

1 Early Concepts

- **Nodes added by left/right:**

$$A_L \leftarrow \{l \in L \mid (\neg \exists b \in B)(l.id = b.id)\}$$

$$A_R \leftarrow \{r \in R \mid (\neg \exists b \in B)(r.id = b.id)\}$$

- **Nodes deleted by left/right:**

$$D_L \leftarrow \{b \in B \mid (\neg \exists l \in L)(b.id = l.id)\}$$

$$D_R \leftarrow \{b \in B \mid (\neg \exists r \in R)(b.id = r.id)\}$$

- **Nodes edited by left/right:**

$$E_L \leftarrow \{l \in L \mid (\exists b \in B)(\exists r \in R)(l.id = b.id = r.id \wedge l.body \neq b.body \wedge b.body = r.body)\}$$

$$E_R \leftarrow \{r \in R \mid (\exists b \in B)(\exists l \in L)(r.id = b.id = l.id \wedge r.body \neq b.body \wedge b.body = l.body)\}$$

2 Semistructured Merge

2.1 Early Concepts

- Every node's origin is set to UNKNOWN beforehand

2.2 Merge Algorithms

Algorithm 1: Merge Files

```

Input: l, b, r, o
1 if  $l.content = b.content$  then
2   |  $o.content \leftarrow r.content$ ;
3 else if  $b.content = r.content \vee l.content = r.content$  then
4   |  $o.content \leftarrow l.content$ ;
5 else
6   |  $L \leftarrow fileToTree(l)$ ;
7   |  $B \leftarrow fileToTree(b)$ ;
8   |  $R \leftarrow fileToTree(r)$ ;
9   |  $M \leftarrow mergeTrees(L, B, R)$ ;
10  |  $H \leftarrow getActiveHandlers()$ ;
11  | foreach  $h \in H$  do
12  |   |  $h.handle(M)$ ;
13  | end
14  |  $o.content \leftarrow treeToText(M)$ ;
15 end

```

Algorithm 2: Merge Trees

```

Input: L, B, R
Output: result of merging left, base and right trees
1  $L.origin \leftarrow LEFT$ ;
2  $B.origin \leftarrow BASE$ ;
3  $R.origin \leftarrow RIGHT$ ;
4  $LB \leftarrow mergeNodes(L, B)$ ;
5  $M \leftarrow mergeNodes(LB, R)$ ;
6 foreach  $d \in D_L \cap D_R$  do
7   |  $removeNode(d, M)$ ;
8 end
9  $runTextualMergeOnLeaves(M)$ ;
10 return  $M$ ;

```

Algorithm 3: Run Textual Merge On Leaves**Input:** T

```

1 foreach  $t \in T.children$  do
2   |  $runTextualMergeOnLeaves(t)$ ;
3 end
4 if  $T.children = \emptyset \wedge SEPARATOR \in T.body$  then
5   |  $l, b, r \leftarrow split(T.body, SEPARATOR)$ ;
6   |  $l \leftarrow l - MARKER$ ;
7   |  $T.body \leftarrow textualMerge(l, b, r)$ ;
8 end

