

TOA Assignment

Q4.

(a) $S \rightarrow abS \mid a$

strings: $a, abS, ababS,$
 $abababS, abababa$

$$L = (ab)^* a$$

(b) $S \rightarrow aSb \mid \lambda$

strings, $ab, aSb, aasbb, \dots$

$$L = a^n b^n$$

c)

$$x = 2y, \quad a^n b^y$$

string

$a a^b, a a a b b$

$a a a a a b b b$

$$S \rightarrow a a S b \mid \lambda$$

d)

$$a^x b^y a^z, \quad z = x + 2y$$

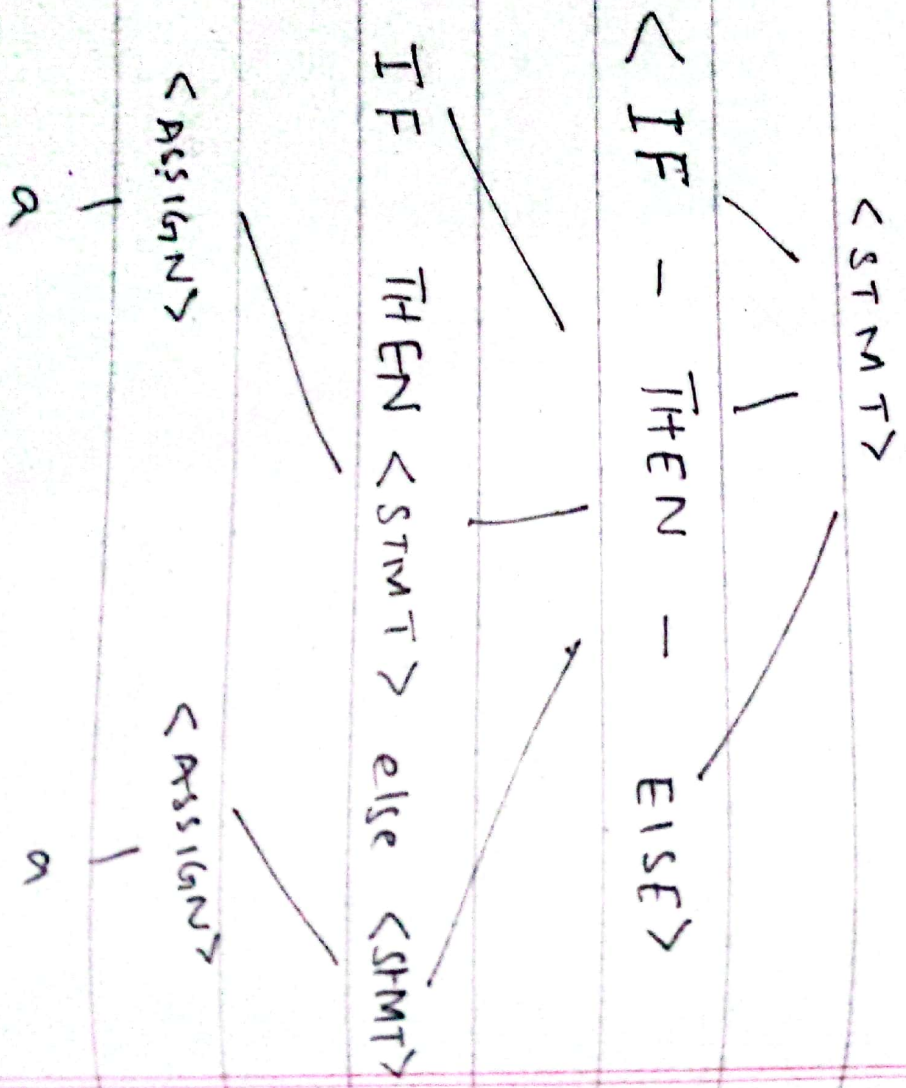
strings

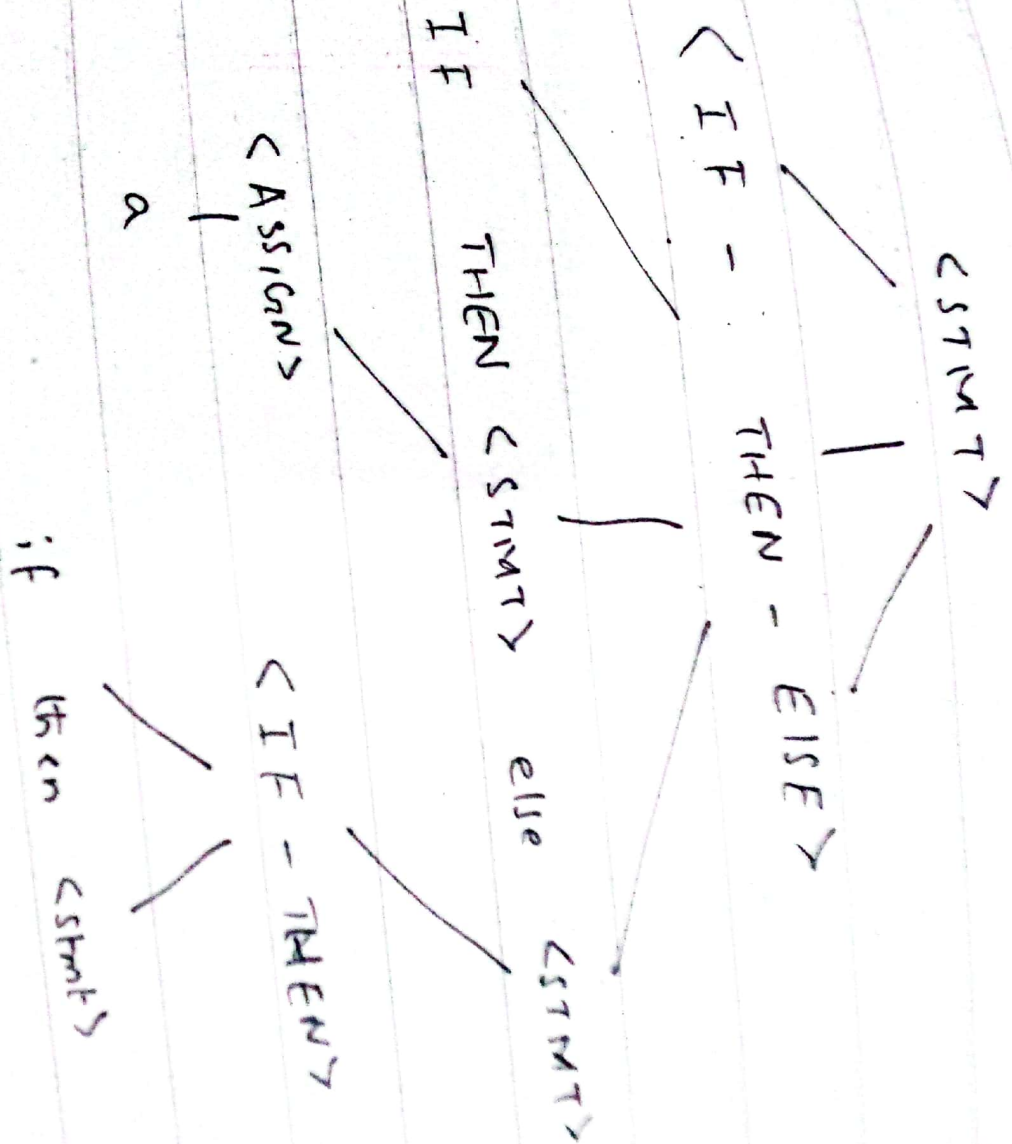
$a b a a a$

$$a b b a a a a a \quad \begin{matrix} x=1, y=2 \\ z=6 \end{matrix}$$

$$S \rightarrow a \mid b b S \mid a S b$$

Q1.





