# Transformation In 3-Dimension

**Course Title: Computer Graphics** 

Course Code: CSE — 413

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## 3D Transformation in Computer Graphics-

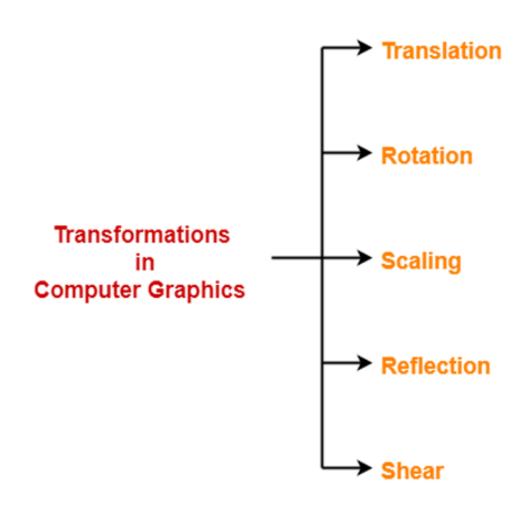
In Computer graphics,

Transformation is a process of modifying and re-positioning the existing graphics.

- 3D Transformations take place in a three dimensional plane.
- 3D Transformations are important and a bit more complex than 2D Transformations.
- Transformations are helpful in changing the position, size, orientation, shape etc of the object.

#### **Transformation Techniques-**

In computer graphics, various transformation techniques are-



#### 3D Translation in Computer Graphics-

In Computer graphics,

3D Translation is a process of moving an object from one position to another in a three dimensional plane.

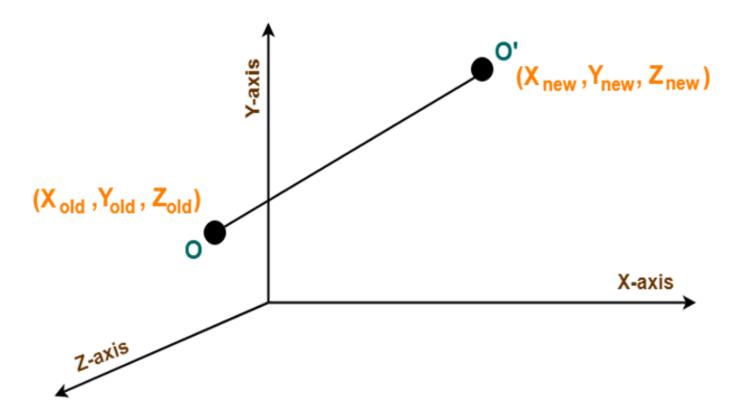
Consider a point object O has to be moved from one position to another in a 3D plane.

#### Let-

- Initial coordinates of the object O = (X<sub>old</sub>, Y<sub>old</sub>, Z<sub>old</sub>)
- New coordinates of the object O after translation = (X<sub>new</sub>, Y<sub>new</sub>, Z<sub>old</sub>)
- Translation vector or Shift vector = (T<sub>x</sub>, T<sub>y</sub>, T<sub>z</sub>)

Given a Translation vector  $(T_x, T_y, T_z)$ -

- T<sub>x</sub> defines the distance the X<sub>old</sub> coordinate has to be moved.
- T<sub>v</sub> defines the distance the Y<sub>old</sub> coordinate has to be moved.
- T<sub>z</sub> defines the distance the Z<sub>old</sub> coordinate has to be moved.

