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SEMANTIC ANALYSIS

- This step of compiler takes an Abstract Syntax Tree generated by the syntax analysis phase as input.
- It performs type checking, scope resolution, and validates semantic consistency

Core Functions:

- ① Type checking
- ② Scope Resolution
- ③ Checking for correct function calls — verifying that the number and type of args passed to a function or method match its definition
- ④ Checking for declaration err
- ⑤ Handling type coercion / casting — semantic analyzer can perform implicit type conversions

Role of Symbol Table

- ↳ Heavily used during semantic analysis
- ↳ perform quick lookups to find an identifier's attr. whenever it is referenced in the code

• Syntax Directed Definition

↳ A high level, declarative specification that attaches semantic rules to the productions of a context-free grammar.

Production	Semantic Rule
$E \rightarrow E \# T$	$E\text{-val} = E\text{-val} + T\text{-val}$
$E \rightarrow T$	$E\text{-val} = T\text{-val}$
$T \rightarrow T \& F$	$T\text{-val} = T\text{-val} - F\text{-val}$
$T \rightarrow F$	$T\text{-val} = F\text{-val}$
$F \rightarrow \text{digit}$	$F\text{-val} = \text{digit-val}$

attribute

↳ production ke saath wala semantic rule attach hai

$N \rightarrow L$	$N\text{-val} = L\text{-val}$
$L \rightarrow LB$	$L\text{-val} = L\text{-val} + B\text{-val}$
$L \rightarrow B$	$L\text{-val} = B\text{-val}$
$B \rightarrow 1$	$B\text{-val} = 1$
$B \rightarrow 0$	$B\text{-val} = 0$

→ If X is a symbol & "a" is its attr then the value is denoted by $X.a$

→ In a parse tree, attr are stored in nodes, much like data fields in an object.

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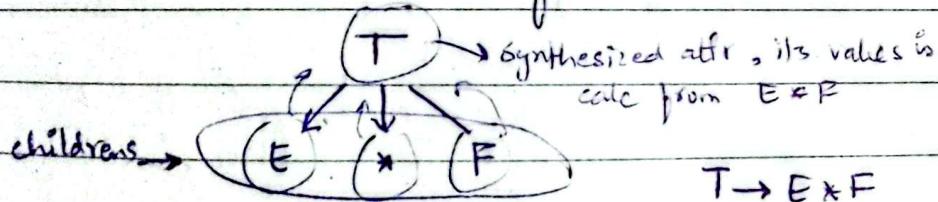
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• Attributes of SSD

- ↳ Attr hold the semantic information that we need to compute and check
- ↳ They can be of various data types
 - Numbers
 - Types (int, float...)
 - Table References
 - String (variable names) (pointer to symbol)
 - code (sequences of intermediate instr) (table entry)
- ↳ Two key types of Attr based on how their values flow through the parse tree

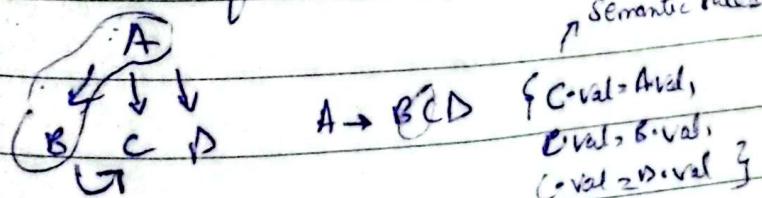
① Synthesized Attributes

- ↳ An attribute for a nonterminal A, whose value is calculated from its children



② Inherited Attributes

- ↳ An attribute for a nonterminal A, whose value is either calculated from its parent or siblings



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Semantic Rules

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$$L \rightarrow E_n \quad \text{ge dond same hi} \quad L\text{-val} = E\text{-val}$$

$$E \rightarrow (E_1 + T) \quad \begin{matrix} \text{hai} \\ \text{bs R.H.S.} \end{matrix} \quad E\text{-val} = E_1\text{-val} + T\text{-val}$$

$$E \rightarrow T \quad \begin{matrix} \text{main subscript} \\ \text{main "1" ikerwa wa} \end{matrix} \quad E\text{-val} = T\text{-val}$$

$$T \rightarrow T_1 * F \quad T\text{-val} = T_1\text{-val} * F\text{-val}$$

$$T \rightarrow F \quad T\text{-val} = F\text{-val}$$

$$F \rightarrow (E) \quad F\text{-val} = E\text{-val}$$

$$F \rightarrow \text{digit} \quad F\text{-val} = \text{digit.lexval}$$

Q: Construct $3 * 5 + 4n$, annotated parse tree

$$L\text{-val} = 19$$

$$\swarrow \quad \searrow$$

$$E\text{-val} = 19 \quad n$$

$$\swarrow \quad \downarrow \quad \searrow$$

$$E_1\text{-val} = 15 + T\text{-val} = 4$$

$$\downarrow$$

$$T\text{-val} = 15$$

$$\downarrow$$

$$F\text{-val} = 4$$

$$\downarrow$$

$$T\text{-val} = 3 \quad F\text{-val} = 5$$

$$\downarrow$$

$$F\text{-val} = 3$$

$$\text{digit.lexval} = 5$$

$$\downarrow$$

$$\text{digit.lexval} = 3$$

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$$T \rightarrow FT'$$

$$T' \rightarrow *FT_1'$$

$$T_1' \rightarrow E$$

$$F \rightarrow \text{digit}$$

$$T.\text{inh} = F.\text{val}, T.\text{val} = T'.\text{syn}$$

$$T_1'.\text{inh} = T'.\text{inh} \times F.\text{val}, T.\text{syn} = T'.\text{syn}$$

