

At this stage of our project we will try to determine the linear regression & significance between different variables in every of our scenarios. Also we will try to represent our data combined with the interval of confidence in a single plot.

At first, we have tried to get results for the scenario of:

### 2011: Births Ratio ~ New House Starts Ratio (aggregated quartiles, divided with population 2011)

However, the significance seems to be low.

Call:

```
lm(formula = ratiobirths ~ ratiohouses, data = test)
```

Residuals:

| Min        | 1Q         | Median    | 3Q        | Max       |
|------------|------------|-----------|-----------|-----------|
| -0.0019917 | -0.0009174 | 0.0002464 | 0.0007987 | 0.0020400 |

Coefficients:

|             | Estimate   | Std. Error | t value | Pr(> t )   |
|-------------|------------|------------|---------|------------|
| (Intercept) | 0.0110886  | 0.0003248  | 34.136  | <2e-16 *** |
| ratiohouses | -0.1891242 | 0.0850545  | -2.224  | 0.0339 *   |

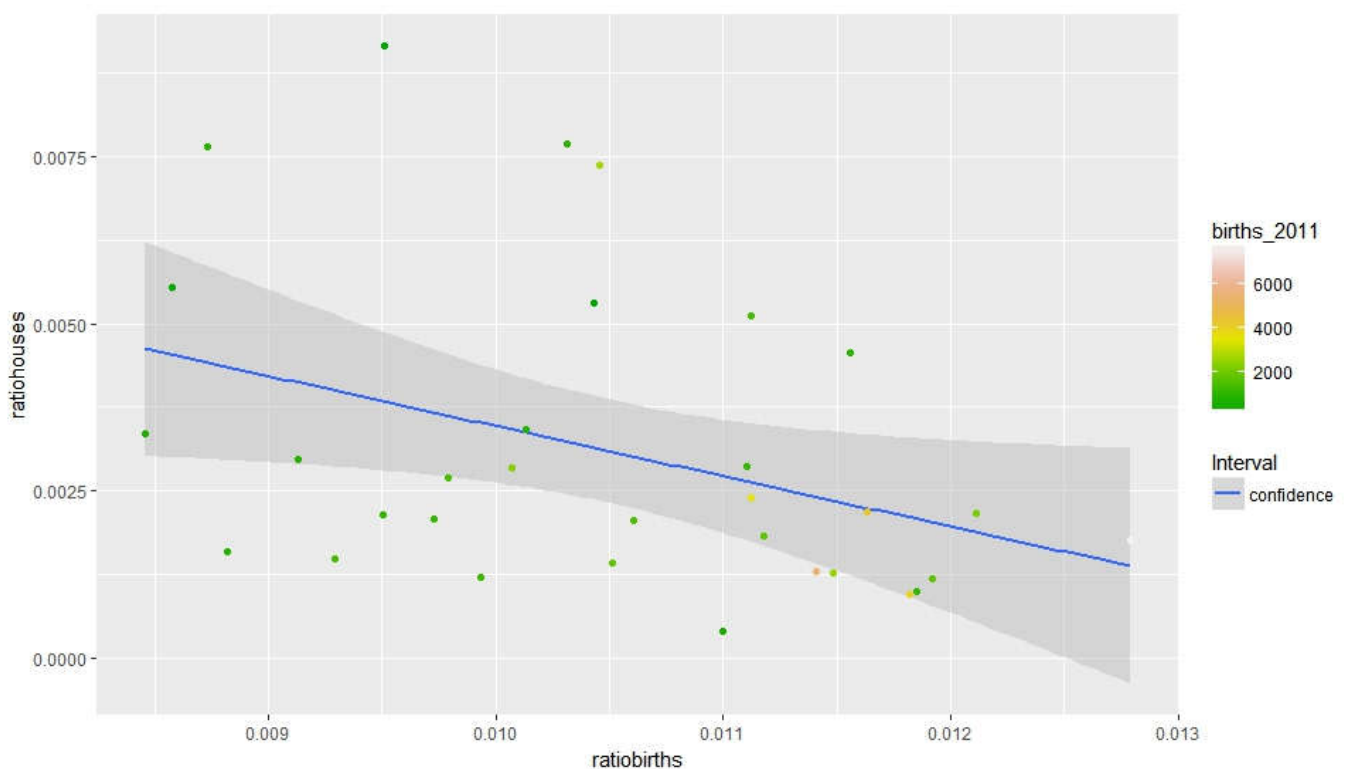
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.001075 on 30 degrees of freedom

Multiple R-squared: 0.1415, Adjusted R-squared: 0.1129

F-statistic: 4.944 on 1 and 30 DF, p-value: 0.03385



Also, the same variables for 2013, seem to have also low significance.

**2013: Births Ratio ~ New House Starts Ratio (aggregated quartiles, divided with population of 2013)**

Call:

```
lm(formula = ratiobirths ~ ratiohouses, data = test)
```

Residuals:

|  | Min        | 1Q         | Median    | 3Q        | Max       |
|--|------------|------------|-----------|-----------|-----------|
|  | -0.0021394 | -0.0006743 | 0.0001916 | 0.0008032 | 0.0021240 |

Coefficients:

|             | Estimate  | Std. Error | t value | Pr(> t )   |
|-------------|-----------|------------|---------|------------|
| (Intercept) | 0.0097650 | 0.0004554  | 21.443  | <2e-16 *** |
| ratiohouses | 0.1286290 | 0.1408104  | 0.913   | 0.368 null |