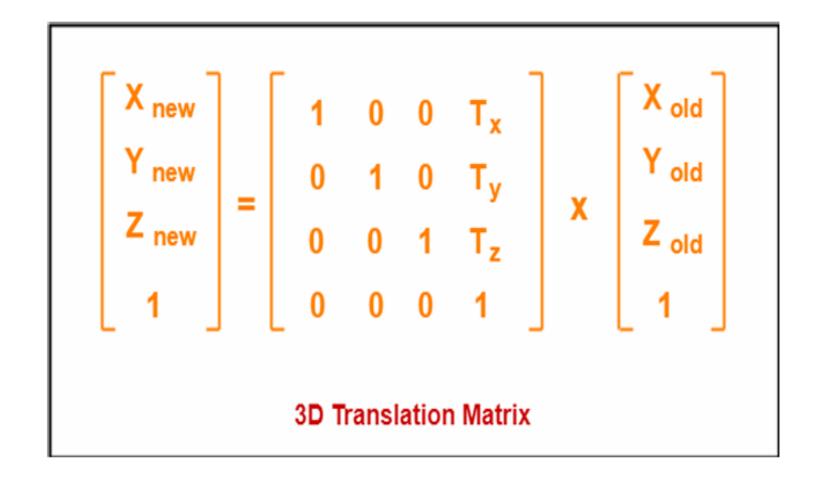


3D Translation in Computer Graphics

This translation is achieved by adding the translation coordinates to the old coordinates of the object as-

- $X_{new} = X_{old} + T_x$  (This denotes translation towards X axis)
- $Y_{new} = Y_{old} + T_y$  (This denotes translation towards Y axis)
- $Z_{new} = Z_{old} + T_z$  (This denotes translation towards Z axis)

In Matrix form, the above translation equations may be represented as-



# PRACTICE PROBLEM BASED ON 3D TRANSLATION IN COMPUTER GRAPHICS-

#### Problem-

Given a 3D object with coordinate points A(0, 3, 1), B(3, 3, 2), C(3, 0, 0), D(0, 0, 0). Apply the translation with the distance 1 towards X axis, 1 towards Y axis and 2 towards Z axis and obtain the new coordinates of the object.

#### Solution-

Given-

- Old coordinates of the object = A (0, 3, 1), B(3, 3, 2), C(3, 0, 0), D(0, 0, 0)
- Translation vector =  $(T_x, T_y, T_z) = (1, 1, 2)$

#### For Coordinates A(0, 3, 1)

Let the new coordinates of A = (X<sub>new</sub>, Y<sub>new</sub>, Z<sub>new</sub>).

Applying the translation equations, we have-

• 
$$X_{new} = X_{old} + T_x = 0 + 1 = 1$$

• 
$$Y_{new} = Y_{old} + T_y = 3 + 1 = 4$$

• 
$$Z_{new} = Z_{old} + T_z = 1 + 2 = 3$$

Thus, New coordinates of A = (1, 4, 3).

#### For Coordinates B(3, 3, 2)

Let the new coordinates of B =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the translation equations, we have-

• 
$$X_{new} = X_{old} + T_x = 3 + 1 = 4$$

Thus, New coordinates of B = (4, 4, 4).

#### For Coordinates C(3, 0, 0)

Let the new coordinates of  $C = (X_{new}, Y_{new}, Z_{new})$ .

Applying the translation equations, we have-

#### For Coordinates D(0, 0, 0)

Let the new coordinates of D =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the translation equations, we have-

• 
$$X_{new} = X_{old} + T_x = 0 + 1 = 1$$

• 
$$Y_{new} = Y_{old} + T_y = 0 + 1 = 1$$

• 
$$Z_{new} = Z_{old} + T_z = 0 + 2 = 2$$

Thus, New coordinates of D = (1, 1, 2).

Thus, New coordinates of the object = A(1, 4, 3), B(4, 4, 4), C(4, 1, 2), D(1, 1, 2).

Thus, New coordinates of C = (4, 1, 2).

To gain better understanding about 3D Translation in Computer Graphics,

#### 3D Rotation in Computer Graphics-

In Computer graphics,

3D Rotation is a process of rotating an object with respect to an angle in a three dimensional plane.

Consider a point object O has to be rotated from one angle to another in a 3D plane.

#### Let-

- Initial coordinates of the object O = (X<sub>old</sub>, Y<sub>old</sub>, Z<sub>old</sub>)
- Initial angle of the object O with respect to origin = Φ
- Rotation angle = θ
- New coordinates of the object O after rotation = (X<sub>new</sub>, Y<sub>new</sub>, Z<sub>new</sub>)