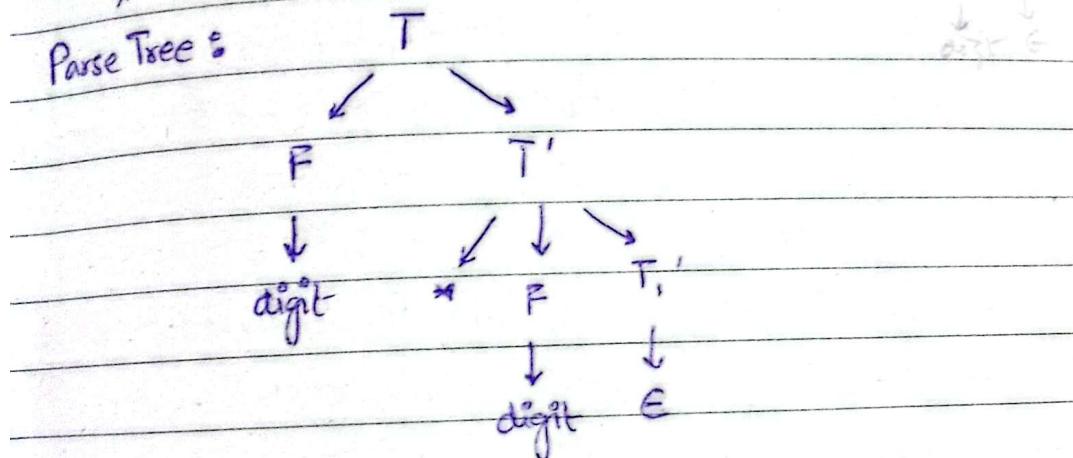
$$T'.\text{syn} = T'.\text{inh}$$

$$F.\text{val} = \text{digit}.lexval$$

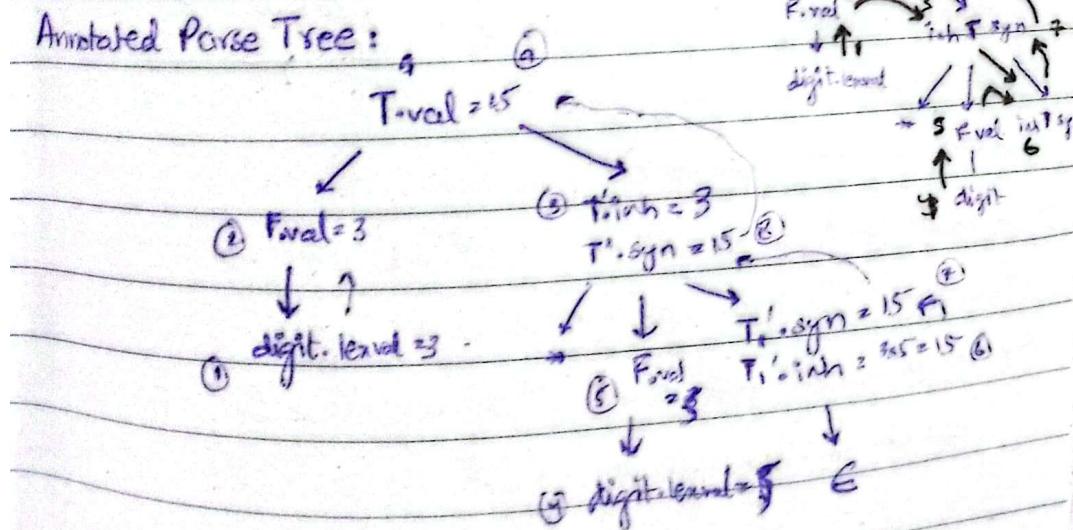
Q: Construct for $3 * 5$

a concrete Parse Tree

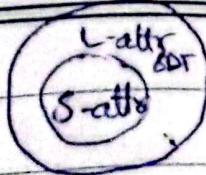
Parse Tree :



Annotated Parse Tree :



• Types of SDD

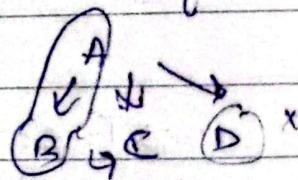


1. S-Attributed

- ↳ An SDD that uses synthesized attributes is called S-attributed SDD
- ↳ Information flows from leaves to root
- ↳ They are guaranteed to be non-cyclic
- ↳ Calculate attribute using Postorder traversal
- ↳ Fits perfectly with Bottom Up Parsing

2. L-Attributed

- ↳ Both synthesized & inherited attributes
- ↳ The value of inherited attribute can only be obtained from its parent or left siblings



- ↳ Information can flow downward or left to right
- ↳ Ideal for top down parsing
- ↳ The left to right restrictions ensure the dependency graph has no cycles
- ↳ Attributes are evaluated by traversing parse tree depth first, left to right.

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• Binary to Decimal SDD

$$S \rightarrow L$$

$$\{ S \cdot dv = L \cdot dv \}$$

$$L \rightarrow LB$$

$$\{ L \cdot dv = 2 \cdot L \cdot dv + B \cdot dv \}$$

$$L \rightarrow B$$

$$\{ L \cdot dv = B \cdot dv \}$$

$$B \rightarrow O$$

$$\{ B \cdot dv = O \}$$

$$B \rightarrow 1$$

$$\{ B \cdot dv = 1 \}$$

S

↓

String = 1010 (10)

$$S \cdot dv = 10$$

$$L \cdot S \quad B \cdot dv = 0$$

$$L \cdot dv_2 \quad B \cdot dv_1$$

$$L \cdot dv_1 \quad B \cdot dv_0$$

$$L \cdot dv_0 \quad B \cdot dv_0$$

$$B \cdot dv_1$$

$$B \cdot dv_0$$

• Evaluation Order For SDD's

↳ The evaluation order of an SDD (if it is any sequence that computes after all their dependencies have been calculated.

↳ It is obtain from a topological sort of the dependency graph

Topological sort:

- (1) calculate indegree of all nodes
- (2) Then choose the node which has $\text{in-degree} = 0$
- (3) Then delete that node from graph
- (4) Then re-calculate indegrees.
- (5) Repeat.

? If multiple nodes has with $\text{in-degree} = 0$, choose any one.

