Mining Maximal Sequential Patterns without Candidate Maintenance

Artificial Intelligence Seminar 10 March 2016

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Reference: Pierre Schaus

Let's take a comparison for the article's authors Pierre Schaus is a UCL professor, you might know him

H-index : **10**

Citations: 283



Authors

Vincent S. Tseng



Cheng-Wei Wu







Authors: Vincent S. Tseng

Ph.D. in Computer Science

Professor, Dept. Computer Science, National Chiao Tung University, Taiwan

H-index: 32

3,2x more

Citations: 3308

11,7x more



Authors: Philippe Fournier-Viger

Ph.D. in Computer Science

Associate Professor, Harbin Institute of Technology, Shenzhen Graduate School

He created the SPMF library

H-index : **17**

1,7x more

Citations: 712

2,5x more



Authors: Cheng-Wei Wu

H-index: 12

1,2x more

Citations: 518

1,83x more



About the article

We can trust the author, but

We found errors in some examples,

Some part of the articles were mathematicaly not clear enough, and some definition were simply wrong,

In the end, the article was a complete mess, we cannot understand who accepted to publish it!

After some search else where we made it possible to understand the content of the articles. But based only on it, it wouldn't have be possible.

It was published in a book: Advanced Data Mining and Applications

This particular article has (when the slides where made) 10 citations

First Concepts

Sequence Database
Sequential pattern
Closed sequential pattern
Maximal sequential pattern

Sequence Database

A sequence database consist of:

```
A set of items
{1, 2, 3, 4, ..., N}

Itemset (set of item, distinct and unordered)
{1, 2, 3, 5} or {4, 5} or {3, 7} or ...

Sequence (set of itemsets)
<{1,2}, {3}, {5}> or <{4}, {6}> or ...
```

The sequence database is a set of sequences What do theses concepts represents?

Sequence Database: Illustration

Let's take as an example a book

```
Set of item → The words
{He, nice, the, is, a, guy, sun, shine, ...}

Itemset → A sentence (where words are distinct and unordered)

{He, a, nice, guy, is}

{The, sun, shine, in, the, sky}

Sequence → A chapter of the book

Sequence Database → The book
```

Sequential pattern

Synonyms are sub-sequence or frequent sequence

It is a sequence of item that appears a certain number of time, that number is the *minimum support threshold* (or *minsup*)

Sequence database

```
<{1,2},{3},{4},{6}><{2},{5},{6}><{1,3},{5},{6}>
```

With minsup = 2, some examples of sequential pattern

```
{5},{6}
{1}
{3},{6}
```

. . .

Closed sequential pattern

A closed sequential pattern is a sequential pattern not included in another closed pattern <u>having the same frequency</u>.

```
<{1},{123},{13},{4},{36}><
<{14},{3},{23},{15}><
<{56},{12},{46},{3},{2}><
<{5},{7},{16},{3},{2},{3}>
```

With support 2 (or 2/4 entry → 50 %), here are some closed sequential pattern

```
{1}, {3} 100 % (4/4)
{1}, {3}, {2} 75 % (3/4)
{5}, {1}, {3}, {2} 50% (2/4)
{5} 75 % (3/4)
```

And this one is **NOT**

{1} 100 % (4/4)

Maximal sequential pattern

The same as the closed sequential pattern, but if one sequence is in another one, it is not maximal.

Interesting property:

You can derive every closed sequential patterns from the maximal sequential patterns

Question 1: Closed and Maximal pattern

Considering the database

- 1. Which one of these is not a closed sequential pattern? Why?
 - \rightarrow < { b}, {f}>
 - \rightarrow <{b}>
 - \rightarrow <{a,b}>
 - \rightarrow <{a},{b},{e}>
- 2. Which one of these is a maximal sequential pattern? Why?
 - \rightarrow <{a},{e}>
 - \rightarrow < {b}, {b}>
 - $\rightarrow < \{b\}, \{f\}, \{e\} >$
 - \rightarrow <{a}, {f}>

<{a,b},{c},{f,g},{g},{e}> <{a,d},{c},{b},{a,b,e,f}> <{a},{b},{f,g},{e}> <{b},{f,g}>

MaxSP Algorithm

Find the maximal sequential pattern It is build uppon the PrefixSpan Algorithm Why the need for a new algorithm?