→ Two derivation of same tree
ambiguous
so, G is ambiguous.

Q2.

CFG \rightarrow CNF

(a)

$A \rightarrow BAB \mid B \mid \lambda$

$B \rightarrow 00 \mid \lambda$

Simplify

$\rightarrow A \rightarrow BAB \mid B \mid \lambda \mid A$

$B \rightarrow 00$

$\rightarrow A \rightarrow \cancel{BAB} \mid \cancel{B} \mid \lambda \mid \cancel{A} \mid 00A00 \mid 00$

$A \rightarrow 00 \mid 00A00 \mid \lambda$

$\rightarrow A \rightarrow 00A00 \mid 00 \mid 0000$

TO CNF

$$\rightarrow A \rightarrow \bar{T}_a \bar{T}_a A T_a T_a \mid T_a T_a \mid T_a T_a T_a T_a$$

$$\bar{T}_a \rightarrow 0$$

$$A \rightarrow T_a V_a \mid T_a T_a \mid T_a V_b$$

$$V_a \rightarrow T_a A T_a T_a$$

$$V_b \rightarrow T_a T_a T_a$$

$$\bar{T}_a \rightarrow 0$$

$$A \rightarrow T_a V_a \mid T_a T_a \mid T_a V_b \quad V_c \rightarrow A \quad V_d$$

$$V_a \rightarrow T_a V_c$$

$$V_d \rightarrow T_a T_a$$

$$V_b \rightarrow T_a V_d$$

$$\bar{T}_a \rightarrow 0$$

⑥

$$S \rightarrow Xa$$

$$B \rightarrow aX \mid bX \mid \lambda$$

\rightarrow B is a useless production

$$S \rightarrow Xa$$

\rightarrow X is undefined

$$S \rightarrow a$$

$$c) S \rightarrow aSa \mid bSb \mid b \mid a \mid aa \mid bb$$

$$S \rightarrow TaSTa \mid TbSTb \mid \overset{b}{\cancel{Ta}} \mid \overset{a}{\cancel{Tb}} \mid TaTa \mid TbTb$$

$$Ta \rightarrow a$$

$$Tb \rightarrow b$$

$$S \rightarrow TaVa \mid TbVb \mid b \mid a \mid TaTa \mid TbTb$$

$$Va \rightarrow STa$$

$$Vb \rightarrow STb$$

$$Ta \rightarrow a$$

$$Tb \rightarrow b$$

Q3

$\lambda, A \rightarrow BAB$

$\lambda, A \rightarrow B$

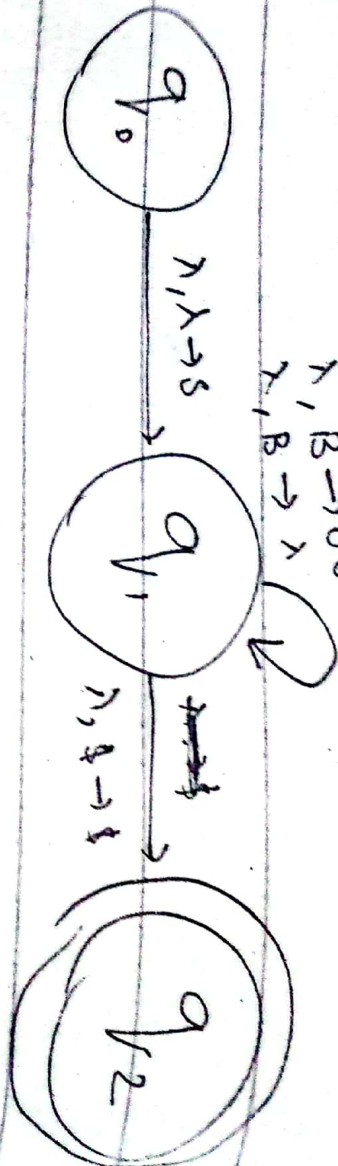
$\lambda, A \rightarrow \lambda$

$\lambda, B \rightarrow \lambda$

$\lambda, B \rightarrow \lambda$

$0, 0 \rightarrow \lambda$

(a)



