

Electronic circuits and systems

ELEC271

Part 4

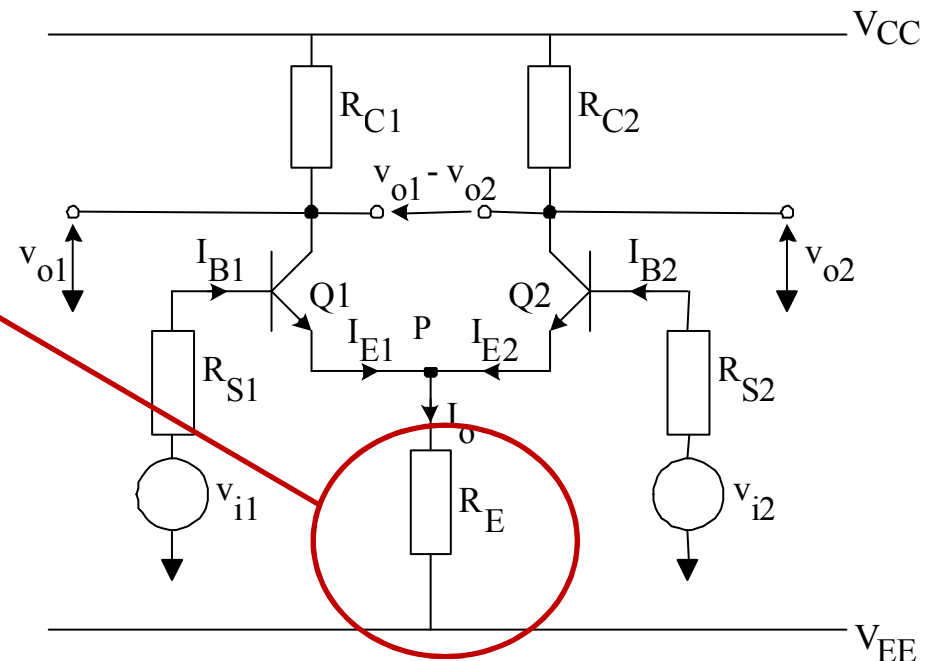
Current sources

Active circuits for biasing
how they work
design issues

Recall the 'problems' with the Diff Amp

We require

- a better bias circuit to replace R_E , which will allow us to set the current I_O , independently of the resistance in the 'tail'.
 - We would also like such a bias circuit to exhibit a very large dynamic resistance to give high common mode rejection ratio (CMRR).
- $A_C \sim 1/R_E$
- a circuit to replace the collector resistors, which will present a high resistance (for high gain) without creating a large voltage drop which causes the transistors to saturate and upsets the symmetry of the voltage swing.



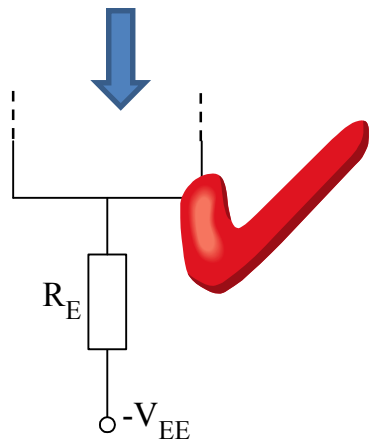
$$A_d = -20I_O R_C$$

$$I_O \sim V_{EE}/R_E$$

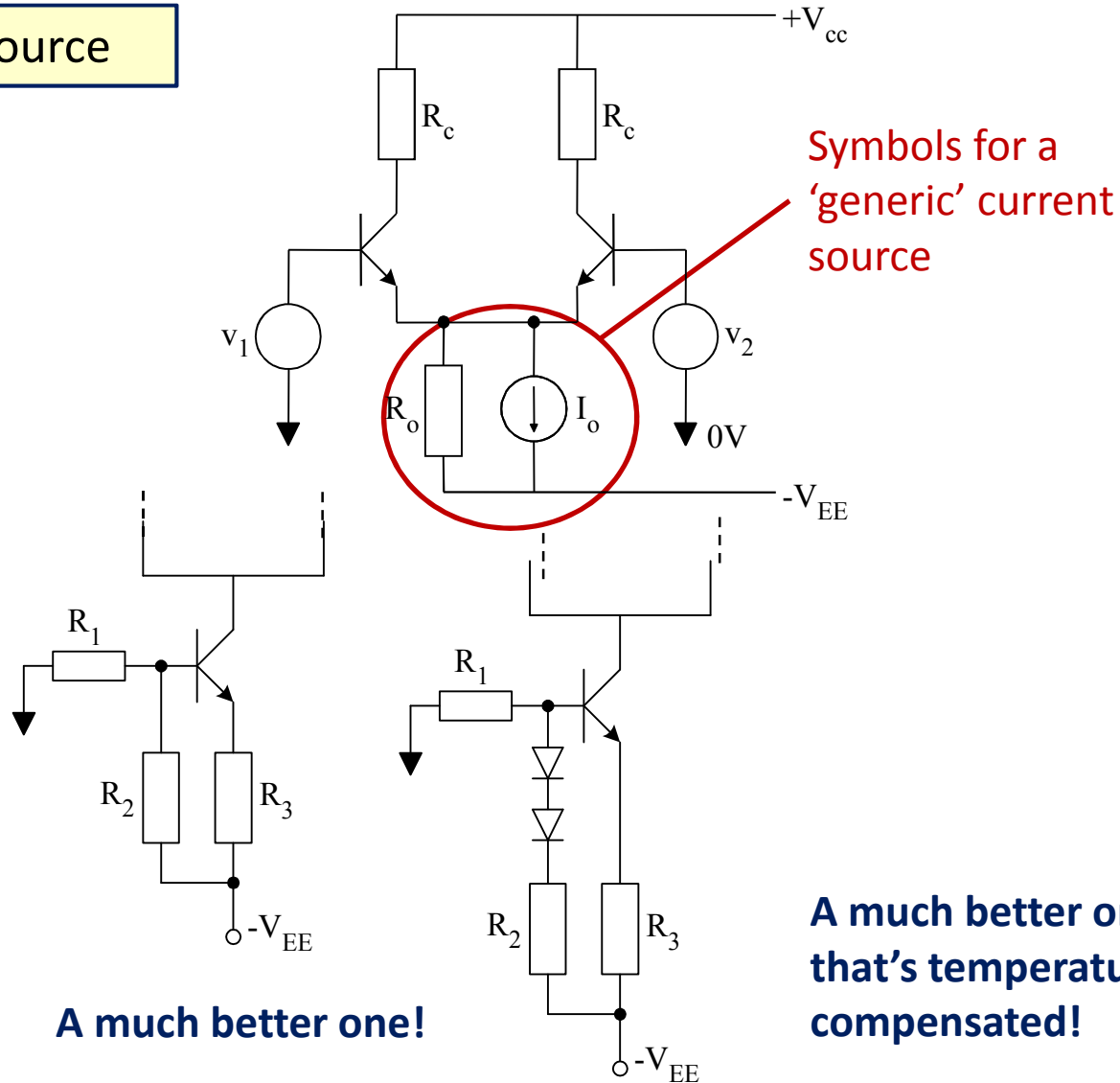
Diff. Amp with Constant current source biasing

