:

doc	'good'	'poor'	'great'	class
d_1	3	0	3	pos
d_2	0	1	2	pos
d_3	1	3	0	neg
d_4	1	5	2	neg
d_5	0	2	0	neg

Vocabulary = { good, poor, great }

Vocabulary size = 3

Prior Probabilities:

$$P(\text{pos}) = \frac{N_{\text{pos}}}{N} \begin{matrix} \text{(no. of + docs)} \\ \text{(Total docs)} \end{matrix}$$
$$= \frac{2}{5} = \boxed{0.4}$$

$$P(\text{neg}) = \frac{3}{5} = \boxed{0.6}$$

(for multinomial NB)

Likelihoods with Add-1 Smoothing:

$$P(\text{word} | \text{Class}) = \frac{\text{no. of times word} + 1}{\text{in class}}$$

$$\frac{\text{total words} + \text{Vocab}}{\text{in class} \quad \text{Size}}$$

(total words
in all classes
w/o repetition)

$$P(\text{'good'} | \text{pos}) = \frac{3+1}{9+3} = \frac{4}{12} = \boxed{0.33}$$

$$P(\text{'poor'} | \text{pos}) = \frac{1+1}{9+3} = \frac{2}{12} = \boxed{0.166}$$

$$P(\text{'great'} | \text{pos}) = \frac{5+1}{9+3} = \frac{6}{12} = \boxed{0.5}$$

$$P(\text{'good'} | \text{neg}) = \frac{2+1}{14+3} = \frac{3}{17} = \boxed{0.176}$$

$$P(\text{'poor'} | \text{neg}) = \frac{10+1}{14+3} = \frac{11}{17} = \boxed{0.647}$$

$$P(\text{'great'} | \text{neg}) = \frac{2+1}{14+3} = \frac{3}{17} = 0.176$$

For Binarized NB:

$$P(w | \text{Class}) = \frac{\text{no. of doc in class} + 1}{\text{Total no. of docs} + 2}$$

$$P(\text{'good'} | \text{pos}) = \frac{1+1}{2+2} = \frac{2}{4} = \boxed{0.5}$$

$$P(\text{'poor'} | \text{pos}) = \frac{1+1}{2+2} = \frac{2}{4} = 0.5$$

$$P(\text{'great'} | \text{pos}) = \frac{2+1}{2+2} = \frac{3}{4} = 0.75$$

$$P(\text{'good'} | \text{neg}) = \frac{2+1}{3+2} = \frac{3}{5} = \boxed{0.6}$$

$$P(\text{'poor'} | \text{neg}) = \frac{3+1}{3+2} = \frac{4}{5} = \boxed{0.8}$$

$$P(\text{great} | \text{neg}) = \frac{1+1}{3+2} = \frac{2}{5} = \boxed{0.4}$$

Classify the Sentence:

Using multinomial NB:

$$P(\text{pos} | \text{Sentence}) = P(\text{pos}) \times P('good' | \text{pos}) \times P('good' | \text{pos}) \times P('poor' | \text{pos}) \times P('great' | \text{pos})$$

drop words that are not present in either class.

$$= 0.4 \times (0.33)^2 \times 0.166 \times 0.5$$

$$= \boxed{0.00361}$$

$$P(\text{neg} | \text{Sentence}) = 0.6 \times (0.176)^2 \times 0.647 \times 0.476$$

$$= \boxed{0.00211}$$

$\therefore P(\text{neg} | \text{Sentence}) > P(\text{pos} | \text{Sentence})$
 \therefore multinomial NB would classify the sentence as Negative.

Using Binarized NB:

$$P(\text{pos} | \text{Sentence}) = P(\text{pos}) \times P('good' | \text{pos}) \times P('poor' | \text{pos}) \times P('great' | \text{pos})$$

multiple Prob for same words are ignored in binary only 1 Prob

$$= 0.4 \times 0.5 \times 0.5 \times 0.75 = \boxed{0.075}$$

$$P(\text{neg} | \text{Sentence}) = P(\text{neg}) \times P(\text{'good'} | \text{neg}) \times P(\text{'poor'} | \text{neg}) \times P(\text{'great'} | \text{neg})$$

$$= 0.6 \times 0.6 \times 0.8 \times 0.4$$

$$= \boxed{0.1152}$$

$$\therefore P(\text{neg} | \text{Sentence}) > P(\text{pos} | \text{Sentence})$$

\therefore Binary NB would also classify the sentence as Negative.

Conclusion: Both the models agree on that the given sentence is a negative sentence.