

# NATIONAL UNIVERSITY OF COMPUTER AND EMERGING SCIENCES (KARACHI CAMPUS) FAST School of Computing FALL 2024

# <u>DESIGN AND ANALYSIS OF ALGORITHMS :</u> <u>PROJECT</u>

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# **Question 1:**

# A: part 1)

```
#include <iostream>
using namespace std;
void LargestAndSmallest(int A[], int low, int high, int &largest, int &smallest) {
  if (low == high) {
    largest = A[low];
    smallest = A[low];
    return;
  }
  else if (high == low + 1) {
    if (A[low] > A[high]) {
      largest = A[low];
       smallest = A[high];
    } else {
       largest = A[high];
       smallest = A[low];
    }
    return;
  }
  else {
    int mid = (low + high) / 2;
    int largest1, smallest1, largest2, smallest2;
    LargestAndSmallest(A, low, mid, largest1, smallest1);
    LargestAndSmallest(A, mid + 1, high, largest2, smallest2);
    largest = max(largest1, largest2);
    smallest = min(smallest1, smallest2);
  }
}
int main() {
  int n;
  cout << "Enter the number of elements in the array: ";
  cin >> n;
  int A[n];
  cout << "Enter the elements of the array:\n";</pre>
  for (int i = 0; i < n; i++) {
```

```
cin >> A[i];
}
int largest, smallest;
LargestAndSmallest(A, 0, n - 1, largest, smallest);
cout << "Largest element: " << largest << endl;
cout << "Smallest element: " << smallest << endl;
return 0;
}</pre>
Time Complexity 0(N)
```

# A: part 2)

The recurrence relation for the number of comparisons made by the algorithm is:

```
T(n) = 2T(n/2) + 2
Solution for n = 2^k:
T(n) = O(3n/2 - 2)
```

# A: part 3)

In brute force algorithm, we will iterate through the entire array once to find minimum and iterate once to find maximum. This is done in time complexity O(n).

However, the divide and conquer algorithm also gives time complexity of O(n), which means that the two algorithms are somehow equal in terms of complexity.

The difference between both divide & conquer and brute force is that divide & conquer performs comparisons in a structural manner, while brute force performs comparisons in a single pass.

### B: part 1)

```
Algorithm Exponentiation(a, n):

if n == 0:

return 1

else if n is even:

half = Exponentiation(a, n // 2)

return half * half

else:

return a * Exponentiation(a, n - 1)
```

# **B:Part 2)**

```
Recurrence Relation for Multiplications:

T(n) = T(n/2) + 1 for even n

The solution to this recurrence is T(n) = O(\log n)
```

# **B:Part 3)**

Comparison with Brute-Force Algorithm:

The brute-force algorithm requires n multiplications, while this divide-and-conquer method performs O(log n) multiplications, making it more efficient.

# <u>C :</u>

```
#include <iostream>
using namespace std;
int merge(int arr[], int start, int end, int mid) {
  int i = start;
  int j = mid + 1;
  int k = 0;
  int inversions = 0;
  int temp[end - start + 1];
  while (i \leq mid && j \leq end) {
    if (arr[i] <= arr[j]) {
       temp[k++] = arr[i++];
    } else {
       temp[k++] = arr[j++];
       inversions += (mid - i + 1);
    }
  }
  while (i <= mid) {
    temp[k++] = arr[i++];
  }
  while (j <= end) {
    temp[k++] = arr[j++];
  }
  for (i = start; i <= end; i++) {
    arr[i] = temp[i - start];
```

```
}
  return inversions;
}
int mergeSort(int arr[], int start, int end) {
  if (start >= end) {
     return 0;
  }
  int mid = (start + end) / 2;
  int inversions = 0;
  inversions += mergeSort(arr, start, mid);
  inversions += mergeSort(arr, mid + 1, end);
  inversions += merge(arr, start, end, mid);
  return inversions;
}
int main() {
  int arr[] = {8, 4, 2, 1,5,7,8,9,15,4};
  int n = sizeof(arr) / sizeof(arr[0]);
  int inversionCount = mergeSort(arr, 0, n - 1);
  cout << "Sorted Array: ";</pre>
  for (int i = 0; i < n; i++) {
     cout << arr[i] << " ";
  }
  cout << endl;
  cout << "Number of Inversions: " << inversionCount << endl;</pre>
  return 0;
// Time Complexity:
// Best: O(n log n)
// Avg: O(n log n)
// Worst: O(n log n)
```

# <u>D:</u>

### Best case:

The best case for quicksort occurs when the pivot element divides the array into two nearly equal halves each time. This results in a balanced division, where each partition step splits the array as evenly as possible. In such a scenario:

- 1. Each partition splits the array in half
- 2. The height of the recursion tree therefore is log 2 n.
- 3. At each level of the tree, the algorithm performs O(n) comparisons.

So, height \* comparisons = O(nlog\_2n)

### Worst case:

The worst case for quicksort occurs when the pivot element is either the smallest or largest element in the array, causing one partition to have n-1 elements and the other partition to be empty (or have just one element) every time. This results in highly unbalanced partitioning. In such a scenario:

- 1. Each partition only reduces the problem size by one element.
- 2. The recursion tree has n levels.
- 3. At each level the algorithm performs O(n) comparisons.

So, height \* comparisons =  $O(n*n) = O(n^2)$ 

# <u>E:</u>

1.

