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$$10 + 79.25 = 89.25$$

Course: COM219

Homework 2

Question 4

20/20

System	Description	Cycle Time (T)	Clock Frequency (f)	Instruction Completion Time	Processor Bandwidth (BW)
A	No pipeline; instruction latency 20 ns, cycle time 5 ns	5 ns (as it states) ✓	$f = 1/T = 1/(5 \times 10^{-9}) = 200 \text{ MHz}$ ✓	20 ns (as it states) ✓	$BW = 1000/\text{latency} = 1000/20 = 50 \text{ MIPS}$ ✓
B	No pipeline; instruction completion time 25 ns, clock frequency 250 MHz.	$T = 1/f = 1/(2.5 \times 10^8) = 4 \text{ ns}$ ✓	250 MHz (as it states) ✓	25 ns (as it states) ✓	$BW = 1000/\text{latency} = 1000/25 = 40 \text{ MIPS}$ ✓
C	7-stage pipeline, instruction completion time 35 ns	Latency = instr. completion time = 35 ns $= nT = 7T$ $\rightarrow T = 5 \text{ ns}$ ✓	$f = 1/t = 1/(5 \times 10^{-9}) = 200 \text{ MHz}$ ✓	35 ns (as it states) ✓	$BW = 1000/T = 1000/5 = 200 \text{ MIPS}$ ✓
D	Pipelined design, instruction completion time 10 ns, clock frequency 1 GHz.	$T = 1/f = 1/10^9 = 1 \text{ ns}$ ✓ (and hence, number of stages = $10/1 = 10$ stages)	1 GHz (as it states) ✓	10 ns (as it states) ✓	$BW = 1000/T = 1000/1 = 1000 \text{ MIPS} \neq 1 \text{ BIPS}$
E	5-stage pipeline, cycle time 5 ns	5 ns (as it states) ✓	$f = 1/T = 1/(5 \times 10^{-9}) = 200 \text{ MHz}$ ✓	Latency = instr. completion time = $nT = 5 \times 5 = 25 \text{ ns}$ ✓	$BW = 1000/T = 1000/5 = 200 \text{ MIPS}$ ✓
F	4-stage pipeline, processor bandwidth 250 MIPS.	$BW = 1000/T$ $\rightarrow T = 1000/BW = 1000/250 = 4 \text{ ns}$ ✓	$f = 1/T = 1/(4 \times 10^{-9}) = 250 \text{ MHz}$ ✓	Latency = instr. completion time = $nT = 4 \times 4 = 16 \text{ ns}$ ✓	250 MIPS (as it states) ✓

✓ → System D is the fastest, since it has the greatest BW = greatest rate of instructions being issued per second

Question 5

14.5 / 15

	01101011	10011001
Pure Binary	$1x2^0 + 1x2^1 + 1x2^3 + 1x2^5 + 1x2^6$ = 107 ✓	$1x2^0 + 1x2^3 + 1x2^4 + 1x2^7$ = 153 ✓
Sign-magnitude	$1x2^0 + 1x2^1 + 1x2^3 + 1x2^5 + 1x2^6$ = 107. The most significant bit is 0 → positive → 107 ✓	$1x2^0 + 1x2^3 + 1x2^4$ = 25 The most significant bit is 1 → negative → -25 ✓
Two's Complement	$0x(-2)^7 + 1x2^0 + 1x2^1 + 1x2^3 + 1x2^5 + 1x2^6$ = 107 ✓	$-2^7 + 1x2^0 + 1x2^3 + 1x2^4$ = -103 ✓
Excess 128	Unsigned base-10 value: 107 107-128 = -21 ✓	Unsigned base-10 value: 153 153-128 = 25 ✓
BCD	Use the lookup table First group: 0110 = 6 Second group: 1011 = N.A → N.A ✓	Use the look up table First group = second group = 1001 = 9 → 99 ✓
Hexadecimal	Use the lookup table First group: 0110 = 6 Second group: 1011 = B → 6BH -0.25	Use the look up table First group = second group = 1001 = 9 → 99H -0.25

Question 6

14.75 / 21

-3 (-0.25 per correct answer) no work/calculations shown

Original Number	Binary Number in Register	Value as interpreted with the new representation
11 (Pure Binary, k=4)	1011 ✓	3 ✓
-14 (Sign-magnitude, k=5)	11110 ✓	-2 ✓
68 (Pure Binary, k=6)	Number out of range ✓	N.A ✓

-27 (Two's Complement, k=6)	100101✓	37✓
-76 (Two's Complement, k=8)	10110100 ✓	B4H -0.25
72 (interpret as 2-digit BCD)	01110001 ✗ -1.5 01110010	113 ✗ -1.5 114
6DH (interpret as 2-digit Hex)	01101101✓	-19✓

Question 2

- (a) Average instruction execution time for type A instruction :

$$\text{Fetch instruction time} + \text{execute time} = 100 + 10 = 110 \text{ cycles}$$

- Average instruction execution time for type B instruction :

$$\text{Fetch instruction time} + \text{fetch operand time} + \text{execute time} = 100 + 100 + 100 = 300 \text{ cycles}$$

$$\rightarrow \text{Average instruction execution time} : \frac{110 \times 80 + 300 \times 20}{100} = 148 \text{ cycles} \checkmark$$

- (b) Cycle time = $\frac{1}{f} = \frac{1}{10^6} = 1000 \text{ ns} = 1 \mu\text{s}$ (microsec)

$$\rightarrow \text{Average instruction execution time} : 148 \times 1 = 148 \mu\text{s}$$

- (c) Average instruction execution time in second : $148 \times 10^{-6} \text{ s}$

$$\rightarrow \text{Instruction execution rate} = \frac{1}{148 \times 10^{-6}} = 6756 \text{ (round down from } 6756.756 \text{) Cips} \checkmark$$

- (d) Cycle time = $\frac{1}{f} = \frac{1}{20 \times 10^6} = 50 \text{ ns}$

$$\rightarrow \text{Average instruction execution time} : 148 \times 50 = 7400 \text{ ns} = 7.4 \times 10^{-6} \text{ s}$$

$$\rightarrow \text{Instruction execution rate} : \frac{1}{7.4 \times 10^{-6}} = 135135 \text{ (Cips)} \checkmark$$

- (e) Program completion time = $M \times t_i = 5,000,000 \times 7.4 \times 10^{-6}$
 $= 37 \text{ (s)} \checkmark$

Question 3

① Longest ALU operations = 12 ns

$$\rightarrow T \geq 4 + 12 = 16 \text{ ns}$$

$$\rightarrow f = \frac{1}{T} = \frac{1}{16 \times 10^{-9}} = 62.5 \text{ MHz} \checkmark$$

Every instruction take 3 cycles to complete

$$\rightarrow BW = \frac{1}{3T} = \frac{1}{16 \times 3 \times 10^{-9}} \approx 20.833 \text{ MIPS} \checkmark$$

② The loading time and ALU time remain the same

$$\rightarrow f \text{ is the same } = 62.5 \text{ MHz}$$

Since now there is new instruction issued every cycles.

$$\rightarrow BW = f = 62.5 \text{ MIPS} \checkmark$$

↓

Since this is number of cycles per sec

③ Program completion time = $M \times \text{instruction completion time}$

$$\text{Part a: } M \times 3T = 0.048 \text{ s} \checkmark$$

$$\text{Part b: } M \times T = 0.016 \text{ s} \checkmark$$