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November 23, 2015

A man in a dark blue suit stands with his back to the camera, looking at a large blackboard filled with complex mathematical formulas, diagrams, and charts. The blackboard is covered in white chalk drawings, including various graphs, equations, and symbols, representing a state of deep thought and problem-solving.

## Abstract

We have implemented the two sorting algorithms, insertion sort and bininsertion sort. Bininsertion sort is a variation of insertion sort where you use a binary search to find the place for any new number. The regular insertion sort uses linear search instead of binary search. We also implemented a merge sort that divides the array into sub-arrays of size equal or less than  $k$  ( $k$  is a positive integer). The sub-arrays are then sorted by insertion sort or bininsertion sort. Finally we merge the sorted sub-arrays back together using standard merge sort algorithm.

We compared the run-times when using insertion sort and bininsertion sort. We found that insertion sort's runtime increases logarithmically while the bininsertion sort takes less time, it also resembles a logarithmic function but it increases much slower. The runtime of insertion sort increases by a factor of two for each time  $k$  has been doubled. This is done because of the merge sort that splits the array in half and gives insertion sort twice the amount of work. In small array sizes, insertion sort may be faster than bininsertion sort. These cases have an array of a very small size. Both algorithms run in  $\theta(nk + n \lg(\frac{n}{k}))$  worst case time. Generally, bininsertion sort is much faster than insertion sort in average case.

## CONTENTS

<b>1</b>	<b>Introduction</b>	<b>3</b>
<b>2</b>	<b>Language</b>	<b>3</b>
<b>3</b>	<b>Implementation</b>	<b>3</b>
<b>4</b>	<b>Test procedure</b>	<b>3</b>
<b>5</b>	<b>Result</b>	<b>4</b>
5.1	Insertion sort . . . . .	5
5.2	Bininsertion sort . . . . .	5
5.3	Graphs . . . . .	6
5.3.1	Test 1, K 1-1000 . . . . .	6
5.3.2	Test 2, K 100-50000 . . . . .	6
5.3.3	Test 3, K 1-524288 . . . . .	7
<b>6</b>	<b>Discussion</b>	<b>8</b>

## 1 INTRODUCTION

We began by looking into how the two algorithms would be implemented. Then both algorithms were then implemented in our language of choice, Python. The first implementation was sloppy and slow, but after a few improvements to the code (reducing function calls and comparisons) we managed to get a faster and better implementation overall while keeping the functionality of the algorithms intact.

## 2 LANGUAGE

We choose Python as our language of choice because of the easy implementation of array splitting. Another contributing factor was the general easy to use syntax. We are aware of the fact that it is ugly compared to other languages due to the fact that there is little structure in the code syntax itself. Although we decided to choose this language we are also aware of it's drawbacks, such as: slow execution time compared to C++ or java, low recursion depth compared to other languages and the lack of variable declarations (implies more error checks). All together we decided that Python was a good choice due to the big advantages the array splitting gives in terms of easy implementation.

## 3 IMPLEMENTATION

By following the convention of merge sort, we recursively split the array into  $k$ -sized segments by splitting the array in half and continued until each segment is of size  $k$  or less. These segments are then sorted using either insertionsort or binsort. The sorted segments are then merged using the standard merging algorithm.

## 4 TEST PROCEDURE

We decided to run the first tests several times and take the average values from the results of each  $k$  and array size. With a larger  $k$  and array we ran the tests fewer times to reduce the total runtime.

The test we conducted were based a single array generated for each arraysize with the numbers in the array randomly generated from 0 to  $10^6$ . If we would have used a fixed array we would get the same results each run. We wanted to test different arrays and compare the average to get as close real-life results as possible.

## 5 RESULT

We decided to do fore tests one with a array of size 1000 wher the  $k$  values ( $k$  is a pisetiv integer) is 1 – 1000 with the interval 1 (graf 5.2). The second test were with a array size 50,000 and the  $k$  value were 100 – 50,000 with the interval 1000 (graf 5.3). The therd thest whare with a array size 200,000 and the  $k$  values were 1 – 200,000 with logaritmic intervals (graf 5.1). the final test

where with a array size of 2,000,000 and the  $k$  value where betwen 1 – 500,000 with a logaritmic intervals (graf 5.4)

Ass we can see in graf 5.3 is the time increasing in steps. the time rises is hapening in logaritmig intervals. Bouth insertionsort and binsortionsort increases thime in the same plases but how mutch thay arr rising differs.