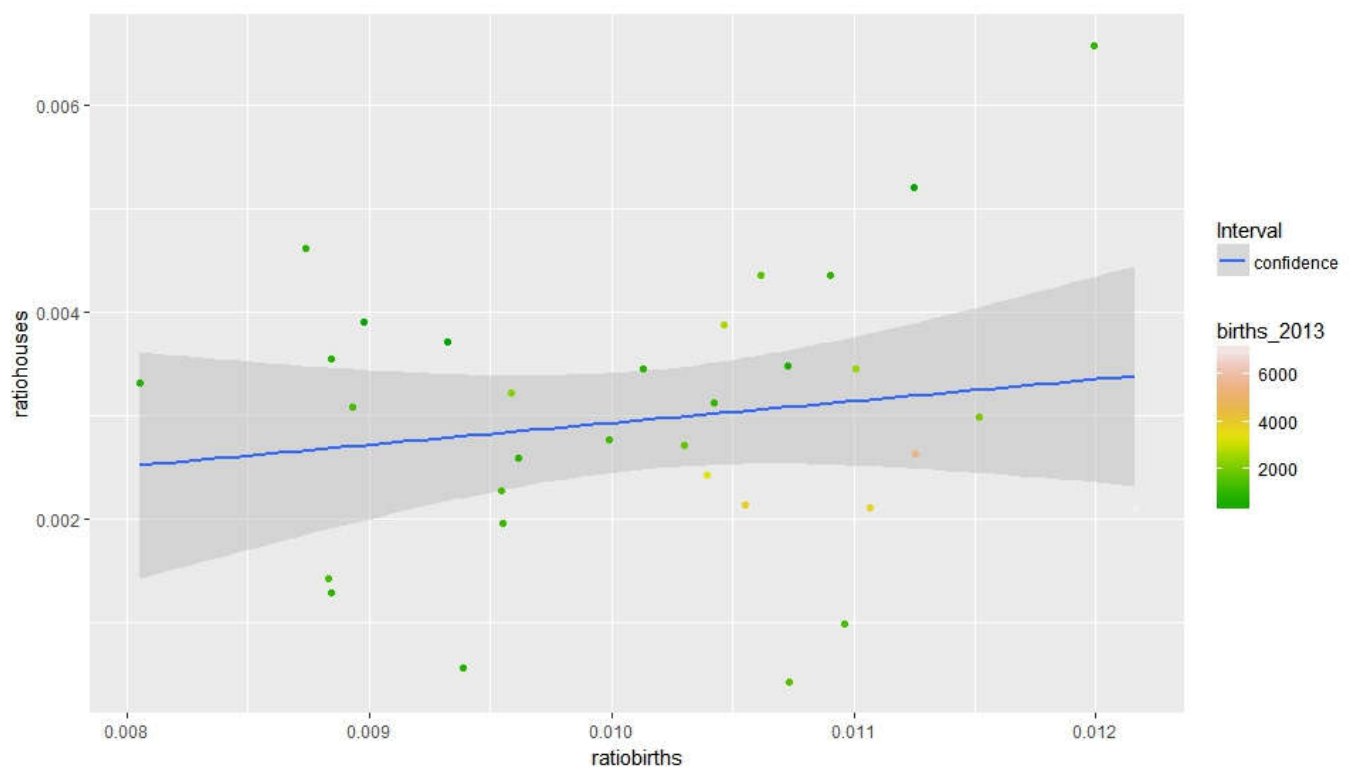
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.001033 on 30 degrees of freedom

Multiple R-squared: 0.02706, Adjusted R-squared: -0.005369

F-statistic: 0.8345 on 1 and 30 DF, p-value: 0.3683



## But why there is a serious difference in the slope of the two linear models between years 2011, 2013?

- From our data, we can see that there was a rise in house building starts in 2013 compared to 2011. This might be the reason that the slope has become positive.

| 2013         |             |         | 2011            |                 |
|--------------|-------------|---------|-----------------|-----------------|
| ratiohouses  | ratiobirths | pop2011 | ratiobirths2011 | ratiohouses2011 |
| 0.0034614876 | 0.011009821 | 222460  | 0.011723456     | 0.0012991100    |
| 0.0038871863 | 0.010462816 | 253650  | 0.010624877     | 0.0074906367    |
| 0.0019692149 | 0.009553702 | 116200  | 0.009939759     | 0.0012220310    |
| 0.0033162976 | 0.008052243 | 88930   | 0.008377375     | 0.003284606     |
| 0.0026381652 | 0.011254257 | 477940  | 0.011633259     | 0.0013181571    |
| 0.0034906396 | 0.010725429 | 51500   | 0.010951456     | 0.0004077670    |

Regarding our second scenario, the results are presented below:

## 2011: Cannabis new clients presenting at specialist drug treatment services ratio ~Number of degree holders ratio (divided with population of 2011)

For our bad luck, slope has low significance

Call:

```
lm(formula = cannabISRratio ~ degreeeratio, data = test)
```

Residuals:

| Min       | 1Q        | Median    | 3Q       | Max      |
|-----------|-----------|-----------|----------|----------|
| -0.036962 | -0.022061 | -0.007906 | 0.011441 | 0.102306 |

Coefficients:

|              | Estimate   | Std. Error | t value | Pr(> t )      |
|--------------|------------|------------|---------|---------------|
| (Intercept)  | 0.0870389  | 0.0186883  | 4.657   | 0.0000657 *** |
| degreeeratio | -0.0016528 | 0.0008366  | -1.976  | 0.0578 .      |