### Steps to follow:

- 1. Sort the array
- 2. Divide the array
- 3. Base case
- Recursive closest distance calculation
- Cross-Pair check (closest pair across the boundary)
- 6. Check midpoint-crossing pairs
- 7. Return the final minimum distance

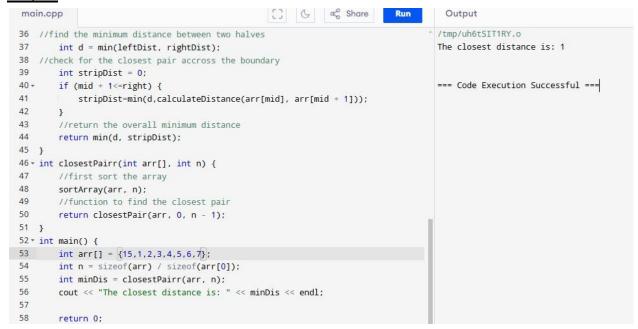
### Code:

```
#include <iostream>
#include <math.h>
#include <climits>
using namespace std;
//calculate distance between two points
int calculateDistance(int a, int b) {
```

```
return abs(a - b);
}
//to sort the points
void sortArray(int arr[], int n){
  for(int i = 0; i < n - 1; i++){
    for(int j = i + 1; j < n; j++){
       if(arr[i] > arr[j]){
         int temp = arr[i];
         arr[i] = arr[j];
         arr[j] = temp;
       }
    }
  }
//to calculate closest pair in the given array
int closestPair(int arr[], int left, int right){
//no need to divide as there are only two elements
  if(right-left==1){
    return calculateDistance(arr[left],arr[right]);
}
//if there is only one element in the array
 if (left>=right){
    return -1;
  }
  //using divide and conquer approach
  int mid=left+(right-left)/2;
//find recursively the minimum distance on left and right side
  int leftDist=closestPair(arr,left,mid);
  int rightDist=closestPair(arr,mid + 1,right);
//find the minimum distance between two halves
  int d = min(leftDist, rightDist);
//check for the closest pair across the boundary
  int stripDist = 0;
  if (mid + 1<=right) {
    stripDist=min(d,calculateDistance(arr[mid], arr[mid + 1]));
  //return the overall minimum distance
  return min(d, stripDist);
```

```
int closestPairr(int arr[], int n) {
    //first sort the array
    sortArray(arr, n);
    //function to find the closest pair
    return closestPair(arr, 0, n - 1);
}
int main() {
    int arr[] = {7, 1, 9, 3, 14};
    int n = sizeof(arr) / sizeof(arr[0]);
    int minDis = closestPairr(arr, n);
    cout << "The closest distance is: " << minDis << endl;
    return 0;
}</pre>
```

### Output:



This divide-and-conquer algorithm operates with a time complexity of O(nlogn) due to the sorting step and the recursive splitting. The cross-boundary check is limited to O(n)in each recursion level, making it efficient.

2.

Yes, for one dimensional closest pair this approach takes less time i.e O(nlogn) as compared to brute force which takes  $O(n^2)$  times.

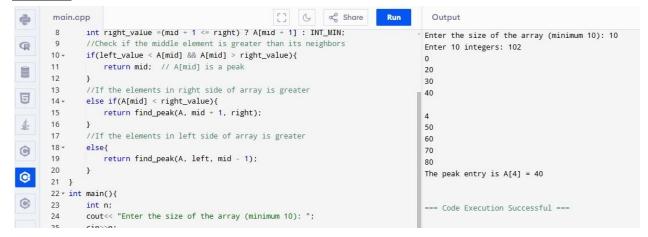
## <u>F:</u>

### CODE:

```
#include<iostream>
#include<limits.h>
using namespace std;
int find peak(int A[], int left, int right){
  int mid=(left + right) / 2;
  //Handle boundaries
  int left value =(mid - 1 >= left) ? A[mid - 1] : INT MIN;
  int right value =(mid + 1 <= right) ? A[mid + 1] : INT_MIN;
  //Check if the middle element is greater than its neighbors
  if(left value < A[mid] && A[mid] > right value){
    return mid; // A[mid] is a peak
  //If the elements in right side of array is greater
  else if(A[mid] < right value){
    return find peak(A, mid + 1, right);
  //If the elements in left side of array is greater
  else{
    return find peak(A, left, mid - 1);
  }
}
int main(){
  int n;
  cout<< "Enter the size of the array (minimum 10): ";
  cin>>n;
  if(n < 10){
    cout<< "Size must be at least 10." << endl;
    return 1;
  }
  int A[n];
  cout<< "Enter" << n << " integers: ";
  for(int i = 0; i < n; i++){
    cin>>A[i];
  int peak_index=find_peak(A, 0, n - 1);
```

```
cout<<"The peak entry is A[" << peak_index << "] = "<<A[peak_index]<<endl;
return 0;
}</pre>
```

### **OUTPUT:**



# <u>G:</u>

So we split the array into two parts: search for minimum price on the left and store the index and maximum price on the right and store index.

Code according to example in book:

```
#include <iostream>
#include <climits>
using namespace std;

void maximum_money(int p[],int left, int right);
void find(int p[],int left, int mid, int right);

int maximum = 0;
int buy_index = 0;
int sell_index = 0;

int main() {
   int n;
   cout<<"Enter number of consecutive days:";
   cin>> n;
   int p[n];
```

```
for(int i=0;i<n;i++)
  {
    cout<<"Enter stock price on day"<<i+1<<": ";
    cin>> p[i];
  }
  maximum_money(p,0,n-1);
  cout<<"buy on:"<< buy index+1<<"\nsell on: "<<sell index+1;</pre>
  return 0;
}
void maximum money(int p[],int left, int right)
{
  if (left >= right)
    return;
  int mid = left + (right - left) / 2;
  maximum money(p, left, mid);
  maximum money(p, mid + 1, right);
  find(p, left, mid, right);
}
void find(int p[],int left, int mid, int right)
{
  int n1 = mid - left + 1;
  int n2 = right - mid;
  int highL=0,highR=0;
  int lowL=INT MAX,lowR=INT MAX;
  int index HL, index HR;
  int index LL, index LR;
  int L[n1],R[n2];
  for (int i = left; i \le mid; i++)
  {
    if (p[i] < lowL) {
      lowL = p[i];
       index_LL = i;
    }
  }
```

```
for (int j = mid + 1; j <= right; j++)
{
    if (p[j] > highR) {
        highR = p[j];
        index_HR = j;
    }
}
int current_profit = highR - lowL;
if (current_profit > maximum)
{
    maximum = current_profit;
    buy_index = index_LL;
    sell_index = index_HR;
}
```

