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## • Non-Deterministic CFGs

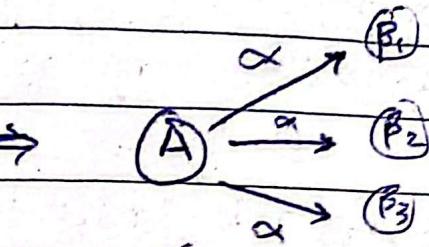
$$A \rightarrow \alpha \beta_1 \mid \alpha \beta_2 \mid \alpha \beta_3$$

or

$$A \rightarrow \alpha \beta_1$$

$$A \rightarrow \alpha \beta_2$$

$$A \rightarrow \alpha \beta_3$$



↳ each symbol per transition

→ Due to non-determinism the compiler needs to  
to do a lot of backtracking

↳ Top-Down parsers tend to suffer from NCFGs

↳ Using Left Factoring procedure we need to  
eliminate the non-determinism

With EK Production ordering

$$A \rightarrow (\alpha AB \mid \alpha BC \mid \alpha AC)$$

$$A \rightarrow \alpha A' \quad \begin{matrix} P_1 \\ P_2 \\ P_3 \end{matrix}$$

$$A \rightarrow \alpha \beta_1 \mid \alpha \beta_2 \mid \alpha \beta_3$$

$$A' \rightarrow AB \mid BC \mid AC$$

$$\hookrightarrow A \rightarrow \alpha A'$$

it is still non-deter

$$A \rightarrow \beta_1 \mid \beta_2 \mid \beta_3$$

$$A'' \rightarrow AA'' \mid Bc$$

$$A'' \rightarrow B \mid Be$$

Determinism cannot  
remove ambiguity

$$S \rightarrow i \cdot ETS \Rightarrow i \cdot ETS \cdot S \mid a$$

$$E \rightarrow b$$

$$S \rightarrow i \cdot S' \cdot ETS \mid a \quad S \rightarrow i \cdot ETS \cdot S' \mid a$$

~~$$S \rightarrow ETS \mid ETS \cdot S \quad S' \rightarrow \epsilon \mid Es$$~~

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$$\cdot S \rightarrow \underline{a}SSbS \mid \underline{a}SaSb \mid abb \mid b$$

$$S \rightarrow aS' \mid b$$

$$\hookleftarrow S' \rightarrow SSbS \mid SaSb \mid bb \times$$

$$\hookleftarrow S'' \rightarrow SS'' \mid abS \mid bb$$

$$S'' \rightarrow SbS \mid aSb$$

$$\cdot S \rightarrow \underline{b}SSaas \mid \underline{b}SSasb \mid \underline{b}Sb \mid a$$

$$S \rightarrow bSS' \mid a$$

$$\hookleftarrow S' \rightarrow \underline{S}aS \mid \underline{S}aSb \mid b$$

$$\hookleftarrow S' \rightarrow SaS'' \mid b$$

$$S'' \rightarrow aS \mid Sb$$

$$\cdot S \rightarrow a \mid ab \mid abc \mid abcd$$

$$S \rightarrow aS' \times$$

$$\hookleftarrow S' \rightarrow \epsilon \mid b \mid bc \mid bcd \times$$

$$\hookleftarrow S' \rightarrow bS'' \mid e$$

$$\hookleftarrow S'' \rightarrow \epsilon \mid c \mid cd \times$$

$$\hookleftarrow S'' \rightarrow cS''' \mid e$$

$$S''' \rightarrow \epsilon \mid d$$

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## ► PARSERS (Syntax Analyzers)

"A parser is a program that generates a parse tree for the given string, if the string is generated from the underlying grammar."

→ Generation of Parse Tree

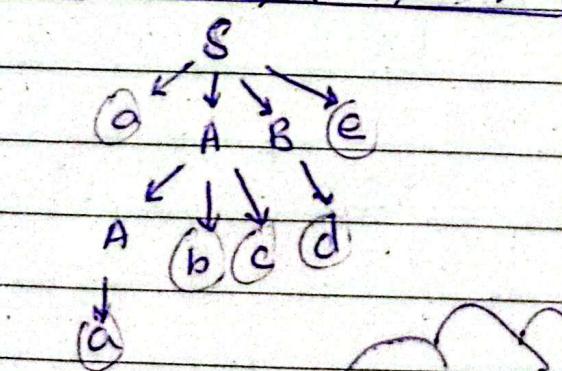
↳ There are two approaches for tree generation