3 types of current source

Already studied
this one



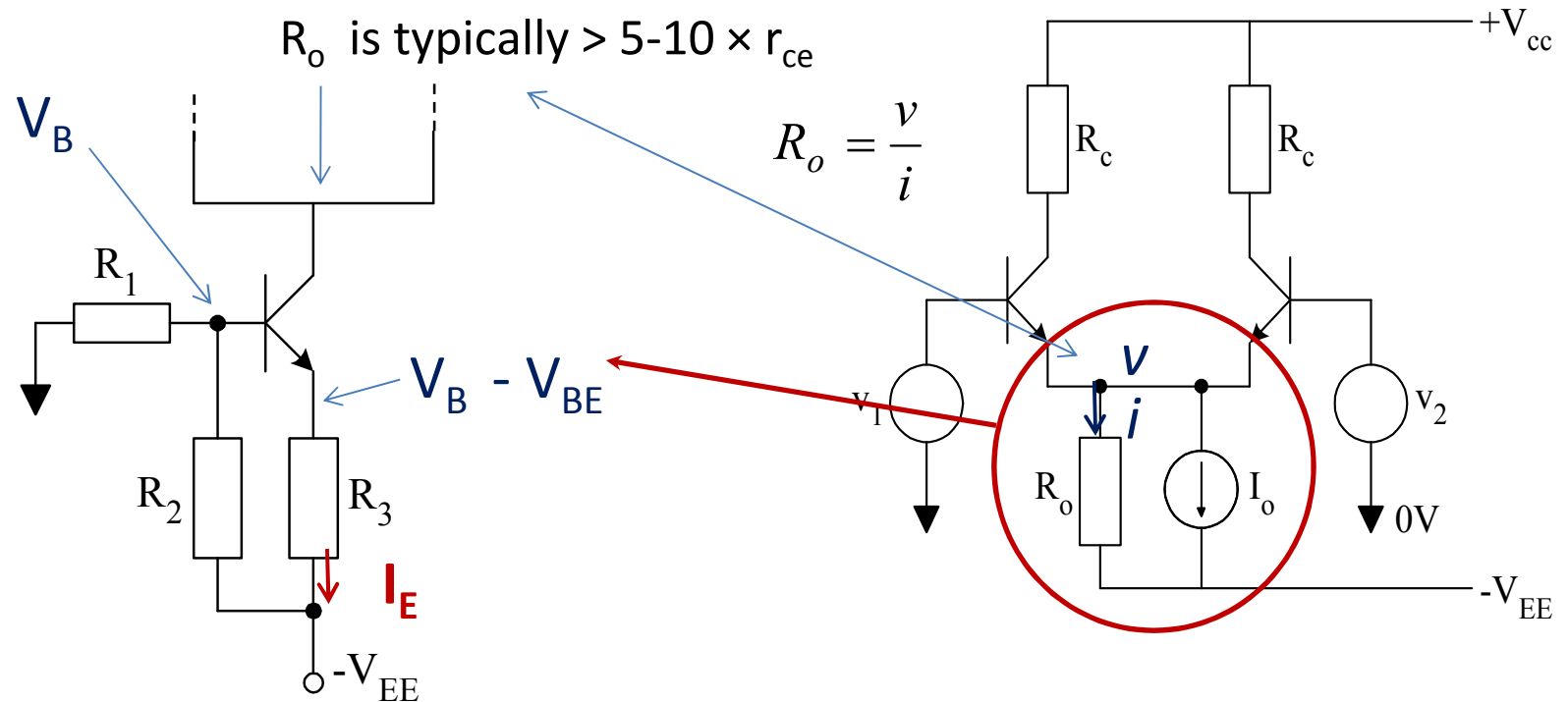
Simple current source
formed by R_E and V_{EE}



A much better one!

A much better one
that's temperature
compensated!

How it works and design



$$V_B \sim -V_{EE} \frac{R_1}{R_1 + R_2}$$

$$I_E = \left| \frac{(|V_B| - V_{BE}) - |V_{EE}|}{R_3} \right| \sim I_C = I_o$$

By potential division
(assuming $I_B \sim 0$)

Exercise: try drawing an ac equivalent circuit!

How it works: large R_o

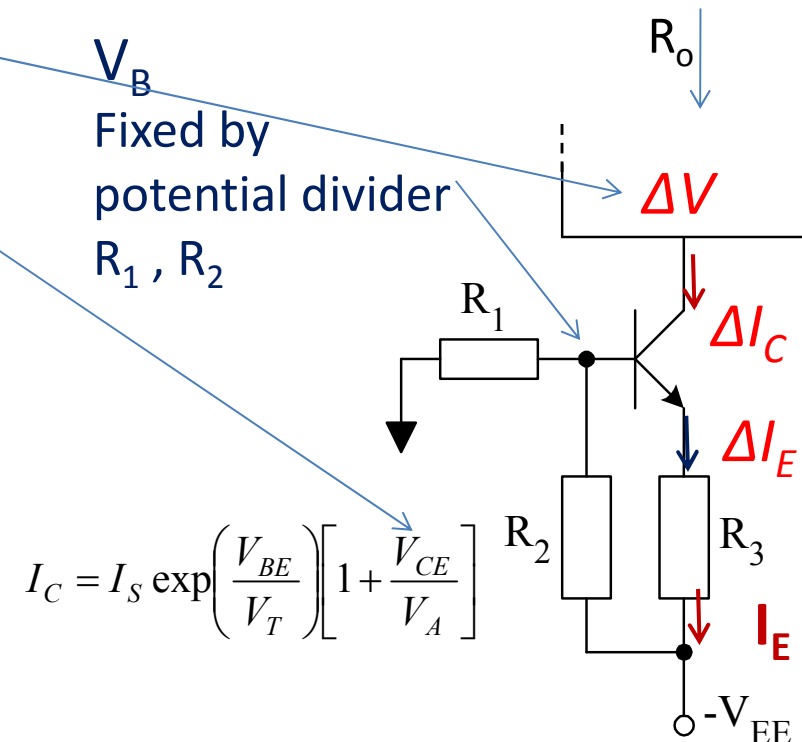
Consider a slight increase in voltage, ΔV

Will get slight increase, ΔI_C (Early effect) and hence ΔI_E .

Hence a slight increase in emitter voltage

and hence a slightly smaller V_{BE} for the transistor!

which in turn causes I_C to decrease.



That is to say, the resistor R_3 provides '**feedback**' and prevents I_C and hence I_o rising. This is the physical effect that gives rise to very large R_o .

Net result? – a tiny increase in collector current

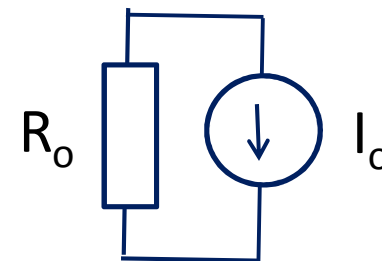
$$\Delta V = v$$

$$\Delta I = i$$

Ac quantities

$$R_o = \frac{\Delta V}{\Delta I}$$

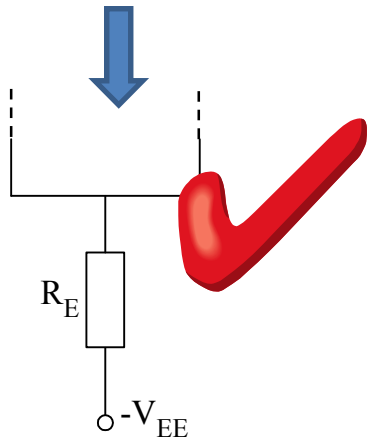
Very large



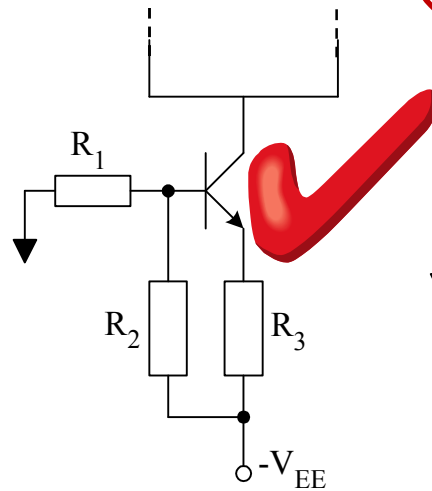
Diff. Amp with Constant current source biasing