### Output screen:

}

```
C++ Online Compiler
        1 #include <iostream>
                                                                                /tmp/8rI39bd0Ii.o
        3 using namespace std;
                                                                               Enter stock price on day1: 130
                                                                               Enter stock price on day2: 122
        5 void maximum_money(int p[],int left, int right);
                                                                                Enter stock price on day3: 900
        6 void find(int p[],int left, int mid, int right);
                                                                               Enter stock price on day4: 12
5
                                                                               Enter stock price on day5: 1222
                                                                                Enter stock price on day6: 23
       9 int buy_index = 0;
10 int sell_index = 0;
                                                                               Enter stock price on day7: 10
                                                                               Enter stock price on day8: 17
                                                                                Enter stock price on day9:
       12 - int main() {
                                                                                144
                                                                               Enter stock price on day10: 135
       13
               cout<<"Enter number of consectuive days : ";</pre>
               cin>> n;
                                                                                sell on : 5
0
       16
               int p[n]:
               for(int i=0;i<n;i++)
                                                                                === Code Execution Successful ===
JS
       18 -
                   cout<<"Enter stock price on day"<<i+1<<"; ";</pre>
               maximum_money(p,0,n-1);
       22
               cout<<"buy on : "<< buy_index+1<<"\nsell on : "<<sell_index
Le
       24
               return 0:
(8)
      26
27 void maximum_money(int p[],int left, int right)
       29
               if (left >= right)
                   return:
```

# H Exercises (1, 5, 6)

# Exercise 1.

You are interested in analyzing some hard-to-obtain data from two separate databases. Each database contains n numerical values—so there are 2n values total—and you may assume that no two values are the same. You'd like to determine the median of this set of 2n values, which we will define here to be the nth smallest value. However, the only way you can access these values is through queries to the databases. In a single query, you can specify a value k to one of the two databases, and the chosen database will return the kth smallest value that it contains. Since queries are expensive, you would like to compute the median using as few queries as possible. Give an algorithm that finds the median value using at most O(log n) queries.

```
//ALGO PROJECT 22K-4413 22K-4448 22K-4499
#include <iostream>
#include <functional>
#include <limits>
using namespace std;
int median(int n, function<int(int)> query db1, function<int(int)> query db2) {}
int main() {
  //sorted databases with different data values in each db
  int db1[] = {1, 3, 5, 7, 9, 11, 13, 15,17,19};
  int db2[] = {0, 2, 4, 6, 8, 10, 12, 14,16,18};
  //assuming data bases have same sizes
  int n = sizeof(db1) / sizeof(db1[0]);
  //to access k-th smallest element in each database
  function<int(int)> queryDb1 = [&](int k) -> int { return db1[k]; };
  function<int(int)> queryDb2 = [&](int k) -> int { return db2[k]; };
  cout << "median: " << median(n, queryDb1, queryDb2) << endl;</pre>
  return 0;
}
//using binary search
int median(int n, function<int(int)> query db1, function<int(int)> query db2)
{
  int I index = 0, r index = n;
  //store values of split points
```

```
int db1 leftval, db1 rightval, db2 leftval, db2 rightval;
//find partition between databases
while (I index < r index)
{
  // midpoint in first database
  int midpointDb1 = (l_index + r_index) / 2;
  // corresponding index in second database
  int midpointDb2 = n - midpointDb1;
  // largest value in the left of database 1
  if (midpointDb1 > 0)
    db1 leftval = query db1(midpointDb1 - 1);
  }
  else
  {
    // min value if out of bounds
    db1_leftval = numeric_limits<int>::min();
  }
  // smallest value in the right of database 1
  if (midpointDb1 < n)
    db1_rightval = query_db1(midpointDb1);
  }
  else
    // max value if out of bounds
    db1 rightval = numeric limits<int>::max();
  }
  // largest value in the left of database 2
  if (midpointDb2 > 0)
    db2_leftval = query_db2(midpointDb2 - 1);
  }
  else
    // min value if out of bounds
    db2 leftval = numeric limits<int>::min();
  }
```

```
// minimum value in the right of database 2
    if (midpointDb2 < n)
    {
      db2_rightval = query_db2(midpointDb2);
    }
    else
      // max value if out of bounds
      db2 rightval = numeric limits<int>::max();
    }
    //if partition valid return max of left values else if db1 leftval > db2 rightval adjust search
range to midpint of database 1 else search right
    if (db1 leftval <= db2 rightval && db2 leftval <= db1 rightval)
    {
      return max(db1 leftval, db2 leftval);
    else if (db1 leftval > db2 rightval)
      r index = midpointDb1;
    }
    else
    {
      l index = midpointDb1 + 1;
    }
  }
  // converge binary search to one point
  int finaldb1 leftval, finaldb2 leftval;
  // get left value from database 1
  if (I_index > 0)
  {
    finaldb1_leftval = query_db1(l_index - 1);
  }
  else
    finaldb1_leftval = numeric_limits<int>::min();
```

```
}
// get left value from database 2
if (n - l_index > 0)
{
    finaldb2_leftval = query_db2(n - l_index - 1);
}
else
{
    finaldb2_leftval = numeric_limits<int>::min();
}

// return the larger of the two left values as the median return max(finaldb1_leftval, finaldb2_leftval);
}
```