- → Less memory usage
- → Faster to find sequential pattern

PrefixSpan: Start

First let's explain the PrefixSpan Algorithm
It's the most efficient pattern mining algorithm
We start with a sequence database

```
<{1}, {1 2 3}, {1 3}, {4}, {3 6}>
<{1 4}, {3}, {2 3}, {1 5}>
<{5 6}, {1 2}, {4 6}, {3}, {2}>
<{5}, {7}, {1 6}, {3}, {2}, {3}>
```

PrefixSpan: Pattern-growth

It works by pattern-growth, which does not generate any candidates (saving memory)

- 1. Scan: Calculate support for each item and existing itemset
- 2. Output : Output item that have enough support
- 3. Projection : Recursively project the database with every item that have enough support

Item	Support
1	
2	
3	
4	
5	
6	
7	

Item	Support
1	100 % (4)
2	
3	
4	
5	
6	
7	

Item	Support
1	100 % (4)
2	100 % (4)
3	
4	
5	
6	
7	

Item	Support
1	100 % (4)
2	100 % (4)
3	100 % (4)
4	
5	
6	
7	

Item	Support
1	100 % (4)
2	100 % (4)
3	100 % (4)
4	75 % (3)
5	
6	
7	

Item	Support
1	100 % (4)
2	100 % (4)
3	100 % (4)
4	75 % (3)
5	75 % (3)
6	
7	

Item	Support
1	100 % (4)
2	100 % (4)
3	100 % (4)
4	75 % (3)
5	75 % (3)
6	75 % (3)
7	

Item	Support
1	100 % (4)
2	100 % (4)
3	100 % (4)
4	75 % (3)
5	75 % (3)
6	75 % (3)
7	25 % (1)

Item	Support
1	100 % (4)
2	100 % (4)
3	100 % (4)
4	75 % (3)
5	75 % (3)
6	75 % (3)
7	25 % (1)

MinSup 75 % (3)

It has to be done for itemsets too...

{123}, {12}, {13}, {36}, {14}, {23}, {46}, {15}, {56}, {46}, {16}

Item	Support	Item	Support
1	100 %	1 3	50 %
2	100 %	4 6	25 %
3	100 %	3 6	25 %
4	75 %	1 4	25 %
5	75 %	23	25 %
6	75 %	1 5	25 %
7	25 %	5 6	25 %
123	25 %	1 6	25 %
12	50 %		

We take each item with the support ≥ minsup, and output it as a sequence with one item.

Here the output:

- <{1}>
- <{2}>
- <{3}>
- $< {4}>$
- <{5}>
- < {6}>

New Concept: Projection

We need to define a new concept → *Projection*

If we project a sequence $<\{1\},\{2\},\{3\}>$ by a prefix $<\{1\}>$, we take the part of the sequence that follow the prefix. Here $<\{2\},\{3\}>$

Some examples:

```
<\{1\},\{2\},\{1\},\{3\}> by <\{1\}> \rightarrow <\{2\},\{1\},\{3\}> 
<\{3\},\{4\},\{5\}> by <\{3\},\{4\}> \rightarrow <\{5\}> 
<\{1\},\{3,4\},\{5\},\{6\}> by <\{3\}> \rightarrow <\{5\},\{6\}> 
<\{2\},\{3\},\{4\},\{5\},\{6\}> by <\{3\},\{5\}> \rightarrow <\{6\}>
```

→ Projecting a database, means to project every sequence

First we will output the result we found with enough support.

Then we will recursively project the database with every of those items.

Lets take the result we have found so far to make it clearer.

We keep minsup of 75 % (3)

1. Scan Database

Item	Support
1	100 % (4)
2	100 % (4)
3	100 % (4)
4	75 % (3)
5	75 % (3)
6	75 % (3)
7	25 % (1)

2. Output first item

$$<\{1\}> \rightarrow Support : 100 \% (4)$$

3. Project first item (2)

```
<{1},{123},{13},{4},{3}6}>
<{14},{3},{23},{15}>
<{56},{12},{46},{3},
{2}>
<{5},{7},{16},{3},{2},
{3}>
```

Item	Support
1	100 % (4)
2	100 % (4)
3	100 % (4)
4	75 % (3)
5	75 % (3)
6	75 % (3)
7	25 % (1)

1. Scan Again

Item	Support
1	50 % (2)
2	100 % (4)
3	100 % (4)
4	50 % (2)
5	25 % (1)
6	50 % (2)
7	25 % (1)

2. Output the sequence

$$<\{1\},\{2\}> \rightarrow Support:$$
 100 % (4)

3. Project first item (2)

Item	Support
1	50 % (2)
2	100 % (4)
3	100 % (4)
4	50 % (2)
5	25 % (1)
6	50 % (2)
7	25 % (1)

1. Scan again

Item	Support
1	50 % (2)
2	0 % (0)
3	50 % (2)
4	25 % (1)
5	25 % (1)
6	25 % (1)
7	0 % (0)

