

# Independent Study Report - CB + DMPs

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## 1 Introduction

In this independent study, I focused my attention to two related approaches to motor control: Control Basis (CB) and Dynamic Movement Primitives (DMPs). CB provides a way of generating complex movement from a sequential composition of simple primitives, while DMPs is a parametric model that allows the reproduction and generalization of demonstrations.

One of the limitations of CB is that it requires convergence of a given component before the next one can begin to execute, which leads to slow execution with little generalization capabilities. By using these movements as demonstrations, DMPs could reproduce these controllers with a high degree of flexibility. In this work, I study the feasibility of a hybrid approach in which CB provides an unsupervised method for generating movements and DMPs generalize and improves the demonstrations.

## 2 Control Basis

The Control Basis is a closed-loop method that allows to create complex behavior by combining feedback control elements. In this framework, movements are generated by taking into account the set of available input resources  $\sigma$  (sensors), and output resources  $\tau$  (actuators). Every action is limited by a "subject to" constraint, which restricts the control actions such that new actions do not draw the system away from achieving higher priority objectives. A control policy, then, is a sequence of controllers that is learned via RL subject to input and output resources.

## 3 Dynamic Movement Primitives

Dynamic Movement Primitives (DMPs) provide a general approach for learning robotic motor skill from demonstration. Given a sample trajectory with start state  $x_0$  and goal state  $g$ , a DMP generates a trajectory by integrating the following equations:

$$\begin{aligned}\tau\dot{v} &= K(g - x) - Dv - K(g - x_0)s + Kf(s) \\ \tau\dot{x} &= v\end{aligned}$$

In these equations,  $\tau$  refers to a time scaling term,  $K$  and  $D$  refer on system specific constant that work as in a PD controller and  $f(s)$  corresponds to a non-linear function composed of several Gaussian basis functions:

$$f(s) = \frac{\sum_i w_i \psi_i(s)s}{\sum_i \psi_i(s)}$$

where  $\psi_i(s) = \exp(-h_i(s - c_i)^2)$  are the basis functions with center  $c_i$  and width  $h_i$ .  $w_i$  are the parameters to be found to minimize the objective function  $J$ .

The variable  $s$  is a phase variable which encompasses the duration of the trajectory and monotonically decreases from 1 to 0. This variable obtained by the canonical system:

$$\tau\dot{s} = -\alpha s$$

When observing a demonstration, a movement  $x(t)$  is recorded and from that its derivative  $v(t)$  and  $\dot{v}$  are obtained. Using this, we can compute the target function:

$$f_{target}(s) = \frac{\tau\dot{v} + Dv}{K} - (g - x) + (g - x_0)s$$

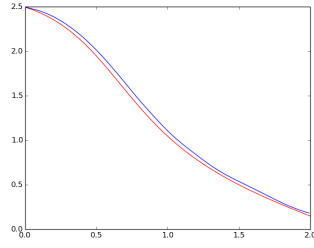
and solve the objective function  $J = \sum_s (f_{target}(s) - f(s))^2$  via gradient descent or least-squares.

Once trained, a new trajectory can be generated by setting  $s$  to 1, updating the positions and velocities and intergrating the canonical system to obtained the new  $s$ .

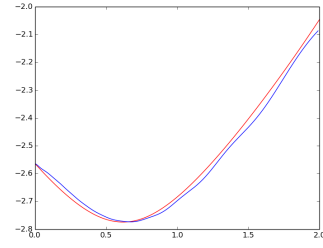
Figure 1 shows the plot of DMPs for a 2-link robotic arm simulator. The x-axis is time measured in seconds, while the y-axis measures the angular position in radians. The line in red is the trajectory of the demonstration, while the line in blue is the approximation generated from the DMP. In this case, the DMPs are set to the same initial and goal positions, so as to recreate the same movement.

## 4 Combining CB and DMPs

As discussed in previous sections, the Control Basis and DMPs provide the potential to a hybrid approach where CB generate demonstrations without the need of human supervision and the DMPs generalize that movement in space and time. In this section, I show some preliminary results showcasing the feasibility of combining these methods.

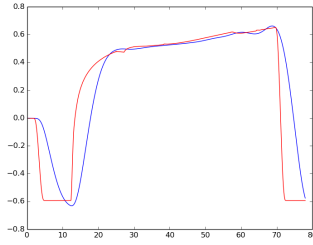


(a) DMP for joint 1

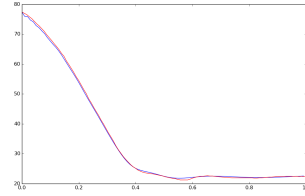


(b) DMP for joint 2

Figure 1: Plot of demonstrations and their corresponding DMP



(a) Trajectory for right shoulder joint.

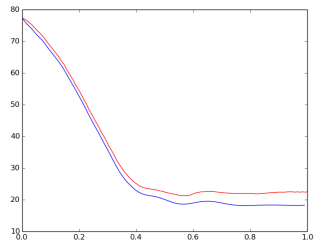


(b) Trajectory for right elbow joint.

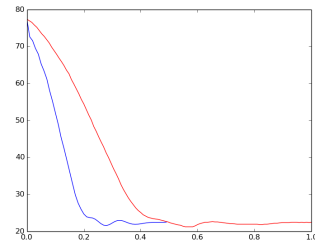
Figure 2: Plot of uBot task trajectories for picking up a box.

Figure 2 shows the trajectory of 2 joints for a simulated task on the uBot. The task consists of picking up a box, lifting it and putting it back down. As we can see, even though the trajectory of the DMP learned in 2b is a similar recreation of the demonstration, the trajectory in 2a is a much smoother trajectory than the one demonstrated.

Figure 3 shows the generalization capabilities of the Control Basis and DMP hybrid framework. Figure 3a shows the demonstration for one of the joints in the aforementioned task, where the goal position has been offset by 5 degrees from the original demonstration. Figure 3b shows the plot of the demonstrated trajectories scaled in time. As we can see, both cases maintain the general shape of the demonstrated trajectory, while achieving different goals or time constraints.



(a) Generalization in joint space.



(b) Generalization in time.

Figure 3: Demonstration of generalization capabilities of CB+DMP.