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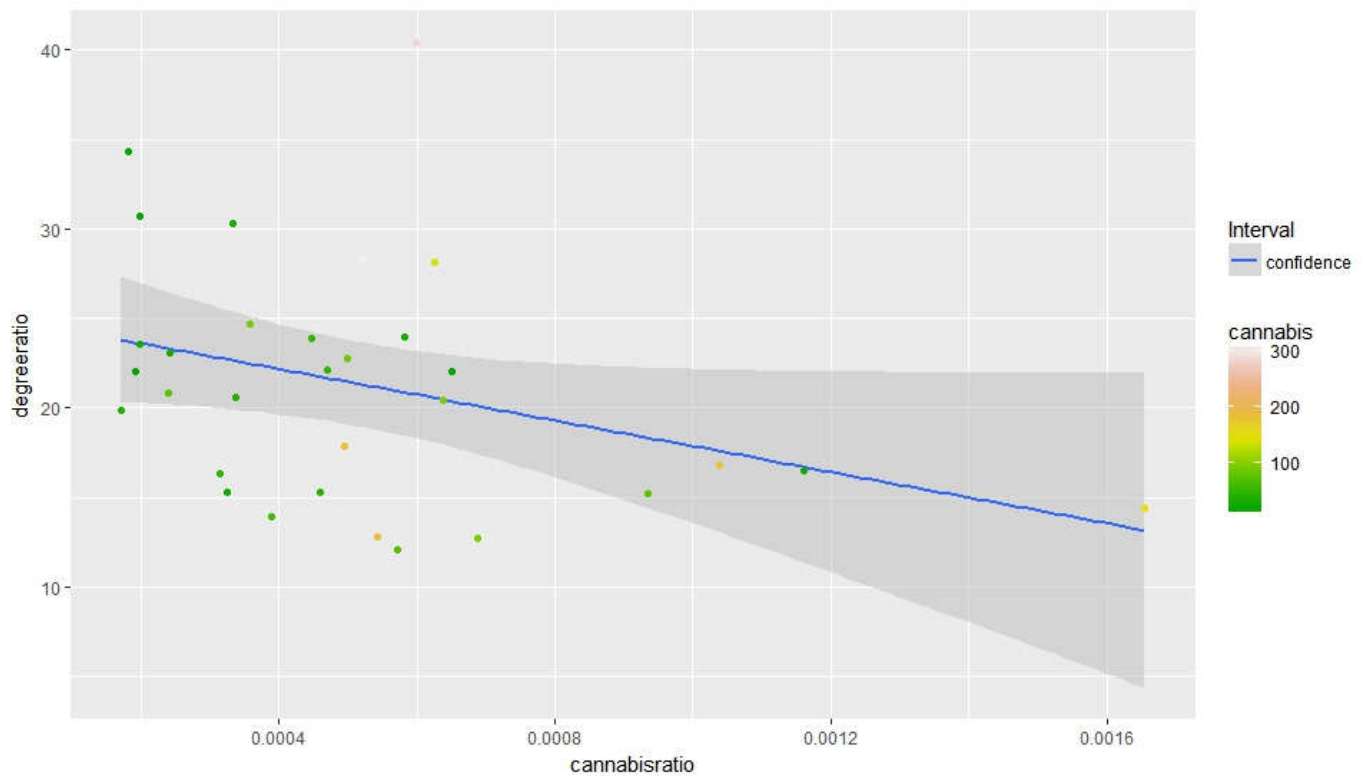
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.03089 on 29 degrees of freedom  
(1 observation deleted due to missingness)

Multiple R-squared: 0.1186, Adjusted R-squared: 0.08824

F-statistic: 3.903 on 1 and 29 DF, p-value: 0.05778

The plot of cannabis client ratio – Number of degree holders ratio.



To sum up, we realize that both of our previous scenarios might have been good ideas to examined, but in the end, **they didn't have a serious significance in their linear models.**

For this reason we had to find this kind of scenario, which it could provide us two variables that can have a serious significance in a linear model.

**Finally, we have decided to use as dependent variable the "Total Labour Costs per Head" , as we believe that is a serious indicator which can have an effect on many other variables.**

**We have tried several combinations with other variables, in order to find strong significance.**

**Below you can find a list of them\*:**

|  |                                      |
|--|--------------------------------------|
| <b>Total Labour Costs per Head with:</b> | <b>Degree Holders ratio</b>          |
|  | <b>Employment/Unemployment ratio</b> |
|  | <b>Total Earnings median</b>         |
|  | <b>Smokers percent</b>               |
|  | <b>Pay Gap Ratio</b>                 |

***\*In the annex of this document you could find more analysis on each variable***

**After several trials we have achieved a high significance with the variable:**

**Business Births per year (confirmed with VAT & PAYE registrations)**

**2011: Total Labour Costs per Head ~ Business Births (divided with population of 2011)**

Call:

```
lm(formula = labourratio2011 ~ registratio2011, data = test)
```

Residuals:

|  | Min        | 1Q         | Median    | 3Q        | Max       |
|--|------------|------------|-----------|-----------|-----------|
|  | -0.0047121 | -0.0016446 | 0.0004222 | 0.0012095 | 0.0106267 |

Coefficients:

|                 | Estimate  | Std. Error | t value | Pr(> t )   |     |
|-----------------|-----------|------------|---------|------------|-----|
| (Intercept)     | -0.006862 | 0.002288   | -2.998  | 0.00541    | **  |
| registratio2011 | 3.529811  | 0.593758   | 5.945   | 0.00000163 | *** |