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→ Binary to Decimal with Fraction

$$S \rightarrow L_1 \cdot L_2 \quad \left\{ S \cdot dv = L_1 \cdot dv + \frac{L_2 \cdot dv}{2^{L_2 \cdot nb}} \right\}$$

$$\text{if } L \rightarrow L \cdot B \quad \left\{ \begin{array}{l} L \cdot dv = 2 \times L \cdot dv + B \cdot dv \\ L \cdot nb = L \cdot nb + B \cdot nb \end{array} \right\}$$

↳ no. of bits

$$L \rightarrow B \quad \left\{ L \cdot dv = B \cdot dv, L \cdot nb = B \cdot nb \right\}$$

$$B \rightarrow 0 \quad \left\{ B \cdot dv = 0, B \cdot nb = 1 \right\}$$

$$B \rightarrow 1 \quad \left\{ B \cdot dv = 1, B \cdot nb = 1 \right\}$$

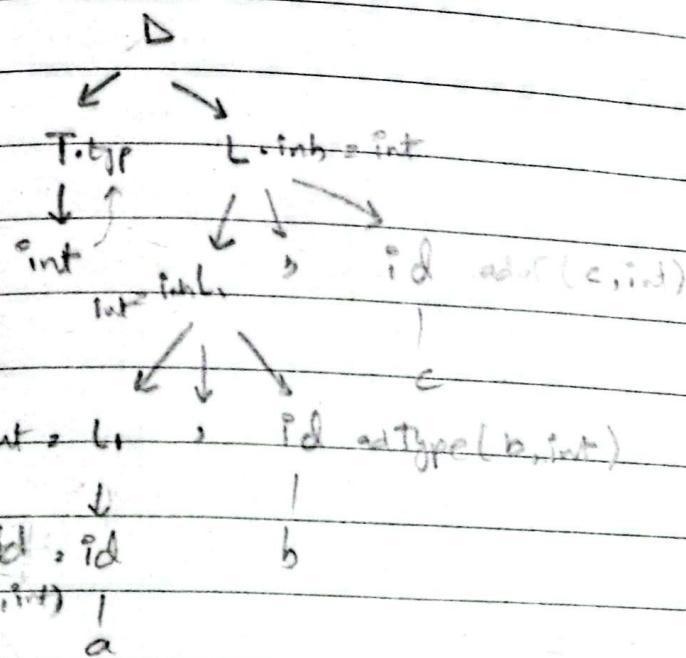
$$\begin{aligned}
 & S + \frac{5}{2^3} = 5.625 \\
 & \overbrace{01 \cdot \overbrace{101}^{nb=3}}^5 + \frac{5}{2^3} \\
 & 5 + \frac{5}{8} = 5 + 0.625 \\
 & 5.625
 \end{aligned}$$

\downarrow
 $3 = nb$
 $L_1 \cdot dv = 1$
 $S \cdot nb \cdot \frac{dv}{2} = 5$
 $2^{nb} \cdot L \cdot dv = 2 \cdot nb \cdot B \cdot dv = 1$
 $2^{nb} \cdot L \cdot dv = 1 \cdot nb \cdot B \cdot dv = 1$
 \downarrow
 (1)
 \downarrow
 $1 = nb \cdot B \cdot dv = 1$
 \downarrow
 (1)
 \downarrow
 $1 = nb \cdot B \cdot dv = 1$
 \downarrow
 (1)

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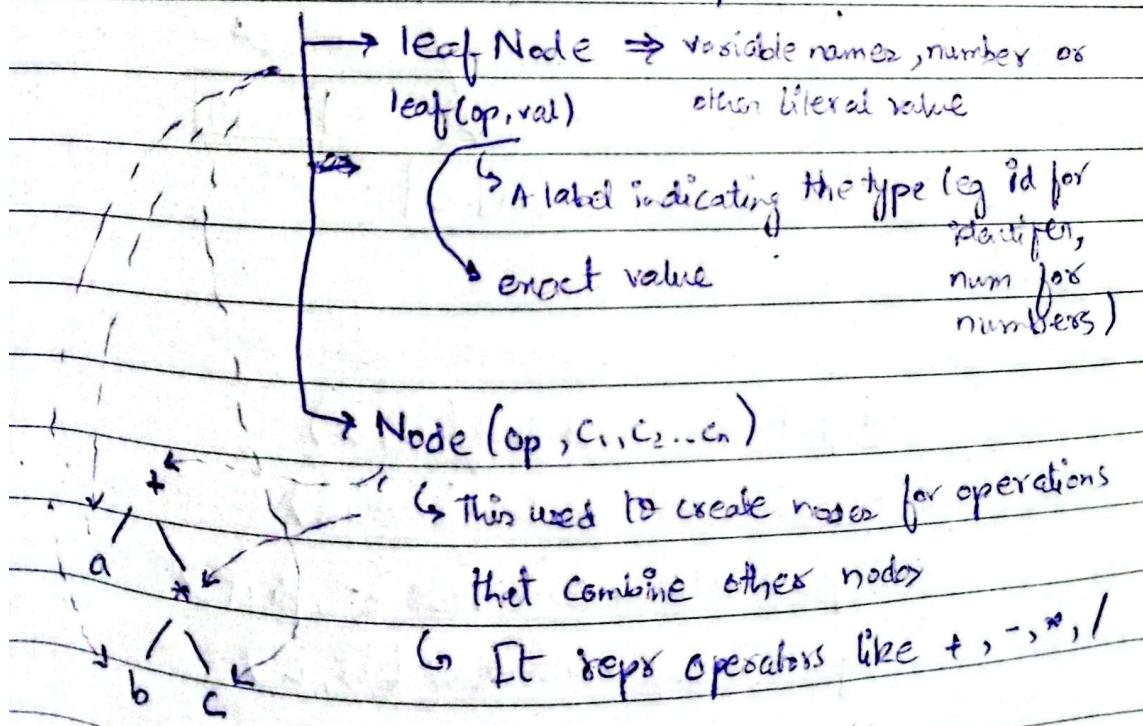
int a,b,c



• SYNTAX TREE CONSTRUCTION:

→ It is a tree representation of source code

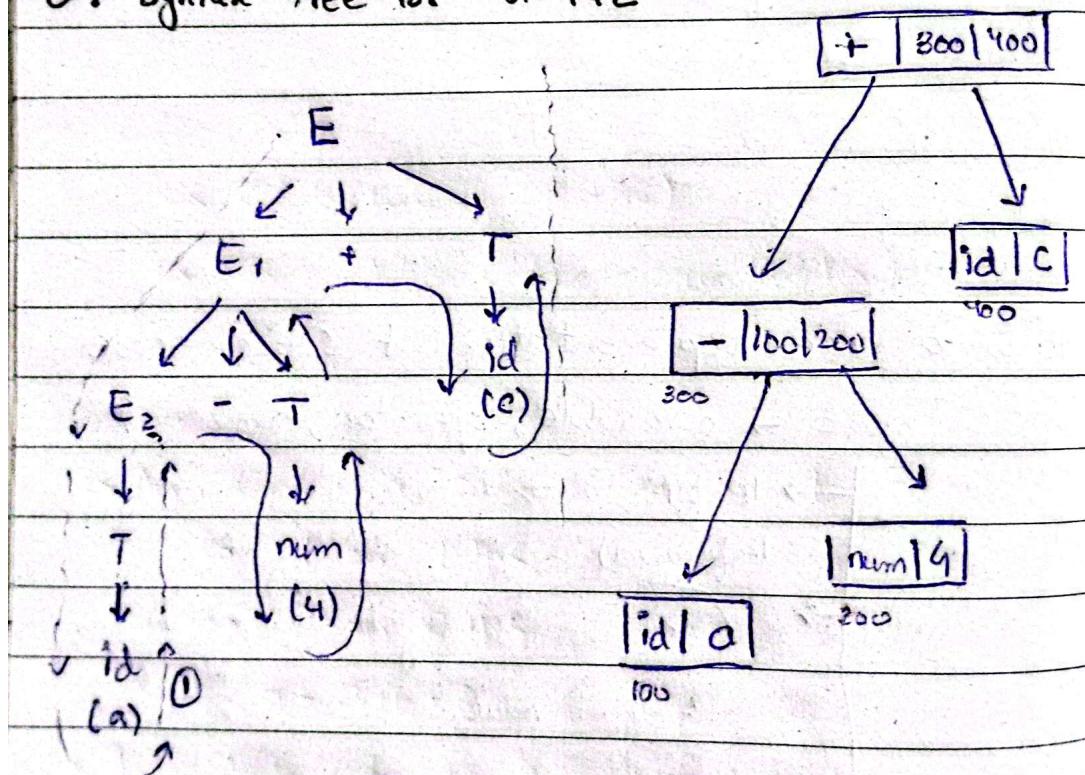
→ where node → a variable, operator, number ..)



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$E \rightarrow E_1 + T$	$E \cdot \text{node} = \text{new Node}('+' , E_1 \cdot \text{node}, T \cdot \text{node})$
$E \rightarrow E_1 - T$	$E \cdot \text{node} = \text{new Node}(' - ', E_1 \cdot \text{node}, T \cdot \text{node})$
$E \rightarrow T$	$E \cdot \text{node} = T \cdot \text{node}$
$T \rightarrow (E)$	$T \cdot \text{node} = E \cdot \text{node}$
$T \rightarrow \text{id}$	$T \cdot \text{node} = \text{new Leaf}(\text{id}, \text{id} \cdot \text{entry})$
$T \rightarrow \text{num}$	$T \cdot \text{node} = \text{new Leaf}(\text{id}, \text{id} \cdot \text{entry})$ $\text{num, num} \cdot \text{val}$

Q: Syntax tree for $a - 4 + c$ (1) $P_1 = T \cdot \text{node} = \text{new Leaf}(\text{id}, a)$ (2) $P_2 = T \cdot \text{node} = \text{new Leaf}(\text{num}, 4)$ (3) $P_3 = E \cdot \text{node} = \text{new Node}(-, P_1, P_2)$ (4) $P_4 = T \cdot \text{node} = \text{new Leaf}(\text{id}, c)$ (5) $P_5 = E \cdot \text{node} = \text{new Node}(+, P_3, P_4)$

• INTERMEDIATE CODE GENERATION

→ In the analysis-synthesis model of a compiler, the frontend of a compiler translates a source program into an independent intermediate code

→ Backend of the Compiler uses this intermediate code to generate the target code.

→ Why Inter. Code needed?

↳ If a src language is directly translated to its target machine code, then for each new machine, a full native compiler is required

↳ Inter. code eliminates this

↳ Analysis portion same for all compilers, only the second part of compiler is changed acc to target machine

→ Two types of Representation

① High Level IR

↳ Very close to the src language itself

↳ But for target machine optimization, it is less preferred

② Low Level IR

↳ Close to target machine

↳ Suitable for register & memory allocation

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→ IC can be language specific (eg: Byte Code for Java) or language independent (eg: three address code)

→ Intermediate Language Types

① Graphical IRs:

↳ Abstract Syntax Tree

↳ DAGs (Directed Acyclic Graph)

↳ Control Flow Graphs

② Linear IRs:

↳ Stack based (Postfix)

↳ Three Addr. Code (quadruples)

→ Three Address Code

↳ An expression can contain almost 3 variable

↳ 1 on LHS

↳ 2 on RHS

$x = a + b * c$

↳ Three Addr code is linearized representation of a Syntax tree or DAG

↳ Common Three Address Instructions forms

- $x = y \text{ op } z$
- $x = \text{op } y$
- $x = y$
- if ($x \text{ relop } y$) goto L1
- goto L (unconditional jump)
- param x call p return

Backpatching: It is a method used in single pass compiler generation of three-address code where the address for jump starts is temporarily left unspecified due to unknown labels; backpatching later fills those address with correct values once the target labels are specified.

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$$\bullet A[i] = x$$

$$\bullet y = A[i]$$

$$\bullet x = *p$$

$$\bullet y = \&x$$

Q: $c = 0$

$c = 0$

do

L1:

{

if ($a < b$) then

if ($a < b$) goto L2

$$T_1 = x + 1$$
$$x = T_1$$

$a++;$

goto L3

else

L2:

$x--;$

$$T_2 = x + 1$$
$$x = T_2$$

$c++$

L3:

} while ($c < 5$)

$$T_3 = c + 1$$
$$c = T_3$$

if ($c < 5$) goto L1:

Q: while ($A < C$ and $B > D$) do : if ($A < C$) goto 3

if $A = L$ then $C = C + 1$ 2 goto

else

3 if ($B > D$) goto 5

while $A <= D$

4 goto

do $A = A + B$

5 if $A == 1$ goto

6 if $A <= D$ goto 8

7 goto 10

8 $A = A + B$

9 goto 6

10

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- 1 if $A < C$ goto 3
- 2 goto 13 → loop exit
- 3 if $B > D$ goto 5
- 4 goto 13 → loop exit
- 5 if $A = 1$ goto 11 → in loop
- 6 if $A \leq D$ goto 8
- 7 goto 11 → exit loop
- 8 $A = A + B$
- 9 goto 6
- 10 $C = C + 12$ → exit else
- 11 goto 1
- 12
- 13

• Representation Types Of TAC

① Quadruple

$a = -b * c + d$

TAC:

	Op	Operand1	Operand2	Result
$t_1 = -b$	(1) \neg	b	\neg	t_1
$t_2 = t_1 * c$	(1) *	t_1	c	t_2
$t_3 = t_2 + d$	(2) +	t_2	d	t_3
$a = t_3$	(3) =	t_3	=	a

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- This representation takes more space
- Changing the order of independent instruction does not affect result

② Triple

↳ Yaha par temp variable mein store kone k

bajae direct memory reference karte hai.