### Exercise 5.

5. Hidden surface removal is a problem in computer graphics that scarcely needs an introduction: when Woody is standing in front of Buzz, you should be able to see Woody but not Buzz; when Buzz is standing in front of Woody,... well, you get the idea. The magic of hidden surface removal is that you can often compute things faster than your intuition suggests. Here's a clean geometric example to illustrate a basic speed-up that can be achieved. You are given n nonvertical lines in the plane, labeled L1,..., Ln, with the i th line specified by the equation y = aix + bi. We will make the assumption that no three of the lines all meet at a single point. We say line Li is uppermost at a given x-coordinate x0 if its y-coordinate at x0 is greater than the y-coordinates of all the other lines at x0: aix0 + bi > ajx0 + bj for all j = i. We say line Li is visible if there is some x-coordinate at which it is uppermost—intuitively, some portion of it can be seen

```
if you look down from "y = \infty." Give an algorithm that takes n lines as input and in O(n log n)
time returns all of the ones that are visible. Figure 5.10 gives an example.
//ALGO PROJECT 22K-4413 22K-4448 22K-4499
#include <iostream>
#include <algorithm>
//Sort lines by slope
//sweep from left to right
//maintain a set of lines that are currently visible at each x-coordinate. As we process each
line:If a new line intersects the current set of visible lines, we check if it is visible at any
x-coordinate. Maintain the lines in a balanced tree structure that allows efficient insertion,
deletion, and querying of the uppermost line.
using namespace std;
class Line {
public:
  double slope, intercept;
  Line(): slope(0), intercept(0) {}
  //constructor with parameters
  Line(double slope, double intercept): slope(slope), intercept(intercept) {}
  // calculate the y-coordinate of the line at a given x
  double y at(double x) const {
    return slope * x + intercept;
  }
  // compare lines based on their slope
  bool operator<(const Line& other) const {
    return slope < other.slope;
  }
};
Line* merge lines(const Line* left, int left size, const Line* right, int right size, int& size) {}
Line* find visible lines rec(const Line* lines, int start, int end, int& size) {}
Line* find visible lines(Line* lines, int line size, int& visible size) {}
int main() {
```

```
Line lines[] = {
    Line(6, 1), // y = 6x + 1
    Line(8, 5), // y = 8x + 5
    Line(5, -5), // y = 5x - 5
    Line(1, 2) // y = x + 2
  };
  int line size = sizeof(lines) / sizeof(lines[0]);
  int visible_size = 0;
  Line* visible lines = find visible lines(lines, line size, visible size);
  cout << "Visible lines:\n";</pre>
  for (int i = 0; i < visible size; i++) {
    cout << "y = " << visible lines[i].slope << "x + " << visible_lines[i].intercept << "\n";</pre>
  }
  delete[] visible lines;
  return 0;
}
// merge two sets of visible lines, maintaining only the upper envelope
Line* merge lines(const Line* left, int left size, const Line* right, int right size, int& size) {
  Line* res = new Line[left size + right size];
  int i = 0, j = 0, k = 0;
  // compare lines from the left and right halves, keeping the uppermost
  while (i < left size && j < right size) {
    if (left[i].y at(0) > right[j].y at(0)) {
       res[k++] = left[i++];
    } else {
       res[k++] = right[j++];
    }
  // append any remaining lines from either half
  while (i < left size) {
    res[k++] = left[i++];
  }
  while (j < right_size) {
    res[k++] = right[j++];
  }
  size = k;
```

```
return res;
}
// recursive function to find visible lines using divide and conquer
Line* find visible lines rec(const Line* lines, int start, int end, int& size) {
  // base case: if there is one line, it is visible
  if (end - start == 1) {
     size = 1;
     return new Line[1]{lines[start]};
  }
  // split the lines into two halves
  int mid = (start + end) / 2;
  int left size = 0, right size = 0;
  Line* left visible = find visible_lines_rec(lines, start, mid, left_size);
  Line* right visible = find visible lines rec(lines, mid, end, right size);
  // merge the visible lines from the left and right halves
  Line* merged visible lines = merge lines(left visible, left size, right visible, right size, size);
  delete[] left visible;
  delete[] right_visible;
  return merged visible lines;
}
Line* find visible lines(Line* lines, int line size, int& visible size) {// find all visible lines in O(n
log n) time
  // sort lines by their slopes
  sort(lines, lines + line size);
  // use divide and conquer to find visible lines
  return find visible lines rec(lines, 0, line size, visible size);
}
```

# Exercise 6.

6. Consider an n-node complete binary tree T, where n = 2d - 1 for some d. Each node v of T is labeled with a real number xv. You may assume that the real numbers labeling the nodes are all distinct. A node v of T is a local minimum if the label xv is less than the label xw for all nodes w that are joined to v by an edge. You are given such a complete binary tree T, but the labeling is only specified in the following implicit way: for each node v, you can determine the value xv by probing the node v. Show how to find a local minimum of T using only O(log n) probes to the nodes of T.

```
//ALGO PROJECT 22K-4413 22K-4448 22K-4499
#include <iostream>
#include <limits>
using namespace std;

// global array for node values
const int MAX_NODES = 1000; // max nodes
int values[MAX_NODES];

// get value of node v
int probe(int v)
```

```
{
  return values[v];
}
int findlocalMin(int n) {
  // start at root
  int v = 1;
  while (true) {
    // get current node value
    int currentValue = probe(v);
    // track min neighbor
    int minNeighbor = v;
    int minValue = currentValue;
    // check left child
    int left = 2 * v;
    if (left <= n) {
       int leftValue = probe(left);
       if (leftValue < minValue) {</pre>
         minNeighbor = left;
         minValue = leftValue;
       }
    }
    // check right child
    int right = 2 * v + 1;
    if (right <= n) {
       int rightValue = probe(right);
       if (rightValue < minValue) {</pre>
         minNeighbor = right;
         minValue = rightValue;
       }
    }
    // check parent
    int parent = v / 2;
    if (parent >= 1) {
       int parentValue = probe(parent);
       if (parentValue < minValue) {</pre>
         minNeighbor = parent;
         minValue = parentValue;
```

```
}
    }
    // if current node is local min, return it
    if (minNeighbor == v) {
      return v;
    // move to min neighbor
    v = minNeighbor;
}
int main() {
  // example tree in binary format
  values[1] = 20;
       values[2] = 11;
       values[3] = 2;
       values[4] = 8;
  values[5] = 13;
       values[6] = 18;
       values[7] = 40;
  int n = 7; // number of nodes
  cout << "Local minimum found at node: " << findlocalMin(n) << "\nValue at local minimum
node: " << probe(findlocalMin(n)) << endl;</pre>
  return 0;
}
```