```

Algorithm 4: Merge Nodes**Input:** A, B **Output:** result of merging nodes A and B

```

1 if  $A = \text{null}$  then return  $B$ ;
2 if  $B = \text{null}$  then return  $A$ ;
3 if  $A.type \neq B.type \vee A.id \neq B.id$  then return null;
4  $M.id \leftarrow B.id$ ;
5  $M.type \leftarrow B.type$ ;
6  $M.origin \leftarrow B.origin$ ;
7  $M.children \leftarrow \emptyset$ ;
8 if  $A.children = \emptyset \wedge B.children = \emptyset$  then
9   | if  $MARKER \in A.body$  then
10    |  $M.body \leftarrow A.body + B.body$ ;
11   | else if  $A.origin = LEFT \wedge B.origin = BASE$  then
12    |  $M.body \leftarrow MARKER + A.body + SEPARATOR + B.body + SEPARATOR$ ;
13   | else if  $A.origin = LEFT$  then
14    |  $M.body \leftarrow MARKER + A.body + SEPARATOR + SEPARATOR + B.body$ ;
15   | else
16    |  $M.body \leftarrow MARKER + SEPARATOR + A.body + SEPARATOR + B.body$ ;
17   | end
18   | return  $M$ ;
19 else if  $A.children \neq \emptyset \wedge B.children \neq \emptyset$  then
20   | foreach  $b \in B.children$  do
21     |  $a \leftarrow \text{find}(a \in A.children \rightarrow a.type = b.type \wedge a.id = b.id)$ ;
22     | if  $a.origin = UNKNOWN$  then  $a.origin \leftarrow A.origin$ ;
23     | if  $b.origin = UNKNOWN$  then  $b.origin \leftarrow B.origin$ ;
24     |  $M.children \leftarrow M.children \cup \text{mergeNodes}(a, b)$ ;
25   | end
26   | foreach  $a \in A.children$  do
27     |  $b \leftarrow \text{find}(b \in B.children \rightarrow a.type = b.type \wedge a.id = b.id)$ ;
28     | if  $a.origin = UNKNOWN$  then  $a.origin \leftarrow A.origin$ ;
29     | if  $b = \text{null}$  then  $M.children \leftarrow M.children \cup a$ ;
30   | end
31   | return  $M$ ;
32 end
33 return null;

```

3 Handlers

3.1 Renaming Handler

3.1.1 Early Concepts

- Nodes possibly renamed by left/right without body changes:

$$R_L = \{b \in B \mid (\neg \exists l \in L)(b.id = l.id) \wedge (\exists l \in L)(b.body = l.body)\}$$

$$R_R = \{b \in B \mid (\neg \exists r \in R)(b.id = r.id) \wedge (\exists r \in R)(b.body = r.body)\}$$

- Nodes possibly deleted or renamed by left/right with body changes:

$$DR_L \leftarrow \{b \in B \mid (\neg \exists l \in L)(b.id = l.id \vee b.body = l.body)\}$$

$$DR_R \leftarrow \{b \in B \mid (\neg \exists r \in R)(b.id = r.id \vee b.body = r.body)\}$$

- Nodes IDs similarity:

$$a.id \approx b.id \leftrightarrow a.id.name = b.id.name \vee a.id.params = b.id.params$$

3.1.2 Match Algorithm

Algorithm 5: Match Algorithm

Input: L, B, R, M

Output: Set of quadruples (l, b, r, m) consisting of the base node b and its corresponding left node l , right node r and merge node m

```

1 matches ← ∅;
2 foreach b ∈ RL ∪ RR ∪ DRL ∪ DRR do
3   l ← correspondentNode(b, L);
4   r ← correspondentNode(b, R);
5   m ← mergeNode(l, r, M);
6   matches ← matches ∪ (l, b, r, m);
7 end
8 return matches

```

Algorithm 6: Correspondent Node

Input: b, T

Output: b's correspondent node on tree T

```

1 t ← findFirst(t ∈ T → t.id = b.id);
2 if t = null then
3   t ← findFirst(t ∈ T → t.body = b.body);
4 end
5 if t = null then
6   t ← findFirst(t ∈ T → t.id ≈ b.id ∧ t.body ≈ b.body);
7 end
8 if t = null then
9   t ← findFirst(t ∈ T → t.body = substring(b.body) ∨ b.body = substring(t.body));
10 end
11 return t;

```

Algorithm 7: Merge Node**Input:** l, r, M **Output:** l and r 's merge node on tree M

```

1 if  $l \neq \text{null}$  then
2   | return find( $m \in M \rightarrow m.id = l.id$ );
3 end
4 if  $r \neq \text{null}$  then
5   | return find( $m \in M \rightarrow m.id = r.id$ );
6 end
7 return null;

```

3.1.3 Handler Algorithms**Algorithm 8: Check References and Merge Methods Variant****Input:** $(l, b, r, m), M$

```

1 if  $l.id = b.id \vee r.id = b.id$  then
2   |  $m.body \leftarrow \text{textualMerge}(l, b, r)$ ;
3   | removeUnmatchedNode( $l, r, m, M$ );
4 else if  $l.id \neq r.id$  then
5   |  $m.body \leftarrow \text{conflict}(l.body, b.body, r.body)$ ;
6   | removeUnmatchedNode( $l, r, m, M$ );
7 else if  $l.body \neq r.body$  then
8   | if newReferenceTo( $l$ )  $\vee$  newReferenceTo( $r$ ) then
9     |  $m.body \leftarrow \text{conflict}(l.body, b.body, r.body)$ ;
10  | else
11  |   |  $m.body \leftarrow \text{textualMerge}(l, b, r)$ ;
12  | end
13  | removeUnmatchedNode( $l, r, m, M$ );
14 end

