

# ASSIGNMENT # 01

— Q1 —

— (b) —

(a) 63.3456

$$\begin{array}{r|l} 2 & 63-1 \\ \hline \end{array}$$

$$0.3456 \times 2 = 0.6912$$

$$\begin{array}{r|l} 2 & 31-1 \\ \hline \end{array}$$

$$0.6912 \times 2 = 1.3824$$

$$\begin{array}{r|l} 2 & 15-1 \\ \hline \end{array}$$

$$0.3824 \times 2 = 0.7648$$

$$\begin{array}{r|l} 2 & 7-1 \\ \hline \end{array}$$

$$0.7648 \times 2 = 1.5296$$

$$\begin{array}{r|l} 2 & 3-1 \\ \hline \end{array}$$

$$0.5296 \times 2 = 1.0592$$

$$\begin{array}{r|l} & 1 \\ \hline \end{array}$$

$$0.0592 \times 2 = 0.1184$$

$$0.1184 \times 2 = 0.2368$$

$$0.2368 \times 2 = 0.4736$$

$$0.4736 \times 2 = 0.9472$$

$$0.9472 \times 2 = 1.8944$$

They cannot be fully represented!

(11111.0101100001)

(b) 47.9232

$$\begin{array}{r|l} 2 & 47-1 \\ \hline \end{array}$$

$$\begin{array}{r|l} 2 & 23-1 \\ \hline \end{array}$$

$$\begin{array}{r|l} 2 & 11-1 \\ \hline \end{array}$$

$$\begin{array}{r|l} 2 & 5-1 \\ \hline \end{array}$$

$$\begin{array}{r|l} 2 & 2-0 \\ \hline \end{array}$$

$$\begin{array}{r|l} 2 & 1 \\ \hline \end{array}$$



2

$$0.9232 \times 2 = 1.8464$$

$$0.1696 \times 2 = 0.3392$$

$$0.8464 \times 2 = 1.6928$$

$$0.3392 \times 2 = 0.6784$$

$$0.6298 \times 2 = 1.3856$$

They cannot be fully represented!

$$0.3856 \times 2 = 0.7712$$

$$0.7712 \times 2 = 1.5424$$

$$(10111.111011000)$$

$$0.5424 \times 2 = 1.0848$$

→ Ans

$$0.0848 \times 2 = 0.1696$$

etc.

~~(a)~~

a)  $100110101.1010$

$$\Rightarrow (2^8 \times 1) + (2^7 \times 0) + (2^6 \times 0) + (2^5 \times 1) + (2^4 \times 1) + (2^3 \times 0) + (2^2 \times 1) + (2^1 \times 0) + (2^0 \times 1) + (2^{-1} \times 1) + (2^{-2} \times 0) + (2^{-3} \times 1) + (2^{-4} \times 0)$$

$$\Rightarrow 256 + 32 + 16 + 4 + 1 + 0.5 + 1/8 +$$

$$\Rightarrow (309.625)_{10} \rightarrow \text{Ans}$$

b)  $10111001.11011$

$$(2^7 \times 1) + (2^6 \times 0) + (2^5 \times 1) + (2^4 \times 1) + (2^3 \times 1) + (2^2 \times 0) + (2^1 \times 0) + (2^0 \times 1) + (2^{-1} \times 1) + (2^{-2} \times 1) + (2^{-3} \times 0) + (2^{-4} \times 1) + (2^{-5} \times 1)$$

$$= 128 + 32 + 16 + 8 + 1 + 0.5 + 1/4 + 1/16 + 1/32$$

$$(185.84375)_{10} \rightarrow \text{Ans}$$

~~(c)~~

-127

- (a) 11111001  $\rightarrow$  sign magnitude  
 (b) 10000110  $\rightarrow$  1's complement  
 (c) 10000111  $\rightarrow$  2's Complement

~~(d)~~

(a) (1010) gray

GC 1 0 1 0  
 Binary 1 1 0 0  $(1100)_2 \rightarrow$  Ans  
 $\downarrow$   
 1  $\rightarrow$  discard

