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OBJECTIVE:

- Empirical Analysis of the Quick-Sort Algorithm
- Empirical Analysis of the Merge-Sort Algorithm
- Binary-Tree Creation and Post-Order, Pre-Order, In-Order Traversals

Q1. Write a Python program that makes the empirical analysis of the quick-sort algorithm by using following algorithm, which uses Hoare's Partitioning Algorithm.

```

ALGORITHM Quicksort( $A[l..r]$ )
//Sorts a subarray by quicksort
//Input: Subarray of array  $A[0..n - 1]$ , defined by its left and right
//      indices  $l$  and  $r$ 
//Output: Subarray  $A[l..r]$  sorted in nondecreasing order if  $l < r$ 
 $s \leftarrow \text{Partition}(A[l..r])$  //  $s$  is a split position
Quicksort( $A[l..s - 1]$ )
Quicksort( $A[s + 1..r]$ )

```

```

Algorithm Partition( $A[l..r]$ )
//Partitions a subarray by using its first element as a pivot
//Input: A subarray  $A[l..r]$  of  $A[0..n - 1]$ , defined by its left and right
//      indices  $l$  and  $r$  ( $l < r$ )
//Output: A partition of  $A[l..r]$ , with the split position returned as
//      this function's value
 $p \leftarrow A[l]$ 
 $i \leftarrow l; j \leftarrow r + 1$ 
repeat
    repeat  $i \leftarrow i + 1$  until  $A[i] \geq p$ 
    repeat  $j \leftarrow j - 1$  until  $A[j] < p$ 
    swap( $A[i], A[j]$ )
until  $i \geq j$ 
swap( $A[i], A[j]$ ) //undo last swap when  $i \geq j$ 
swap( $A[l], A[j]$ )
return  $j$ 

```

- Program generates a random array. Size of the array is 10000 and the numbers between 0-100.

Output:

None

0.0156233 seconds

Q2. Write a Python program that makes the empirical analysis of the merge-sort algorithm by using following algorithm;

ALGORITHM *Mergesort*($A[0..n - 1]$)

//Sorts array $A[0..n - 1]$ by recursive mergesort
 //Input: An array $A[0..n - 1]$ of orderable elements
 //Output: Array $A[0..n - 1]$ sorted in nondecreasing order

if $n > 1$

 copy $A[0..\lfloor n/2 \rfloor - 1]$ to $B[0..\lfloor n/2 \rfloor - 1]$
 copy $A[\lfloor n/2 \rfloor..n - 1]$ to $C[0..\lceil n/2 \rceil - 1]$
 Mergesort($B[0..\lfloor n/2 \rfloor - 1]$)
 Mergesort($C[0..\lceil n/2 \rceil - 1]$)
 Merge(B, C, A)

ALGORITHM *Merge*($B[0..p - 1], C[0..q - 1], A[0..p + q - 1]$)

//Merges two sorted arrays into one sorted array
 //Input: Arrays $B[0..p - 1]$ and $C[0..q - 1]$ both sorted
 //Output: Sorted array $A[0..p + q - 1]$ of the elements of B and C

$i \leftarrow 0; j \leftarrow 0; k \leftarrow 0$

while $i < p$ **and** $j < q$ **do**

if $B[i] \leq C[j]$
 $A[k] \leftarrow B[i]; i \leftarrow i + 1$
 else $A[k] \leftarrow C[j]; j \leftarrow j + 1$
 $k \leftarrow k + 1$

if $i = p$
 copy $C[j..q - 1]$ to $A[k..p + q - 1]$
else copy $B[i..p - 1]$ to $A[k..p + q - 1]$

- Program generates a random array using numpy module. Size of the array is 10000 and numbers will be between 1-1000.

Output:

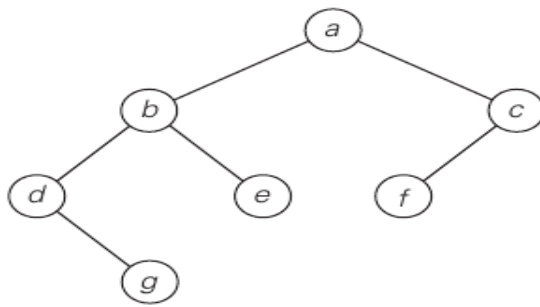
0.12713909149169922 seconds
 [1 1 1 ... 396 396 981]

Q3. Write a OOP-Python program that gets 10 numbers from the user, to construct a sorted binary-tree. Then program displays the **post-order**, **pre-order** and **in-order** traversals of the given tree. Please write down :

Insert_node(new_node_value) recursive function,
 get_right_child()
 get-left_child()
 set_root_val()
 get_root_val()
 preorderTrav()
 inorderTrav()
 postorderTrav()

functions

Check the given examples.



preorder: *a, b, d, g, e, c, f*
 inorder: *d, g, b, e, a, f, c*
 postorder: *g, d, e, b, f, c, a*

Output:

The binary tree will be created with your numbers.
 Please enter 10 numbers to create sorted binary tree
 Enter a number:35
 root: None
 Enter a number:60
 root: 35
 right child <__main__.BinaryTree object at 0x03E09410>
 Enter a number:90
 root: 35
 right child <__main__.BinaryTree object at 0x03E09A70>
 right tree <__main__.BinaryTree object at 0x03E09410>
 Enter a number:5
 root: 35
 left child <__main__.BinaryTree object at 0x03E09E10>
 Enter a number:4
 root: 35
 left child <__main__.BinaryTree object at 0x03E09E30>
 left tree <__main__.BinaryTree object at 0x03E09E10>
 Enter a number:40
 root: 35
 left child <__main__.BinaryTree object at 0x03E09E50>
 right tree <__main__.BinaryTree object at 0x03E09410>
 Enter a number:3
 root: 35
 left child <__main__.BinaryTree object at 0x03E09E70>
 left tree <__main__.BinaryTree object at 0x03E09E30>
 left tree <__main__.BinaryTree object at 0x03E09E10>
 Enter a number:15
 root: 35
 right child <__main__.BinaryTree object at 0x03E09E90>
 left tree <__main__.BinaryTree object at 0x03E09E10>
 Enter a number:37
 root: 35
 left child <__main__.BinaryTree object at 0x03E09EB0>
 left tree <__main__.BinaryTree object at 0x03E09E50>
 right tree <__main__.BinaryTree object at 0x03E09410>
 ...***...
 Pre-Order
 35
 5
 4
 3
 15
 60
 40
 37
 90

```
...***...
Post-Order
3
4
15
5
37
40
90
60
35
...***...
In-Order
3
4
5
15
35
37
40
60
90
>>>
```