```

Algorithm 9: Merge Methods Variant**Input:** $(l, b, r, m), M$

```

1  $m.body \leftarrow \text{textualMerge}(l, b, r)$ ;
2 removeUnmatchedNode( $l, r, m, M$ );

```

Algorithm 10: Check Textual and Keep Both Methods Variant**Input:** $(l, b, r, m), M$

```

1 if  $l.id = b.id \vee r.id = b.id$  then
2   | if textualMergeHasConflictInvolvingSignature( $b$ ) then
3     |  $m.body \leftarrow \text{conflict}(l.body, b.body, r.body)$ ;
4     | removeUnmatchedNode( $l, r, m, M$ );
5   | end
6 else if  $l.id \neq r.id \wedge l.body = r.body$  then
7   |  $m.body \leftarrow \text{conflict}(l.body, b.body, r.body)$ ;
8   | removeUnmatchedNode( $l, r, m, M$ );
9 end

```

Algorithm 11: Keep Both Methods Variant**Input:** $(l, b, r, m), M$

```

1 if  $(l.id = b.id \vee r.id = b.id) \wedge \text{hasConflict}(m)$  then
2   | removeConflict( $m$ );
3 end

```

Algorithm 12: Remove Unmatched Node**Input:** l, r, m, M

```

1 if  $l.id = m.id \wedge r.id \neq m.id$  then
2   |  $\text{removeNode}(r, M)$ ;
3 end

```

3.2 Initialization Blocks Handler

3.2.1 Handler Algorithm

Algorithm 13: Handle**Input:** L, B, R, M

```

1  $IB_L \leftarrow \{n \in A_L \mid n.type = INITBLOCK\}$ ;
2  $IB_R \leftarrow \{n \in A_R \mid n.type = INITBLOCK\}$ ;
3  $IB_B \leftarrow \{n \in D_L \cap D_R \mid n.type = INITBLOCK\}$ ;
4  $matches \leftarrow \emptyset$ ;
5 if  $|IB_L| = 1 \wedge |IB_B| = 1 \wedge |IB_R| = 1$  then
6   |  $matches \leftarrow matches \cup (IB_{L_1}, IB_{B_1}, IB_{R_1})$ ;
7 else
8   foreach  $b \in IB_B$  do
9     |  $l \leftarrow \text{findFirst}(l \in IB_L \rightarrow l.body \approx b.body)$ ;
10    |  $r \leftarrow \text{findFirst}(r \in IB_R \rightarrow r.body \approx b.body)$ ;
11    |  $IB_L \leftarrow IB_L - l$ ;
12    |  $IB_R \leftarrow IB_R - r$ ;
13    | if  $l \neq \text{null} \wedge r \neq \text{null}$  then
14      |  $matches \leftarrow matches \cup (l, b, r)$ ;
15    | end
16  end
17  foreach  $l \in IB_L$  do
18    |  $r \leftarrow \text{findFirst}(r \in IB_R \rightarrow r.body \approx l.body)$ ;
19    |  $IB_R \leftarrow IB_R - r$ ;
20    | if  $r \neq \text{null}$  then
21      |  $matches \leftarrow matches \cup (l, \text{null}, r)$ ;
22    | end
23  end
24 end
25 foreach  $(l, b, r) \in matches$  do
26   |  $m \leftarrow \text{find}(m \in M \rightarrow m.body = l.body)$ ;
27   |  $m.body \leftarrow \text{textualMerge}(l.body, b.body, r.body)$ ;
28   |  $m \leftarrow \text{find}(m \in M \rightarrow m.body = r.body)$ ;
29   |  $\text{removeNode}(m, M)$ ;
30 end