Operation are over We continue with other items

Item	Support
1	50 % (2)
2	0 % (0)
3	50 % (2)
4	25 % (1)
5	25 % (1)
6	25 % (1)
7	0 % (0)

2. Output the sequence

$$<\{1\},\{3\}> \rightarrow Support:$$
 100 % (4)

3. Project second item(2)

```
<{123},{13},{4},{36}><
<{3},{23},{15}><
<{46},{3},{2}>
<{3},{2},{3}>
```

Item	Support
1	50 % (2)
2	100 % (4)
3	100 % (4)
4	50 % (2)
5	25 % (1)
6	50 % (2)
7	25 % (1)

1. Scan again

Item	Support
1	50 % (2)
2	75 % (3)
3	75 % (3)
4	25 % (1)
5	25 % (1)
6	25 % (1)
7	0 % (0)

2. Output the sequence

$$<\{1\}, \{3\}, \{2\} > \rightarrow Support:$$
 75 % (3)

3. Project first item (2)

Item	Support
1	50 % (2)
2	75 % (3)
3	75 % (3)
4	25 % (1)
5	25 % (1)
6	25 % (1)
7	0 % (0)

Do all recursive projection would take a certain amount of times

We will skip the projection, as the process repeat itself

Pattern	Support (≥ 75%)	Pattern	Support (≥ 75%)
<{1}>	100 %	<{3},{2}>	75 %
<{1},{2}>	100 %	<{3},{3}>	75 %
<{1},{3}>	100 %	<{4}>	75 %
<{1},{3},{2}>	75 %	<{4},{3}>	75 %
<{1},{3},{3}>	75 %	<{5}>	75 %
<{2}>	100 %	<{6}>	75 %
<{2},{3}>	75 %		
<{3}>	100 %		

Question 2: Projection

Considering the database

- 1. What is the result of the projection of < {b}, {f} > on the database?
- 2. In previous sequence, which are not closed and which are maximal?

Pattern	Support (≥ 75%)	Pattern	Support (≥ 75%)
<{1}>	100 %	<{3},{2}>	75 %
<{1},{2}>	100 %	<{3},{3}>	75 %
<{1},{3}>	100 %	<{4}>	75 %
<{1},{3},{2}>	75 %	<{4},{3}>	75 %
<{1},{3},{3}>	75 %	<{5}>	75 %
<{2}>	100 %	<{6}>	75 %
<{2},{3}>	75 %		
<{3}>	100 %		

Here are the closed.

Pattern	Support (≥ 75%)	Pattern	Support (≥ 75%)
<{1}>	100 %	<{3},{2}>	75 %
<{1},{2}>	100 %	<{3},{3}>	75 %
<{1},{3}>	100 %	<{4}>	75 %
<{1},{3},{2}>	75 %	<{4},{3}>	75 %
<{1},{3},{3}>	75 %	<{5}>	75 %
<{2}>	100 %	<{6}>	75 %
<{2},{3}>	75 %		
<{3}>	100 %		

Here are the closed and maximal.

Pattern	Support (≥ 75%)	Pattern	Support (≥ 75%)
<{1}>	100 %	<{3},{2}>	75 %
<{1},{2}>	100 %	<{3},{3}>	75 %
<{1},{3}>	100 %	<{4}>	75 %
<{1},{3},{2}>	75 %	<{4},{3}>	75 %
<{1},{3},{3}>	75 %	<{5}>	75 %
<{2}>	100 %	<{6}>	75 %
<{2},{3}>	75 %		
<{3}>	100 %		

MaxSp: Basic Idea

MaxSP extends the PrefixSpan

A naïve approach would be to keep all sequence in memory and to check every time a new sequence arrives if it is maximal.

That is CloSpan

- → Inefficient
- → Memory consuming

MaxSp: Basic Idea

The question is

How to know if a pattern P is maximal, without maintening pattern in memory?

The solution: Can P be extended by appending items?

→ YES? It isn't a maximal sequential pattern

Two check:

- 1. Maximal backward extension check
- 2. Maximal forward extension check

MaxSp: Maximal backward extension check

With sequence database and minsup = 75 % (3/4)

```
<{1}, {2}, {3}, {4}><
<{1}, {3}, {5}, {2}><
<{1}, {2}, {5, 6}><
<{1}, {4, 5}, {4}>
```

1. Maximal backward extension check

MaxSp: Maximal forward extension check

With the same idea but going in the other direction

MaxSp Algorithm

Concretly, how does one implement MaxSP based on PrefixSpan?

Question 3: Checks