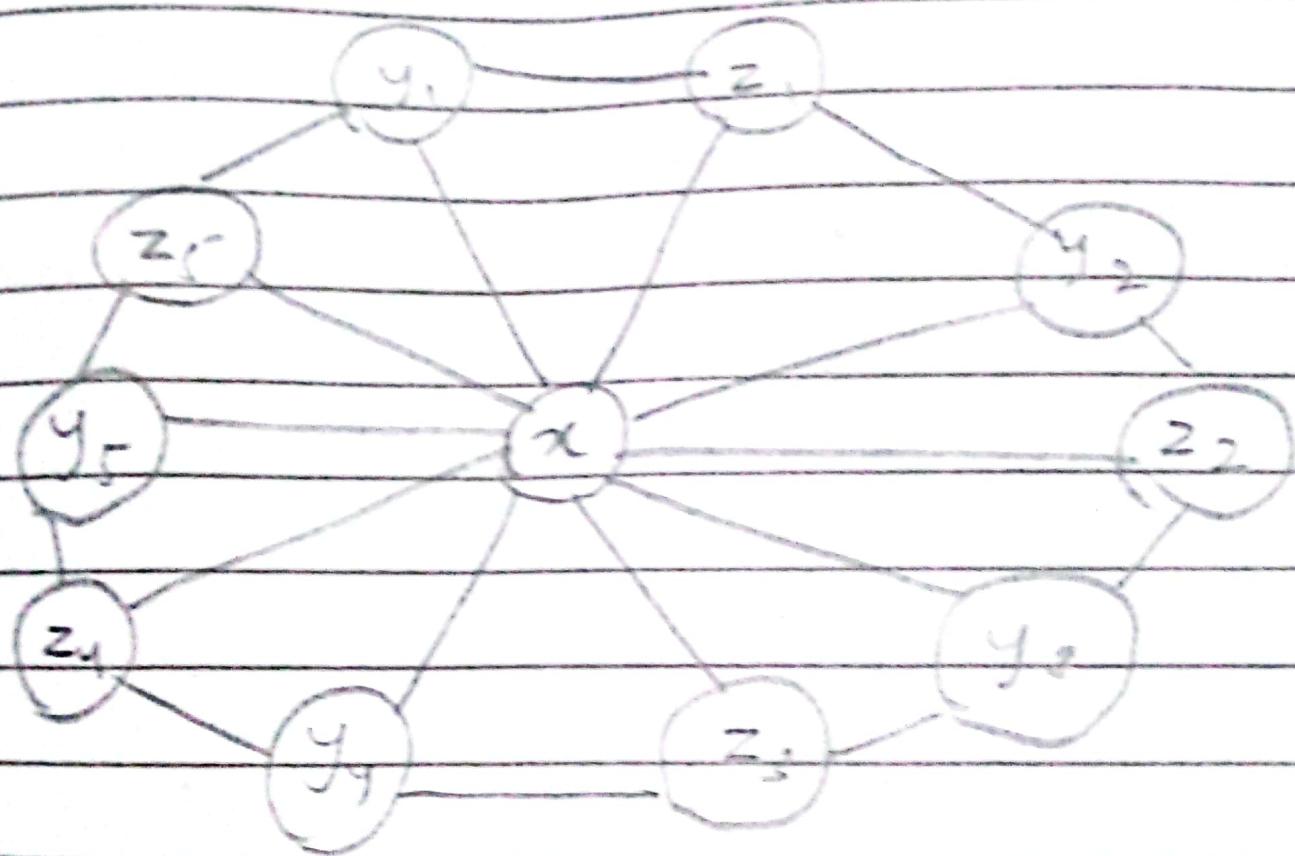


Q1 (a) F_5 $n = 5$ $2n+1 = 11$



Signature _____

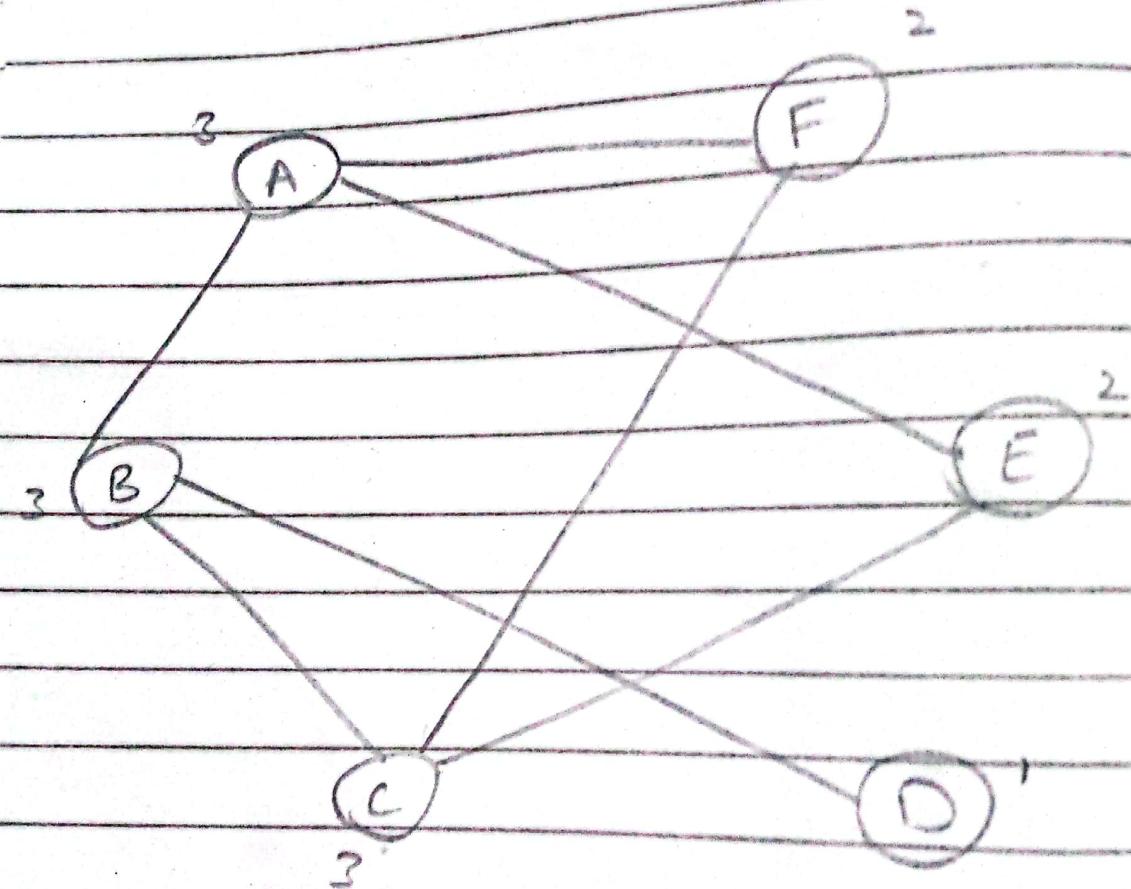
DG

No. _____

Date _____

(6)

$$n = 6$$

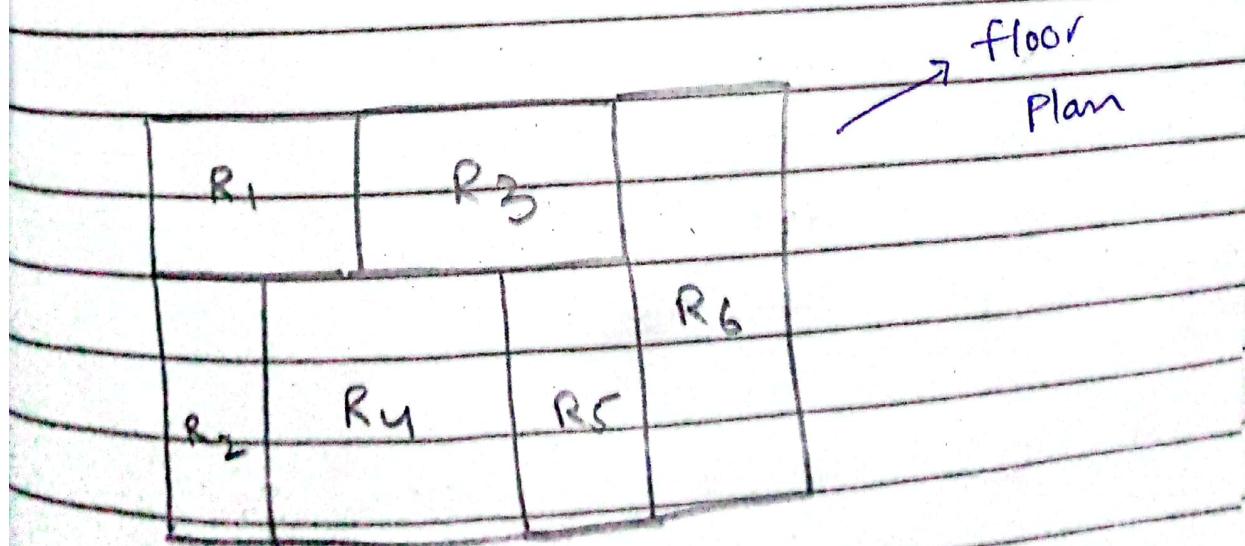


$$\text{sum}(d) = 14$$

(c) room = 6

adjacency Matrix:

| | 1 | 2 | 3 | 4 | 5 | 6 |
|---|---|---|---|---|---|---|
| 1 | 0 | 1 | 1 | 1 | 0 | 0 |
| 2 | 1 | 0 | 0 | 1 | 1 | 0 |
| 3 | 1 | 0 | 0 | 1 | 1 | 1 |
| 4 | 1 | 1 | 1 | 0 | 1 | 0 |
| 5 | 0 | 1 | 1 | 1 | 0 | 1 |
| 6 | 0 | 0 | 1 | 0 | 1 | 0 |



Date _____

(d)

$$m = 5$$

| | 1 | 2 | 3 | 4 | 5 |
|---|---|---|---|---|---|
| 1 | 0 | 1 | 1 | 1 | 1 |
| 2 | 1 | 0 | 1 | 1 | 1 |
| 3 | 1 | 1 | 0 | 1 | 1 |
| 4 | 1 | 1 | 1 | 0 | 1 |
| 5 | 1 | 1 | 1 | 1 | 0 |

