

Mid-term Exam Solutions

Student Name:

Student ID:

Exam date: 2015-07-10, 6-8pm

Close Books & Notes, calculators only

Problem 1) Python programming (20 pts.)

a) What is the output of the following Python code?

```
from numpy import array
a = array([0,1,2,3,4,5,6])
print a[1:-1:2]
```

b) What is the output of the following Python code?

```
foo = {1:'1', 2:'2', 3:'3'}
del foo[1]
foo[1] = '10'
del foo[2]
print len(foo)
```

c) What is the output of the following Python code?

```
list = [1, 2, 3, 4, 5]
list1 = [2, 4, 6, 8]
def doStuff(list, counter=0):
    for i in list:
        counter += i
    counter /= (len(list)+1)
    return counter
counter = 5
counter = doStuff(list1+list)
print counter
```

d) What is the output of the following Python code?

```
names1 = ['Adam', 'Bravo', 'Charlie', 'Delta']
names2 = names1
names3 = names1[:]

names2[0] = 'Alice'
names3[1] = 'Bob'

sum = 0
for ls in (names1, names2, names3):
    if 'Charlie' in ls:
        sum += 5
    if 'Bob' in ls:
        sum += 10

print sum
```

Answers:

- a) [1, 3, 5]
- b) 2
- c) 3
- d) 20

Problem 2) Bayes Rule (10 pts.)

You are given 2 boxes, one Red and one Green.

- The Red box contains 6 Orange, 3 Apples and 6 Cherries.
- The Green box contains 4 Orange, 7 Apples and 4 Cherries.

Assume a prior distribution of [Red Green] = [0.4 0.6] for the box. If we have drawn a cherry, what are probabilities that it comes from a Red or Green box, respectively?

	Orange	Apple	Cherry	Sum
Red	6	3	6	15
Green	4	7	4	15
Sum	10	10	10	

Answers:

$$P(\text{Cherry}) = P(\text{Cherry} \mid \text{Red}) * P(\text{Red}) + P(\text{Cherry} \mid \text{Green}) * P(\text{Green}) = 4/10 * 6/15 + 6/10 * 4/15 = 48/150 = 4/25$$

$$P(\text{Red} \mid \text{Cherry}) = P(\text{Cherry} \mid \text{Red}) * P(\text{Red}) / P(\text{Cherry}) = 4/10 * 6/15 / (4/25) = \mathbf{0.5}$$

$$P(\text{Green} \mid \text{Cherry}) = P(\text{Cherry} \mid \text{Green}) * P(\text{Green}) / P(\text{Cherry}) = 6/10 * 4/15 / (4/25) = \mathbf{0.5}$$

Problem 3) Naïve Bayes Classifier (20 pts.)

You are given the following customers summary table from *MicroShop* as training data:

age	income	student	buys computer
<=30	high	no	no
<=30	high	no	no
>40	low	yes	no
<=30	medium	no	no
<=30	medium	no	no
>40	medium	no	no
> 40	low	no	no
31...40	low	yes	no
<=30	medium	yes	yes
31...40	high	no	yes
>40	medium	no	yes
>40	high	yes	yes
31...40	medium	no	yes
31...40	low	yes	yes
<=30	low	yes	yes
>40	high	yes	yes
<=30	medium	yes	yes
31...40	medium	no	yes
31...40	high	yes	yes
>40	high	no	yes

Please answer the following questions by using Naïve Bayes classifier and Laplace smoothing if necessary.

- Derive the conditional probabilities of $P(\text{high_income} \mid \text{buys_computer})$, $P(<=30 \mid \text{buys_computer})$, $P(\text{student} \mid \text{buys_computer})$,
- Using Naïve Bayes classifier, what is the probability of a customer with the following profile $P(<=30, \text{high_income}, \text{student})$ buying a computer from *MicroShop*?

Answers:

- a) $P(\leq 30 \mid \text{buys_computer}) = 3/12$
 $P(\text{high} \mid \text{buys_computer}) = 5/12$
 $P(\text{student} \mid \text{buys_computer}) = 7/12$

$$\begin{aligned}P(\text{buys_computer}) &= 12/20 \\P(31 \dots 40 \mid \text{buys_computer}) &= 5/12 \\P(>40 \mid \text{buys_computer}) &= 4/12 \\P(\text{medium} \mid \text{buys_computer}) &= 5/12 \\P(\text{low} \mid \text{buys_computer}) &= 2/12 \\P(\text{not_student} \mid \text{buys_computer}) &= 5/12 \\P(\text{student} \mid \text{not_buys_computer}) &= 2/8 \\P(\text{high} \mid \text{not_buys_computer}) &= 2/8 \\P(\leq 30 \mid \text{not_buys_computer}) &= 4/8\end{aligned}$$

- b) $\text{Likelihood}(\text{buys_computer} \mid \leq 30, \text{high_income}, \text{student}) = 12/20 * 3/12 * 5/12 * 7/12 = 0.03646$
 $\text{Likelihood}(\text{not_buys_computer} \mid \leq 30, \text{high_income}, \text{student}) = 8/20 * 2/8 * 2/8 * 4/8 = 0.0125$
 $P(\text{buys_computer} \mid \leq 30, \text{high_income}, \text{student}) = 0.03646 / (0.03646 + 0.0125) = 0.7447$

Problem 4) k-Nearest Neighbors (20 pts.)

We have the following training data for height/weight vs gender:

Height	70	65	66	60	58	62
Weight	175	170	168	150	155	160
Gender	0	0	0	1	1	1

Gender=0 is male and Gender=1 is female. Now we have 2 test cases: (h=68, w=160) and (h=60, w=162). Predict the gender for both cases using the kNN classifier with the following properties: k=3, distance = Manhattan, weight = uniform

Answers:

Distance for (h=68, w=160):

Height	70	65	66	60	58	62
Weight	175	170	168	150	155	160
Gender	0	0	0	1	1	1
h=68, w=160	17	13	10	18	15	6

(h=68, w=160) is closest to (62,160) (66, 180) (65, 170) => gender=0

Distance for (h=60, w=162):

Height	70	65	66	60	58	62
Weight	175	170	168	150	155	160
Gender	0	0	0	1	1	1
h=60, w=162	23	13	12	12	9	4

(h=60, w=162) is closest to (62,160) (58,155) (60,150) => gender=1

Problem 5) K-means clustering (10 pts.)

You are given the following 10 data points of height & weight:

ID	1	2	3	4
Height	78	72	60	64
Weight	174	172	156	164

Apply k-means algorithms to get 2 clusters with the following parameters:

- a) Initialize with ID=3 and ID=4
- b) Euclidean distance

What are the final groupings and the cluster means?

Hint: In computing Euclidean distance to determine groupings, it is not necessary to take the square root, since the square root operation preserves the order of positive real numbers.

Answer:

step- 0: $[(60.0, 156.0), [3]], [(64.0, 164.0), [1, 2, 4]]$

step- 1: $[(60.0, 156.0), [3, 4]], [(71.3, 170.0), [1, 2]]$

step- 2: $[(62.0, 160.0), [3, 4]], [(75.0, 173.0), [1, 2]]$

Final: 2 clusters $[(62.0, 160.0), [3,4)]$ and $[(75.0, 173.0), [1, 2)]$