In 3 dimensions, there are 3 possible types of rotation-

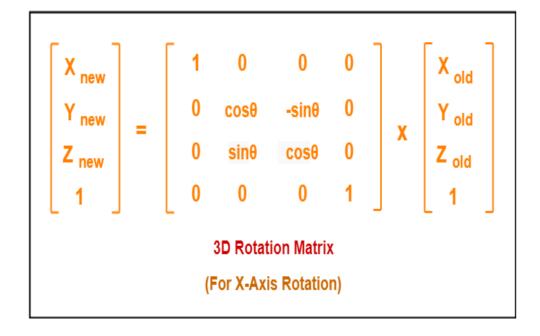
- · X-axis Rotation
- Y-axis Rotation
- Z-axis Rotation

#### For X-Axis Rotation-

This rotation is achieved by using the following rotation equations-

- X<sub>new</sub> = X<sub>old</sub>
- $Y_{new} = Y_{old} x \cos\theta Z_{old} x \sin\theta$
- Z<sub>new</sub> = Y<sub>old</sub> x sinθ + Z<sub>old</sub> x cosθ

In Matrix form, the above rotation equations may be represented as-



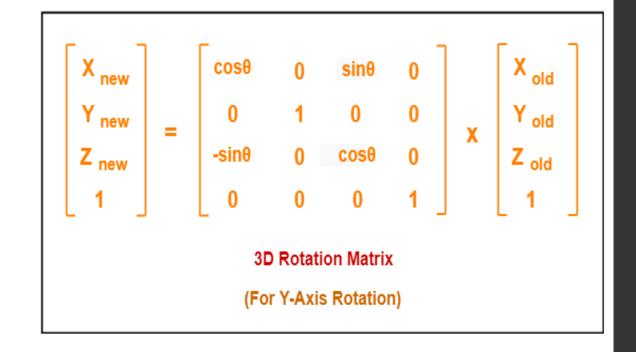
#### For Y-Axis Rotation-

This rotation is achieved by using the following rotation equations-

• 
$$X_{new} = Z_{old} x \sin\theta + X_{old} x \cos\theta$$

- Y<sub>new</sub> = Y<sub>old</sub>
- Z<sub>new</sub> = Y<sub>old</sub> x cosθ X<sub>old</sub> x sinθ

In Matrix form, the above rotation equations may be represented as-

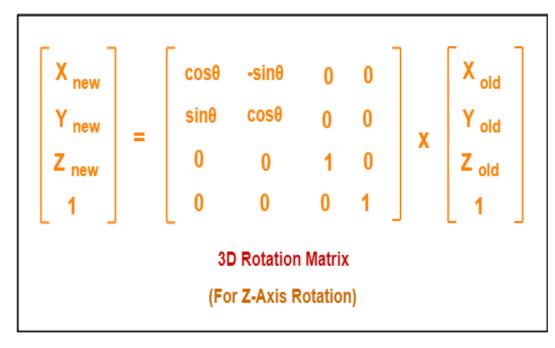


#### For Z-Axis Rotation-

This rotation is achieved by using the following rotation equations-

- X<sub>new</sub> = X<sub>old</sub> x cosθ Y<sub>old</sub> x sinθ
- $Y_{new} = X_{old} x \sin\theta + Y_{old} x \cos\theta$
- Z<sub>new</sub> = Z<sub>old</sub>

In Matrix form, the above rotation equations may be represented as-



# PRACTICE PROBLEMS BASED ON 3D ROTATION IN COMPUTER GRAPHICS-

#### Problem-01:

Given a homogeneous point (1, 2, 3). Apply rotation 90 degree towards X, Y and Z axis and find out the new coordinate points.

#### Solution-

Given-

- Old coordinates = (X<sub>old</sub>, Y<sub>old</sub>, Z<sub>old</sub>) = (1, 2, 3)
- Rotation angle = θ = 90°

#### For X-Axis Rotation-

Let the new coordinates after rotation =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the rotation equations, we have-

- X<sub>new</sub> = X<sub>old</sub> = 1
- $Y_{new} = Y_{old} x \cos\theta Z_{old} x \sin\theta = 2 x \cos 90^{\circ} 3 x \sin 90^{\circ} = 2 x 0 3 x 1 = -3$
- $Z_{new} = Y_{old} x \sin\theta + Z_{old} x \cos\theta = 2 x \sin90^{\circ} + 3 x \cos90^{\circ} = 2 x 1 + 3 x 0 = 2$

Thus, New coordinates after rotation = (1, -3, 2).