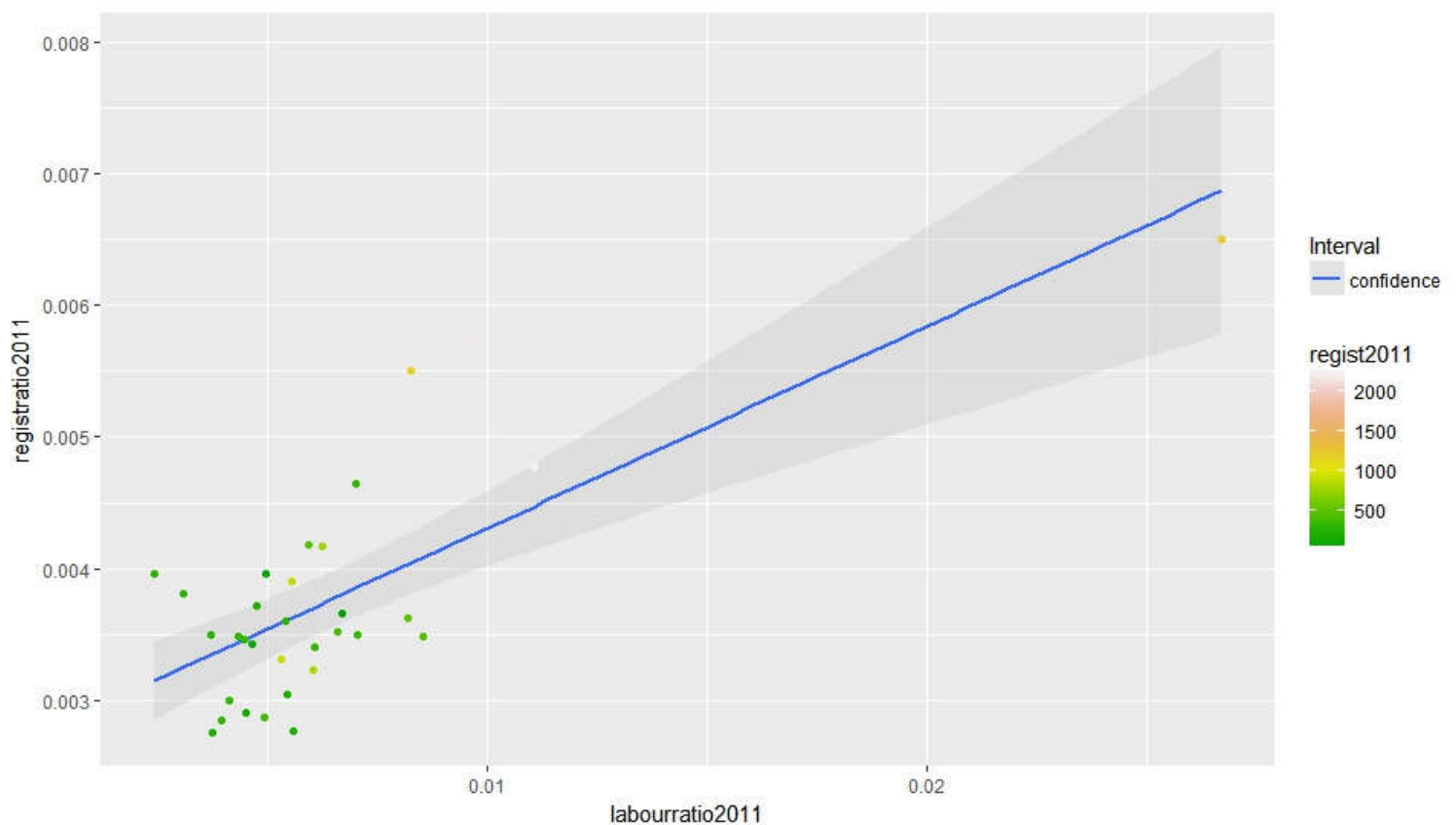
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.002858 on 30 degrees of freedom

Multiple R-squared: **0.5409**, Adjusted R-squared: 0.5256

F-statistic: 35.34 on 1 and 30 DF, p-value: 0.000001627



### **2013: Total Labour Costs per Head ~ Business Births (divided with population of 2013)**

Call:

```
lm(formula = labourratio2013 ~ registratio2013, data = test)
```

Residuals:

|  | Min        | 1Q         | Median    | 3Q        | Max       |
|--|------------|------------|-----------|-----------|-----------|
|  | -0.0047400 | -0.0017672 | 0.0003785 | 0.0015150 | 0.0124289 |

Coefficients:

|                 | Estimate  | Std. Error | t value | Pr(> t ) |     |
|-----------------|-----------|------------|---------|----------|-----|
| (Intercept)     | -0.009070 | 0.002657   | -3.414  | 0.00186  | **  |
| registratio2013 | 4.226564  | 0.693581   | 6.094   | 1.07e-06 | *** |