Q2

(a)

- (a) Not \Rightarrow
- (b) Not
- (c) Yes
- (d) ~~Not~~ Not

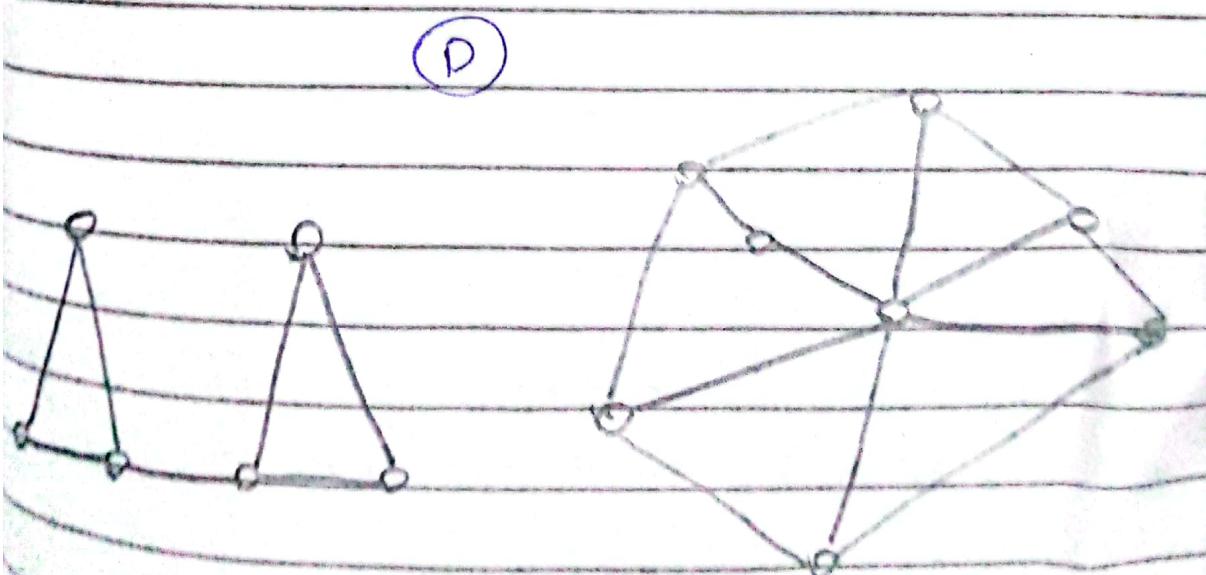
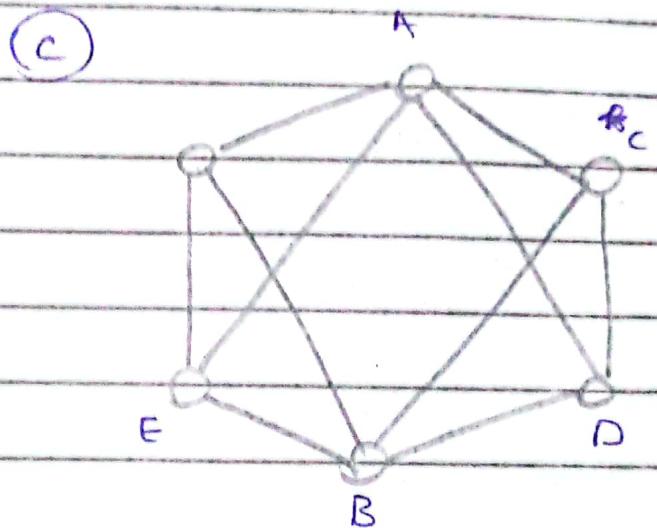
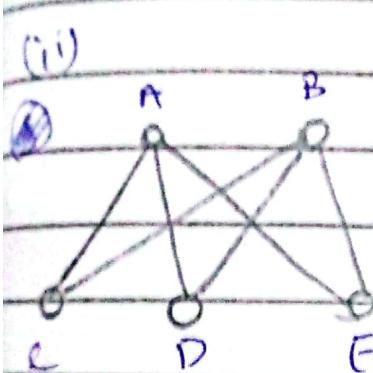
- (i) (a) Not all vertices and adjacent edge found in right side.

Signature _____



No.

Q. 3 vertices are found but the last 4-th vertex does not have the corresponding edge.



Not a
sub graph

Signature _____



No. _____

Q2

(b)

By using Handshaking lemma:

$$2 \sum \deg(v) = 2E$$

(i)

$$E = 28, v = 12 (3, 4)$$

$$\text{Min} = 12 \times 3 = 36 > \text{edges}$$

$$\text{Max} = 12 \times 4 = 48$$

where,

$$\text{org} = 2(28) = 56$$

should be

\Rightarrow Not Possible

(ii) (3 or 6)

$$\text{Min} = 12 \times 3 = 36$$

$$\text{Max} = 12 \times 6 = 72$$

$$\text{org } \sum \deg(v) = 56,$$

so, it is possible.