(b) (00010) gray code

GC 0 0 0 1 0  
 Bin 0 0 0 1 1  $(0011)_2 \rightarrow$  Ans

(c) (11000010001) gray code

1 1 0 0 0 0 1 0 0 0 1  
 + + + + + + + + + +  
 1 0 0 0 0 0 0 1 1 1 0

$(10000011110)_2 \rightarrow$  Ans



(4)

~~(c)~~

$$\begin{array}{r|l}
 2 & 68-0 \\
 2 & 34-0 \\
 2 & 17-1 \\
 2 & 8-0 \\
 2 & 4-0 \\
 2 & 2-0 \\
 & 1
 \end{array}$$

$$(10111100)_2 \rightarrow \text{Ans}$$

↳ 8 bit 2's complement

(ii)

$$\begin{array}{cccccc}
 00 & 11 & 1001 \\
 \hline
 84 & 21 & 84 & 21
 \end{array}$$

3      9

$$(39)_{16} \rightarrow \text{Ans}$$

$$(iii) \quad 1 \quad 1000001 \quad 010010011100010000000000$$

S

E

F

1

100001

010010011100010000000000

$$\text{Number} = (-1)^S (1+F)(2^{E-127}) \quad ; S=1$$

$$= (-1)^1 (1.0100100111001)(2^{129-127})$$

$$= (-1)(1.0100100111001)(2^2)$$

$$\text{Number} = (-101.00100111001)_2 \rightarrow \text{Ans}$$

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(iv)  $01100100 (BCD) + 00110011 (BCD) = ?$

$$\begin{array}{r} 0110 \ 0100 \\ + 0011 \ 0011 \\ \hline 1001 \ 0111 \\ \hline \end{array}$$

$\underbrace{1001}_9 \quad \underbrace{0111}_7$

$\rightarrow (97)_{10}$

$(10001 \ 0111)_2 \rightarrow \text{Ans}$

~~(f)~~

(i)  $(1110)_2 \times (1110)_2$

$$\begin{array}{r} 1110 \\ \times 1110 \\ \hline 0000 \\ + 1110 \times \\ \hline \end{array}$$

$$\begin{array}{r} 1110 \ 0 \\ + 1110 \times \times \\ \hline \end{array}$$

$$\begin{array}{r} 1010100 \\ + 1110 \times \times \times \\ \hline \end{array}$$