# **Question 2:**

# <u>i :</u>

```
#include<iostream>
#include<fstream>
#include<sstream>
#include<ctime>
#include<cmath>
#include<cstdlib>
#include<algorithm>
#include<string>
using namespace std;
class Point{
public:
  int x, y;
};
Point closestPair[2];//for storing closest pair
//sort X coordinate
bool sortX(const Point& p1, const Point& p2){
  return p1.x < p2.x;
}
//sort y coordinate
```

```
bool sortY(const Point& p1, const Point& p2){
  return p1.y < p2.y;
}
//calculate the distance between two points
float distancee(Point p1, Point p2) {
  return sqrt(pow(p1.x - p2.x, 2) + pow(p1.y - p2.y, 2));
}
//brute force to return the smallest distance between two points
float bruteForce(Point P[], int n){
  float minD = INT MAX;
  for(int i = 0; i < n; ++i){
    for(int j = i + 1; j < n; ++j){
       if (distancee(P[i], P[j]) < minD){</pre>
         minD = distancee(P[i], P[j]);
         closestPair[0]=P[i];
         closestPair[1]=P[j];
       }
     }
  }
  return minD;
}
// A utility function to find the minimum of two float values
float min(float x, float y){
  return (x < y)? x : y;
//find the distance between the closest points in a strip
float stripClosest(Point strip[], int size, float d){
  float minD=d; //initialize the minimum distance as d
  sort(strip, strip + size, sortY); //sort by Y-coordinate
  for(int i = 0; i < size; ++i){
     for(int j = i + 1; j < size && (strip[j].y - strip[i].y) < minD; ++j){
       if(distancee(strip[i], strip[j]) < minD){</pre>
         minD = distancee(strip[i], strip[j]);
         closestPair[0]=strip[i];
         closestPair[1]=strip[j];
       }
```

```
}
  }
  return minD;
}
//recursive function to find the smallest distance
float closestDtil(Point P[], int n) {
  if (n \le 3) {//BASE CASE
    return bruteForce(P, n);
  }
  int mid = n/2;
  Point midPoint=P[mid];
//LEFT DISTANCE CALCULATE
  float dl=closestDtil(P, mid);
  float dr=closestDtil(P + mid, n - mid);//RIGHT DISTANCE CALCULATE
  float d=min(dl, dr);
  Point strip[n];
  int j = 0;
  //strip point distance calculate
  for(int i = 0; i < n; i++){
    if(abs(P[i].x - midPoint.x) < d){
       strip[j] = P[i];
      j++;
    }
  return min(d, stripClosest(strip, j, d));
}
//closest point find
float closest(Point P[], int n){
  sort(P, P + n, sortX);
  return closestDtil(P, n);
}
// function to generate filenames
string filename(int k){
  stringstream fileName;
  fileName<<"file"<<k<<".txt";
  return fileName.str();
}
```

```
int main(){
  ofstream fout;
  srand(time(0));
  double x,y;
  for(int k=0; k<10; k++){
  string file =filename(k);
  fout.open(file.c_str());
  if(!fout){
    cout<<"Failed to open file.\n";
    return 1;
  }
  int n=rand()%150+101;
 for(int i=0;i< n;i++){
    float x = rand() \% 1000 + 0.0;
   float y = rand() \% 1000 + 0.0;
   fout << x << " " << y << endl;
  }
  fout.close();}
  //DISPLAY FILES NAMES
  string fileName;
  int count=0;
  while(count!=10){
  cout<<"Enter file name from below listed Files.\n";
  for(int i=0;i<10;i++){
  cout<<i+1<<". file"<<i-".txt"<<endl;
  }
  while(true){
    cin>>fileName;
    ifstream file(fileName.c str());
    if(file){
      file.close();
      break;
    } else {
      cout << "File \"" << fileName << "\" does not exist. Please try again: ";
    }
  }
```

```
ifstream file(fileName.c_str());
  int i=0;
  Point P[1000];
  while (file \Rightarrow P[i].x \Rightarrow P[i].y) {
    i++;
  }
  file.close();
  cout << "The smallest distance is: " << closest(P, i) << endl;</pre>
  cout << "The closest pair of points is: (" << closestPair[0].x << ", " << closestPair[0].y << ") and
("
     << closestPair[1].x << ", " << closestPair[1].y << ")" << endl;
                count++;}
  return 0;
}
<u>li:</u>
//ALGO PROJECT 22K-4413 22K-4448 22K-4499
#include <iostream>
#include <fstream>
#include <ctime>
#include <cstdlib>
#include <sstream>
#include<math.h>
using namespace std;
// function to generate filenames
string filename(int i) {
  stringstream fileName;
  fileName << "iifile" << i + 1 << ".txt";
  return fileName.str();
}
// function to create 20 files with random numbers
```