(b)

$\lambda, S \rightarrow \lambda a$

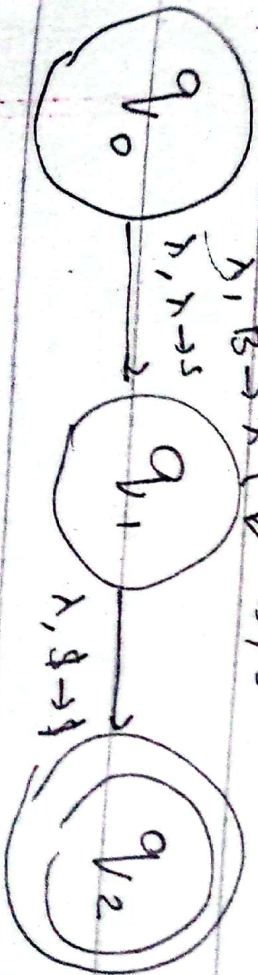
$\lambda, B \rightarrow a \lambda$

$\lambda, B \rightarrow b \lambda$

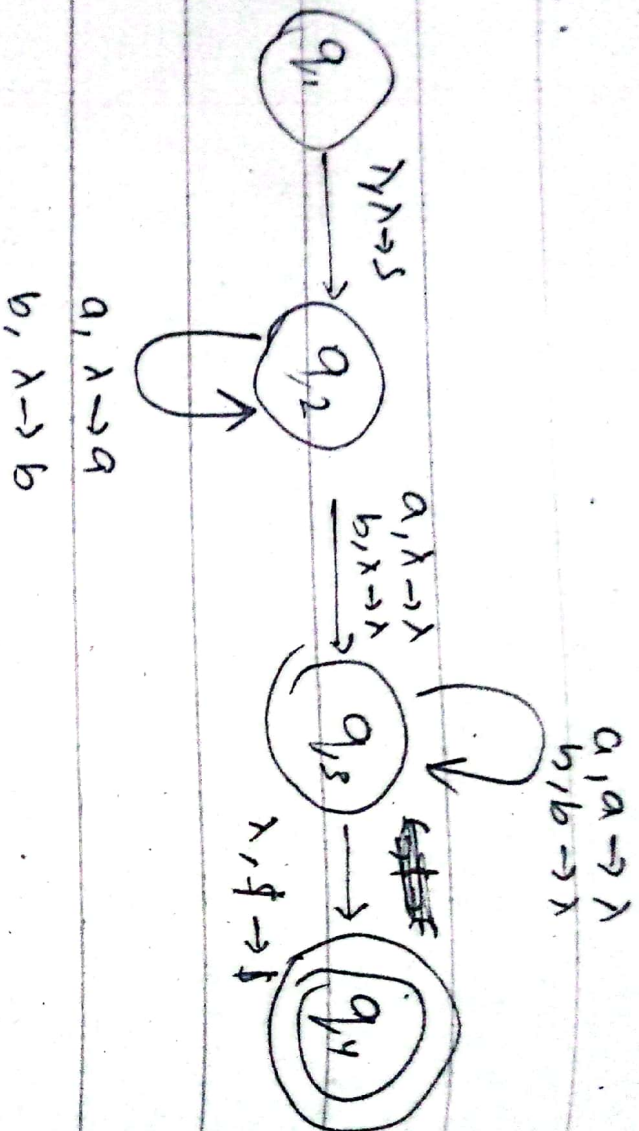