#### For Y-Axis Rotation-

Let the new coordinates after rotation =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the rotation equations, we have-

- $X_{new} = Z_{old} x \sin\theta + X_{old} x \cos\theta = 3 x \sin\theta0^{\circ} + 1 x \cos\theta0^{\circ} = 3 x 1 + 1 x 0 = 3$
- Y<sub>new</sub> = Y<sub>old</sub> = 2
- $Z_{new} = Y_{old} \times \cos\theta X_{old} \times \sin\theta = 2 \times \cos90^{\circ} 1 \times \sin90^{\circ} = 2 \times 0 1 \times 1 = -1$

#### For Z-Axis Rotation-

Let the new coordinates after rotation =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the rotation equations, we have-

- $X_{new} = X_{old} x \cos\theta Y_{old} x \sin\theta = 1 x \cos 90^{\circ} 2 x \sin 90^{\circ} = 1 x 0 2 x 1 = -2$
- $Y_{new} = X_{old} x \sin\theta + Y_{old} x \cos\theta = 1 x \sin90^{\circ} + 2 x \cos90^{\circ} = 1 x 1 + 2 x 0 = 1$
- Z<sub>new</sub> = Z<sub>old</sub> = 3

Thus, New coordinates after rotation = (-2, 1, 3).

Thus, New coordinates after rotation = (3, 2, -1).

#### 3D Scaling in Computer Graphics-

In computer graphics, scaling is a process of modifying or altering the size of objects.

- · Scaling may be used to increase or reduce the size of object.
- Scaling subjects the coordinate points of the original object to change.
- Scaling factor determines whether the object size is to be increased or reduced.
- If scaling factor > 1, then the object size is increased.
- . If scaling factor < 1, then the object size is reduced.

Consider a point object O has to be scaled in a 3D plane.

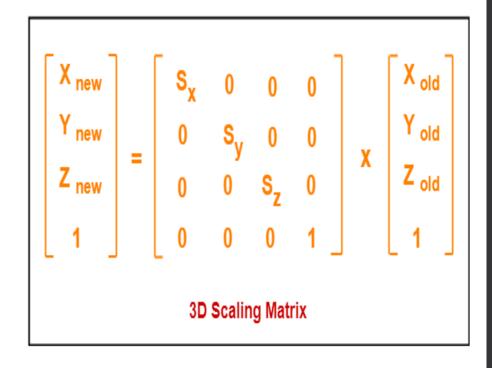
#### Let-

- Initial coordinates of the object O = (X<sub>old</sub>, Y<sub>old</sub>, Z<sub>old</sub>)
- Scaling factor for X-axis = S<sub>x</sub>
- Scaling factor for Y-axis = S<sub>V</sub>
- Scaling factor for Z-axis = S<sub>z</sub>
- New coordinates of the object O after scaling = (X<sub>new</sub>, Y<sub>new</sub>, Z<sub>new</sub>)

This scaling is achieved by using the following scaling equations-

• 
$$Z_{new} = Z_{old} \times S_z$$

In Matrix form, the above scaling equations may be represented as-



### PRACTICE PROBLEMS BASED ON 3D SCALING IN COMPUTER GRAPHICS-

#### Problem-01:

Given a 3D object with coordinate points A(0, 3, 3), B(3, 3, 6), C(3, 0, 1), D(0, 0, 0). Apply the scaling parameter 2 towards X axis, 3 towards Y axis and 3 towards Z axis and obtain the new coordinates of the object.

#### Solution-

Given-

- Old coordinates of the object = A (0, 3, 3), B(3, 3, 6), C(3, 0, 1), D(0, 0, 0)
- Scaling factor along X axis = 2
- Scaling factor along Y axis = 3
- Scaling factor along Z axis = 3

#### For Coordinates A(0, 3, 3)

Let the new coordinates of A after scaling =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the scaling equations, we have-

• 
$$X_{new} = X_{old} \times S_x = 0 \times 2 = 0$$

- Y<sub>new</sub> = Y<sub>old</sub> x S<sub>v</sub> = 3 x 3 = 9
- Z<sub>new</sub> = Z<sub>old</sub> x S<sub>z</sub> = 3 x 3 = 9

Thus, New coordinates of corner A after scaling = (0, 9, 9).