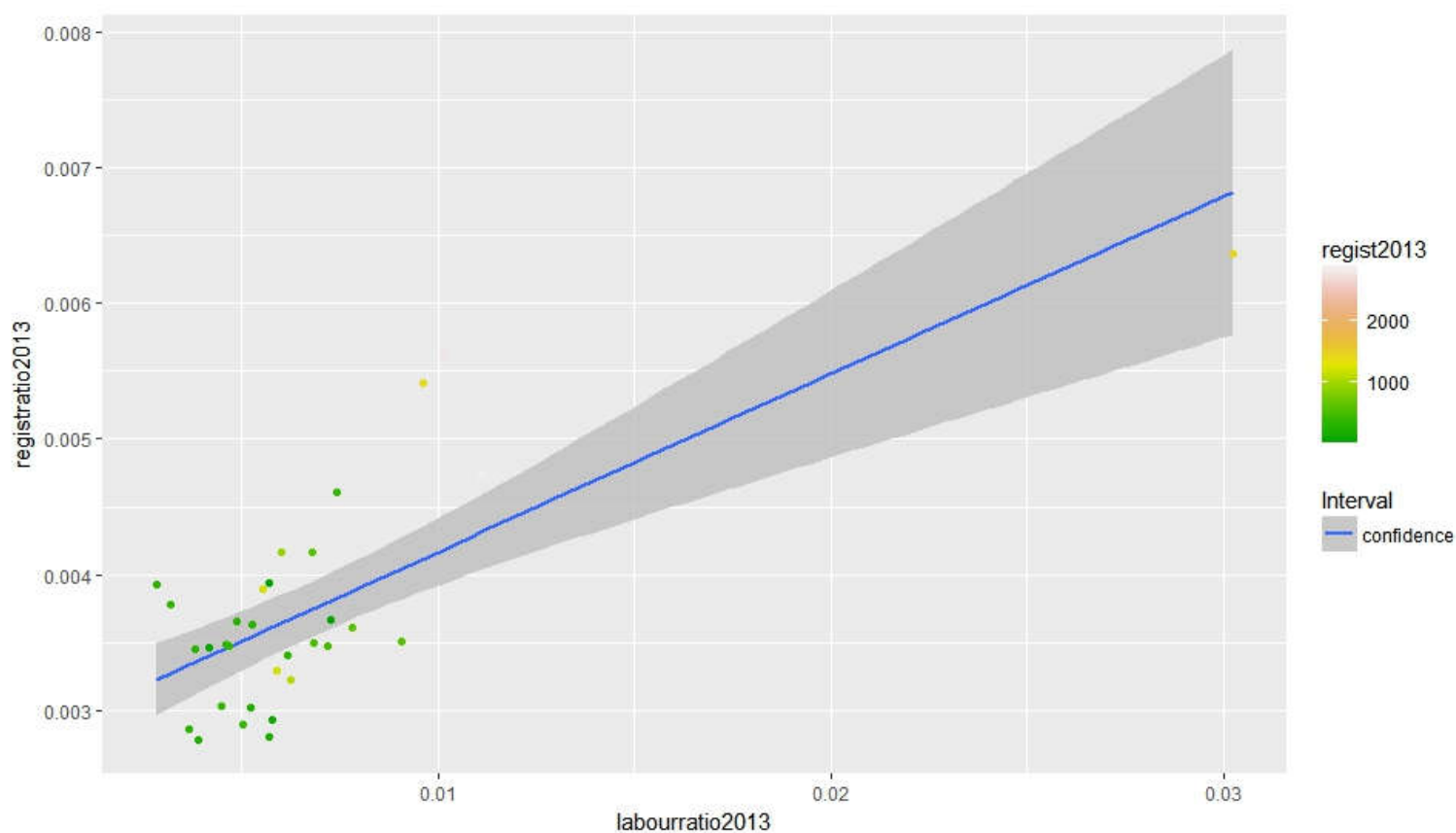
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.00321 on 30 degrees of freedom

Multiple R-squared: **0.5531**, Adjusted R-squared: 0.5382

F-statistic: 37.13 on 1 and 30 DF, p-value: 1.073e-06



## Findings:

From the final two linear models we can assume that the labour costs, on different territories of Scotland, are related positively with the number of new companies.

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### Annex: Total Labour Costs per Head trials with...

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#### 1) Unemployment

Call:

```
lm(formula = labourcosts ~ unemployment, data = test)
```

Residuals:

| Min   | 1Q    | Median | 3Q   | Max   |
|-------|-------|--------|------|-------|
| -5064 | -2311 | -1149  | 1614 | 20846 |

Coefficients:

|              | Estimate | Std. Error | t value | Pr(> t )         |
|--------------|----------|------------|---------|------------------|
| (Intercept)  | 20918.49 | 2765.81    | 7.563   | 0.0000000196 *** |
| unemployment | 54.42    | 345.17     | 0.158   | 0.876            |

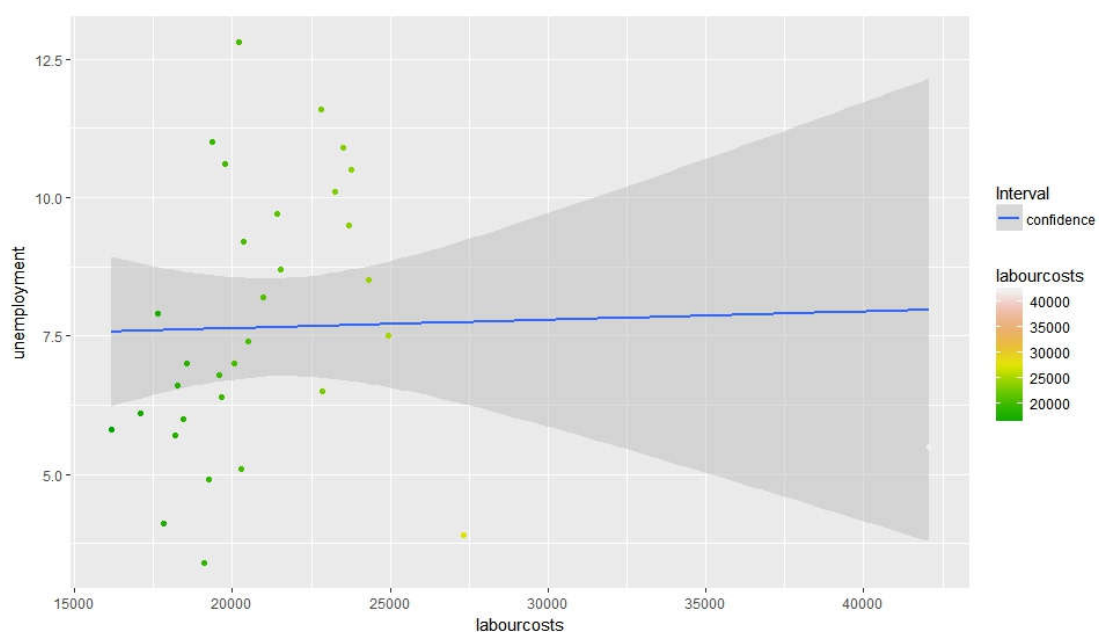
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4636 on 30 degrees of freedom