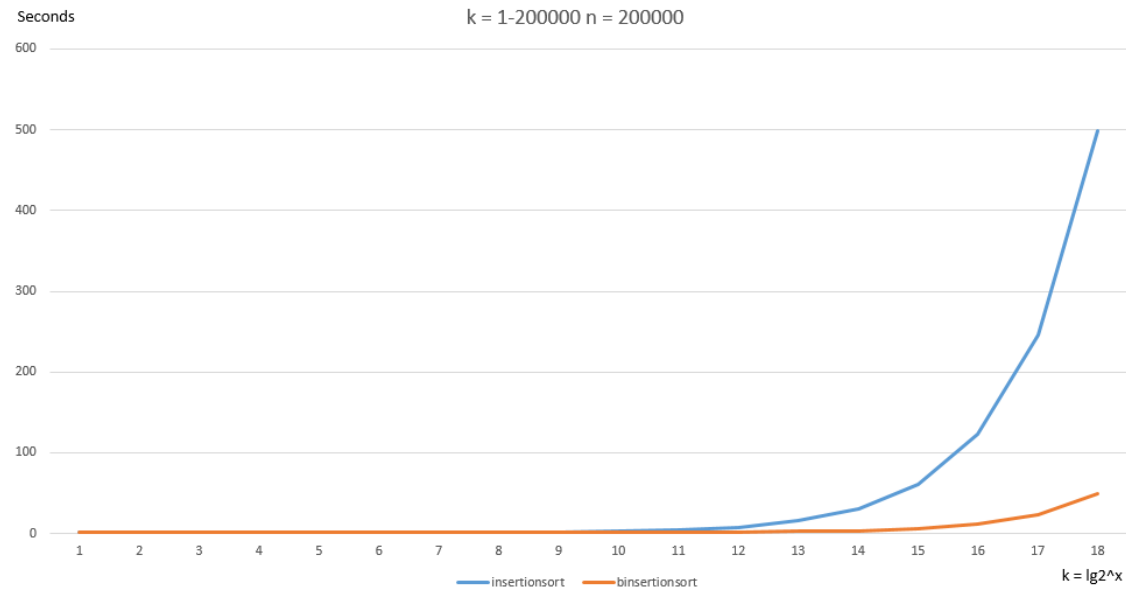


Figure 5.1: A graf of a test whith a array size of 200,000 and the  $k$  walue warius between 1 and 200,000 when the time metserd for evry logaritmic increase of  $k$ .

In graf 5.1 wher  $k$  is increasing logarity can we se that the time is increasing exponential wen  $k$  grows big.

Bouth algoritms is increasing wen  $k$  passes a outer power of 2. This id done becos of the merge thet first splits the arrays. Wen  $k$  increase ower a power of 2 the mearge nedade to split the arrat ounne mor time withe mend it get tow arrays of the size of the prevues. Obesly tow arrays take the double time of one.

Sense it is the algoritms insertionsort and binsortionsort that take time is the time barly increasing wen the array size increse and the  $k$  value is low. When the  $k$  value gets higer the array that reatche the algoritms (insertionsort and binsortionsort)is biger ant it tace time for the algoritms to sovel the problem.

## 5.1 INSERTIONSORT

From the grafes is it clear that insertionsort gets rely bad wen deling wid huge data sets. From graf 5.1 and graf 5.4 is it clear that the time get redicules hige.

A intresting thing that can be sen clearly in graf 5.3 thet the time dubels in logaritmi intervals. This geiv as the nice star loging graf.

## 5.2 BINSERTIONSORT

Ass insertionsort seam binsortionsort to incrise i logaritmik intervals, but binsortionsort do not increse as mutch. Sens binsortionsort splitt the array ín tow multible times is it lodgik tht it incresees wen an pasing the line of a power of 2, becos it the neds to split the array in tow equal long arrays that prevues wer the howl array.