#### For Coordinates B(3, 3, 6)

Let the new coordinates of B after scaling =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the scaling equations, we have-

Thus, New coordinates of corner B after scaling = (6, 9, 18).

#### For Coordinates C(3, 0, 1)

Let the new coordinates of C after scaling =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the scaling equations, we have-

Thus, New coordinates of corner C after scaling = (6, 0, 3).

#### For Coordinates D(0, 0, 0)

Let the new coordinates of D after scaling =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the scaling equations, we have-

• 
$$X_{new} = X_{old} \times S_x = 0 \times 2 = 0$$

• 
$$Z_{new} = Z_{old} \times S_z = 0 \times 3 = 0$$

Thus, New coordinates of corner D after scaling = (0, 0, 0).

#### 3D Reflection in Computer Graphics-

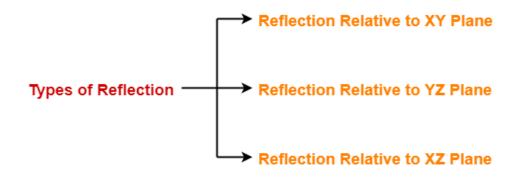
- . Reflection is a kind of rotation where the angle of rotation is 180 degree.
- · The reflected object is always formed on the other side of mirror.
- . The size of reflected object is same as the size of original object.

Consider a point object O has to be reflected in a 3D plane.

#### Let-

- Initial coordinates of the object O = (X<sub>old</sub>, Y<sub>old</sub>, Z<sub>old</sub>)
- New coordinates of the reflected object O after reflection =  $(X_{new}, Y_{new}, Z_{new})$

In 3 dimensions, there are 3 possible types of reflection-



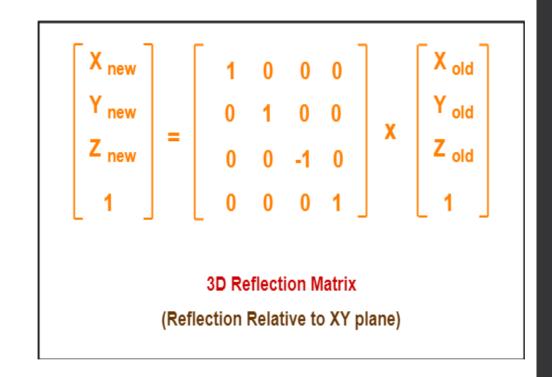
- · Reflection relative to XY plane
- · Reflection relative to YZ plane
- · Reflection relative to XZ plane

#### Reflection Relative to XY Plane:

This reflection is achieved by using the following reflection equations-

- X<sub>new</sub> = X<sub>old</sub>
- Y<sub>new</sub> = Y<sub>old</sub>
- $Z_{new} = -Z_{old}$

In Matrix form, the above reflection equations may be represented as-



#### Reflection Relative to YZ Plane:

This reflection is achieved by using the following reflection equations-

- X<sub>new</sub> = -X<sub>old</sub>
- Y<sub>new</sub> = Y<sub>old</sub>
- Z<sub>new</sub> = Z<sub>old</sub>

In Matrix form, the above reflection equations may be represented as-

$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \\ 1 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} X \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$

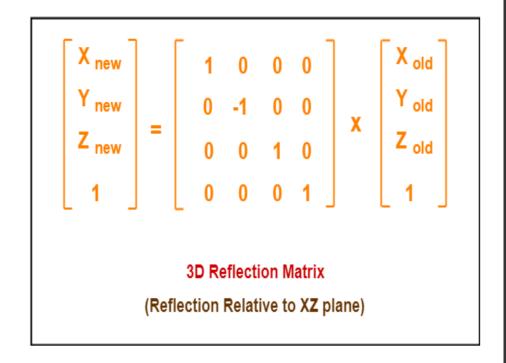
$$3D \text{ Reflection Matrix}$$
(Reflection Relative to YZ plane)

#### Reflection Relative to XZ Plane:

This reflection is achieved by using the following reflection equations-

- X<sub>new</sub> = X<sub>old</sub>
- Y<sub>new</sub> = -Y<sub>old</sub>
- Z<sub>new</sub> = Z<sub>old</sub>

In Matrix form, the above reflection equations may be represented as-



# PRACTICE PROBLEMS BASED ON 3D REFLECTION IN COMPUTER GRAPHICS-

For Coordinates B(6, 4, 2)

Problem-01:

Let the new coordinates of corner B after reflection =  $(X_{new}, Y_{new}, Z_{new})$ .