$\lambda, B \rightarrow \lambda$

$a, a \rightarrow \lambda$

$b, b \rightarrow \lambda$

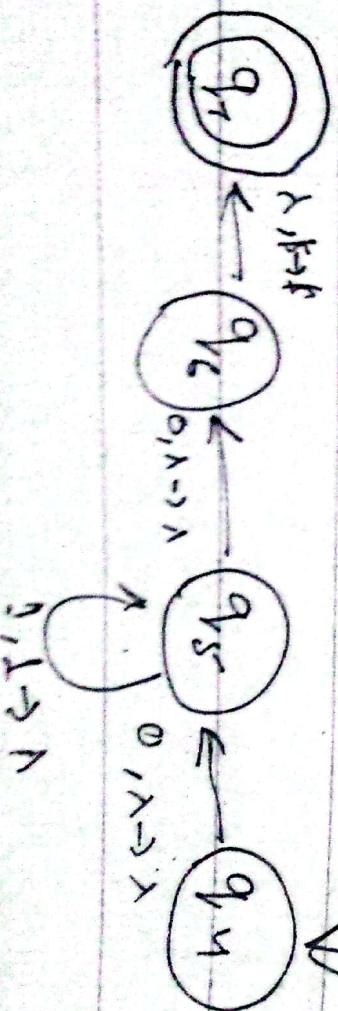
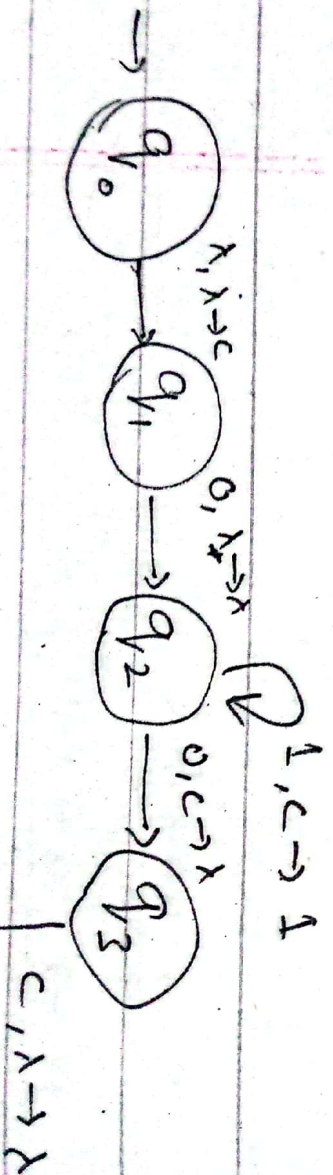


Q6.