Multiple R-squared: 0.0008277, Adjusted R-squared: -0.03248

F-statistic: 0.02485 on 1 and 30 DF, p-value: 0.8758



## 2) Degree Holders Ratio

Call:

```
lm(formula = labour2011 ~ degreeratio2011, data = test)
```

Residuals:

| Min     | 1Q      | Median | 3Q     | Max     |
|---------|---------|--------|--------|---------|
| -6143.2 | -2362.4 | -669.1 | 1486.4 | 20016.4 |

Coefficients:

|                 | Estimate | Std. Error | t value | Pr(> t )        |
|-----------------|----------|------------|---------|-----------------|
| (Intercept)     | 19176.6  | 2706.8     | 7.085   | 0.000000706 *** |
| degreeratio2011 | 102.2    | 122.3      | 0.836   | 0.41            |

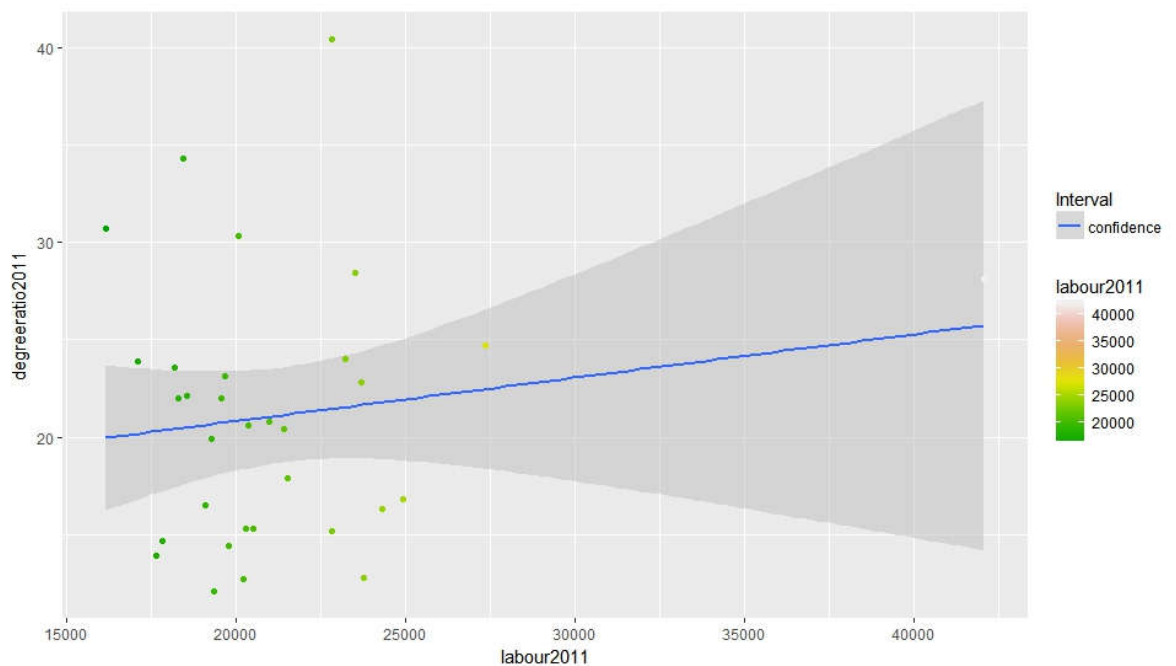
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4584 on 30 degrees of freedom

Multiple R-squared: 0.02275, Adjusted R-squared: -0.009824

F-statistic: 0.6984 on 1 and 30 DF, p-value: 0.4099





### 3) Employment Ratio

Call:

```
lm(formula = labour2011 ~ employmentratio, data = test)
```

Residuals:

| Min     | 1Q      | Median | 3Q    | Max     |
|---------|---------|--------|-------|---------|
| -5300.1 | -2199.8 | -871.5 | 877.6 | 20255.3 |