Thus, New coordinates of corner B after reflection = (6, 4, -2).

Let the new coordinates of corner C after reflection =  $(X_{new}, Y_{new}, Z_{new})$ .

Given a 3D triangle with coordinate points A(3, 4, 1), B(6, 4, 2), C(5, 6, 3). Apply the reflection on the XY plane and find out the new coordinates of the object.

Applying the reflection equations, we have-

- X<sub>new</sub> = X<sub>old</sub> = 6
- Y<sub>new</sub> = Y<sub>old</sub> = 4
- $Z_{new} = -Z_{old} = -2$

Solution-

Given-

- Old corner coordinates of the triangle = A (3, 4, 1), B(6, 4, 2), C(5, 6, 3)
- Reflection has to be taken on the XY plane

For Coordinates C(5, 6, 3)

For Coordinates A(3, 4, 1)

Let the new coordinates of corner A after reflection = (X<sub>new</sub>, Y<sub>new</sub>, Z<sub>new</sub>).

Applying the reflection equations, we have-

- X<sub>new</sub> = X<sub>old</sub> = 3
- Y<sub>new</sub> = Y<sub>old</sub> = 4
- $Z_{new} = -Z_{old} = -1$

Applying the reflection equations, we have-

- X<sub>new</sub> = X<sub>old</sub> = 5
- Y<sub>new</sub> = Y<sub>old</sub> = 6
- $Z_{new} = -Z_{old} = -3$

Thus, New coordinates of corner C after reflection = (5, 6, -3).

Thus, New coordinates of the triangle after reflection = A (3, 4, -1), B(6, 4, -2), C(5, 6, -3).

Thus, New coordinates of corner A after reflection = (3, 4, -1).

#### Problem-02:

Given a 3D triangle with coordinate points A(3, 4, 1), B(6, 4, 2), C(5, 6, 3). Apply the reflection on the XZ plane and find out the new coordinates of the object.

#### Solution-

Given-

- Old corner coordinates of the triangle = A (3, 4, 1), B(6, 4, 2), C(5, 6, 3)
- . Reflection has to be taken on the XZ plane

#### For Coordinates A(3, 4, 1)

Let the new coordinates of corner A after reflection =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the reflection equations, we have-

- X<sub>new</sub> = X<sub>old</sub> = 3
- Y<sub>new</sub> = -Y<sub>old</sub> = -4
- Z<sub>new</sub> = Z<sub>old</sub> = 1

Thus, New coordinates of corner A after reflection = (3, -4, 1).

#### For Coordinates B(6, 4, 2)

Let the new coordinates of corner B after reflection =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the reflection equations, we have-

- X<sub>new</sub> = X<sub>old</sub> = 6
- $Y_{new} = -Y_{old} = -4$
- Z<sub>new</sub> = Z<sub>old</sub> = 2

Thus, New coordinates of corner B after reflection = (6, -4, 2).

#### For Coordinates C(5, 6, 3)

Let the new coordinates of corner C after reflection =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the reflection equations, we have-

- X<sub>new</sub> = X<sub>old</sub> = 5
- Y<sub>new</sub> = -Y<sub>old</sub> = -6
- Z<sub>new</sub> = Z<sub>old</sub> = 3

Thus, New coordinates of corner C after reflection = (5, -6, 3).

Thus, New coordinates of the triangle after reflection = A (3, -4, 1), B(6, -4, 2), C(5, -6, 3).

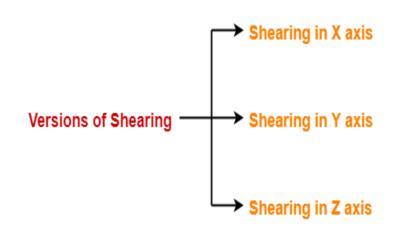
#### 3D Shearing in Computer Graphics-

In Computer graphics,

3D Shearing is an ideal technique to change the shape of an existing object in a three dimensional plane

In a three dimensional plane, the object size can be changed along X direction, Y direction as well as Z direction.