3 types of current source

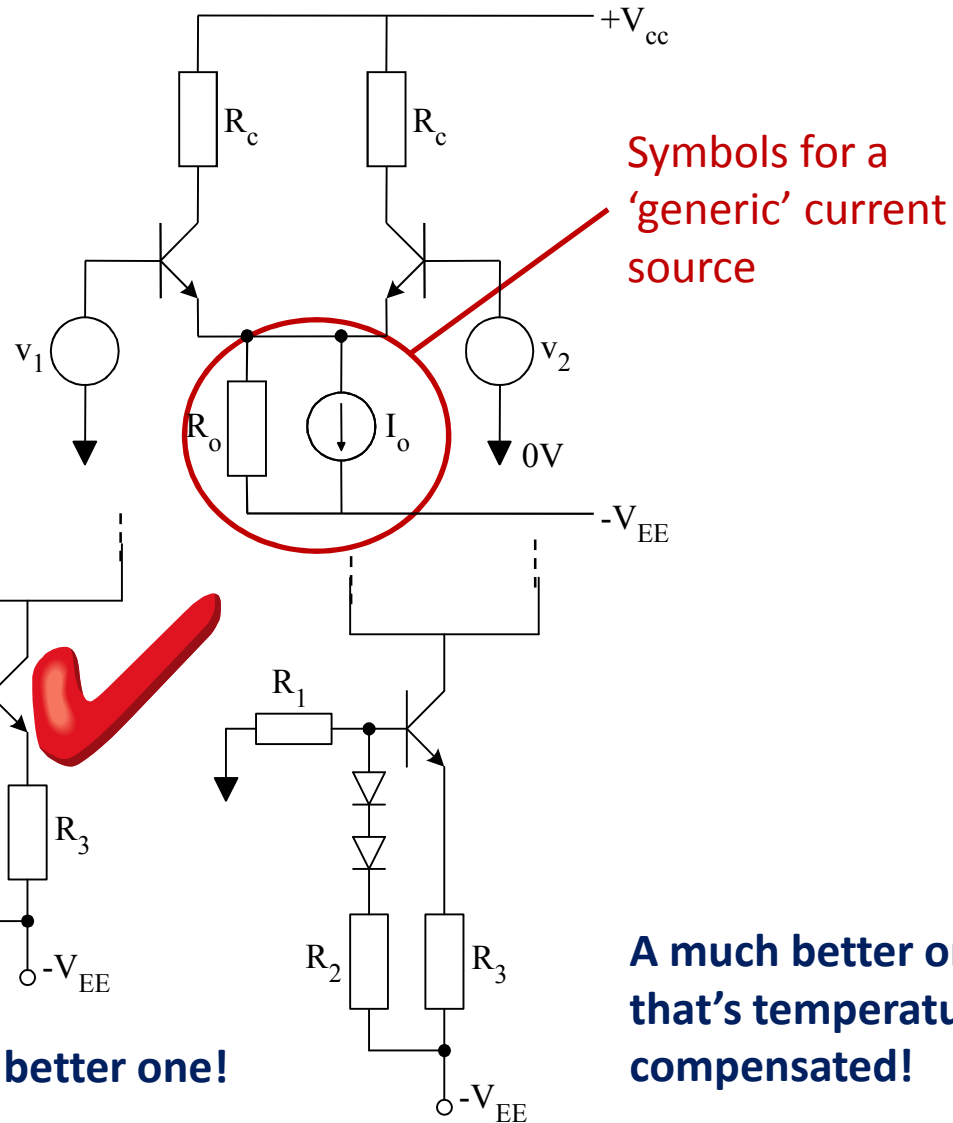
Already studied
this one



Simple current source
formed by R_E and V_{EE}



A much better one!



A much better one
that's temperature
compensated!

3rd circuit: temperature compensated

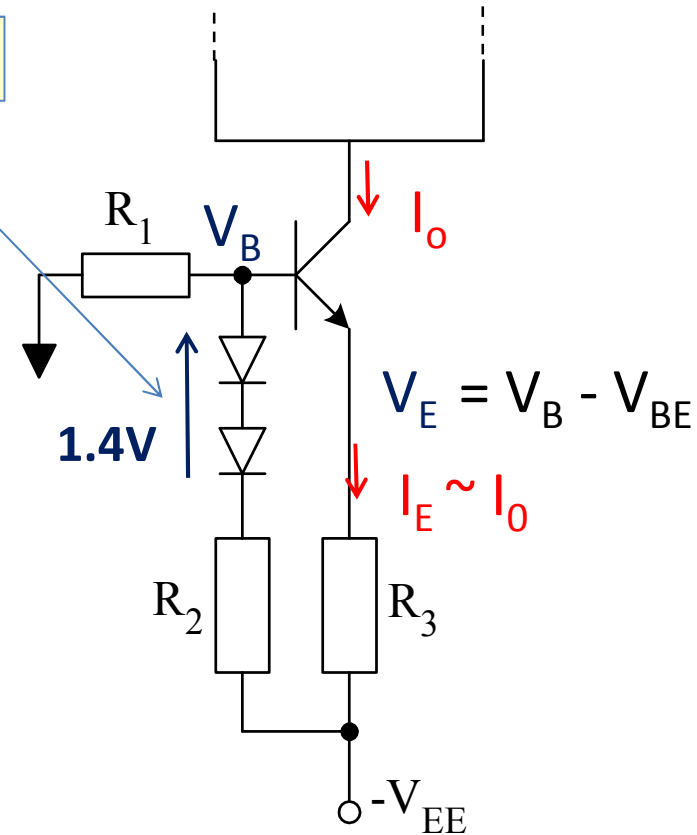
Design equations

2 diode drops

$$V_B \sim -(|V_{EE}| - 1.4) \frac{R_1}{R_1 + R_2}$$

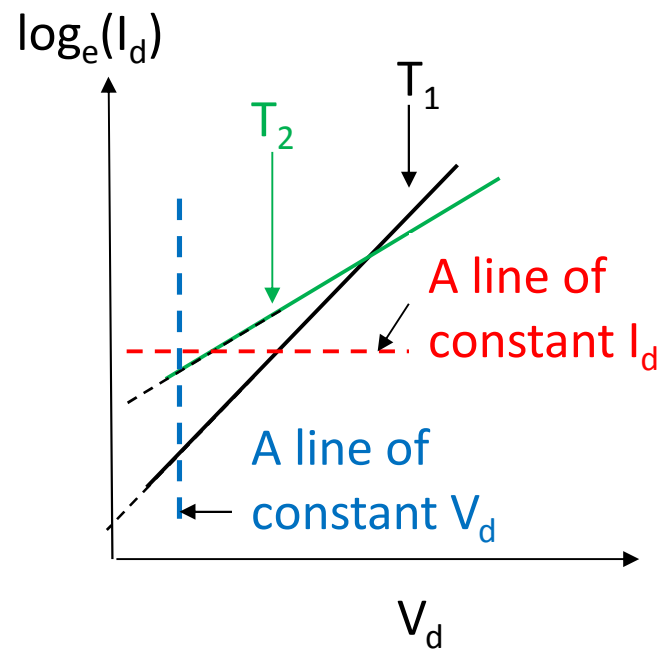
$$V_E \sim -(|V_{EE}| - 1.4) \frac{R_1}{R_1 + R_2} - V_{BE}$$

$$I_E = \frac{(|V_{EE}| - |V_E|)}{R_3} \sim I_C = I_o$$



Why the diodes?

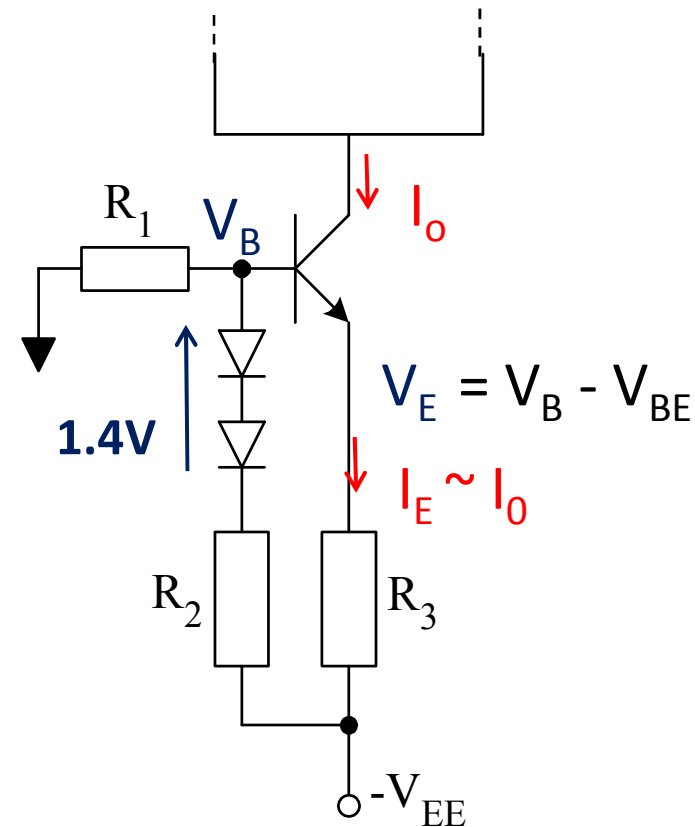
Consider diode characteristics at
2 temperatures, T_1, T_2



$$I_d = I_S(T) \exp\left(\frac{qV_d}{kT}\right)$$

$$V_d = \frac{kT}{q} \ln\left(\frac{I_d}{I_S(T)}\right)$$

As $T \uparrow$,
 $I \uparrow$ (for constant V)
and $V \downarrow$ (for constant I)



$$\frac{\partial I_C}{\partial T} \propto \text{Const} \frac{\partial V_{\text{diodes}}}{\partial T} - \frac{\partial V_{BE}}{\partial T}$$