## 5.3 GRAPHS

### 5.3.1 TEST 1, K 1-1000

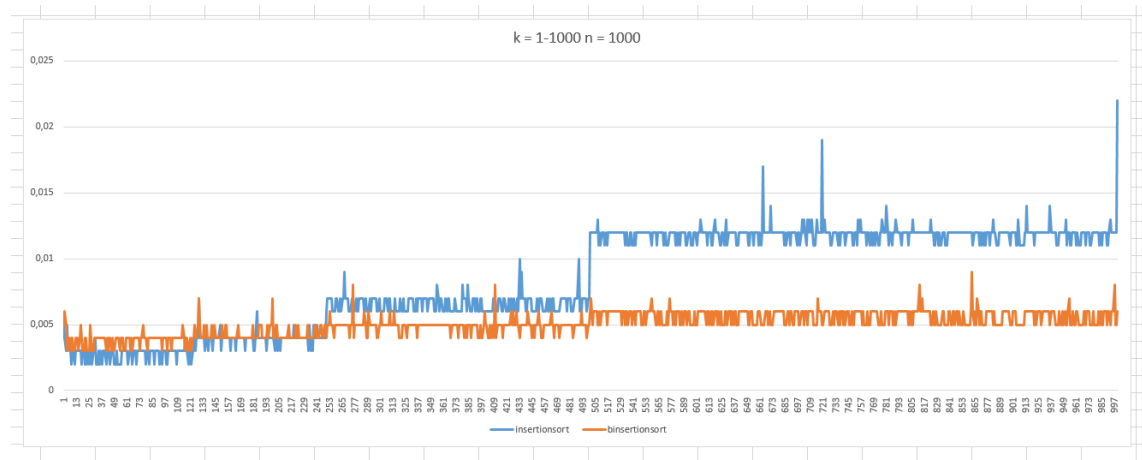


Figure 5.2: A graf of a test whith a array size of 50000 and the  $k$  value wariius between 100 and 50000 wher the time metserd ouns evry 1000.

Here we see that small values are in some cases worse with binsortionsort. There is however a volume in witch binsortionsort switches as the better choise than regular insertionsort. Although the arraysize is only 1000, we see the small difference. We decided to run even bigger arrays with values from 1 to 2000000.

### 5.3.2 TEST 2, K 100-50000

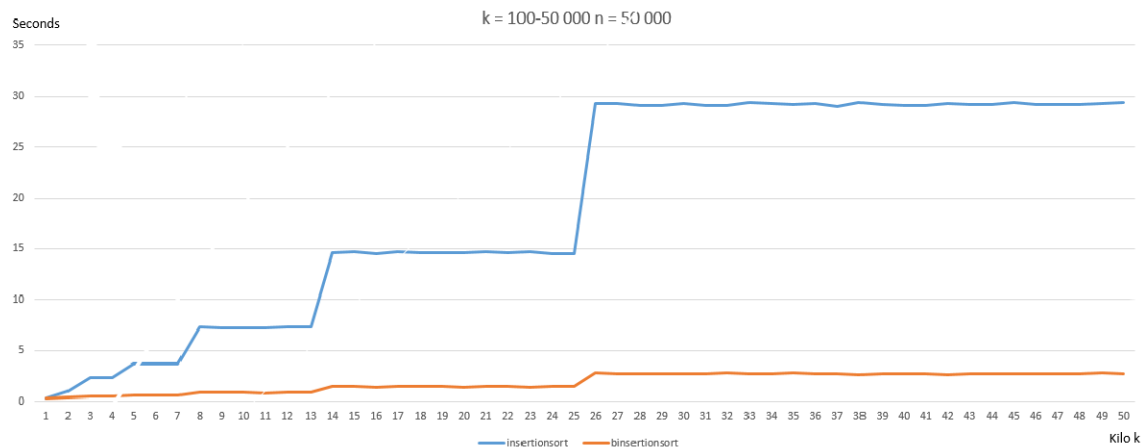


Figure 5.3: A graf of a test whith a array size of 50000 and the  $k$  value wariius between 100 and 50000 wher the time metserd ouns evry 1000.

Here we can figure 5.3 ease see the increase of both algorithms and the difference of the two. while insertionsort quickly increases, bininsertionsort doesn't increase nearly as much. This is when  $K=100-50000$  and an array of size 50000.