① Top-Down Approach → Top Down Parser

② Bottom-Up " → Bottom Up "

$S \rightarrow aABe, A \rightarrow Abc | a, B \Rightarrow d$  aabbcde

Top Down Approach



$C \Rightarrow aABe$

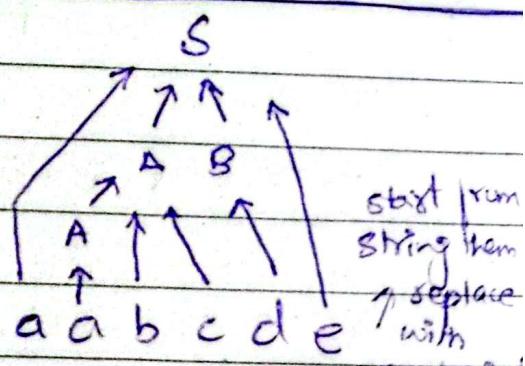
$\Rightarrow aAbcBe$

$\Rightarrow aabcBe$

$\Rightarrow abcBe$

left most derivation

Bottom Up Approach



$S \Rightarrow aABe$

$S \Rightarrow aAde$

$S \Rightarrow aAbcde$

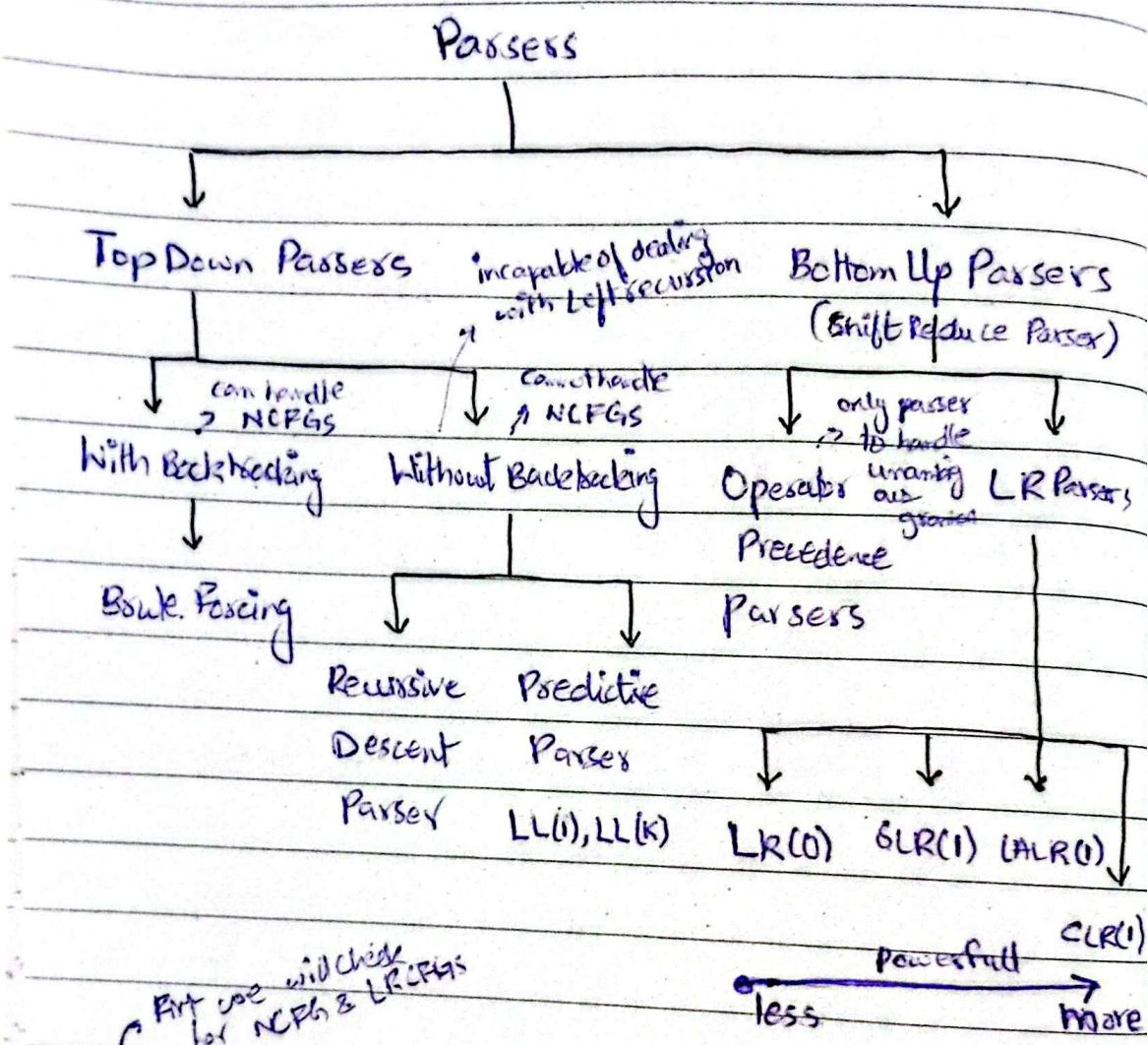
$S \Rightarrow aa bcde$

(right most Dev) - in reverse

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## Classification of Parser

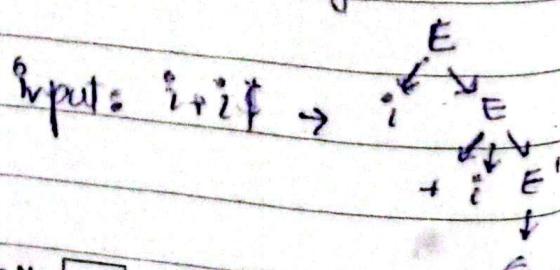


### ► Recursive Descent Parser :

- In this parser we convert each of the Non-terminal into an equivalent Function. Then all those function becomes exactly like the grammar.