Diodes provide 'temperature compensation'
Prevent I rising much as T rises

Temperature compensation - analysis

n diode drops

$$V_B \sim -(|V_{EE}| - n \times V_d) \frac{R_1}{R_1 + R_2}$$

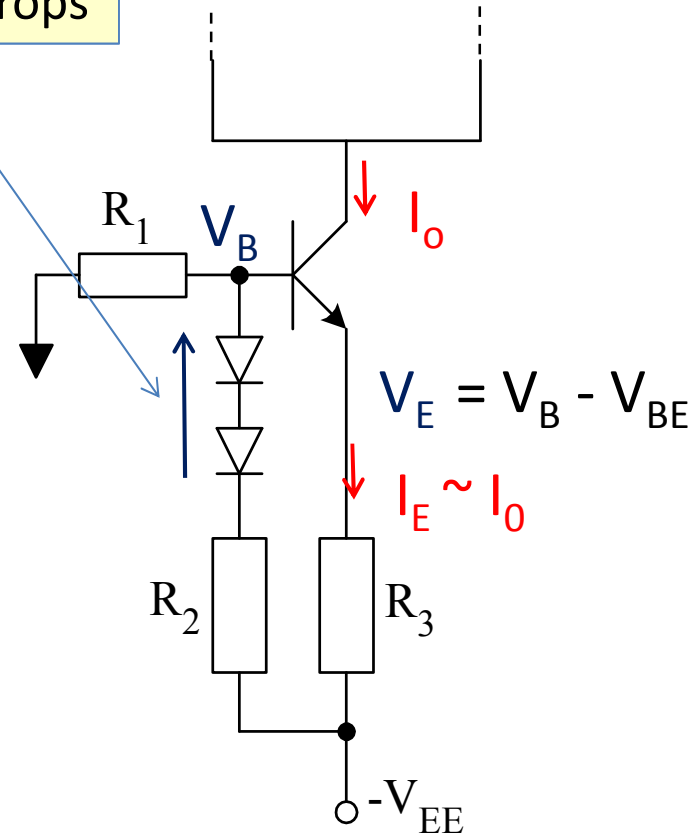
$$V_E \sim -(|V_{EE}| - n \times V_d) \frac{R_1}{R_1 + R_2} - V_{BE}$$

$$\frac{dV_E}{dT} \sim n \times \frac{dV_d}{dT} \frac{R_1}{R_1 + R_2} - \frac{dV_{BE}}{dT}$$

$$I_E = \frac{(|V_{EE}| - |V_E|)}{R_3} \sim I_C = I_o$$

$$\frac{dI_o}{dT} = -\frac{1}{R_3} \frac{dV_E}{dT}$$

$$\Rightarrow \frac{dI_o}{dT} \sim -\frac{1}{R_3} \left(n \times \frac{dV_d}{dT} \frac{R_1}{R_1 + R_2} - \frac{dV_{BE}}{dT} \right)$$



Design: Aim to make the 2 temperature dependent terms on the RHS equal so that dI_o/dT tends to 0

Worked example (Summer 2018 exam)

Design the circuit to meet the specification:

$I_O = 1 \text{ mA}$, DC level at $V_{OUT} = 0 \text{ V}$.

Hints: Allow 2 V across R_E , $I_b = 0.1 \times I_O$

ideal transistors with high DC current gain.

Solution

$$I_b = 0.1 \times I_O = 0.1 \text{ mA}$$

$$R_E? \quad R_E = \frac{2}{1 \text{ mA}} = 2 \text{ k}\Omega$$

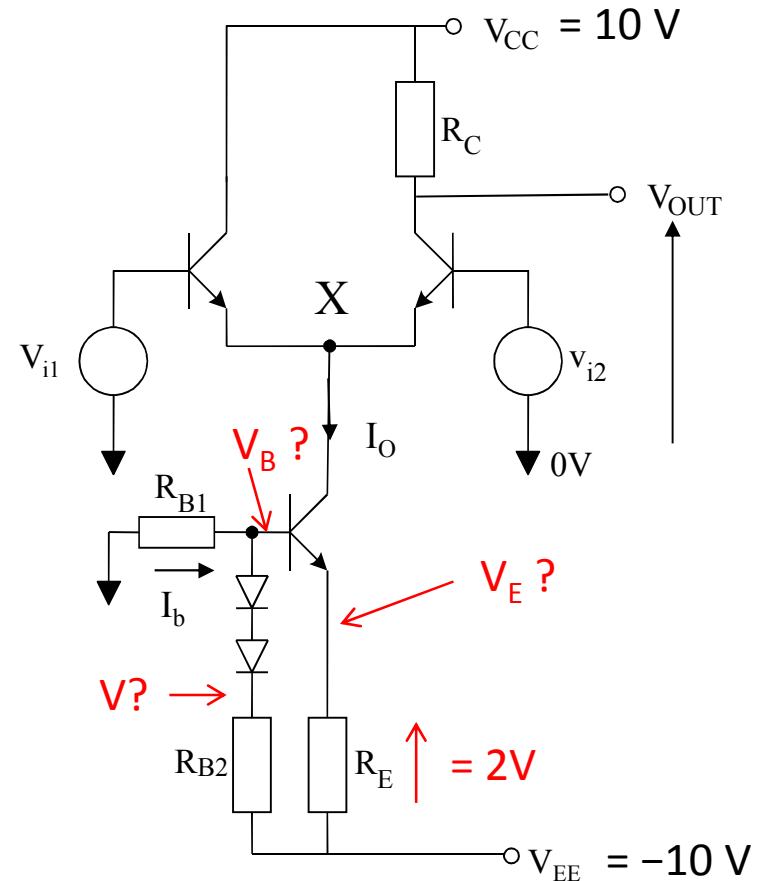
$$V_E? \quad V_E = -10 + 2 = -8 \text{ V}$$

$$V_B? \quad V_B = -8 \text{ V} + 0.6 = -7.4 \text{ V}$$

$$R_{B1}? \quad R_{B1} = \frac{0 - (-7.4)}{0.1 \text{ mA}} = 74 \text{ k}$$

$$V? \quad V = -7.4 - 2 \times 0.6 = -8.6$$

$$R_{B2}? \quad R_{B2} = \frac{-8.6 - (-10)}{0.1 \text{ mA}} = 14 \text{ k}\Omega$$