So, there are three versions of shearing-



- 1. Shearing in X direction
- 2. Shearing in Y direction
- 3. Shearing in Z direction

Consider a point object O has to be sheared in a 3D plane.

Let-

- Initial coordinates of the object O = (X<sub>old</sub>, Y<sub>old</sub>, Z<sub>old</sub>)
- Shearing parameter towards X direction = Sh<sub>X</sub>
- . Shearing parameter towards Y direction = Shv
- Shearing parameter towards Z direction = Sh<sub>Z</sub>
- New coordinates of the object O after shearing = (X<sub>new</sub>, Y<sub>new</sub>, Z<sub>new</sub>)

#### Shearing in X Axis-

Shearing in X axis is achieved by using the following shearing equations-

- X<sub>new</sub> = X<sub>old</sub>
- Y<sub>new</sub> = Y<sub>old</sub> + Sh<sub>v</sub> x X<sub>old</sub>
- Z<sub>new</sub> = Z<sub>old</sub> + Sh<sub>z</sub> x X<sub>old</sub>

In Matrix form, the above shearing equations may be represented as-

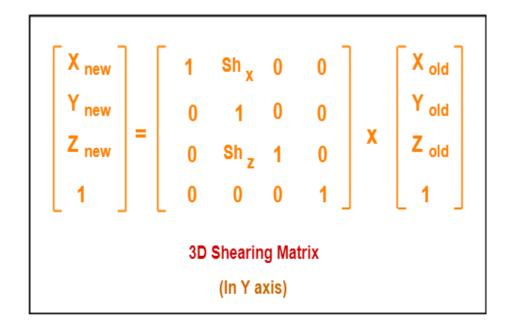
$$\begin{bmatrix} X_{new} \\ Y_{new} \\ Z_{new} \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ Sh_y & 1 & 0 & 0 \\ Sh_z & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} X \begin{bmatrix} X_{old} \\ Y_{old} \\ Z_{old} \\ 1 \end{bmatrix}$$
3D Shearing Matrix
(In X axis)

#### **Shearing in Y Axis-**

Shearing in Y axis is achieved by using the following shearing equations-

- X<sub>new</sub> = X<sub>old</sub> + Sh<sub>x</sub> x Y<sub>old</sub>
- Y<sub>new</sub> = Y<sub>old</sub>
- Z<sub>new</sub> = Z<sub>old</sub> + Sh<sub>z</sub> x Y<sub>old</sub>

In Matrix form, the above shearing equations may be represented as-

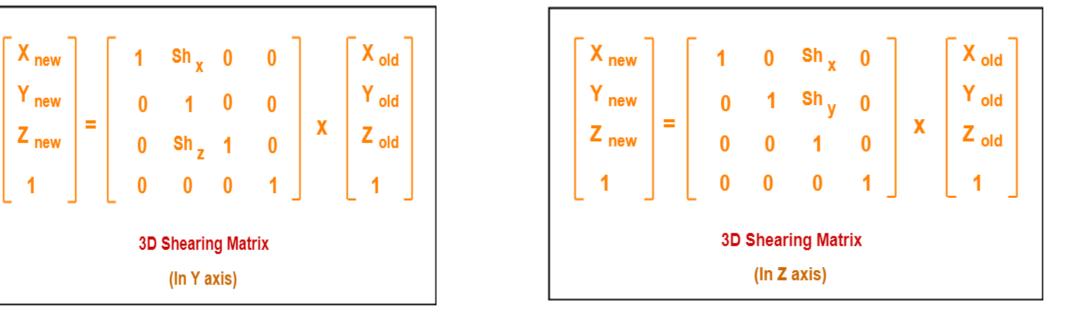


#### **Shearing in Z Axis-**

Shearing in Z axis is achieved by using the following shearing equations-

- X<sub>new</sub> = X<sub>old</sub> + Sh<sub>x</sub> x Z<sub>old</sub>
- Y<sub>new</sub> = Y<sub>old</sub> + Sh<sub>v</sub> x Z<sub>old</sub>
- Z<sub>new</sub> = Z<sub>old</sub>

In Matrix form, the above shearing equations may be represented as-



# PRACTICE PROBLEMS BASED ON 3D SHEARING IN COMPUTER GRAPHICS-

#### Problem-01:

Given a 3D triangle with points (0, 0, 0), (1, 1, 2) and (1, 1, 3). Apply shear parameter 2 on X axis, 2 on Y axis and 3 on Z axis and find out the new coordinates of the object.