### 5.3.3 TEST 3, K 1-524288

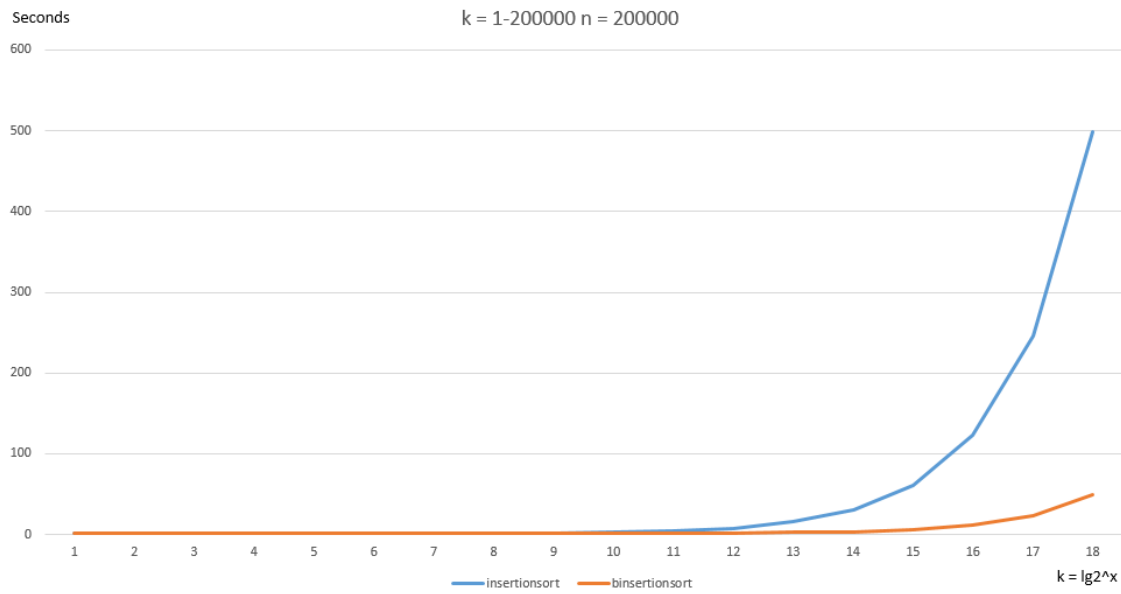


Figure 5.4: A graf of a test whith a array size of 200000 and the  $k$  value wariius between 1 and 524288.

K	insertionsort	binsortionsort
1	15.2799999714	16.0329999924
2	13.4079999924	13.9700000286
4	12.1639997959	13.2150001526
8	11.5429999828	12.6840000153
16	10.5320000648	12.4670000076
32	10.8150000572	13.3180000782
64	11.7960000038	14.0509998798
128	14.1679999828	14.9419999123
256	19.7150001526	16.2039999962
512	30.8680000305	17.6510000229
1024	53.9000000954	19.7840001583
2048	100.339999914	23.3710000515
4096	194.943000078	30.0620000362
8192	384.326999903	44.7890000343
16384	752.871000051	79.0769999027
32768	1526.60899997	152.967000008
65536	3139.0769999	303.378000021
131072	6468.52200007	667.940000057
262144	13433.013	1536.90400004
524288	25904.4170001	5946.81500006

Table 5.1: K from 1 to 524288, Array size 2000000

The graph 5.4 and its values of table 5.1 is generated by starting with K=1 and array size=2000000. The values in the array are between 1 to 2000000. In this test we double the K value each step and watching the differences in both algorithms. The results are plotted in graph 5.4. The table shows us that insertionsort doubles its time to sort by a factor of two while binsortionsort takes less time but also starts to (almost) double its values at a larger K value.

## 6 DISCUSSION

The results we got were not surprising. We suspected in pre-test that insertionsort was worse than binsortionsort. Though we had not foreseen that there would be such clear steps in the graphs. (clear seen in graf 5.3). Although it was surprising, when you think about it it is fairly obvious that it should be that clear steps due to the algorithms. When we look at merge sort we can clearly see this. For example an array split into segments of 4 will take, roughly, half the time of an array split into segments of 8 due to the fact that bigger arrays take longer to sort. It was a bit surprising that binsortionsort increased runtime so slowly however.

Over implementation and chose to use random arrays may had inflicted the result so it did not end up in a clean,nice & exact graphs. The OS might have had an influences on the test result aswell due to other process running in the background. We have minimised the risk of



that by using a computer that had enough computer power to not be interrupted. We where able to find a trend that where similar to the function  $\theta(nk + n\lg(\frac{n}{k}))$ .

In the lab we learned that python is a really bad optimised language. When we talked to friends about their solution and their array sizes, they where much bigger. Yet their algorithms where faster aswell. We conclude that it was because of other language selections. The longest test we did took 7 hours and it had an array size of only 2,000,000. If the algorithms is to be analysed in bigger datasets it would be necessary to rewrite them in a different language.