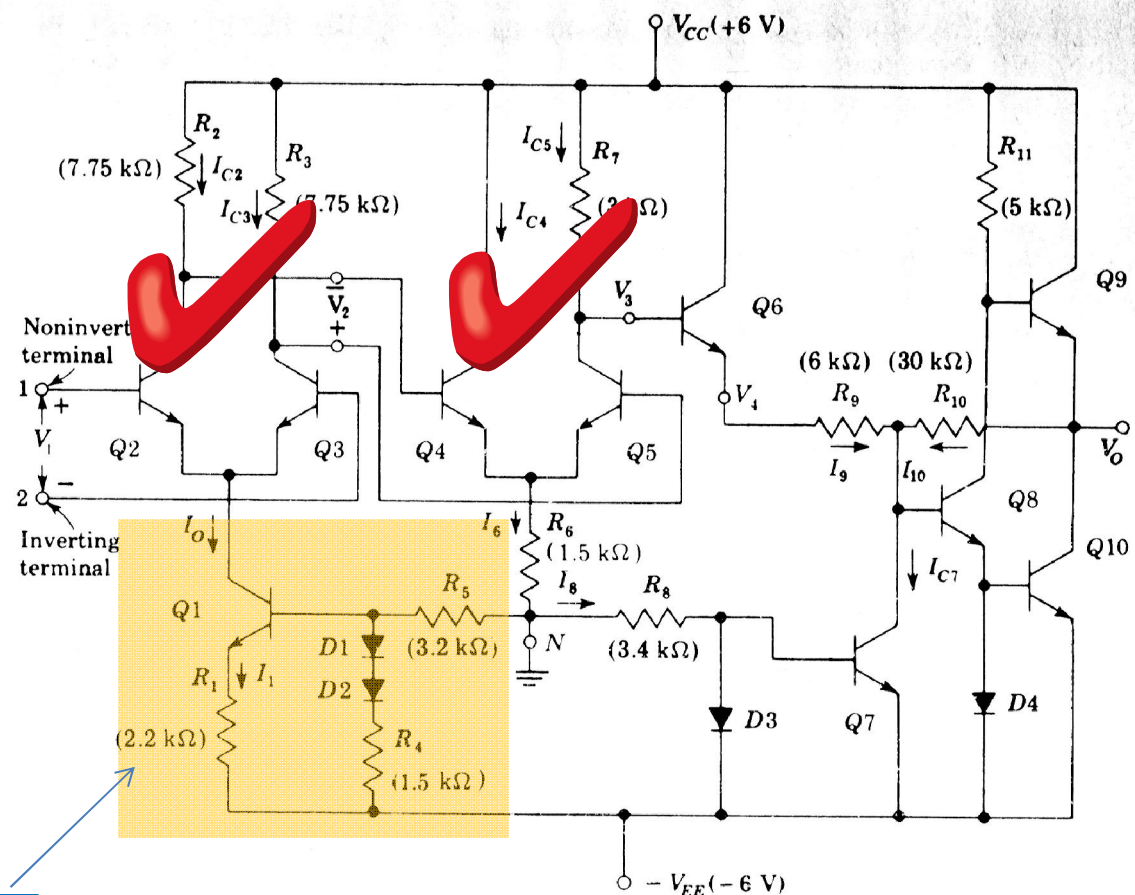
$$\text{Diff Gain} = \frac{g_m \times R_C}{2}$$

A target for week 4...

By about week 4 we will be able to:

- Identify circuit 'building blocks'
- Perform a dc analysis to estimate all currents and voltages
- Perform an ac analysis to estimate gain of amplifier

Temperature compensated current source which provides the biasing



Motorola MC1350 operational amplifier

Further biasing techniques

- Current mirrors and current repeaters

Simple current mirror

- $V_{BE1} = V_{BE2}$
- assume transistors are identical
- **So $I_{C1} = I_{C2} = I_O$**

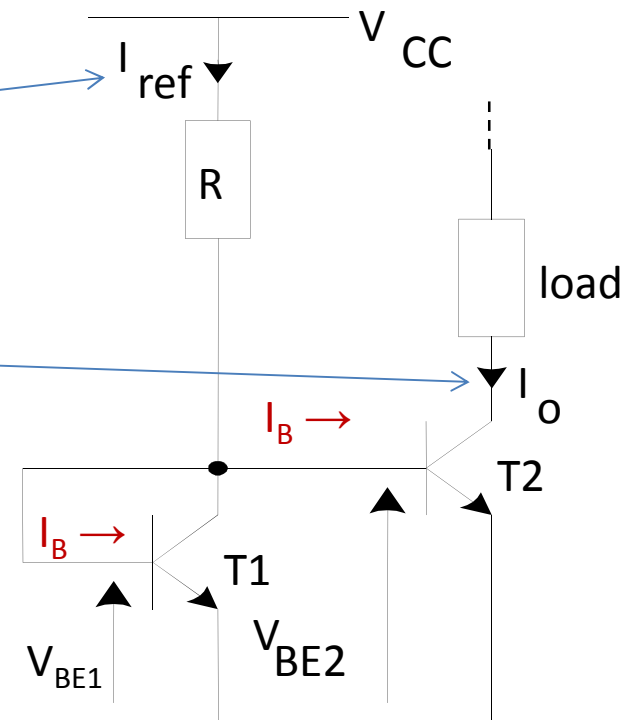
$$I_C = I_S \exp\left[\frac{V_{BE}}{V_T}\right] \quad V_T = \frac{kT}{q} \sim 25mV$$

$$I_{ref} = I_{C1} + 2I_B = I_C + 2\frac{I_C}{\beta}$$

$$I_{ref} = I_O + 2\frac{I_O}{\beta}$$

$$I_O = \frac{I_{ref}}{1 + 2/\beta} \approx I_{ref} \quad \beta \equiv h_{FE} \text{ large!}$$

$$I_{ref} = \frac{V_{CC} - V_{BE}}{R}$$



- Set I_{ref} choosing R - current is 'mirrored' in T_2 to provide I_O .
- a number of current sources can be created to provide bias in different parts of a more complex circuit as shown on next slide.....

A current 'repeater'

$$I_C = I_S \exp\left[\frac{V_{BE}}{V_T}\right]$$

$$I_{ref} = \frac{V_{CC} - V_{BE}}{R}$$

$$I_{ref} = I_B + NI_B + I_o \quad \leftarrow I_c = I_o$$

- it's easy to show that

$$I_o = \frac{I_{ref}}{1 + (N + 1) / \beta}$$

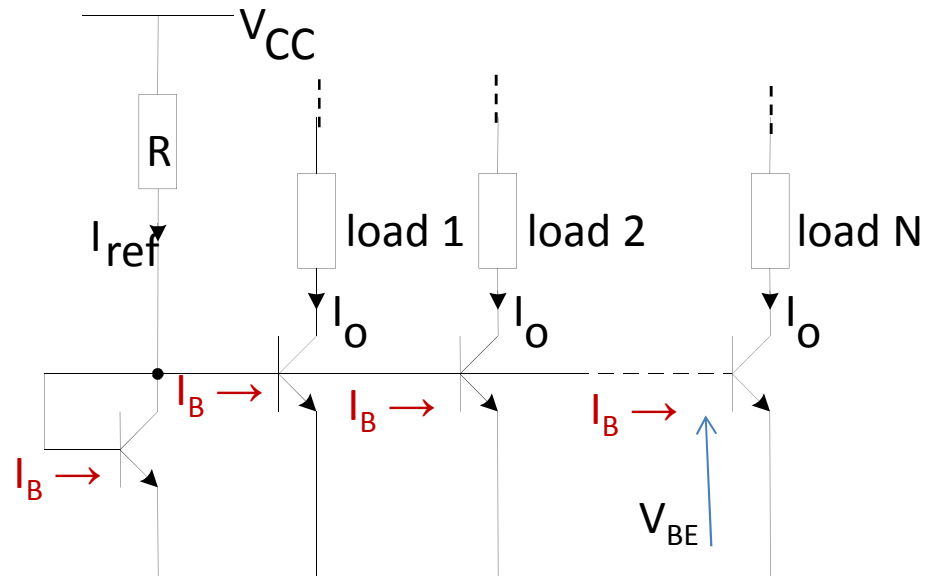
- But all bias currents are the same!**
- Could make the transistor larger; that is make I_S larger by factor 'n'

$$I_{C1} = I_{S1} \exp\left(\frac{V_{BE}}{V_T}\right)$$

$$I_{C2} = I_{S2} \exp\left(\frac{V_{BE}}{V_T}\right)$$

$I_S \sim \text{device area}$

$$\frac{I_{C1}}{I_{C2}} = \frac{I_{S1}}{I_{S2}} = n \quad I_o = nI_{ref}$$



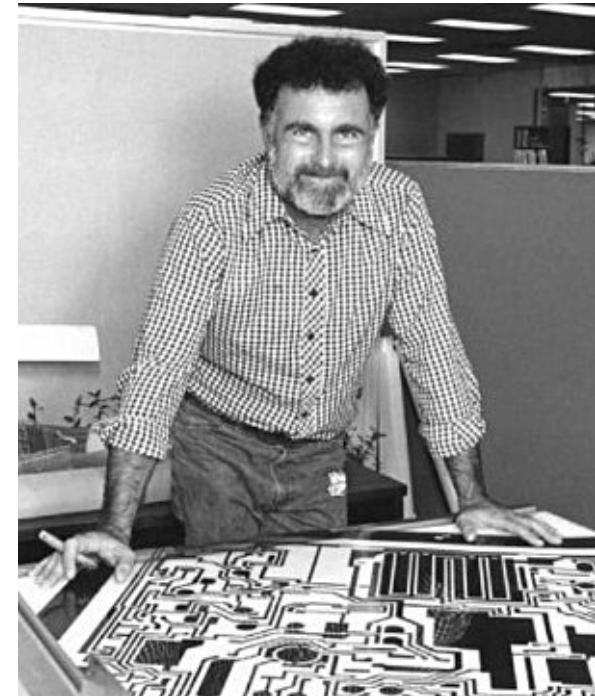
small values of 'n' can be produced this way but bias currents may differ by factors of ten and more...

so the transistors would have to be **very large**.