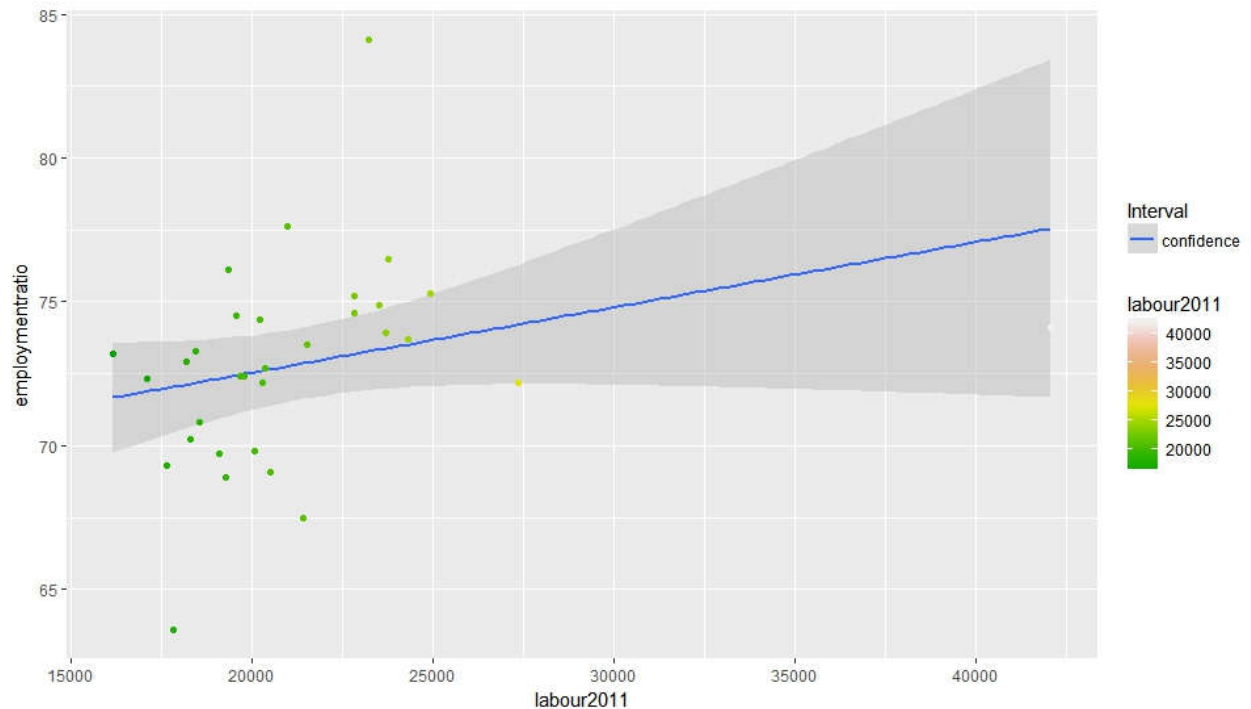
Coefficients:

|                 | Estimate | Std. Error | t value | Pr(> t ) |
|-----------------|----------|------------|---------|----------|
| (Intercept)     | -6065.2  | 16386.5    | -0.370  | 0.714    |
| employmentratio | 376.2    | 224.7      | 1.674   | 0.105    |

Residual standard error: 4435 on 30 degrees of freedom

Multiple R-squared: 0.08543, Adjusted R-squared: 0.05495

F-statistic: 2.802 on 1 and 30 DF, p-value: 0.1045



#### 4) Total Earning Ratio

Call:

```
lm(formula = labour2011 ~ earnmedian, data = test)
```

Residuals:

| Min     | 1Q      | Median | 3Q     | Max     |
|---------|---------|--------|--------|---------|
| -7158.8 | -2003.9 | -316.6 | 1506.5 | 13081.9 |

Coefficients:

|             | Estimate  | Std. Error | t value | Pr(> t )     |
|-------------|-----------|------------|---------|--------------|
| (Intercept) | -10924.82 | 7492.93    | -1.458  | 0.155226     |
| earnmedian  | 68.14     | 15.77      | 4.321   | 0.000157 *** |

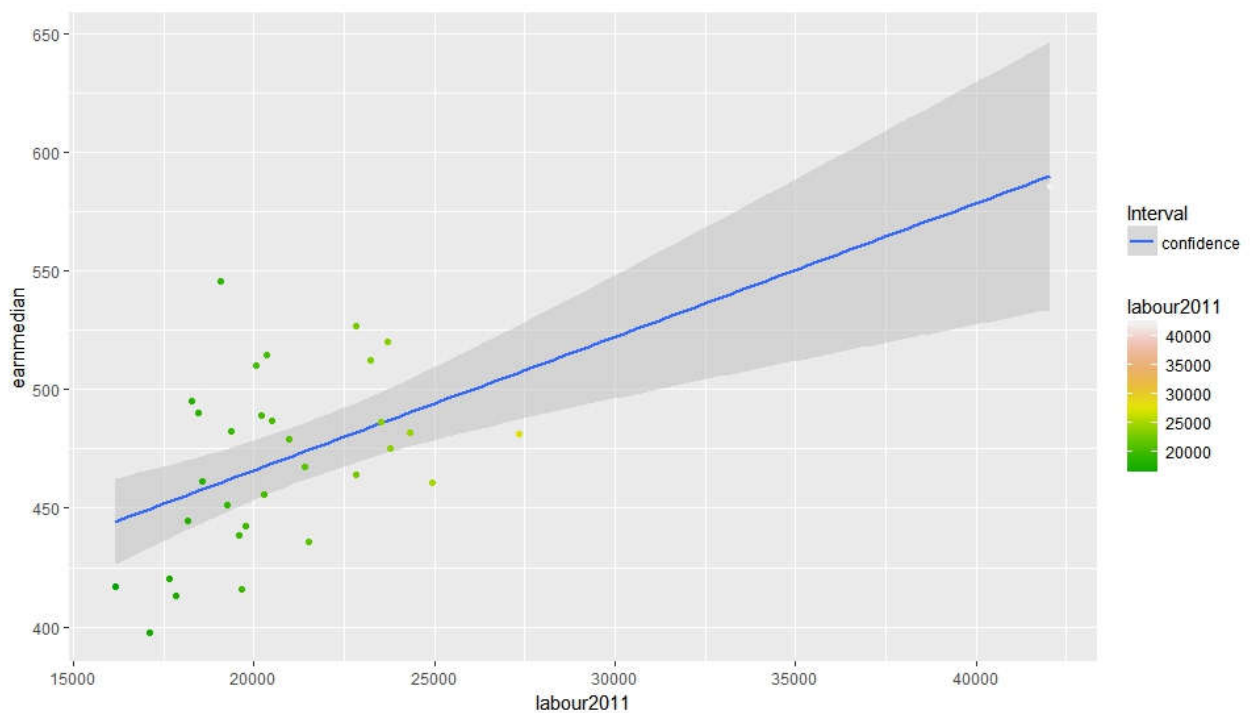
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3641 on 30 degrees of freedom