↳ Space not wasted

	Op	Operands1	Operands2
0	-	b	
1	*	(0)	c
2	+	(1)	d
3	=	(2)	

of the stnts

↳ Changing the order affects the result

0 → +	(1)	d	→ changed the order,
1 → *	(0)	c	→ iske andar
2 → -	b		→ b ka answer

accha Chahiye telen
humne ordering change

krdi to ab wore andar

ghalat answer ajaayega.

③ Indirect Tuples

↳ Yaha par hum ek list of pointers store kerenge.

↳ The pointers will reference to each of the results of the stnts

↳ Here we can reorder the stnts.

↳ But it requires two memory references.

	Stnt
100	(0)
101	(1)
102	(2)
103	(3)

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Q: for (i=1 ; i<n ; i++)

$$x = a + b * c$$

condition reverse

1) $i = 1$ \nearrow break

2) if ($i > n$) goto 9

3) $t_1 = b * c$

4) $t_2 = a + t_1$

5) $x = t_2$

6) $t_3 = i + 1$

7) $i = t_3$

8) goto 2

9)

Q: switch (i)

 f case 1:

$x_1 = a_1 + b_1$, ~~t₁~~; $t_1 =$

break;

1) if ($i == 1$) goto 6

2) if ($i == 2$) goto 9

3) $t_1 = a_3 + b_3$

4) $x_3 = ct_1$

case 2:

5) goto 11

$x_2 = a_2 + b_2$, ~~t₂~~; $t_2 =$

break;

6) $t_2 = a_1 + b_1$

7) $x_1 = t_2$

default

8) goto 11

$x_3 = a_3 + b_3$; $t_3 =$

9) $t_3 = a_2 + b_2$

break;

10) $x_2 = t_2$

}

11)

$A[i] = \text{Base Address} + i \times \text{size of each element}$ $\text{Base Address: } 200$ $i: 0, 1, 2, 3, 4$ $\text{size of each element: } 2$ $\text{Address: } 200, 202, 204, 206, 208$	<p>Day</p> <ol style="list-style-type: none"> 1) $x = 0$ 2) $i = 0$ 3) $t_1 = \text{base Address A}$ 4) $t_2 = \text{base Address B}$ 5) $\text{if } (i \geq 10) \text{ goto 14}$ 6) $t_3 = i \times 2$ 7) $t_4 = t_1[t_3]$ 8) $t_5 = t_2[t_3]$ 9) $t_6 = t_4 * t_5$ 10) $t_7 = x + t_6$ 11) $x = t_7$ 12) $i = i + 1$ 13) goto 5 14) <p>$Q: x = A[i][j]$</p> <p>$t_1 = \text{Address of A}$</p> <p>$t_2 = 4 \text{ (no. of col)}$</p> <p>$t_3 = i * t_2$</p> <p>$t_4 = t_3 + j$ → size of an element</p> <p>$t_5 = t_4 * 2$</p> <p>$x = t_1[t_5]$</p> <p>$A[i][j] = \text{Base} + (i \times \text{len} + j) \times 2$</p> <p>$\text{Base} = \text{Base} + i \times 2 \times \text{len} + j \times 2$</p> <p>$\text{len} = 16 + 6$</p> <p>$\text{Address: } 200, 202, 204, 206, 208$</p>
<p>$Q: x = A[32][32][8]$</p> <p>$i = A[i][j][k]$</p> <p>$x = A[(i \times 32 \times 8 + j \times 8 + k)] \times 2$</p>	<p>$A[i][j] = \text{Base} + (i \times \text{len} + j) \times 2$</p> <p>$\text{len} = 16 + 6$</p> <p>$\text{Base} = \text{Base} + i \times 2 \times \text{len} + j \times 2$</p> <p>$\text{len} = 16 + 6$</p>

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→ Directed Acyclic Graphs

↳ Similar to syntax tree but with shared common subexpressions

↳ Key Diff: Nodes can have multiple parents

DAG

Syntax Tree

→ Replicates common subexpression → Replicates common subexpression

→ Single node represents multiple occurrence → Each occurrence gets its own subtree