A better way to scale the bias currents is to use a **'Widlar'** current mirror.

Who is 'Widlar'?

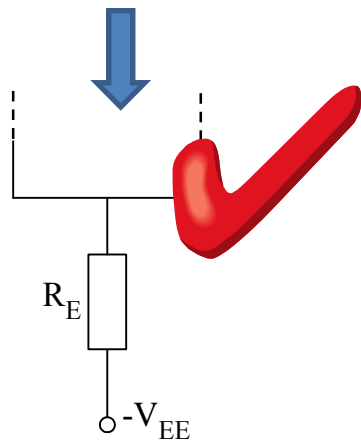
- a pioneer of [linear \(analog\) integrated circuit](#) (IC) design. **Bob Widlar** invented the basic building blocks of linear ICs like the
- [Widlar current source](#)
- [Widlar bandgap voltage reference](#)
- [Widlar output stage](#)
- From 1964 to 1970, Widlar, together with David Talbert, created the first mass-produced [operational amplifiers](#) ICs (μ A702, μ A709), the first integrated [voltage regulator](#) IC (LM100), the first operational amplifiers employing [full internal compensation](#) (LM101), [field-effect transistors](#) (LM101A), and super-beta transistors (LM108). **Each of Widlar's circuits had "at least one feature which was far ahead of the crowd" and became a "product champion" in its class.**
- They made his employers, [Fairchild Semiconductor](#) and [National Semiconductor](#), the leaders in linear integrated circuits.



Diff. Amp with Constant current source biasing

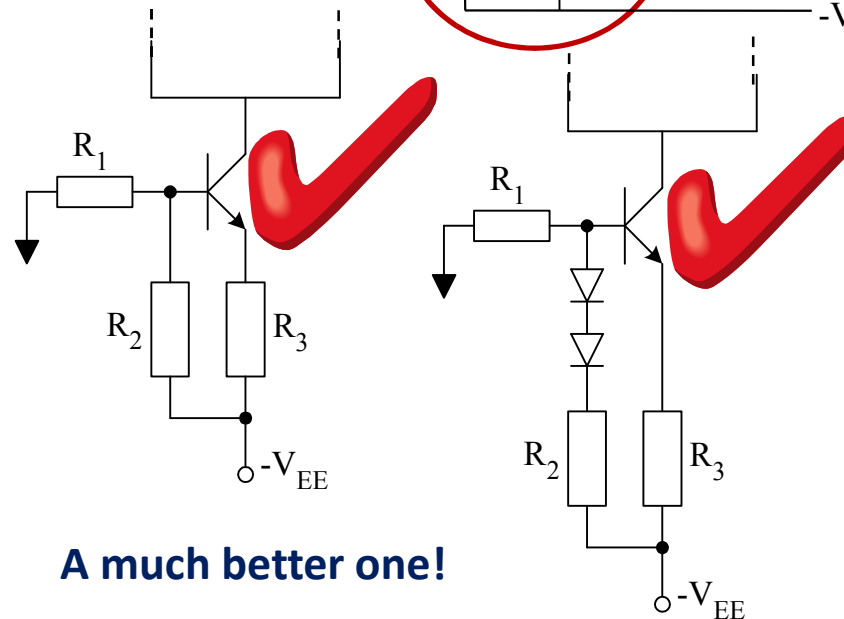
3 types of current source

Already studied
this one

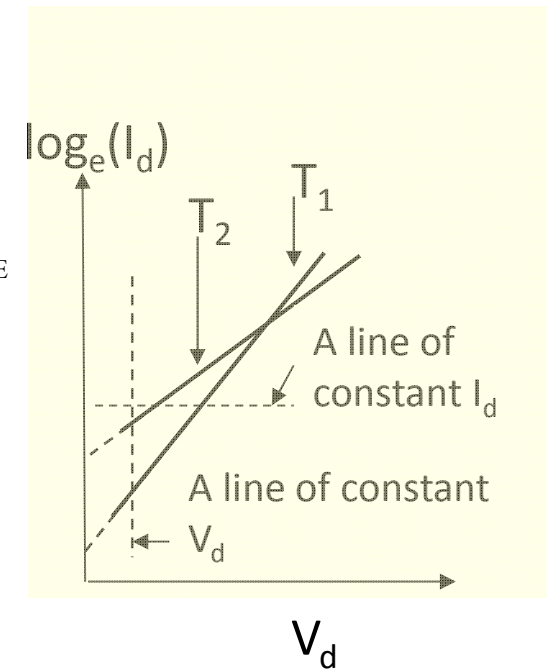
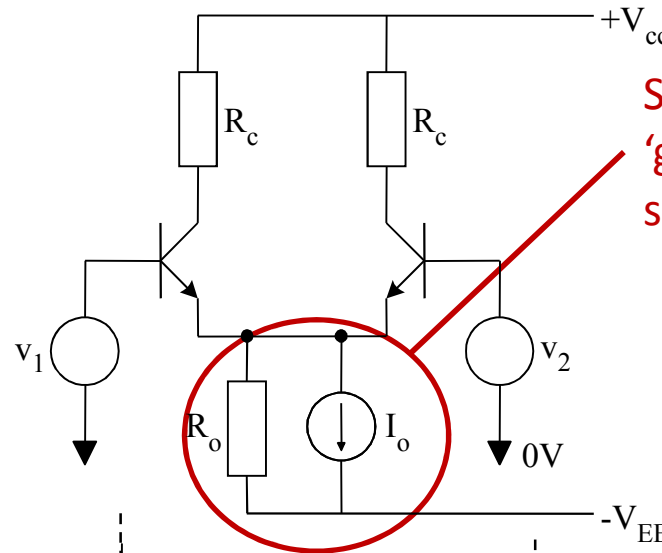


Simple current source
formed by R_E and V_{EE}

A much better one!



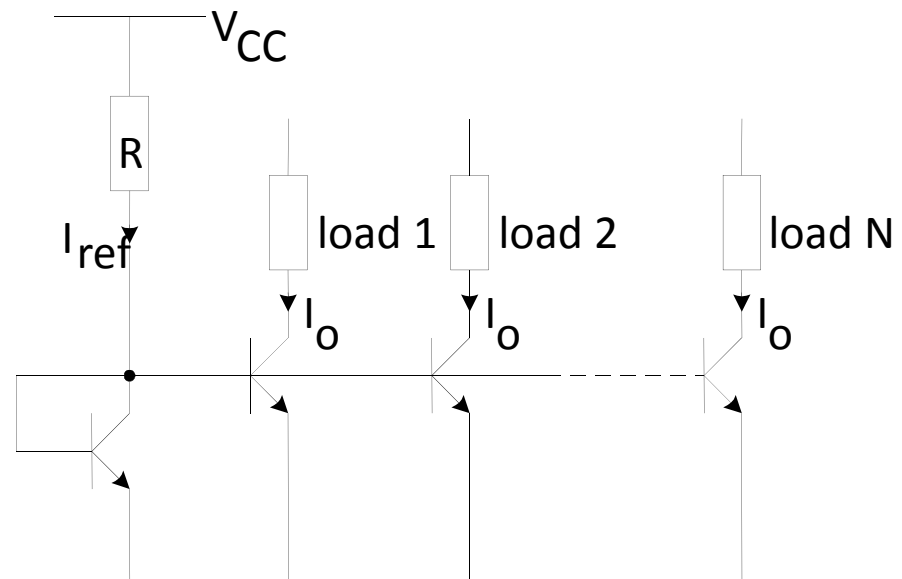
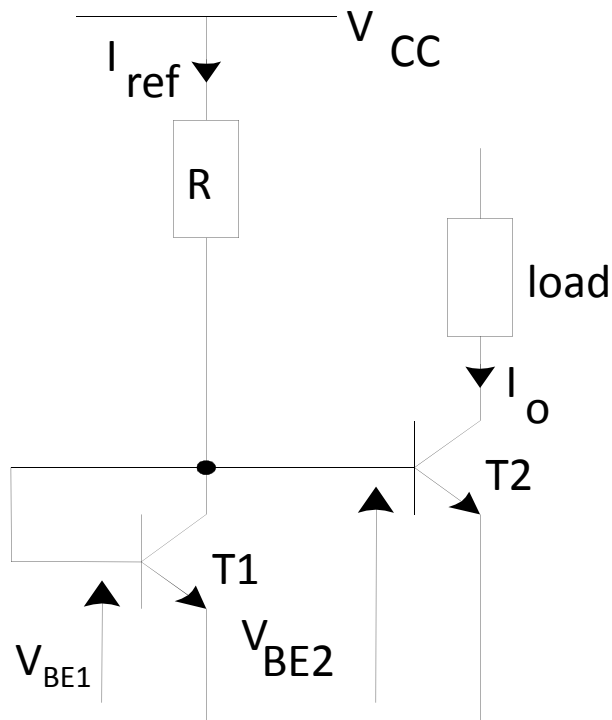
Symbols for a
'generic' current
source



