

**function** ENUMERATION-ASK( $X, \mathbf{e}, bn$ ) **returns** a distribution over  $X$

**inputs:**  $X$ , the query variable

$\mathbf{e}$ , observed values for variables  $\mathbf{E}$

$bn$ , a Bayes net with variables  $\{X\} \cup \mathbf{E} \cup \mathbf{Y}$     */\*  $\mathbf{Y} = \text{hidden variables}$  \*/*

$\mathbf{Q}(X) \leftarrow$  a distribution over  $X$ , initially empty

**for each** value  $x_i$  of  $X$  **do**

$\mathbf{Q}(x_i) \leftarrow$  ENUMERATE-ALL( $bn.VARS, \mathbf{e}_{x_i}$ )

        where  $\mathbf{e}_{x_i}$  is  $\mathbf{e}$  extended with  $X = x_i$

**return** NORMALIZE( $\mathbf{Q}(X)$ )

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**function** ENUMERATE-ALL( $vars, \mathbf{e}$ ) **returns** a real number

**if** EMPTY?( $vars$ ) **then return** 1.0

$Y \leftarrow$  FIRST( $vars$ )

**if**  $Y$  has value  $y$  in  $\mathbf{e}$

**then return**  $P(y \mid \text{parents}(Y)) \times$  ENUMERATE-ALL(REST( $vars$ ),  $\mathbf{e}$ )

**else return**  $\sum_y P(y \mid \text{parents}(Y)) \times$  ENUMERATE-ALL(REST( $vars$ ),  $\mathbf{e}_y$ )

        where  $\mathbf{e}_y$  is  $\mathbf{e}$  extended with  $Y = y$