```

3.3 Multiple Initialization Blocks Handler

3.3.1 Handler Algorithm

Algorithm 14: Handle

```

Input: L, B, R, M
1   $IB_L \leftarrow \{n \in A_L \mid n.type = INITBLOCK\};$ 
2   $IB_R \leftarrow \{n \in A_R \mid n.type = INITBLOCK\};$ 
3   $IB_B \leftarrow \{n \in D_L \cap D_R \mid n.type = INITBLOCK\};$ 
4   $eIB_L \leftarrow \text{editedNodes}(IB_L, IB_B);$ 
5   $eIB_R \leftarrow \text{editedNodes}(IB_R, IB_B);$ 
6   $dIB_L \leftarrow \text{deletedNodes}(IB_L, IB_B, eIB_L);$ 
7   $dIB_R \leftarrow \text{deletedNodes}(IB_R, IB_B, eIB_R);$ 
8  foreach  $b \in IB_B$  do
9       $l \leftarrow eIB_L[b];$ 
10      $r \leftarrow eIB_R[b];$ 
11     if  $l \neq \text{null} \wedge r \neq \text{null}$  then
12          $\text{updateMergeTree}(l, b, r, M);$ 
13     else if  $l \neq \text{null} \vee r \neq \text{null}$  then
14         if  $l \neq \text{null}$  then
15              $r \leftarrow \text{find}(r \in dIB_R \rightarrow r.body = b.body);$ 
16             if  $r \neq \text{null}$  then  $\text{removeNode}(b, M);$ 
17         else
18              $l \leftarrow \text{find}(l \in dIB_L \rightarrow l.body = b.body);$ 
19             if  $l \neq \text{null}$  then  $\text{removeNode}(b, M);$ 
20         end
21          $\text{updateMergeTree}(l, b, r, M);$ 
22     else
23          $m \leftarrow \text{find}(m \in M \rightarrow m.body = b.body);$ 
24          $\text{removeNode}(m, M);$ 
25     end
26 end
27  $aIB_L \leftarrow \text{addedNodes}(IB_L, IB_B, eIB_L);$ 
28  $aIB_R \leftarrow \text{addedNodes}(IB_R, IB_B, eIB_R);$ 
29  $DEP \leftarrow \text{dependentNodes}(aIB_L, aIB_R);$ 
30 foreach  $(l, rs) \in DEP$  do
31      $s \leftarrow \varepsilon;$ 
32     foreach  $r \in rs$  do
33          $s \leftarrow s + r.body;$ 
34          $m \leftarrow \text{find}(m \in M \rightarrow m.body = r.body);$ 
35          $\text{removeNode}(r, M);$ 
36     end
37      $m \leftarrow \text{find}(m \in M \rightarrow m.body = l.body);$ 
38      $m.body \leftarrow \text{conflict}(l.body, \varepsilon, s);$ 
39 end
40 foreach  $l \in aIB_L$  do
41     foreach  $r \in aIB_R$  do
42         if  $l.body = r.body$  then
43              $m \leftarrow \text{find}(m \in M \rightarrow m.body = r.body);$ 
44              $\text{removeNode}(m, M);$ 
45         end
46     end
47 end

```

Algorithm 15: Edited Nodes**Input:** IB, IB_B **Output:** map associating a deleted base node b in IB_B and its correspondent added branch node a in IB

```

1  $D \leftarrow \{d \in IB_B \mid (\neg \exists a \in IB)(d.body = a.body)\};$ 
2  $A \leftarrow \{a \in IB \mid (\neg \exists d \in IB_B)(a.body = d.body)\};$ 
3  $matches \leftarrow \emptyset;$ 
4 foreach  $a \in A$  do
5    $S \leftarrow \{d \in D \mid a.body \approx d.body\};$ 
6    $b \leftarrow \underset{s \in S}{\operatorname{argmax}} (\operatorname{similarity}(s.body, a.body));$ 
7   if  $b \neq \text{null}$  then  $matches \leftarrow matches \cup \{b : a\};$ 
8 end
9 return  $matches$ 

```

Algorithm 16: Added Nodes**Input:** IB, IB_B, eIB **Output:** set of initialization block nodes added by branch

```

1  $A \leftarrow \{n \in IB \mid (\neg \exists b \in IB_B)(n.body = b.body)\};$ 
2  $A \leftarrow \{n \in A \mid (\neg \exists e \in eIB)(n.body = e.value.body)\};$ 
3 return  $A;$ 