Multiple R-squared: **0.3837** , Adjusted R-squared: 0.3631

F-statistic: 18.67 on 1 and 30 DF, p-value: 0.0001568



## 5) Smokers percent

Call:

```
lm(formula = labour2012 ~ smoking2012percent, data = test)
```

Residuals:

| Min   | 1Q    | Median | 3Q   | Max   |
|-------|-------|--------|------|-------|
| -4680 | -2624 | -1441  | 1093 | 21617 |

Coefficients:

|                    | Estimate | Std. Error | t value | Pr(> t )     |
|--------------------|----------|------------|---------|--------------|
| (Intercept)        | 18174.5  | 4276.3     | 4.250   | 0.000191 *** |
| smoking2012percent | 175.2    | 191.8      | 0.913   | 0.368263     |

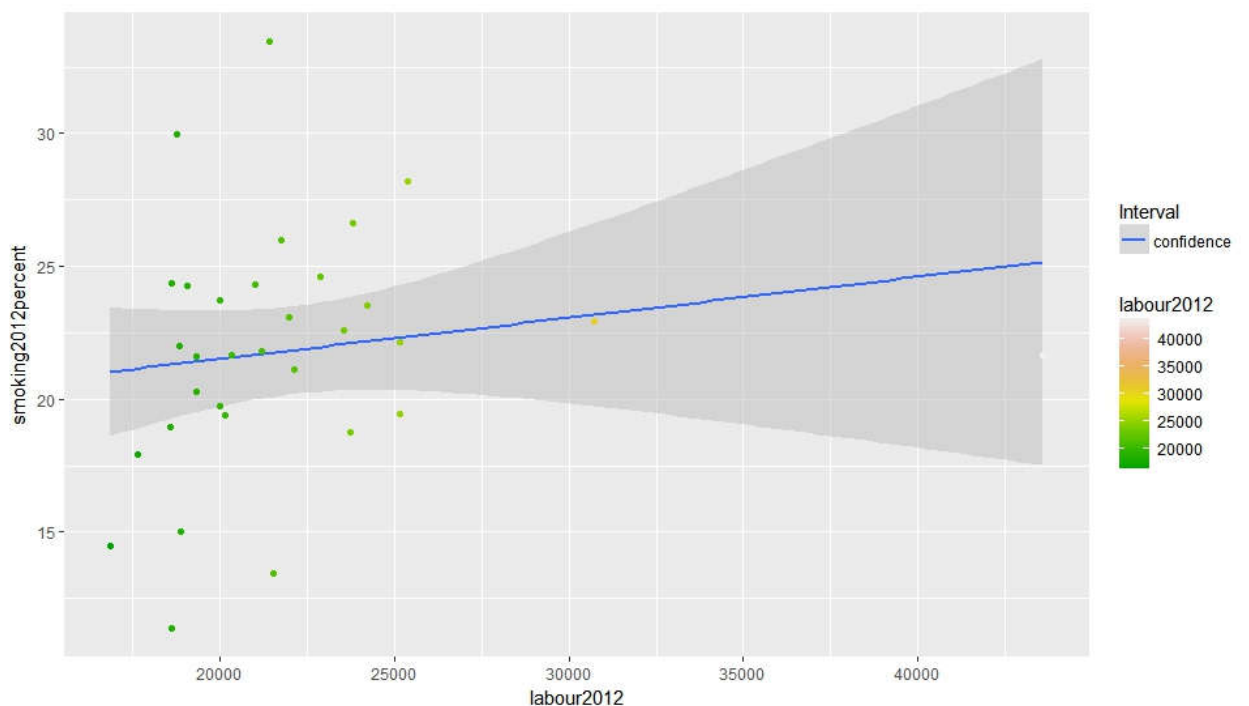
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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4893 on 30 degrees of freedom

Multiple R-squared: 0.02706, Adjusted R-squared: -0.005368

F-statistic: 0.8345 on 1 and 30 DF, p-value: 0.3683



## 6) Pay Gap Ratio

Call:

```
lm(formula = labour2011 ~ paygap2010ratio, data = test)
```

Residuals:

| Min   | 1Q    | Median | 3Q   | Max   |
|-------|-------|--------|------|-------|
| -4702 | -2734 | -1317  | 2095 | 19035 |

Coefficients:

|             | Estimate | Std. Error | t value | Pr(> t )           |
|-------------|----------|------------|---------|--------------------|
| (Intercept) | 20346.7  | 1334.1     | 15.251  | 0.0000000000000036 |
| ***         |          |            |         |                    |

|                 |       |       |       |       |
|-----------------|-------|-------|-------|-------|
| paygap2010ratio | 176.5 | 125.2 | 1.409 | 0.171 |
| ---             |       |       |       |       |

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4676 on 25 degrees of freedom

(5 observations deleted due to missingness)

Multiple R-squared: 0.07358, Adjusted R-squared: 0.03652

F-statistic: 1.985 on 1 and 25 DF, p-value: 0.1711