Signature _____



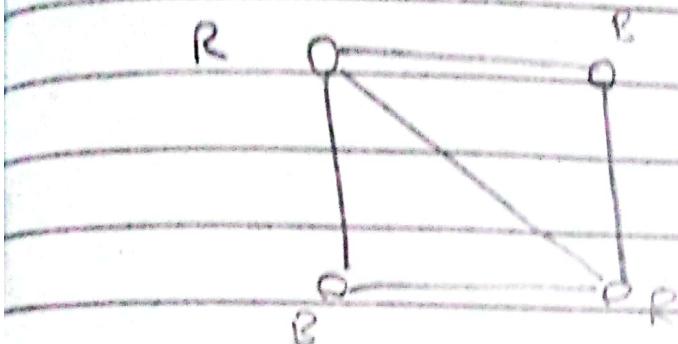
Na

Q2

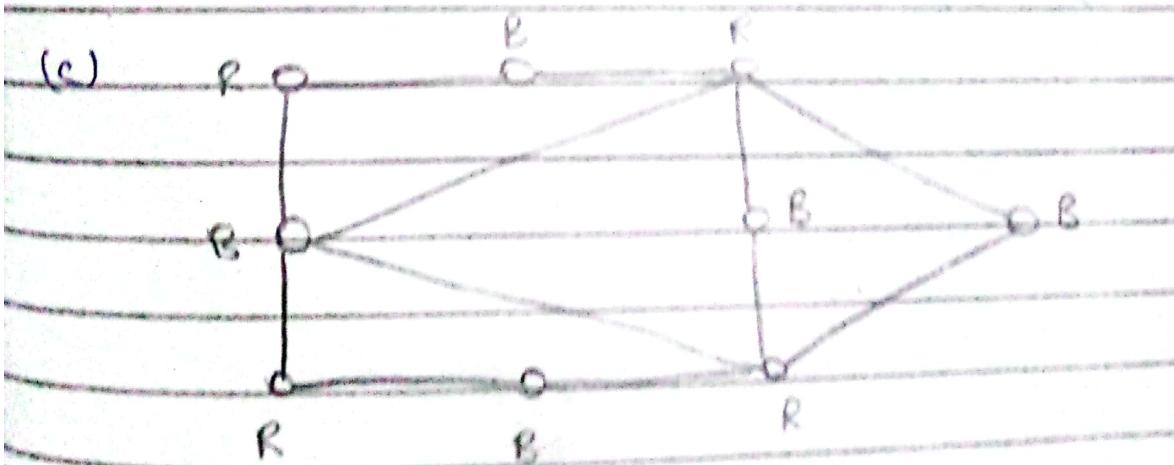
(c)

Date _____

(a) Not bipartite



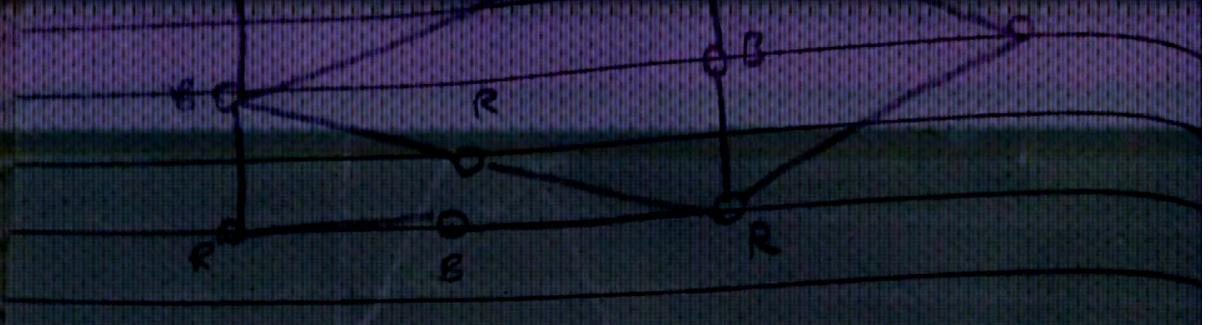
(b) Yes. bipartite.



graph is Bipartite.

Q2

No. _____



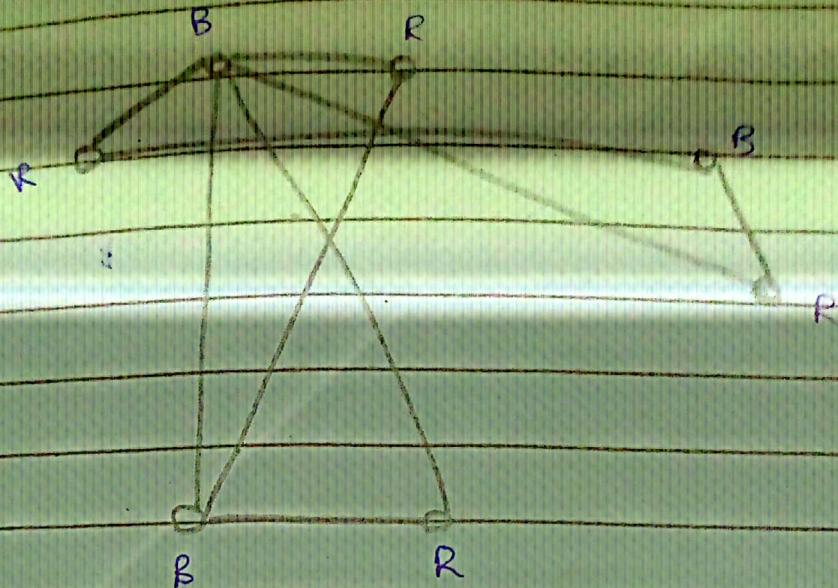
R - R Nor

B; favorite -



Graph is B-partite

(H)



B-B graph is not Bipartite.