```

Algorithm 17: Deleted Nodes**Input:** IB, IB_B, eIB **Output:** set of initialization block nodes deleted by branch

```

1  $D \leftarrow \{b \in IB_B \mid (\neg \exists n \in IB)(b.body = n.body)\};$ 
2  $D \leftarrow \{n \in D \mid (\neg \exists e \in eIB)(n.body = e.key.body)\};$ 
3 return  $D;$ 

```

Algorithm 18: Update Merge Tree**Input:** l, b, r, M

```

1  $m \leftarrow \operatorname{find}(m \in M \rightarrow m.body = l.body);$ 
2  $m.body \leftarrow \operatorname{textualMerge}(l.body, b.body, r.body);$ 
3  $m \leftarrow \operatorname{find}(m \in M \rightarrow m.body = r.body);$ 
4 removeNode $(m, M);$ 

```

Algorithm 19: Dependent Nodes**Input:** aIB_L, aIB_R **Output:** map associating an added left node l in aIB_L and all added right nodes r in aIB_R with common global variables

```

1  $DEP \leftarrow \emptyset;$ 
2 foreach  $l \in aIB_L$  do
3    $DEP \leftarrow DEP \cup \{l : \emptyset\};$ 
4    $V_L \leftarrow \operatorname{globalVariables}(l);$ 
5   foreach  $r \in aIB_R$  do
6      $V_R \leftarrow \operatorname{globalVariables}(r);$ 
7     if  $V_L \cap V_R \neq \emptyset$  then  $DEP[l] \leftarrow DEP[l] \cup r;$ 
8   end
9 end
10 return  $DEP;$ 

```

3.4 Type Ambiguity Error Handler

3.4.1 Handler Algorithm

Algorithm 20: Handle	
	<p>Input: L, B, R, M</p> <pre> 1 $ID_L \leftarrow \{n \in A_L \mid n.type = IMPORTDECL\};$ 2 $ID_R \leftarrow \{n \in A_R \mid n.type = IMPORTDECL\};$ 3 if $ID_L = \emptyset \vee ID_R = \emptyset$ then return; 4 $T_L \leftarrow \text{treeToText}(L);$ 5 $T_B \leftarrow \text{treeToText}(B);$ 6 $T_R \leftarrow \text{treeToText}(R);$ 7 $M_U \leftarrow \text{textualMerge}(T_L, T_B, T_R);$ 8 $I_L, I_R \leftarrow \text{extractInsertions}(M_U);$ 9 $cs \leftarrow \text{extractConflicts}(M_U);$ 10 $c \leftarrow \text{compile}(M_U);$ 11 $ps \leftarrow \text{problems}(c);$ 12 foreach $l \in ID_L$ do 13 $m_l \leftarrow \text{extractPackageMember}(l.body);$ 14 foreach $r \in ID_R$ do 15 $m_r \leftarrow \text{extractPackageMember}(r.body);$ 16 if $m_l = m_r$ then 17 $p \leftarrow \text{importDeclarationsProblem}(l, r, ps);$ 18 if $p \neq \text{null}$ then 19 $m \leftarrow \text{find}(m \in M \rightarrow m.body = l.body);$ 20 $m.body \leftarrow \text{conflict}(l.body, \varepsilon, r.body);$ 21 $m \leftarrow \text{find}(m \in M \rightarrow m.body = r.body);$ 22 $\text{removeNode}(m, M);$ 23 $ps \leftarrow ps - p;$ 24 break; 25 end 26 else if $(m_l = * \vee m_r = *) \wedge \text{importDeclarationsConflict}(l, r, cs)$ then 27 if $m_l \neq *$ then 28 $I \leftarrow I_R;$ 29 $m \leftarrow m_l;$ 30 else 31 $I \leftarrow I_L;$ 32 $m \leftarrow m_r;$ 33 end 34 $i \leftarrow \text{find}(i \in I \rightarrow \text{IMPORT} \notin i \wedge m \in i);$ 35 if $i \neq \text{null}$ then 36 $m \leftarrow \text{find}(m \in M \rightarrow m.body = l.body);$ 37 $m.body \leftarrow \text{conflict}(l.body, \varepsilon, r.body);$ 38 $m \leftarrow \text{find}(m \in M \rightarrow m.body = r.body);$ 39 $\text{removeNode}(m, M);$ 40 break; 41 end 42 end 43 end 44 end </pre>