A much better one
that's temperature
compensated!

Further biasing techniques

- Current mirrors and current repeaters



Next: The Widlar current mirror

– note that there are many other types of current source/mirrors

Widlar current mirror

Circuit analysis – DC: how to set I_o

$$V_{BE1} = V_{BE2} + I_o R_E$$

$$I_o R_E = V_{BE1} - V_{BE2}$$

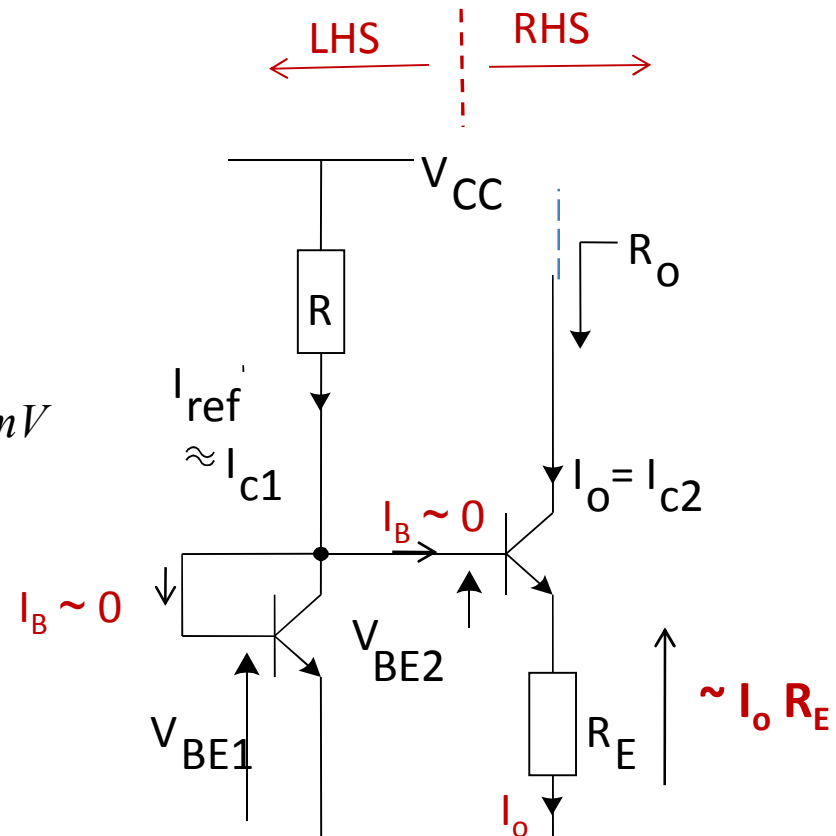
$$I_{C1} = I_S \exp\left(\frac{V_{BE1}}{V_T}\right) \sim I_{ref} \quad V_T = \frac{kT}{q} \sim 25mV$$

$$I_{C2} = I_S \exp\left(\frac{V_{BE2}}{V_T}\right) \sim I_o$$

hence

$$\begin{cases} V_{BE1} = V_T \ln\left(\frac{I_{ref}}{I_S}\right) \\ V_{BE2} = V_T \ln\left(\frac{I_o}{I_S}\right) \end{cases}$$

$$I_o R_E = V_T \ln\left(\frac{I_{ref}}{I_o}\right) \quad \text{DESIGN EQUATION}$$



Set different currents in **current repeaters** by incorporating different R_E

Worked example

- Find R , R_E to give bias current $I_o = 0.1\text{mA}$. (assume $V_{RE} \sim 4V_T = 0.1\text{V}$ for stability).
- Given: $V_{CC} = 5\text{V}$, $V_{EE} = -5\text{V}$, transistors have current gains $\beta = \beta_o = 100$ and $V_A = 150\text{V}$.
- What will be the value of I_{ref} ? Comment on your answer.

Solution

Widlar current mirror: $I_o = \frac{V_T}{R_E} \ln \left(\frac{I_{ref}}{I_o} \right) \dots (1)$

For stability: set about $4V_T \sim 0.1\text{V}$ across R_E .

So try $R_E = \frac{0.1}{1 \times 10^{-4}} = 1\text{k}\Omega$

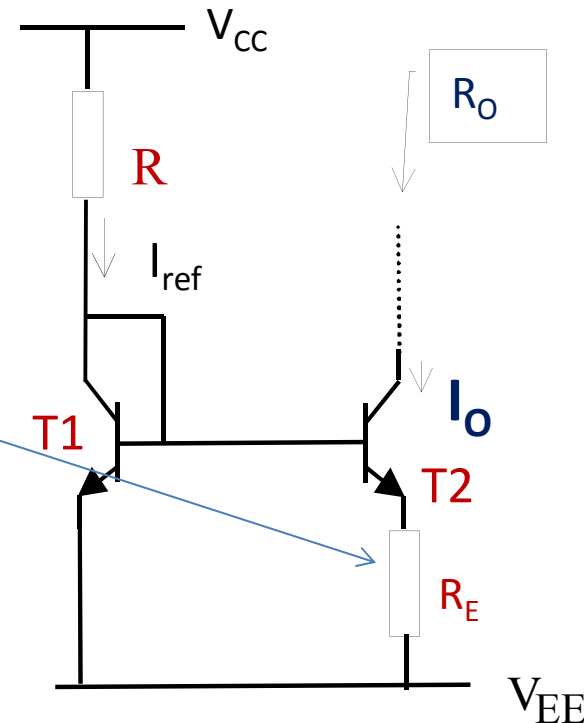
Re-arrange (1) to get required value for I_{ref} .

$$I_{ref} = I_o \exp \left[\frac{R_E I_o}{V_T} \right] \quad I_{ref} = 5.5\text{mA}$$

$$R = \frac{V_{CC} - (V_{EE}) - V_{BE}}{5.5\text{ mA}}$$

$$R = \frac{5 - (-5) - 0.7}{5.5\text{ mA}} = \frac{10 - 0.7}{5.5\text{ mA}} \approx 1.7\text{ k}\Omega$$

$R_E = 1\text{ k}\Omega$, $R = 1.7\text{ k}\Omega$ -small values!