$$11000100 \rightarrow \text{Ans.}$$

(ii)  $(110000)_2 - (1111)_2$

$$\begin{array}{r} 110000 \\ - 1111 \\ \hline \end{array}$$

$$100001 \rightarrow \text{Ans}$$

$100001 \rightarrow \text{Ans}$

$0011 \rightarrow \text{Ans.}$

(iii)  $101 \mid 1111$

$$\begin{array}{r} 1111 \\ - 101 \\ \hline \end{array}$$

$$0101$$

$$\begin{array}{r} 0101 \\ - 101 \\ \hline \end{array}$$

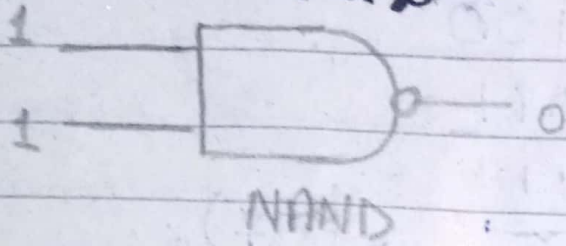
$\times \times$



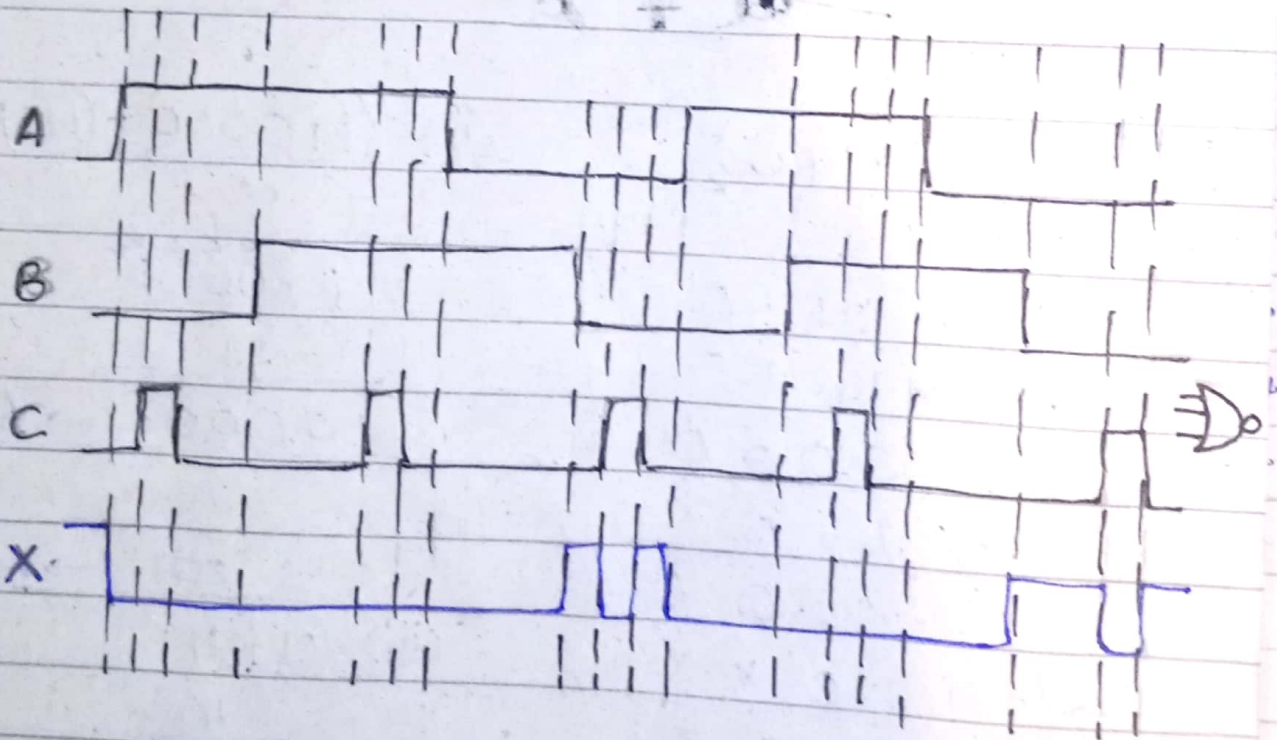
6

Q2

(a)



(b)



# Q3 ~~da~~

$$\begin{aligned}
 & (\overline{A}B) \cdot (\overline{B}+C) + C \\
 &= [(\overline{A}B) + (\overline{B}+C)] \cdot C' \\
 &= [(AB) + (\overline{B}+C)] \cdot C' \\
 &= [B(A+1) + C] \cdot C' \\
 &= (B+C) \cdot CC' \\
 &= BC' + CC' \quad \rightarrow CC'=0 \\
 &= BC' \rightarrow \underline{A}
 \end{aligned}$$

## ~~db~~

$$\begin{aligned}
 & X' + XY + XZ' + XY'Z' \\
 &= \{X' + Y + XZ'(1 + X')\} \\
 &= X' + Y + XZ'(1) \\
 &= X' + XZ' + Y \\
 &= X' + Z' + Y \rightarrow \text{Standard POS form}
 \end{aligned}$$

X	Y	Z	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1



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$$X' + XY + XZ' + XY'Z'$$

$$X'(Y+Y')(Z+Z') + XY(Z+Z') + XZ'(Y+Y') + XY'Z'$$

$$X'YZ + X'Y'Z'$$

$$(X'Y + X'Y')(Z+Z') + XYZ + XYZ' + XZ'Y + XY'Z' + XY'Z'$$

$$X'YZ + X'YZ' + X'Y'Z + X'Y'Z' + XYZ + XYZ' + XZ'Y + XY'Z'$$

$$X'YZ + X'YZ' + X'Y'Z + X'Y'Z' + XYZ + XYZ' + XY'Z'$$

011 010 001 000 111 110 100

Standard  
SOP

$X' + Y + Z' \rightarrow$  Standard POS form

84

No. of bits to encode 0-9999 (decimal)

in binary  $\rightarrow$  1-14 bits

in BCD  $\rightarrow$  4-16 bits

27

0010 0111

0000 0000 0010 0111