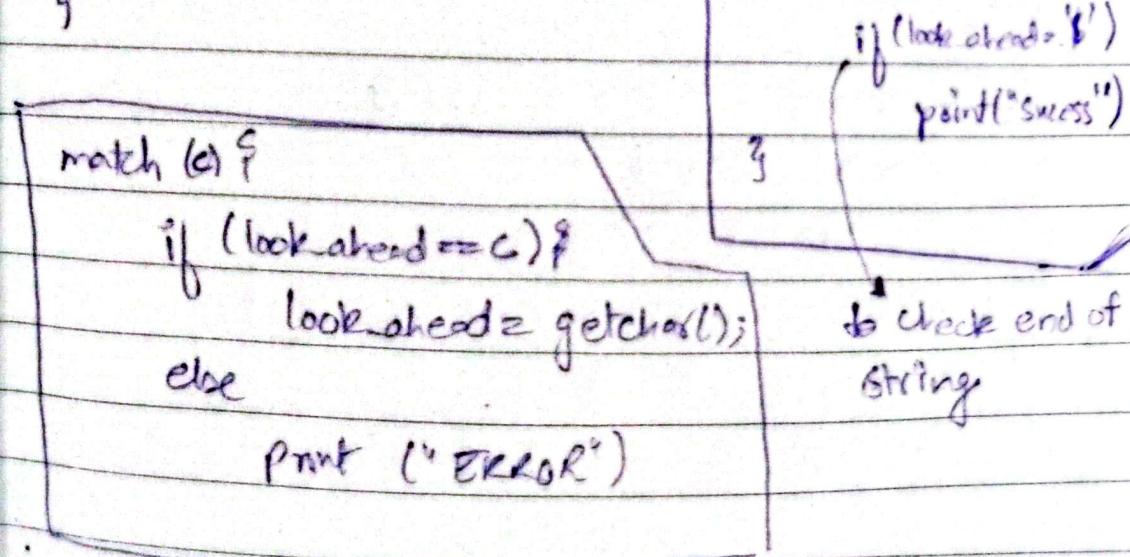
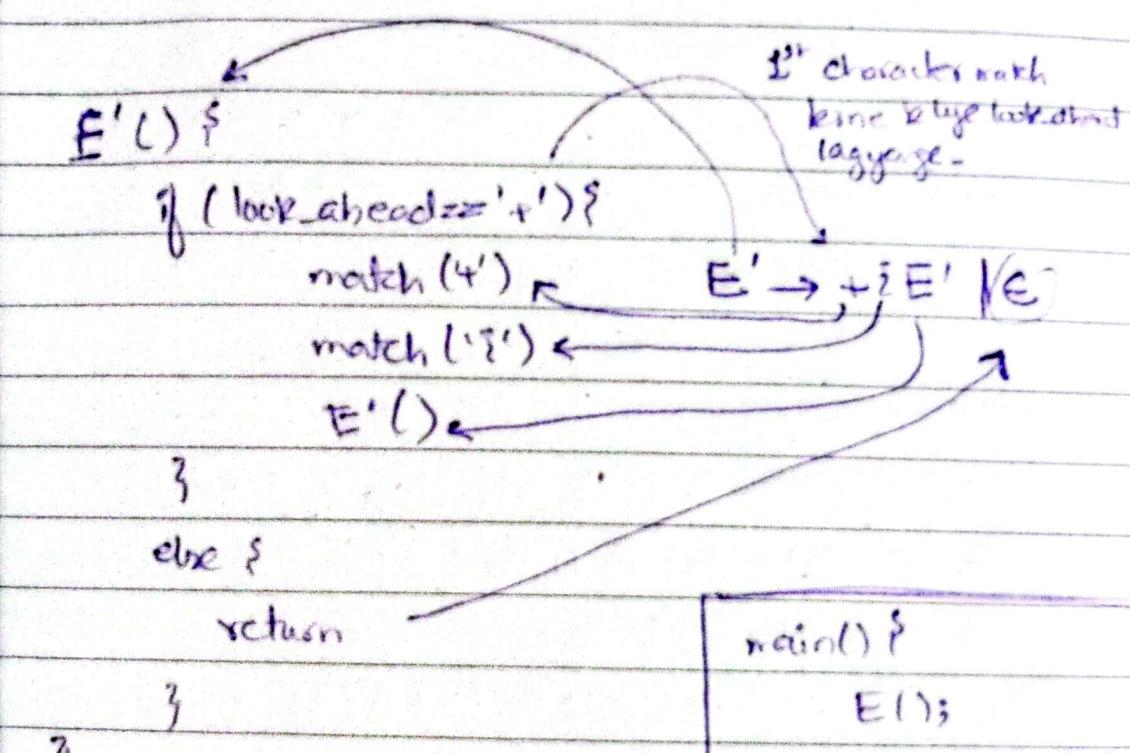
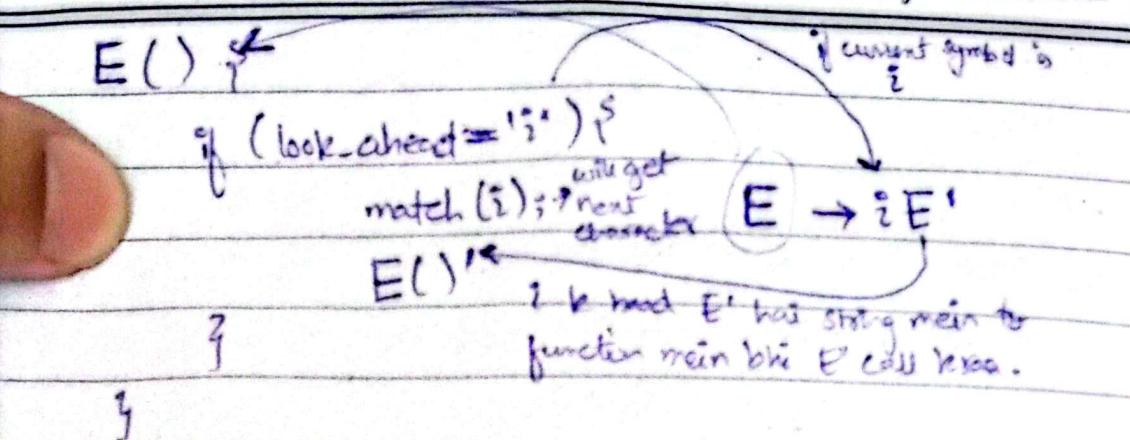
$$E \rightarrow i E'$$

$$E' \rightarrow + i E' | G$$



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" We dedication functions to all procedure  
which will miss the grammar "



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## ► FIRST() & FOLLOW()

### • FIRST()

→ First(A) → gives set of terminals that begins in all strings derive from A.