Algorithm 21: Import Declarations Problem**Input:** l, r, ps **Output:** compilation problem in ps concerning l and r import declarations, if there is one

```

1 foreach  $p \in ps$  do
2   if  $p.type = COLLISION$  then
3     foreach  $a \in p.arguments$  do
4       if  $a \in l.body \vee a \in r.body$  then return  $p$ ;
5     end
6   else if  $p.type = AMBIGUITY$  then return  $p$ ;
7 end
8 return null;

```

Algorithm 22: Import Declarations Conflict**Input:** l, r, cs **Output:** whether there is an unstructured conflict in cs concerning l and r import declarations

```

1 foreach  $c \in cs$  do
2   if  $l.body \in c.left \wedge r.body \in c.right$  then return true;
3 end
4 return false;

```

3.5 New Element Referencing Edited One Handler

3.5.1 Handler Algorithm

Algorithm 23: Handle	
<p>Input: L, B, R, M</p> <pre> 1 $T_L \leftarrow \text{treeToText}(L);$ 2 $T_B \leftarrow \text{treeToText}(B);$ 3 $T_R \leftarrow \text{treeToText}(R);$ 4 $M_U \leftarrow \text{textualMerge}(T_L, T_B, T_R);$ 5 $cs \leftarrow \text{extractConflicts}(M_U);$ 6 $aMFD_L \leftarrow \{l \in A_L \mid l.type = \text{METHODDECL} \vee l.type = \text{FIELDDECL}\};$ 7 $aMFD_R \leftarrow \{r \in A_R \mid r.type = \text{METHODDECL} \vee r.type = \text{FIELDDECL}\};$ 8 $eMFD_L \leftarrow \{l \in E_L \mid l.type = \text{METHODDECL} \vee l.type = \text{FIELDDECL}\};$ 9 $eMFD_R \leftarrow \{r \in E_R \mid r.type = \text{METHODDECL} \vee r.type = \text{FIELDDECL}\};$ 10 foreach $a_l \in aMFD_L$ do 11 foreach $e_r \in eMFD_R$ do 12 if $\text{nodesConflict}(a_l, e_r, cs) \wedge e_r.id.name \in a_l.body$ then 13 $b \leftarrow \text{find}(b \in B \rightarrow b.id = e_r.id);$ 14 $m \leftarrow \text{find}(m \in M \rightarrow m.body = e_r.body);$ 15 $m.body \leftarrow \text{conflict}(e_r.body, b.body, a_l.body);$ 16 $m \leftarrow \text{find}(m \in M \rightarrow m.body = a_l.body);$ 17 $\text{removeNode}(m, M);$ 18 end 19 end 20 end 21 foreach $a_r \in aMFD_R$ do 22 foreach $e_l \in eMFD_L$ do 23 if $\text{nodesConflict}(a_r, e_l, cs) \wedge e_l.id.name \in a_r.body$ then 24 $b \leftarrow \text{find}(b \in B \rightarrow b.id = e_l.id);$ 25 $m \leftarrow \text{find}(m \in M \rightarrow m.body = e_l.body);$ 26 $m.body \leftarrow \text{conflict}(e_l.body, b.body, a_r.body);$ 27 $m \leftarrow \text{find}(m \in M \rightarrow m.body = a_r.body);$ 28 $\text{removeNode}(m, M);$ 29 end 30 end 31 end</pre>	

Algorithm 24: Nodes Conflict	
<p>Input: a, b, cs</p> <p>Output: whether there is an unstructured conflict in cs concerning a and b nodes</p> <pre> 1 foreach $c \in cs$ do 2 if $c.left = a.body \wedge c.right = b.body$ then return true; 3 if $c.left = b.body \wedge c.right = a.body$ then return true; 4 end 5 return false;</pre>	