→ Compact Representation → Inefficient Representation

$$x = ((\underline{a+a}) + \underline{a+a}) + ((a+a) + (\underline{a+a}))$$

$$t_1 = a+a$$

$$t_7$$

$$t_2 = a+a$$

$$t_3 = t_1 + t_2 \quad \text{Syntax Tree:}$$

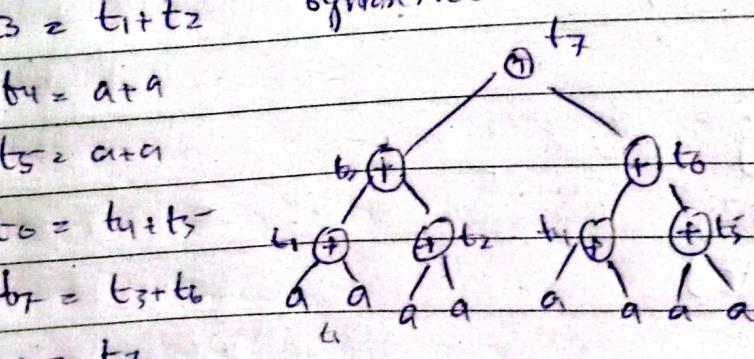
$$t_4 = a+a$$

$$t_5 = a+a$$

$$t_6 = t_4 + t_5$$

$$t_7 = t_3 + t_6$$

$$n = t_7$$



Gab yaha 'a' eighth times repeat ho raha

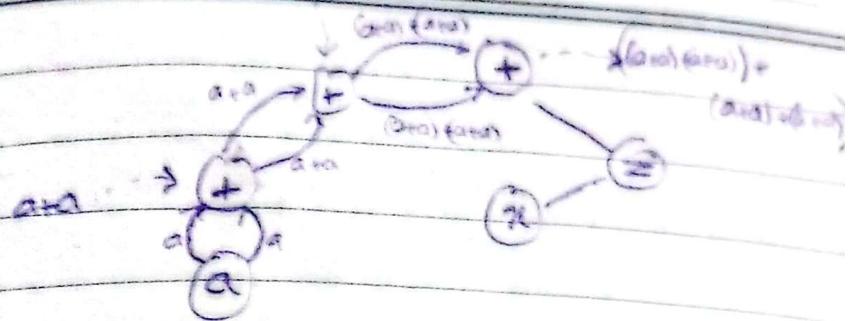
G DAG mein sirf ek data ayege

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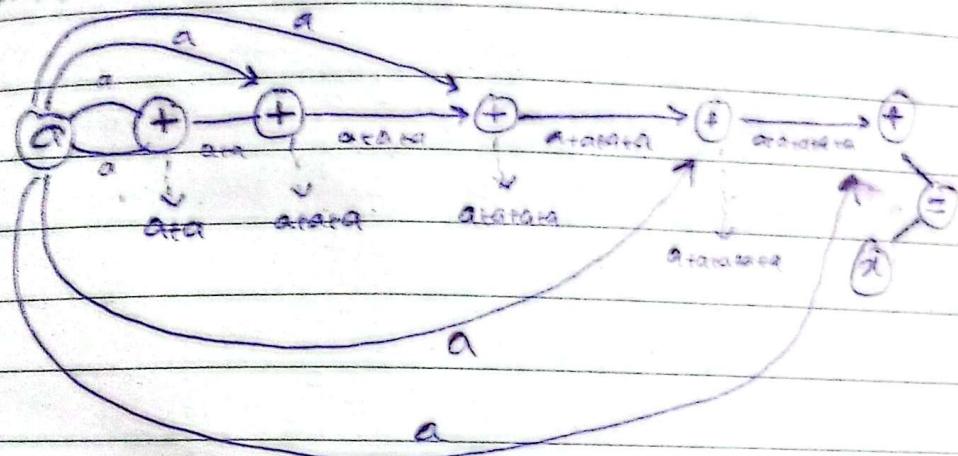
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• DATA :

$$(a+a) + (a+a)$$



$$x = a + a + a + a + a + a$$



$$x = a + a * (b - c) + (b - c) * d$$

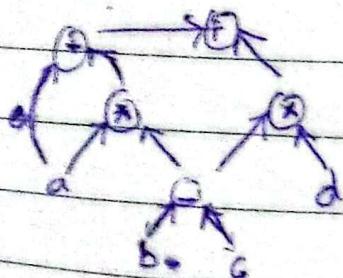
$$t_1 = b - c$$

$$t_2 = a * t_1$$

$$t_3 = d * t_2$$

$$t_4 = t_2 + t_3$$

$$t_5 = t_4 + t_3$$



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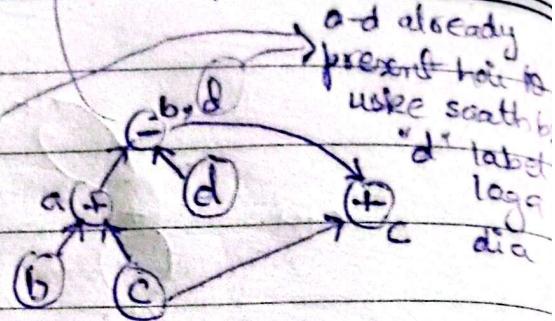
ye wala "b" ab ha
saga use hoga instead of
the leafnode "b".
because upar
wala updated hai Day

$$a = b + c$$

$$b = a - d$$

$$c = b + c$$

$$d = a - d$$



$$d = b * c$$

$$e = a + b$$

$$b = b * c$$

$$a = e - d$$

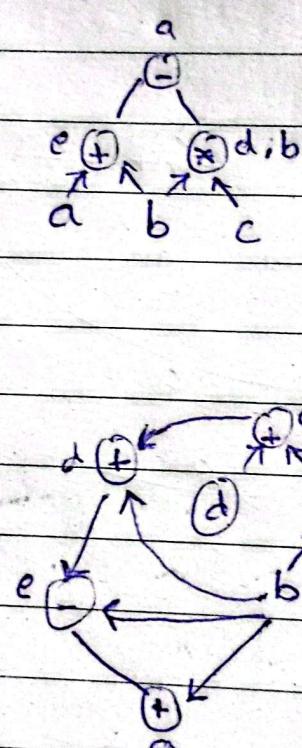
$$a = b + c$$

$$c = a + d$$

$$d = b + c$$

$$e = d - b$$

$$a = e + b$$



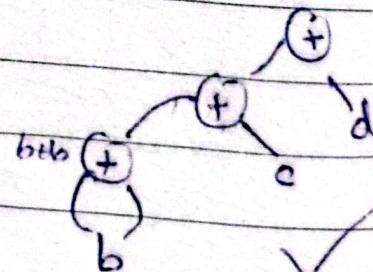
For minimum no. of nodes & edges we 1st simplify
the equation by substituting values.