1. If  $A \rightarrow a\alpha$  → any terminal / non-terminal

$$\text{First}(A) = \{a\}$$

2. If  $A \rightarrow \epsilon$

$$A \rightarrow bScB$$

$$\text{First}(A) = \{b\}$$

$$\text{First}(A) = \{\epsilon\}$$

3. If  $A \rightarrow BC$

i-  $\text{First}(A) = \text{First}(B)$  → if  $\text{First}(B)$  doesn't contain  $\epsilon$

ii-  $\text{First}(A) = \text{First}(B) \cup \text{First}(C)$  if  $\text{First}(B)$  contains  $\epsilon$

iii-  $\text{First}(A) = \{ \epsilon \}$

↳  $\text{First}(B), \text{First}(C) \cup \{\epsilon\}$  if both B & C have  $\epsilon$

$$A \rightarrow BC \rightarrow \text{First}(A) = \{b, d\}$$

$$B \rightarrow b, C \rightarrow d$$

$$\text{First}(B) = \{b\} \quad \text{First}(C) = \{d\}$$

$$A \rightarrow BC \rightarrow \text{First}(A) = \{b, d\}$$

$$B \rightarrow b | \epsilon, C \rightarrow d$$

$$\text{First}(B) = \{b, \epsilon\} \quad \text{First}(C) = \{d\}$$

↳ is main  $\epsilon$  back to C which change.

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$$A \rightarrow BC \rightarrow \text{First}(A) = \{b, d, E\}$$

$$B \rightarrow bIE \rightarrow \text{First}(B) = \{b, E\} \quad \begin{matrix} \text{get tabhi} \\ \text{daskta hai} \end{matrix}$$

$$C \rightarrow dIE \rightarrow \text{First}(C) = \{d, E\} \quad \begin{matrix} \text{jab dono B \&} \\ \text{E mein E} \\ \text{hota} \end{matrix}$$

→ Follow() is set mein "E" niu auto karta

### • Follow()

1. If S is start symbol then

$$\text{Follow}(S) = \$$$

2. If  $A \rightarrow \alpha B \beta$ , then  $\beta$  can be terminal or non-terminal

$$\text{Follow}(B) = \text{First}(\beta)$$

3. If  $A \rightarrow \alpha \beta$ , then

$$\text{Follow}(\beta) = \text{Follow}(A)$$

### ○ Solved Examples of First() & Follow()

	First	Follow
$E \rightarrow TE'$	$\{id, ()\}$	$\{\$, \$, (), ()\}$
$E' \rightarrow +TE'   \epsilon$	$\{+, \epsilon\}$	$\{\$, \$, (), ()\}$
$T \rightarrow FT'$	$\{id, ()\}$	$\{+, \$, ()\}$
$T' \rightarrow *FT'   \epsilon$	$\{* , \epsilon\}$	$\{+, \$, ()\}$
$F \rightarrow id   (E)$	$\{id, ()\}$	$\{* , \$, \$, (), ()\}$

Always start with bottom terminal in first

↑      ↑      ↑      ↓      ↓      ↓      ↓      ↓

$\text{Follow}(C) = \text{Follow}(B)$

Date	First(S)	Follow(D)
$S \rightarrow aBDh$	$\{a\}$	$\{b, g\}$
$B \rightarrow CC$	$\{c\}$	$\{g, f, h\}$
$C \rightarrow bC   \epsilon$	$\{b, \epsilon\}$	$\{g, f, h\}$
$D \rightarrow EF$	$\{g, f, e\}$	$\{h\}$
$E \rightarrow g   \epsilon$	$\{g, \epsilon\}$	$\{f, h\}$
$F \Rightarrow f   \epsilon$	$\{f, \epsilon\}$	$\{h\}$

Follow(B):

$S \rightarrow aBDh$

First(D) =  $\{g, f, \epsilon\}$

(g)  $S \rightarrow aB\overset{g}{|}h$

Follow(B) =  $\{g\}$

(f)  $S \rightarrow aB\overset{f}{|}h$

Follow(B) =  $\{g, f\}$

(E)  $S \rightarrow aB\overset{\epsilon}{|}h$

Follow(B) =  $\{g, f, h\}$

↳ epsilon but krenge to "h" hojayeg follow of B.

Follow(E):