Q3

(a) (i)

$$\textcircled{a} \quad G_1 = \begin{matrix} 2 & 3 & 3 & 2 & 2 & 1 & 1 \\ \Rightarrow & 3 & 3 & 2 & 2 & 1 & 1 \end{matrix}$$

$$G_2 = \begin{matrix} 1 & 3 & 1 & 1 & 3 & 2 & 2 \\ 3 & 3 & 2 & 2 & 1 & 1 & 1 \end{matrix}$$

$$\textcircled{b} \quad G_1 = 332211$$

$$G_2 = \begin{matrix} 2 & 3 & 1 & 1 & 3 & 2 & 2 \\ = & 3 & 3 & 2 & 2 & 1 & 1 \end{matrix}$$

Signature _____

DG

No. _____

(c) $G_1 = 131221$
 $= 322111$

$$G_2 = 123121$$
 $= 322111$

(ii)

(a) Deg sequence is not same so the graphs are not isomorphic.

(b) Graphs are isomorphic.

Vertices

$$A = P$$

$$B = T$$

$$E = Q$$

$$C = U$$

$$F = R$$

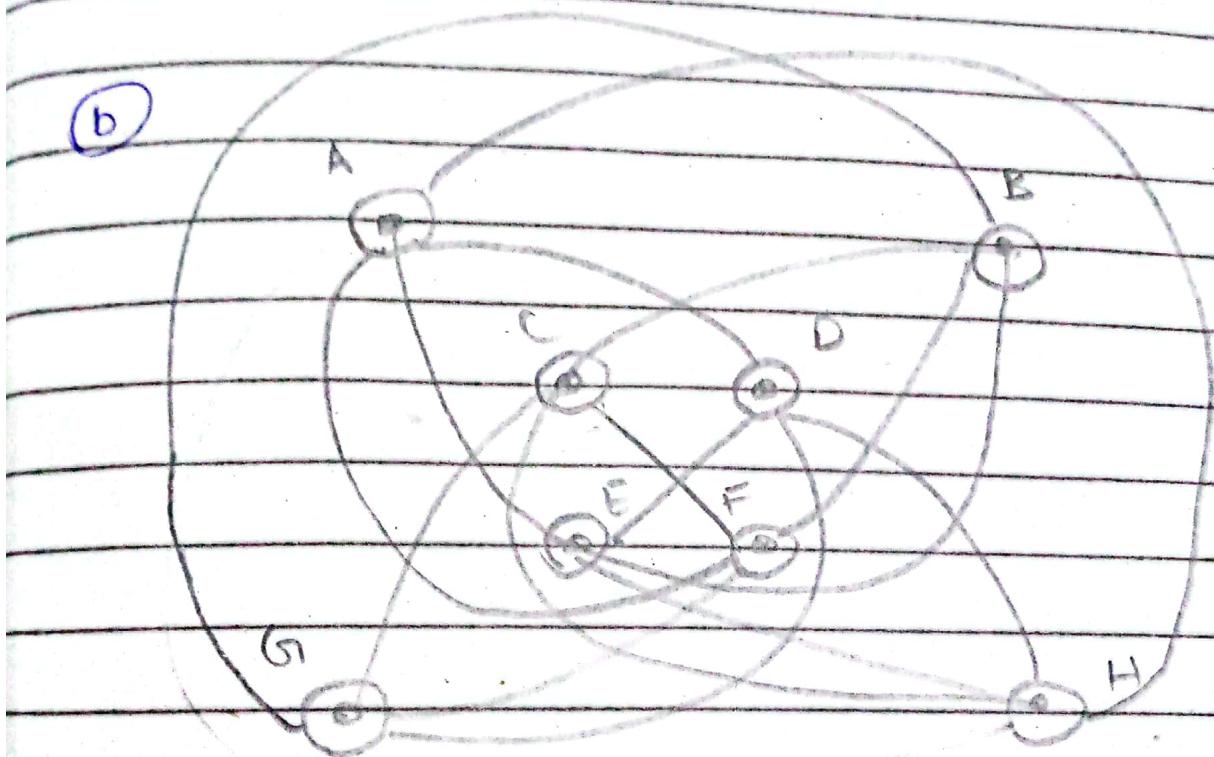
$$D = V$$

$$G = S$$

(c)

Cannot be mapped on each other even though the sequence is same.