int createfiles() {

```
srand(time(0));
  int n = rand() \% 100 + 50; // number of random integers between 50 and 150
  for (int i = 0; i < 20; i++) {
    string file = filename(i);
    ofstream out(file, ios::out);
    if (!out) {
      cout << "error opening file " << i + 1 << " for writing." << endl;</pre>
      return 0; // return 0 if file can't be created
    }
    // write n random integers to the file
    for (int j = 0; j < n; j++) {
       out << rand() % 200 + 10 << endl;
    }
    out.close();
  return n; // return the number of integers generated in each file
}
// function to implement karatsuba's algorithm
long long karatsuba(long long x, long long y) {
  if (x < 10 \mid | y < 10) { // base case: single-digit multiplication
    return x * y;
  }
  // calculate the size of the numbers
  int n = max(to string(x).length(), to string(y).length());
  int m = n / 2;
  // split the numbers into two halves
  long long high x = x / (long long)pow(10, m);
  long long low x = x \% (long long)pow(10, m);
  long long high y = y / (long long)pow(10, m);
  long long low y = y \% (long long)pow(10, m);
  // recursively compute the three products
  long long p1 = karatsuba(high x, high y);
  long long p2 = karatsuba(low x, low y);
  long long p3 = karatsuba(high_x + low_x, high_y + low_y);
```

```
// combine the results using karatsuba's formula
  return p1 * pow(10, 2 * m) + (p3 - p1 - p2) * pow(10, m) + p2;
}
int main() {
  string file1, file2;
  int n = createfiles(); // create files and get the number of elements
  if (n == 0) {
     cout << "error: files not created properly." << endl;</pre>
     return 1;
  }
  int x[n] = \{0\}, y[n] = \{0\};
  int count1 = 0, count2 = 0;
  // display file names
  cout << "displaying file names: \n";</pre>
  for (int i = 0; i < 10; i++) {
     cout << filename(i) << " ";</pre>
  }
  // user input for file names
  cout << "\nenter file 1 to choose inputs for x: ";
  cin >> file1;
  cout << "\nenter file 2 to choose inputs for y: ";
  cin >> file2;
  // open the files for reading
  ifstream f1(file1);
  ifstream f2(file2);
  if (!f1) {
     cout << "error opening file 1!" << endl;</pre>
     return 1;
  }
  if (!f2) {
```

```
cout << "error opening file 2!" << endl;
  return 1;
}
string line1, line2;
// read lines from both files and convert them to integers
while (getline(f1, line1) && getline(f2, line2)) {
  stringstream ss1(line1), ss2(line2);
  int num1, num2;
  // convert line 1 to an integer and store it in x
  if (ss1 >> num1) {
    x[count1++] = num1;
  } else {
    cout << "can't convert line to integer: " << line1 << endl;</pre>
  }
  // convert line 2 to an integer and store it in y
  if (ss2 >> num2) {
    y[count2++] = num2;
  } else {
    cout << "can't convert line to integer: " << line2 << endl;
  }
  // print the product of the values from both arrays using karatsuba's algorithm
  if (count1 > 0 \&\& count2 > 0) {
    long long result = karatsuba(x[count1 - 1], y[count2 - 1]);
    cout << result << " ";
    ofstream out("OUTPUTQ2(ii)", ios::out);
               if (!out) {
                  cout << "error opening file for writing." << endl;</pre>
                  return 0; // return 0 if file can't be created
                }
                out << result << " ";
               out.close();
  }
}
```

```
// close the files after reading
f1.close();
f2.close();
return 0;
}
```

# **Question 3:**

<u>i</u>

```
C:\Users\Aafrren Mughal\Desktop\closestPair.exe
Enter file name from below listed Files.
1. file0.txt
2. file1.txt
3. file2.txt
4. file3.txt
5. file4.txt
6. file5.txt
7. file6.txt
8. file7.txt
9. file8.txt
10. file9.txt
file8.txt
The smallest distance is: 5.38516
The closest pair of points is: (992, 584) and (970, 591)
 C:\Users\Aafrren Mughal\Desktop\closestPair.exe
Enter file name from below listed Files.
1. file0.txt
file1.txt
file2.txt
4. file3.txt
file4.txt
file5.txt
7. file6.txt
8. file7.txt
9. file8.txt
10. file9.txt
file9.txt
The smallest distance is: 4
The closest pair of points is: (995, 459) and (997, 480)
```

```
C:\Users\Aafrren Mughal\Desktop\closestPair.exe

Enter file name from below listed Files.
1. file0.txt
2. file1.txt
3. file2.txt
4. file3.txt
5. file4.txt
6. file5.txt
7. file6.txt
8. file7.txt
9. file8.txt
10. file9.txt
file7.txt
The smallest distance is: 1
The closest pair of points is: (992, 489) and (998, 665)
```

```
C:\Users\Aafrren Mughal\Desktop\closestPair.exe

Enter file name from below listed Files.

1. file0.txt

2. file1.txt

3. file2.txt

4. file3.txt

5. file4.txt

6. file5.txt

7. file6.txt

8. file7.txt

9. file8.txt

10. file9.txt

file2.txt

The smallest distance is: 10

The closest pair of points is: (974, 300) and (988, 314)
```

```
Enter file name from below listed Files.

1. file0.txt
2. file1.txt
3. file2.txt
4. file3.txt
5. file4.txt
6. file5.txt
7. file6.txt
8. file7.txt
9. file8.txt
10. file9.txt
file0.txt
The smallest distance is: 4.12311
The closest pair of points is: (990, 642) and (998, 656)
```

```
C:\Users\Aafrren Mughal\Desktop\closestPair.exe

Enter file name from below listed Files.

1. file0.txt

2. file1.txt

3. file2.txt

4. file3.txt

5. file4.txt

5. file5.txt

7. file6.txt

8. file7.txt

9. file8.txt

10. file9.txt

File3.txt

The smallest distance is: 6.32456

The closest pair of points is: (989, 655) and (993, 426)
```

```
C:\Users\Aafrren Mughal\Desktop\closestPair.exe

Enter file name from below listed Files.

1. file0.txt

2. file1.txt

3. file2.txt

4. file3.txt

5. file4.txt

6. file5.txt

7. file6.txt

8. file7.txt

9. file8.txt

10. file9.txt

file6.txt

The smallest distance is: 10.4403

The closest pair of points is: (498, 895) and (501, 905)
```

```
Enter file name from below listed Files.

1. file0.txt

2. file1.txt

3. file2.txt

4. file3.txt

5. file4.txt

6. file5.txt

7. file6.txt

8. file7.txt

9. file8.txt

10. file9.txt

file4.txt

The smallest distance is: 3.60555

The closest pair of points is: (967, 280) and (988, 309)
```

```
C:\Users\Aafrren Mughal\Desktop\closestPair.exe

Enter file name from below listed Files.

1. file0.txt

2. file1.txt

3. file2.txt

4. file3.txt

5. file4.txt

6. file5.txt

7. file6.txt

8. file7.txt

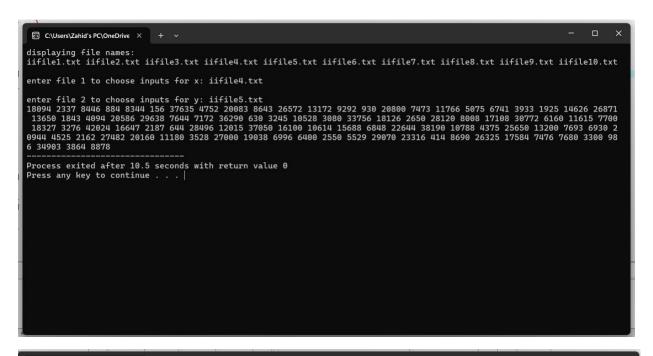
9. file8.txt

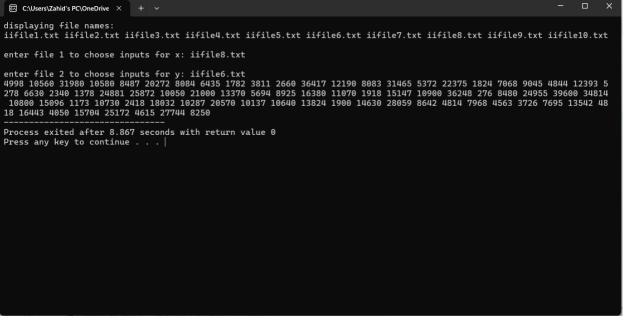
10. file9.txt
file1.txt

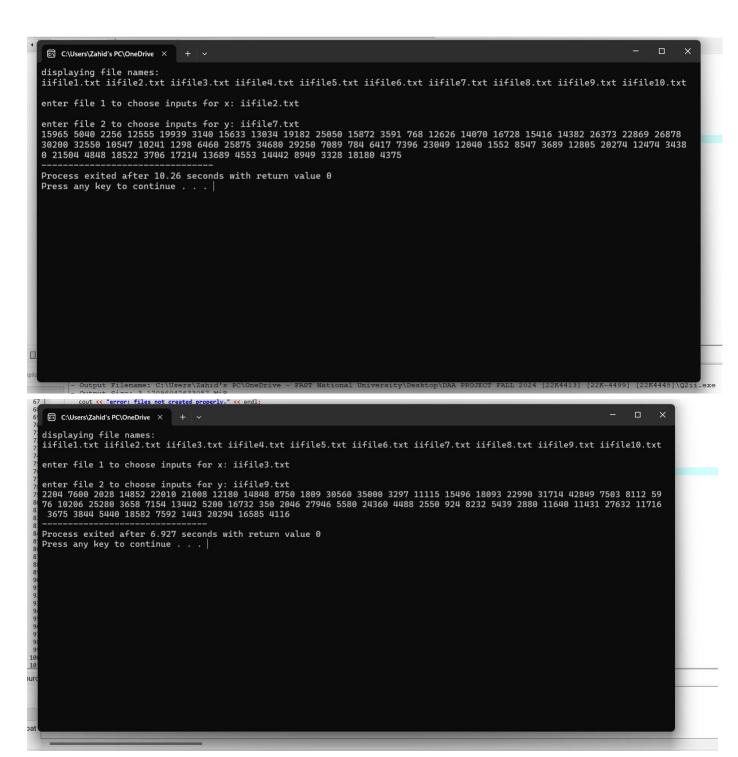
The smallest distance is: 2

The closest pair of points is: (982, 264) and (994, 284)
```