$D \rightarrow E(F)$

First(F) =  $\{f, \epsilon\}$

(F)  $D \rightarrow E\overset{f}{|}$

Follow(E) =  $\{f\}$

(E)  $D \rightarrow E$

Follow(E) =  $\{f, h\}$

Follow of  $D \rightarrow ph$

Date	First()	Last
$E \rightarrow TE'$ $E' \rightarrow E \mid +TE'$ $T \rightarrow FT'$ $T' \rightarrow E \mid *FT'$ $F \rightarrow id \mid (E)$		
$S \rightarrow Bb \mid Cd$ $B \rightarrow aB \mid \epsilon$ $C \rightarrow CC \mid \epsilon$	$\{a, b, c, d\}$ $\{a, \epsilon\}$ $\{c, \epsilon\}$	$\{\$\}$ $\{b\}$ $\{d\}$
$S \rightarrow AaAb \mid BbBa$ $A \rightarrow E$ $B \rightarrow E$	$\{e, ab\}$ $\{e\}$ $\{e\}$	$\{\$\}$ $\{a, b\}$ $\{b, a\}$
$P \rightarrow xQRS$ $Q \rightarrow yz \mid z$ $R \rightarrow w \mid \epsilon$ $S \rightarrow y$	$\{x\}$ $\{y, z\}$ $\{w, e\}$ $\{y\}$	$\{\$\}$ $\{w, y\}$ $\{y\}$ $\{\$\}$
$S \rightarrow ABCDE$ $A \rightarrow a \mid \epsilon$ $B \rightarrow b \mid \epsilon$ $C \rightarrow c$ $D \rightarrow d \mid \epsilon$ $E \rightarrow e \mid \epsilon$	$\{a, b, c\}$ $\{a, \epsilon\}$ $\{b, \epsilon\}$ $\{c\}$ $\{d, \epsilon\}$ $\{e, \epsilon\}$	$\{\$\}$ $\{b, c\}$ $\{c\}$ $\{e, f, d\}$ $\{e, \$\}$ $\{\$\}$

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$S \rightarrow Bb \mid Cd$	$\{a, b, c, d\}$	$\{B\}$
$B \rightarrow aB \mid \epsilon$	$\{a, \epsilon\}$	$\{b\}$
$c \rightarrow CC \mid \epsilon$	$\{c, \epsilon\}$	$\{d\}$

$S \rightarrow ACB \mid CBB \mid Ba$	$\{d, g, h, \epsilon, b, a\}$	$\{\$\}$
$A \rightarrow da \mid BC$	$\{d, g, h, \epsilon\}$	$\{f, g, \epsilon\}$
$B \rightarrow gle$	$\{g, \epsilon\}$	$\{f, a, h, g\}$
$C \rightarrow h \mid \epsilon$	$\{h, \epsilon\}$	$\{f, g, h, g, \epsilon\}$

Non-recursive Descent Parser

► LL(1) Parser's They are predictive parser

→ "L" look-ahead symbol

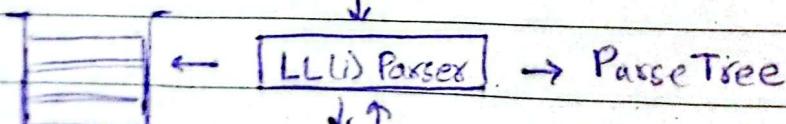
Use "L" left most derivation

→ Scan from "L" left to right

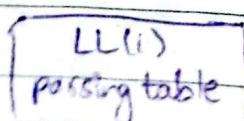
Input Buffer



↓



↓↑



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	First()	Follow()
$E \rightarrow TE'$	{id, C}	{\$, +}
$E' \rightarrow E \mid T E'$	{E, +}	{\$, +}
$T \rightarrow FT'$	{id, C}	{+, \$, +}
$T' \rightarrow E \mid FT'$	{E, *}	{+, \$, +}
$F \rightarrow id \mid (E)$	{id, C}	{*, +, \$, +}