(b)



$\text{Seq} = 4444444444$



$\text{Seq} = 4444444444$

$$A = B'$$

$$B = A'$$

$$H = G'$$

$$G = H'$$

$$C = F'$$

Signature _____

$D = E'$, No. —

Seq is same graph are
isomorphic

G₁

(iii)

$$G_1 = 44444444$$

$$G_2 = 4445344 \\ \Rightarrow 5444443$$

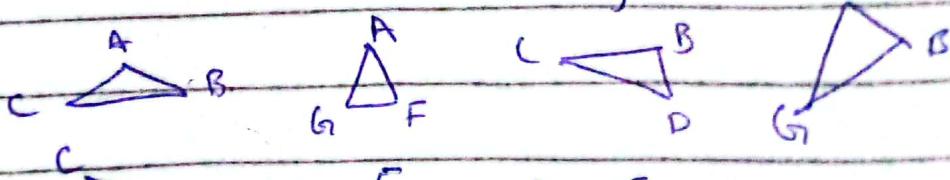
$$G_3 = 4443454 \\ = 5444443$$

(ii)

G_1 : ACB, AGF, BCD, BA, G,
CED, DFE, FEG,

GP

\Rightarrow 7 Triangle

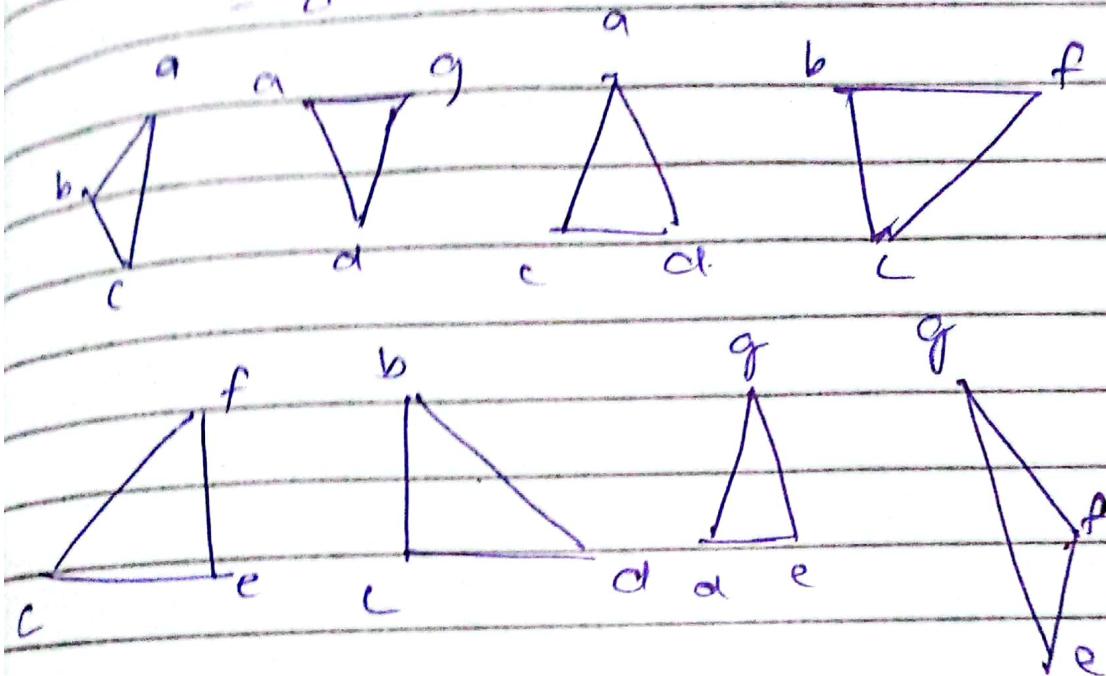


Signature _____

No. -

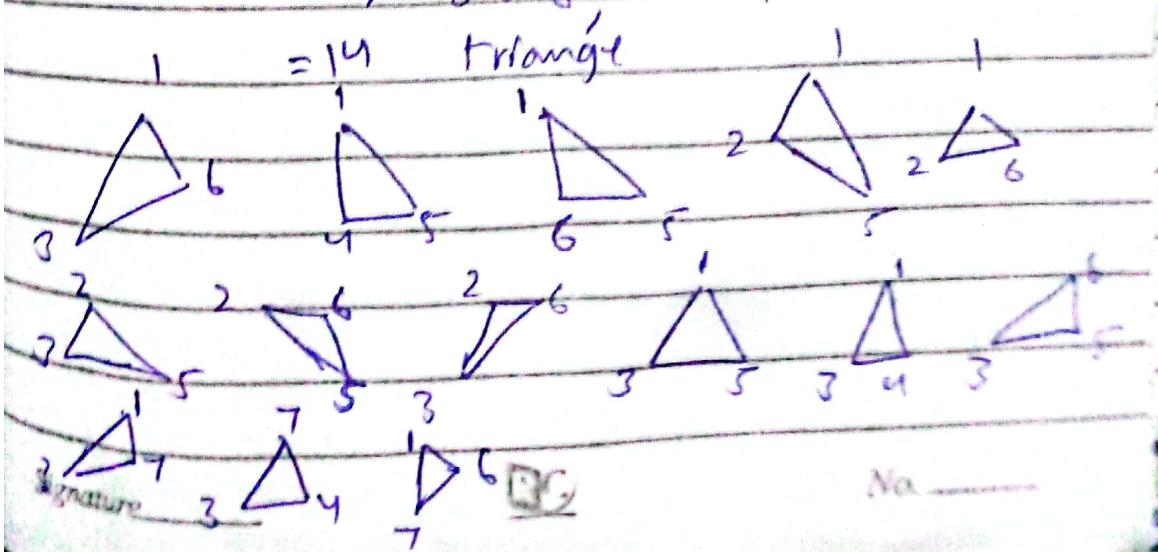
Q2: abc, adg, acd, bfc,
cfe, dbc, deg, feg