$$\Rightarrow a = (d - b) + b$$

$$a = b + c$$

$$a = b + \cancel{a} + d$$

$$a = b + \cancel{b + c} + d$$



$$a = b \times c$$

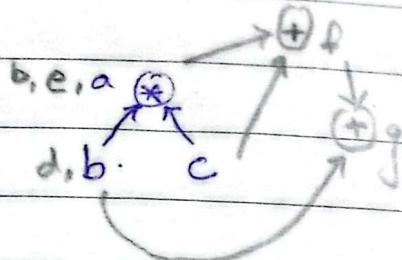
$$d = b$$

$$e = d \times c$$

$$b = e$$

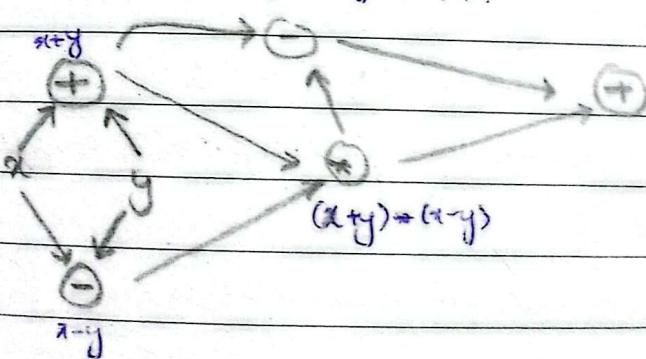
$$f = b + c$$

$$g = f + d$$



$$((x+y) - ((x+y)*(x-y))) + ((x+y)*(x-y))$$

$$(x+y) - ((x+y)*(x-y))$$



→ Application Of DAG in Compiler

- ① Code Optimization — DAGs identify & eliminate redundant computations, also known as common subexpression, to make code more efficient
- ② Code generation — They assist in generating efficient machine code by representing intermediate code & helping with tasks like register allocation

• INTERMEDIATE CODE OPTIMIZATION

- The phase of compiler tends to improve the code by making it consume fewer resources so that faster-running machine code will result.
- The optimized code should always give same o/p on same i/p as before.
- Compilation time must be kept reasonable
- Should increase the speed & performance

→ Types of Code Optimization

① Machine Independent

- ↳ Performed on intermediate code before target code generation
- ↳ It improves program efficiency without considering the target machine architecture
- ↳ It does not involve CPU registers or absolute memory addresses
- ↳ Examples:
 - Constant Folding
 - common subexpression elimination
 - dead code elimination
 - loop optimization

② Machine-Dependent

- ↳ This optimization is applied after target code generation
- ↳ It is specific to the target machine architecture and uses CPU registers & memory hierarchy
- ↳ It focuses on
 - ↳ register allocation
 - ↳ instruction selection
 - ↳ instruction scheduling
 - ↳ addressing modes
 - ↳ Peephole optimization
- ↳ Redundant LOAD/STORE
- ↳ Flow of Control Optimization

• Loop Optimization

① First detect loop

② Loop detect kaise k liye we do Control Flow

Analysis on Control Program Flow Graph

③ CFG k liye we need to find Basic Blocks

④ A basic block is a sequence of 3-Address Code
stmts where control enters at the beginning &
leaves only at the end without any jump stmts

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* Agar normally loop identify ho sakte hai then
ye sab lambi kare ki need nahi

→ Finding Basic Blocks

- i - In order to find basic block we need to find "leaders" in TAC
- ii - A basic block will start from one leader to the next leader, but the next wala includ kri hoga.

iii - Finding leaders

- a) The 1st line of TAC is a leader
- b) Any instruction that is the target of a conditional or unconditional jump is a leader like " if ($i > 10$) goto 3" → the 3rd line will be leader
- c) Any instruction that immediately follows the conditional or unconditional jump is a leader.

2 if ($i > 10$) goto 34

$C = C + 2$ → leader

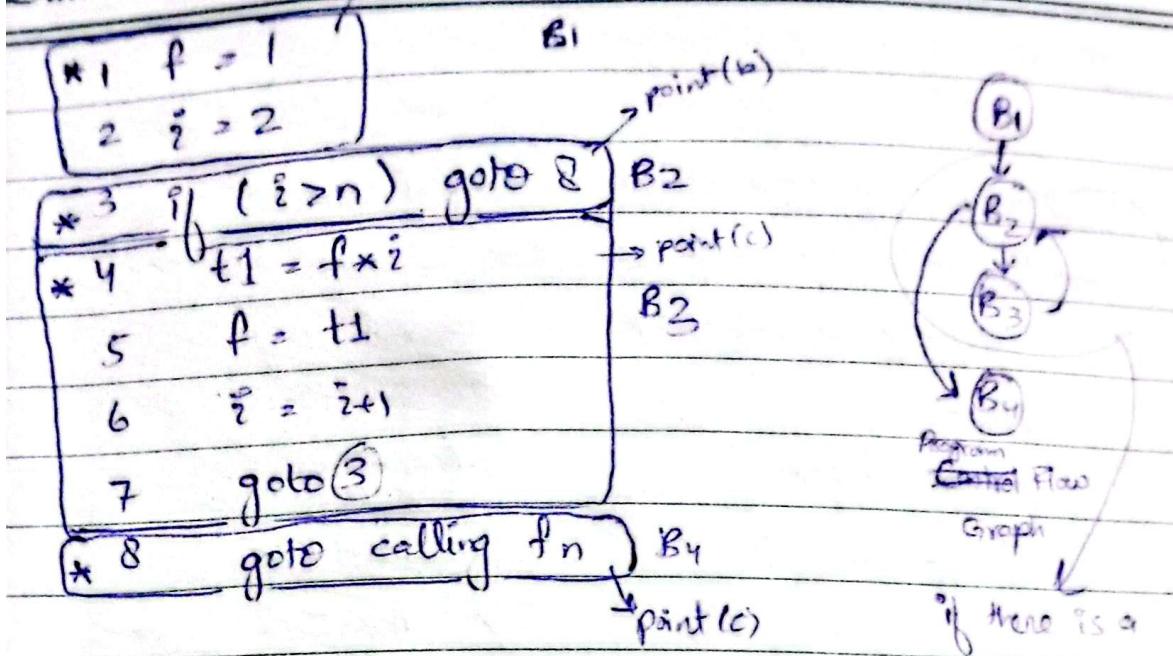
=

34 a = b + d → leader

Date

point (a)

Day



Q: * 1. $i = 11$ B₁

* 2. $j = 1$ B₂

* 3. $t_1 = 5 * i$

4. $t_2 = t_1 + j$

5. $t_3 = 4 * t_2$

6. $t_4 = t_3$

7. $a[t_4] = -1$

8. $j = j + 1$

9. $\text{if } (j \leq 5) \text{ goto } 3$

* 10. $i = i + 1$

11. $\text{if } (i \leq 5) \text{ goto } 2$

Date

→ Techniques of Loop Optimization

① Frequency Reduction (Code Motion)

Frequency Reduction
↳ If after Agr. loop mein ROI esist nit ho jiske
Agr. loop se baki kidein to ROI farq na
pare

eg: $i = 0$ $t = a/b$
while ($i < 100$) { while ($i < 100$) {

$$A = \frac{a}{b} + i \Rightarrow A = t + i$$

\downarrow

96. 100 baar evaluate hogé

to isko ele baas evaluate koke value
nde kelenge

→ getting the same output with less no. of iteration

(2) Loop Unrolling

↳ Reducing the no. of times comparison are made in a loop

↳ eg: 10 corporations ↑

```
for (i=0; i<10; i++)
```

$\text{printf} (^4\text{He}^4); \Rightarrow$

for (i=0; i<5; i++)

$$PF(\mathbb{H}^{u_1}) ;$$

ya 5 point
likhdein
& i>i+5

Kodlein

$\text{f}_{02} \quad (i=0; i<10; i+=2)$

5 Comparisons

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② Loop Jamming

↳ Combining the bodies of two loops.