Q7

$C = \{0^m 0^c 0^m 0^c \mid c \geq 0\}$



Q8

$S \rightarrow CABb$

$A \rightarrow BAs \mid \lambda$

$B \rightarrow 011$

$\lambda, S \rightarrow CABb$

$\lambda, A \rightarrow BAs$

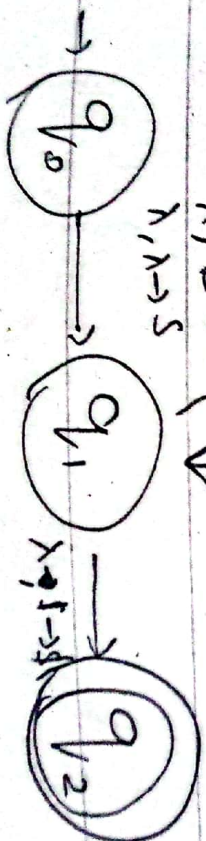
$\delta, a \rightarrow \lambda$

$\lambda, A \rightarrow \lambda$

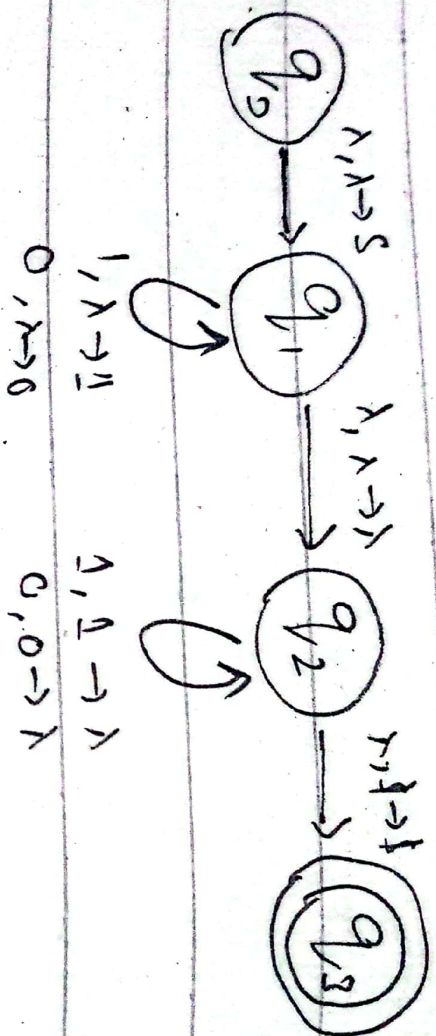
$\lambda, B \rightarrow 0$

$\lambda, B \rightarrow 1$

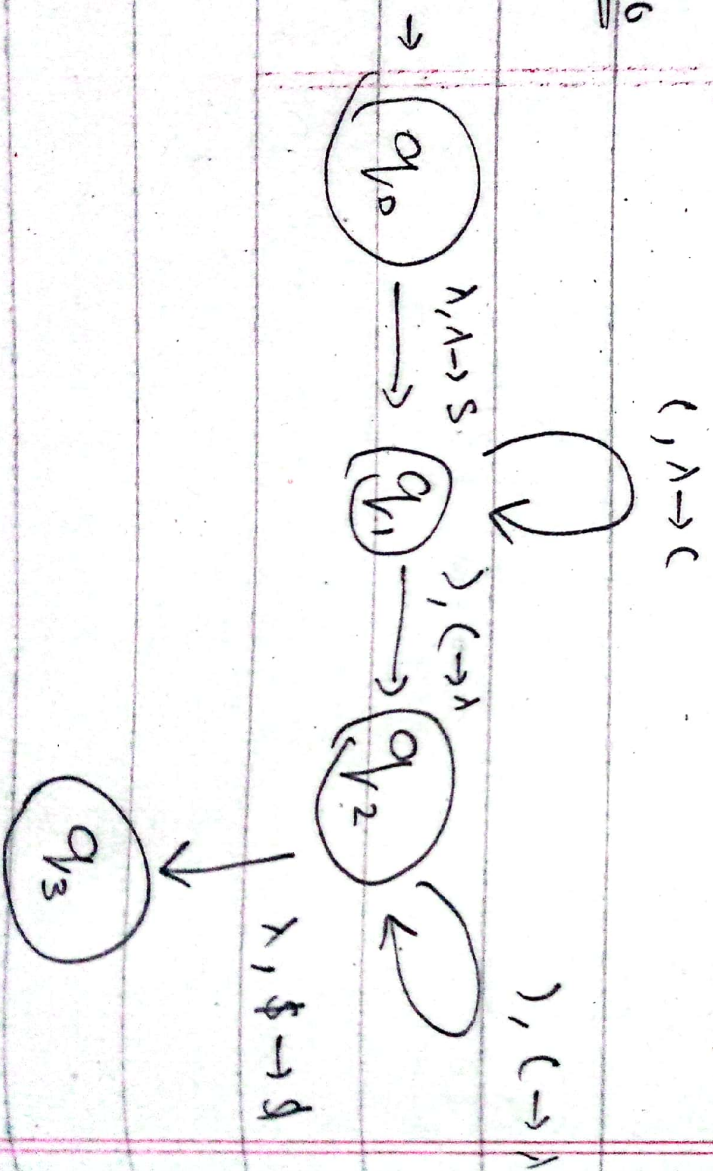
$\lambda, \lambda \rightarrow S$

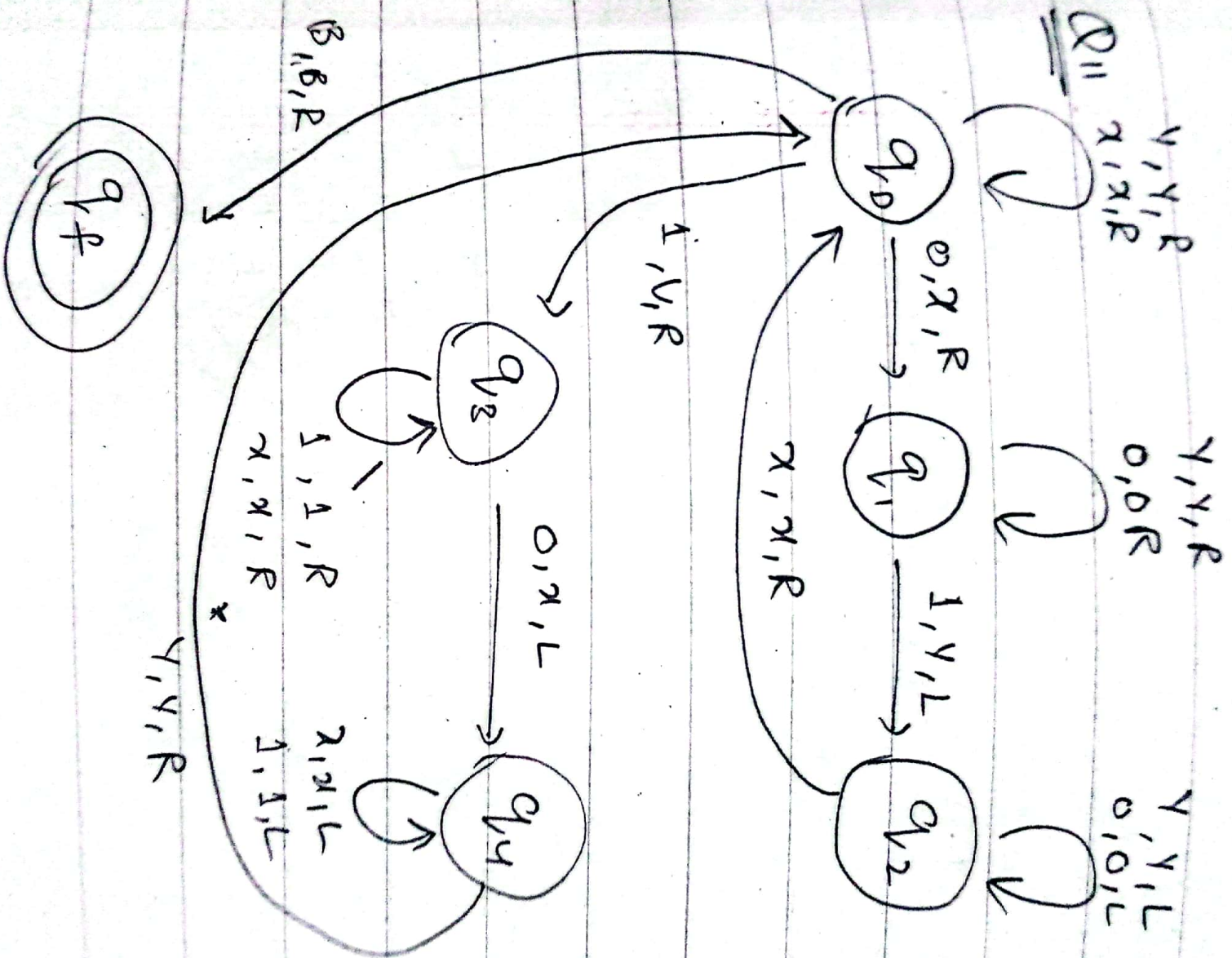


Q9



Q10





\mathcal{Q}_B

1, 1, R

(a)