= 8



Q3: 136, 145, 156, 251, 261,
235, 256, 236, 351,
341, 356, 371, 473, 671

1 = 14 triangle



No. _____

Q4 (b)

$$\sum \deg(v) = 2E$$

$$= 2(62) = 124$$

$$v = 20, E = 62,$$

(3 or 7)

$7x$ — vertices with degree 7

$3(20-x)$ — vertices with degree 3

$$7x + 3(20-x) = 124$$

$$\Rightarrow 7x + 60 - 3x = 124$$

$$\Rightarrow 4x + 60 = 124$$

$$4x = 64$$

$$x = 16$$

\Rightarrow 16 vertices with degree 7.

Signature _____



No. _____

Date _____

Q5

$$\text{Beta} = \frac{\text{No. edges}}{\text{Ind vertices}}$$

(a)

Gr1 :

$$\text{Beta} = \frac{7}{5} = 1.4$$

Gr2

$$\text{Beta} = \frac{7}{7} = 1$$

(b) verifying by Havel-Hakemi method,

(i)

8, 5, 4, 4, 3, 2

Not graphical

(ii)

8, 6, 4, 2, 2, 2, 1

5, 3, 1, 1, 1, 0, 1

8, 3, 1, 1, 1, 1, 0

2, 0, 0, 0, 0, 0, 0

-1, -1, 0, 0, 0

Not

graphical

Signature _____

Q5

No. _____

(iii) $\textcircled{3} 3, 3, \textcircled{3} 3, 3$

$2, 2, 2, 3, 3$

$3, 3, 2, \textcircled{2}, 2$

$2, 1, 1, 2$

$2, 2, \textcircled{1}$

$1, 0, 1$

$1, 1, 0$

Graphical