3.6 Deletions Handler

3.6.1 Handler Algorithm

Algorithm 25: Handle	
	Input: L, B, R, M
1	$T_L \leftarrow \text{treeToText}(L);$
2	$T_B \leftarrow \text{treeToText}(B);$
3	$T_R \leftarrow \text{treeToText}(R);$
4	foreach $d_l \in D_L$ do
5	if $d_l.\text{children} \neq \emptyset$ then
6	$r \leftarrow \text{find}(r \in R \rightarrow r.\text{id} = d_l.\text{id});$
7	$m \leftarrow \text{find}(m \in M \rightarrow m.\text{id} = d_l.\text{id});$
8	if $\text{sameShape}(d_l, r) \wedge d_l.\text{body} = r.\text{body}$ then $\text{removeNode}(m, M);$
9	else if $\text{newReference}(d_l.\text{id}, T_B, T_R)$ then $m.\text{parent.addChild}(r, m.\text{index});$
10	else
11	$\text{removeNode}(m, M);$
12	$a_l \leftarrow \text{renamingMatch}(A_L, d_l, T_B, T_L);$
13	if $a_l \neq \text{null}$ then
14	$r.\text{id} \leftarrow a_l.\text{id};$
15	$\text{removeNode}(a_l, M);$
16	$m.\text{parent.addChild}(r, m.\text{index});$
17	else
18	$n.\text{id} \leftarrow r.\text{id};$
19	$n.\text{type} \leftarrow r.\text{type};$
20	$n.\text{body} \leftarrow \text{conflict}(\varepsilon, d_l, r);$
21	$m.\text{parent.addChild}(n, m.\text{index});$
22	end
23	end
24	end
25	end
26	foreach $d_r \in D_R$ do
27	if $d_r.\text{children} \neq \emptyset$ then
28	$l \leftarrow \text{find}(l \in L \rightarrow l.\text{id} = d_r.\text{id});$
29	$m \leftarrow \text{find}(m \in M \rightarrow m.\text{id} = d_r.\text{id});$
30	if $\text{sameShape}(d_r, l) \wedge d_r.\text{body} = l.\text{body}$ then $\text{removeNode}(m, M);$
31	else if $\text{newReference}(d_r.\text{id}, T_B, T_L)$ then $m.\text{parent.addChild}(l, m.\text{index});$
32	else
33	$\text{removeNode}(m, M);$
34	$a_r \leftarrow \text{renamingMatch}(A_R, d_r, T_B, T_R);$
35	if $a_r \neq \text{null}$ then
36	$l.\text{id} \leftarrow a_r.\text{id};$
37	$\text{removeNode}(a_r, M);$
38	$m.\text{parent.addChild}(l, m.\text{index});$
39	else
40	$n.\text{id} \leftarrow l.\text{id};$
41	$n.\text{type} \leftarrow l.\text{type};$
42	$n.\text{body} \leftarrow \text{conflict}(l, d_r, \varepsilon);$
43	$m.\text{parent.addChild}(n, m.\text{index});$
44	end
45	end
46	end
47	end

Algorithm 26: Same Shape**Input:** A, B **Output:** whether nodes A and B have same shape

```

1 if  $A.children = \emptyset \wedge B.children = \emptyset$  then return  $A.type = B.type$ ;
2 if  $A.children = \emptyset \vee B.children = \emptyset$  then return false;
3 if  $|A.children| \neq |B.children|$  then return false;
4  $result \leftarrow \mathbf{true}$ ;
5 foreach  $(a, b) \in (A.children, B.children)$  do
6    $result \leftarrow result \wedge \mathbf{sameShape}(a, b)$ ;
7 end
8 return  $result$ ;

```

Algorithm 27: New Reference**Input:** id, T_B, T **Output:** whether there is a new reference to id in T

```

1 return  $\mathbf{countReferences}(id, T) > \mathbf{countReferences}(id, T_B)$ ;

```

Algorithm 28: Renaming Match**Input:** A, d, T_B, T **Output:** added node a in A with the same shape and similar body as deleted node d , such that there are no new references to a 's id in T

```

1 return  $\mathbf{find}(a \in A \rightarrow \mathbf{sameShape}(a, d) \wedge a.body \approx d.body \wedge \neg \mathbf{newReference}(a.id, T_B, T))$ ;

```