### ii







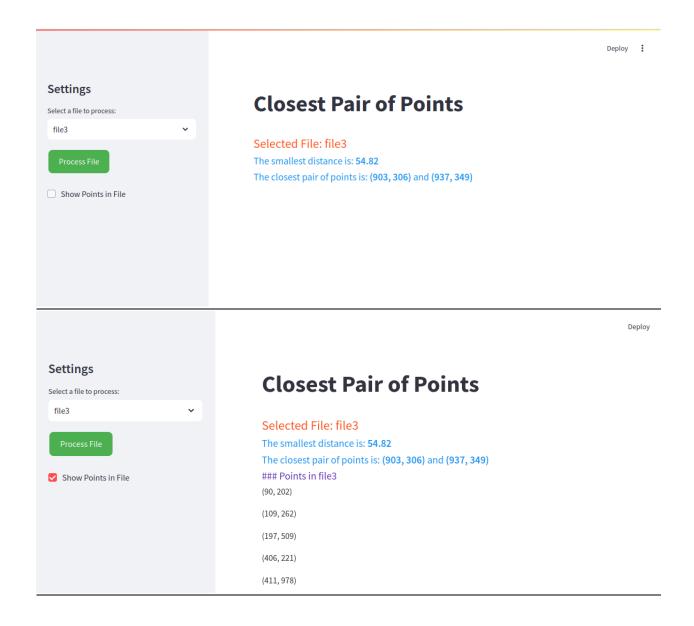
# **Question 4:**

```
<u>i</u>
import streamlit as st
import math
import random
from typing import List
class Point:
  def init (self, x=0, y=0):
     self.x = x
    self.y = y
closest pair = [None, None]
def calculate distance(p1: Point, p2: Point) -> float:
  return math.sqrt((p1.x - p2.x) ** 2 + (p1.y - p2.y) ** 2)
def brute force closest(points: List[Point]) -> float:
  global closest pair
  min distance = float('inf')
  n = len(points)
  for i in range(n):
    for j in range(i + 1, n):
       dist = calculate distance(points[i], points[j])
       if dist < min distance:
         min distance = dist
         closest pair[0], closest pair[1] = points[i], points[j]
  return min distance
def closest_in_strip(strip: List[Point], d: float) -> float:
  global closest pair
  strip.sort(key=lambda p: p.y)
  min distance = d
  for i in range(len(strip)):
    for j in range(i + 1, len(strip)):
       if (strip[j].y - strip[i].y) < min distance:
         dist = calculate distance(strip[i], strip[j])
         if dist < min distance:
            min distance = dist
            closest_pair[0], closest_pair[1] = strip[i], strip[i]
  return min_distance
def closest pair recursive(points: List[Point]) -> float:
  if len(points) <= 3:
```

```
return brute force closest(points)
  mid = len(points) // 2
  mid_point = points[mid]
  dl = closest pair recursive(points[:mid])
  dr = closest pair recursive(points[mid:])
  d = min(dl, dr)
  strip = [p for p in points if abs(p.x - mid point.x) < d]
  return min(d, closest_in_strip(strip, d))
def find_closest(points: List[Point]) -> float:
  points.sort(key=lambda p: p.x)
  return closest pair recursive(points)
st.title("Closest Pair of Points")
st.sidebar.title("Settings")
# Add custom CSS for colors and styling
st.markdown(
  111111
  <style>
  .main-title {
    font-size: 2em;
    color: #4CAF50;
    text-align: center;
    margin-bottom: 20px;
  }
  .file-title {
    font-size: 1.5em;
    color: #FF5722;
  }
  .distance-text {
    font-size: 1.2em;
    color: #2196F3;
  }
  .points-text {
    font-size: 1.2em;
    color: #673AB7;
  }
  .custom-button {
    background-color: #4CAF50; /* Green */
    border: none;
    color: white;
    padding: 10px 20px;
    text-align: center;
```

```
text-decoration: none;
    display: inline-block;
    font-size: 16px;
    margin: 4px 2px;
    cursor: pointer;
    border-radius: 8px;
  }
  .custom-checkbox {
    font-size: 1.2em;
    color: #FF9800;
  }
  </style>
  unsafe allow html=True,
# Generate random files
if 'generated files' not in st.session state:
  st.session state.generated files = []
  for i in range(10):
    num points = random.randint(10, 50)
    points = [Point(random.randint(0, 1000), random.randint(0, 1000)) for in range(num points)]
    st.session state.generated files.append(points)
file index = st.sidebar.selectbox(
  "Select a file to process:",
  [f"file{i}" for i in range(len(st.session state.generated files))]
)
# Add a custom button for file processing
if st.sidebar.markdown('<button class="custom-button">Process File</button>', unsafe allow html=True):
  selected points = st.session state.generated files[int(file index[-1])]
  smallest distance = find closest(selected points)
  p1, p2 = closest pair
  st.markdown(f'<div class="file-title">Selected File: {file_index}</div>', unsafe_allow_html=True)
  st.markdown(f'<div class="distance-text">The smallest distance is: <b>{smallest distance:.2f}</b></div>',
unsafe allow html=True)
  st.markdown(
    f'<div class="distance-text">The closest pair of points is: <b>({p1.x}, {p1.y})</b> and <b>({p2.x},
{p2.y})</b></div>',
    unsafe allow html=True,
  )
# Checkbox to show points
if st.sidebar.checkbox("Show Points in File"):
```