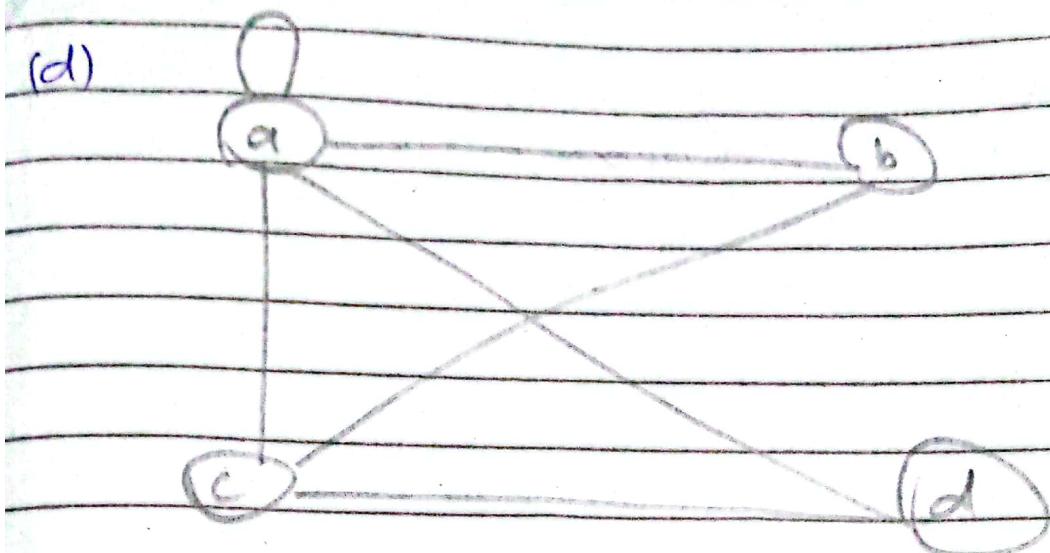


~~19~~ clique size $\Rightarrow 4$

max independent set $= 2$

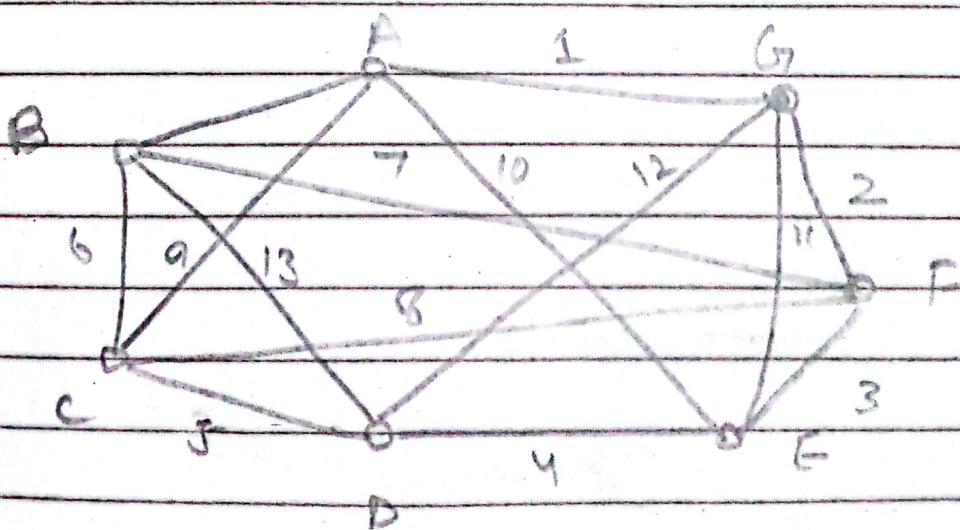
Date _____

(d)



Q# 6

(a) (a) Graph is eulerian as



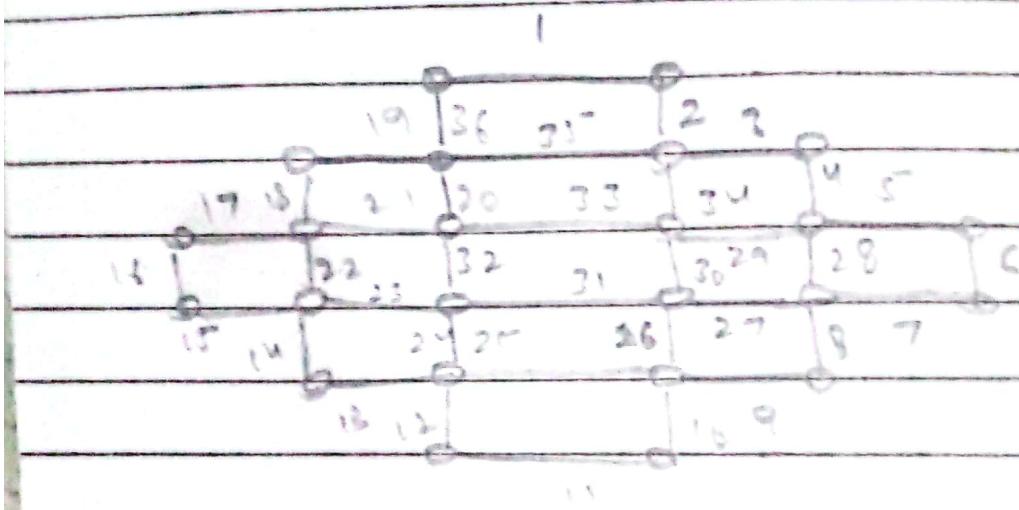
Signature _____

PG

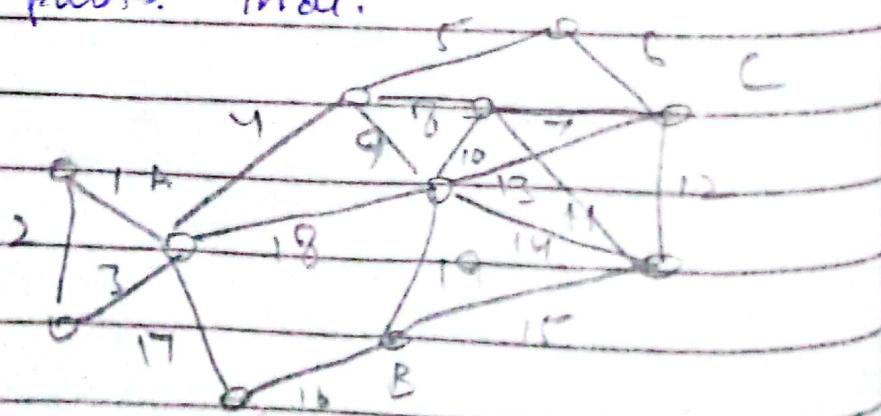
No. _____

(b)

every vertex is having even degree, the graph is eulerian.



Q6(b) Exactly 2 vertices have odd degree so there must be an eulerian path. Trial.



Signature _____

Q6

No. _____

Q7
Q7)

(i) The graph is Hamiltonian

$$A \rightarrow E \rightarrow B \rightarrow D \rightarrow C \rightarrow A$$

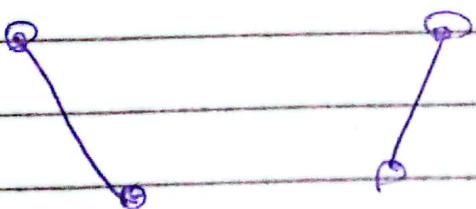
(ii) Yes there exist a Hamiltonian Path.

$$A \rightarrow E \rightarrow B \rightarrow D \rightarrow C$$

(iii) Graph is not Eulerian, it doesn't have ~~exactly~~ exactly 2 odd vertices

IV) Graph does not have a Eulerian trail.

Q8
Q8)



(ii) $|S| = 3$ $c(G-S) - 2$
clique size.

(iii) No $|S|$ is $> c(G-S)$

(iv) Graph ain't hamiltonian.

Signature _____

DG

No. _____