1. Add  $A \rightarrow \alpha$  under  $N[A, a]$ where  $a \in \text{first}(\alpha)$ 

→ Simply bcs

 $\text{First}(A)$  nukalne  
ge

or un terminals

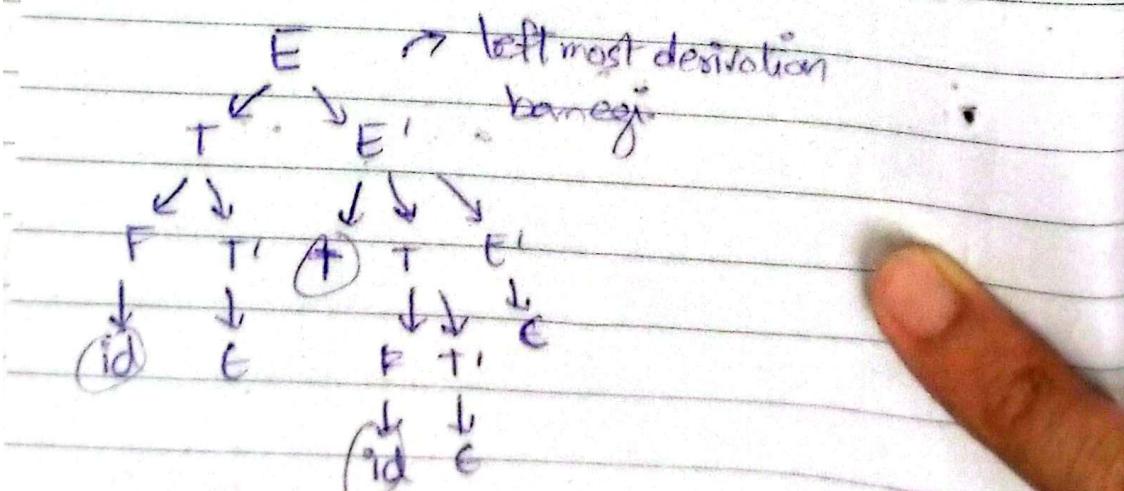
pos value pos  
krdenge.2. Add  $A \rightarrow \alpha$  under  $M[A, a]$ where  $a \in \text{follow}(A)$ Aug us mein  
hoy to follow(A)if  $\text{first}(\alpha)$  contain  $\epsilon$ K set mein  
 $A \rightarrow \epsilon$  likhoge.

M	id	+	*	(	)	\$	
$E$	$E \rightarrow TE'$			$E \rightarrow TE'$			
$E'$		$E \rightarrow AE'$			$E' \rightarrow E$	$E' \rightarrow \epsilon$	
$T$	$T \rightarrow FT'$			$T \rightarrow FT'$			
$T'$		$T \rightarrow E$	$T' \rightarrow FT'$		$T' \rightarrow E$	$T' \rightarrow E$	
$F$	$F \rightarrow id$			$F \rightarrow (E)$			

6 Aug ek cell mein do entries aajyein so that  
Grammar cannot be passed thru L(1) parser.

Date ↗ seven mein doo rang  
production rule: Day

Stack	Input	Production
\$ E	id + id \$	$E \rightarrow TE'$
\$ E' T	id + id \$	$T \rightarrow FT'$
\$ E' T F	id + id \$	$F \rightarrow id$
\$ E' T (id	id + id \$	pop()
\$ E' T' pop	+ id \$	$T' \rightarrow G$
A E' pop	+ id \$	$E' \rightarrow +TE'$
\$ E' T F	id \$	pop()
\$ E' T F id	id \$	pop()
A E' T' pop	\$	$T' \rightarrow E$
\$ E'	\$	$E' \rightarrow E$
\$ E	\$	Accept!



Date IDENTIFYING LL(1) Grammar Day not LL(1)

$\rightarrow$  If G is Ambiguous,  
NFCs, LR CFGs  
then also it is  
not LL(1).

- If G doesn't contain  $\epsilon$

$$A \rightarrow \alpha_1 \mid \alpha_2 \mid \alpha_3$$

$$\text{First}(\alpha_1) \cap \text{First}(\alpha_2) = \emptyset$$

$$\text{First}(\alpha_1) \cap \text{First}(\alpha_3) = \emptyset$$

$$\text{First}(\alpha_2) \cap \text{First}(\alpha_3) = \emptyset$$

→ no production pair of longer

- If G contains  $\epsilon$

$$A \rightarrow \alpha_1 \mid \alpha_2 \mid \epsilon$$

$$\text{First}(\alpha_1) \cap \text{First}(\alpha_2) = \emptyset$$

$$\text{First}(\alpha_1) \cap \text{Follow}(A) = \emptyset$$

$$\text{First}(\alpha_2) \cap \text{Follow}(A) = \emptyset$$

- $S \rightarrow E \mid a$        $a \cap a = a$

$$E \rightarrow a \quad ? \quad \text{LL(1)} X$$

$$\text{First}(E) = a$$

- $S \rightarrow aABb$  ✓ → only one production  
so rule not applied

$$A \rightarrow a \mid \epsilon \rightarrow a \cap \{d, b\} = \emptyset$$

$$B \rightarrow d \mid \epsilon \rightarrow d \cap \{d\} = \emptyset$$

- $S \rightarrow aSA \mid \epsilon \rightarrow aA \cap \{\}\} = \emptyset$

$$A \rightarrow c \mid \epsilon \rightarrow c \cap \{\}\} = \emptyset X$$

LL(1) X