st.markdown(f'<div class="points-text">### Points in {file\_index}</div>', unsafe\_allow\_html=True) for point in st.session\_state.generated\_files[int(file\_index[-1])]: st.write(f"({point.x}, {point.y})")



# <u>li</u>

```
import os
import random
import math
import streamlit as st
# Custom CSS for button styling
st.markdown(
  <style>
  .custom-button {
    background-color: #4CAF50; /* Green */
    border: none;
    color: white;
    padding: 10px 20px;
    text-align: center;
    text-decoration: none;
    display: inline-block;
    font-size: 16px;
    margin: 4px 2px;
    cursor: pointer;
    border-radius: 8px;
  }
  .custom-button-red{
    background-color: #f44336;
    border: none;
    color: white;
    padding: 10px 20px;
    text-align: center;
    text-decoration: none;
    display: inline-block;
    font-size: 16px;
    margin: 4px 2px;
    cursor: pointer;
    border-radius: 8px;
  }
  </style>
  unsafe_allow_html=True
def gen_file_name(idx):
  return f"file {idx + 1}.txt"
def create files():
  random.seed()
```

```
n nums = random.randint(50, 150)
  for i in range(20):
    fname = gen file name(i)
    with open(fname, "w") as f:
      for in range(n nums):
         f.write(f"{random.randint(10, 209)}\n")
  return n nums
def karatsuba(x, y):
  if x < 10 or y < 10: # Base case
    return x * y
  n = max(len(str(x)), len(str(y)))
  half = n // 2
  high1, low1 = divmod(x, 10 ** half)
  high2, low2 = divmod(y, 10 ** half)
  z1 = karatsuba(high1, high2)
  z2 = karatsuba(low1, low2)
  z3 = karatsuba(high1 + low1, high2 + low2)
  return z1 * (10 ** (2 * half)) + (z3 - z1 - z2) * (10 ** half) + z2
st.title("Karatsuba Multiplication")
st.sidebar.title("File Operations")
# Add colored button for generating files
if st.sidebar.markdown('<button class="custom-button">Generate Random Files</button>',
unsafe allow html=True):
  n nums = create files()
  st.sidebar.success(f"20 files created with {n nums} random numbers each.")
file list = [gen file name(i) for i in range(20) if os.path.exists(gen_file_name(i))]
if file list:
  st.sidebar.write("Available Files:")
  for f in file list:
    st.sidebar.write(f)
file1 = st.sidebar.selectbox("Select File 1 for X values", file list)
file2 = st.sidebar.selectbox("Select File 2 for Y values", file list)
# Add colored button for processing files
if st.sidebar.markdown('<button class="custom-button-red">Process Selected Files</button>',
unsafe allow html=True):
  if not file1 or not file2:
    st.error("Please select two valid files.")
  elif file1 == file2:
```

```
st.error("Please select two different files.")
else:
  x vals = []
  y_vals = []
  results = []
  try:
    with open(file1, "r") as f1, open(file2, "r") as f2:
       x lines = f1.readlines()
      y_lines = f2.readlines()
       for x line, y line in zip(x lines, y lines):
         x = int(x_line.strip())
         y = int(y line.strip())
         x vals.append(x)
         y_vals.append(y)
         prod = karatsuba(x, y)
         results.append(prod)
    with open("output.txt", "w") as out:
       for res in results:
         out.write(f"{res}\n")
    st.success("Processing complete. Results saved in 'output.txt'.")
    st.write("### Results:")
    for r in results:
       st.write(r)
  except ValueError as e:
    st.error(f"Error processing files: {e}")
```