For ($i=0; i<5; i++$)

$a = i+5$

For ($i=0; i<5; i++$)

$b = i+5$

For ($i=0; i<5; i++$)

$a = i+5$

$b = i+5$

→ both loop runs 5, 5 times \Rightarrow Reduce that total 10 times to only 5

→ Optimization of Basic Blocks

① Constant Folding

↳ Replacing the value of expression before compilation is called as constant folding.

$x = a+b + 2*3+4$ → this will be computed

$x = a+b+10$ at compile time

② Constant Propagation

↳ Replacing the value of constant before compile time

$x = 8 \Rightarrow x = 8$

$y = x/4 \Rightarrow y = 2$

int k=2

if (k) goto L3 \Rightarrow goto L3

condition will always be true

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③ Copy Propagation

↳ if a variable is assigned the value of another variable, all subsequent uses of the copied variable are replaced with original variable as long as the original value doesn't change

e.g.

$$\begin{array}{l} x = y \\ z = x + 1 \end{array} \Rightarrow \begin{array}{l} x = y \\ z = y + 1 \end{array}$$

④ Common Subexpression Elimination

$$\begin{array}{ll} t_1 = a + b & t_1 = a + b \\ t_2 = a + b & \Rightarrow t_2 = t_1 * d; \\ t_2 = t_2 * d; & \end{array}$$

⑤ Dead Code Elimination

↳ Remove stmts which never executes or they are unreachable

$$\begin{array}{ll} i = 0; & i = 0 \\ \text{will never get executed} & \end{array} \quad \left[\begin{array}{l} \text{if } (i == 1); \\ a = a + 5; \end{array} \right] \Rightarrow$$

⑥ Strength Deduction

↳ Replacing the costly operator by cheaper operators

$$\text{e.g. } y = 2 * x \Rightarrow y = x + x \hookrightarrow A \ll 1$$

$$y = x^2 = x * x, \sqrt{x} \Rightarrow x * 0.5$$

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⑦ Algebraic Simplification

$$\text{eg: } \begin{array}{l} a = b + 1 \\ c = d + 0 \end{array} \Rightarrow \begin{array}{l} a = b \\ c = d \end{array}$$

⑧ Function Inlining

↳ Function call replaced by the body, so it saves a lot of time in copying all the params, storing the return addrs etc.

```
int multiply(int a, int b) {
```

```
    return a * b;
```

```
}
```

 \Rightarrow

```
int main() {
```

```
    x = multiply(3, 4);
```

 $x = 3 * 4$

→ Peephole Optimization → Machine Dependent

↳ Machine dependent optimization technique that examines a small window ("peephole") of consecutive target instructions & replaces inefficient with more efficient ones.

a) Redundant LOAD / STORE Elimination

$$a = b + c$$

$$d = a + e$$

 \rightarrow

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LOAD R₀, b R₀ = b
 ADD R₀, c R₀ = b + c
 STORE a, R₀ } x redundant a = R₀
 LOAD R₀, a R₀ = a
 ADD R₀, e R₀ = R₀ + e
 STORE d, R₀ d = R₀

b) Flow Of Control Optimization

6

1) Avoid jumps on jumps

L1: jump L2 L1 & jump L3

= \Rightarrow =

L2: jump L3 x extra jump

= L3: =

L3: =

2) Eliminate Dead Code

Constant Propagation

Ex:

$$\begin{aligned} b &= 5 \\ c &= 4 * b \\ c &> b \end{aligned}$$

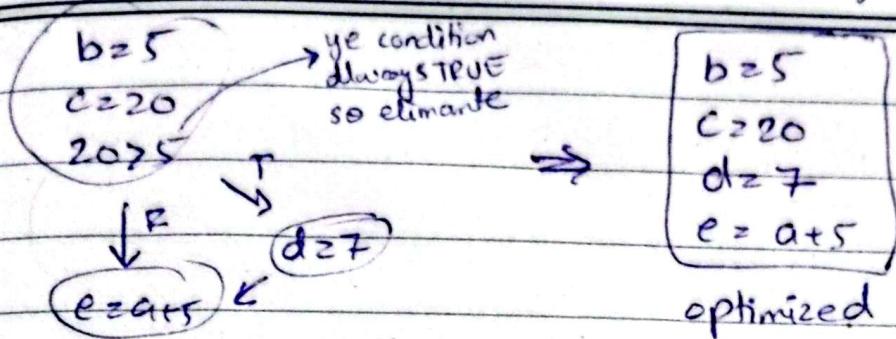
$$\begin{aligned} b &= 5 \\ c &= 20 \\ c &> b \end{aligned}$$

$$d = 7$$

$$e = a + 5$$

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→ Matrix Multiplication Optimization

for ($i=1 \rightarrow n$) \uparrow^A elements are accessed across rows, spatial locality is exploited for cache

for ($j=1 \rightarrow n$) \uparrow^B elements are accessed along columns, unless can hold all of B, cache will have problem

for ($k=1 \rightarrow n$) \uparrow

$$C[i, j] = C[i, j] + A[i, k] + B[k, j]$$

\downarrow
Single element accessed per loop

Optimized

for ($i=1 \rightarrow n$)

 for ($k=1 \rightarrow n$) \uparrow^j

 for ($j=1 \rightarrow n$) \uparrow^k

$$C[i, j] = C[i, j] + A[i, k] + B[k, j]$$

A → Single element loaded for loop body

B → Elements are accessed in row major

C → Extra loading storing, but across rows