Applying the shearing equations, we have-

• 
$$Y_{new} = Y_{old} + Sh_y \times X_{old} = 0 + 2 \times 0 = 0$$

• 
$$Z_{new} = Z_{old} + Sh_z \times X_{old} = 0 + 3 \times 0 = 0$$

Thus, New coordinates of corner A after shearing = (0, 0, 0).

#### Solution-

#### Given-

- Old corner coordinates of the triangle = A (0, 0, 0), B(1, 1, 2), C(1, 1, 3)
- Shearing parameter towards X direction (Sh<sub>x</sub>) = 2
- Shearing parameter towards Y direction (Sh<sub>v</sub>) = 2
- Shearing parameter towards Y direction (Sh<sub>7</sub>) = 3

#### **Shearing in X Axis-**

#### For Coordinates A(0, 0, 0)

#### For Coordinates B(1, 1, 2)

Let the new coordinates of corner B after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the shearing equations, we have-

• 
$$Z_{new} = Z_{old} + Sh_z \times X_{old} = 2 + 3 \times 1 = 5$$

Thus, New coordinates of corner B after shearing = (1, 3, 5).

Let the new coordinates of corner A after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

#### For Coordinates C(1, 1, 3)

Let the new coordinates of corner C after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the shearing equations, we have-

• 
$$Z_{new} = Z_{old} + Sh_z \times X_{old} = 3 + 3 \times 1 = 6$$

Thus, New coordinates of corner C after shearing = (1, 3, 6).

Thus, New coordinates of the triangle after shearing in X axis = A (0, 0, 0), B(1, 3, 5), C(1, 3, 6).

#### **Shearing in Y Axis-**

#### For Coordinates A(0, 0, 0)

Let the new coordinates of corner A after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the shearing equations, we have-

• 
$$X_{new} = X_{old} + Sh_x x Y_{old} = 0 + 2 x 0 = 0$$

• 
$$Z_{new} = Z_{old} + Sh_z \times Y_{old} = 0 + 3 \times 0 = 0$$

Thus, New coordinates of corner A after shearing = (0, 0, 0).

#### For Coordinates B(1, 1, 2)

Let the new coordinates of corner B after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the shearing equations, we have-

• 
$$Z_{new} = Z_{old} + Sh_z \times Y_{old} = 2 + 3 \times 1 = 5$$

Thus, New coordinates of corner B after shearing = (3, 1, 5).

#### For Coordinates C(1, 1, 3)

Let the new coordinates of corner C after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the shearing equations, we have-

• 
$$Z_{new} = Z_{old} + Sh_7 \times Y_{old} = 3 + 3 \times 1 = 6$$

Thus, New coordinates of corner C after shearing = (3, 1, 6).

Thus, New coordinates of the triangle after shearing in Y axis = A (0, 0, 0), B(3, 1, 5), C(3, 1, 6).

#### **Shearing in Z Axis-**

#### For Coordinates A(0, 0, 0)

Let the new coordinates of corner A after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the shearing equations, we have-

• 
$$X_{new} = X_{old} + Sh_x \times Z_{old} = 0 + 2 \times 0 = 0$$

Thus, New coordinates of corner A after shearing = (0, 0, 0).

#### For Coordinates B(1, 1, 2)

Let the new coordinates of corner B after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the shearing equations, we have-

Thus, New coordinates of corner B after shearing = (5, 5, 2).

#### For Coordinates C(1, 1, 3)

Let the new coordinates of corner C after shearing =  $(X_{new}, Y_{new}, Z_{new})$ .

Applying the shearing equations, we have-

Thus, New coordinates of corner C after shearing = (7, 7, 3).

Thus, New coordinates of the triangle after shearing in Z axis = A (0, 0, 0), B(5, 5, 2), C(7, 7, 3).