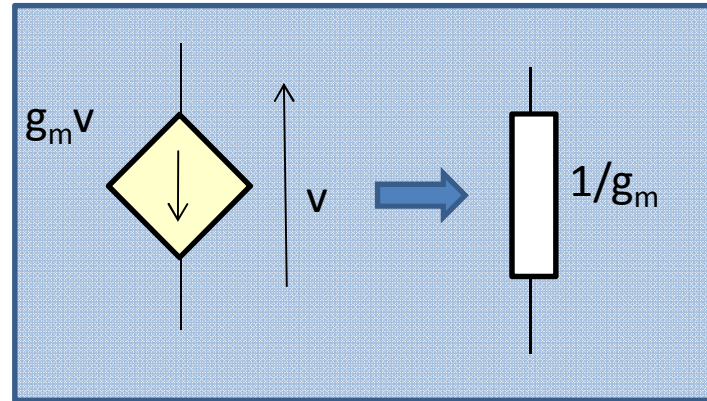
And

$$g_{m1} = (40 \times 5.5\text{mA}) = 220\text{ mA/V},$$

$$g_{m2} = (40 \times 0.1\text{ mA}) = 4\text{ mA/V},$$

$$r_{ce2} = V_A / 0.1\text{mA} = 150 / 0.1\text{mA} = 1.5\text{M}\Omega$$

Note



A dependent current source of value $g_m v$ with a voltage across it of value, v is equivalent to a resistance $1/g_m$ by Ohm's Law.

$$v = i \times r$$

$$v = g_m v \times r$$

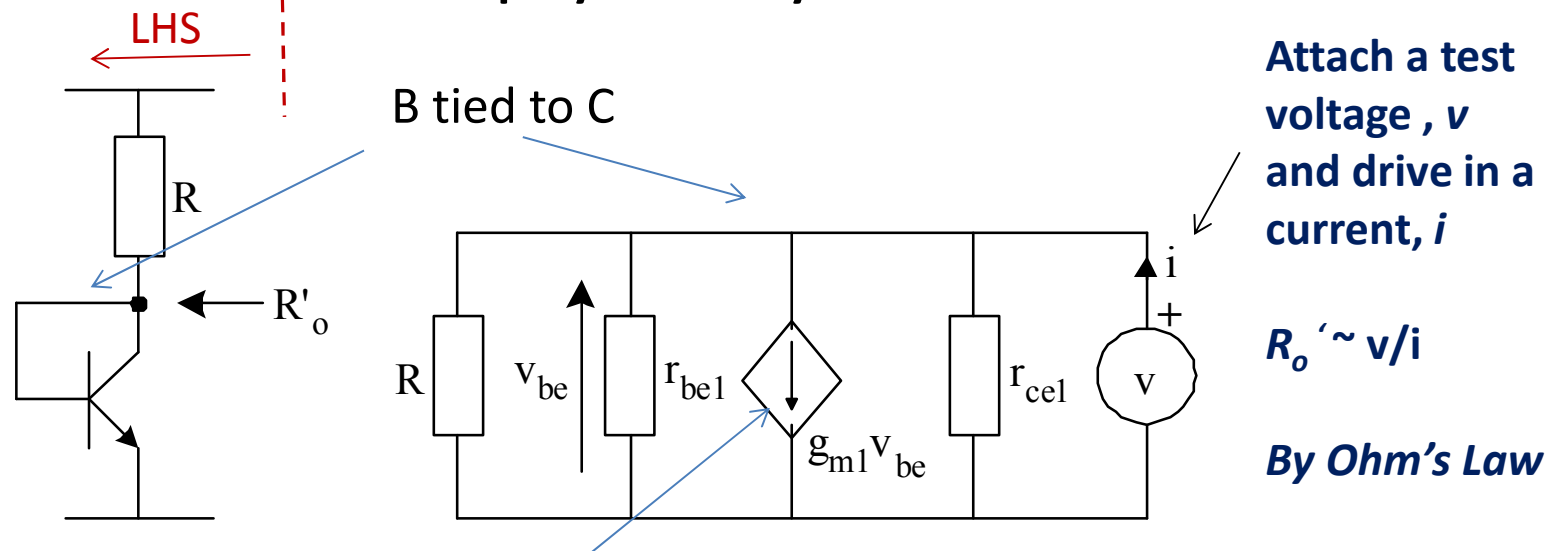
$$r = \frac{1}{g_m}$$

**So can replace current source
with a conductance, g_m**

Or a resistance, $r = 1/g_m$

Now work out an expression for the **ac resistance, R_o**
and hence find a numerical value for R_o .

- Split the circuit into 2 to simplify the analysis



Note that the dependent current source, $g_{m1}v_{be1} = g_{m1}v$ as $v_{be} = v$!
- Write as $1/g_m$

so.....

$$R_o' = R // r_{be1} // r_{ce1} // \frac{1}{g_{m1}} \approx \frac{1}{g_{m1}}$$

R = 1.7 k Ω

Justify approximation: $g_{m1} = 40 \times I_{ref} = 40 \times 5.46mA \sim 218mA/V$

$$r_{be1} \sim \frac{\beta_o}{g_{m1}} = \frac{100}{218 \times 10^{-3}} \sim 460\Omega$$

$$r_{ce} \sim \frac{V_A}{I_{ref}} = \frac{150}{5.5 \times 10^{-3}} = 28k\Omega$$

$$\frac{1}{g_{m1}} = \frac{1}{218m} \sim 5\Omega$$

Now find R_o

Apply a voltage source to force a current, i into the output of our current source.

The aim then is to find $R_o = v/i$

Can we make a further approximation?

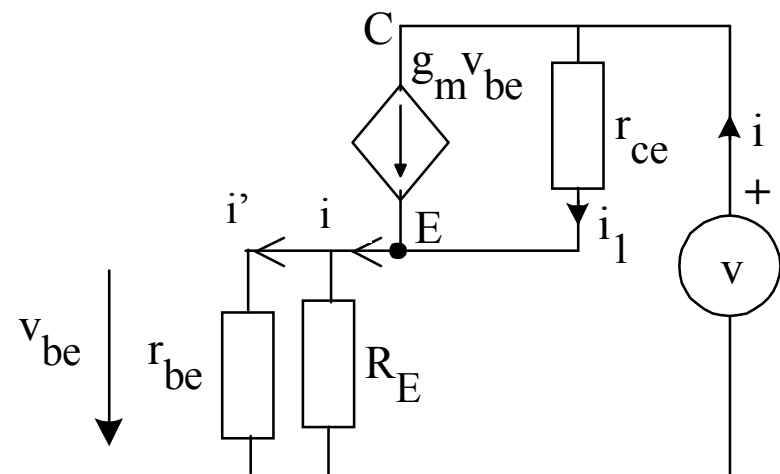
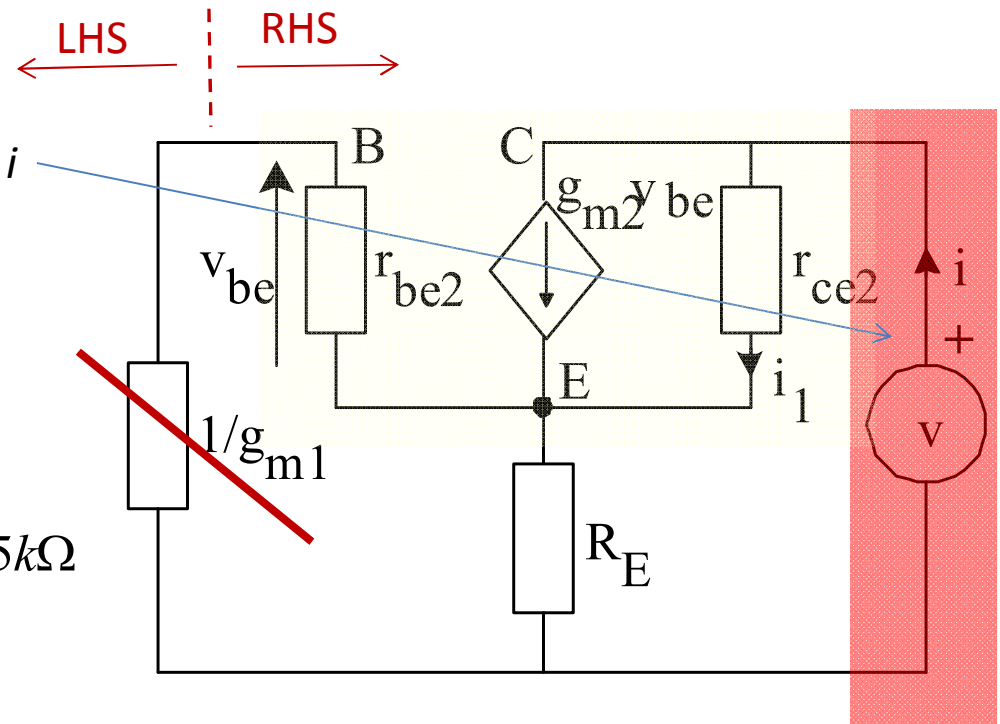
$$r_{be2} = \frac{\beta_o}{g_{m2}} = \frac{100}{40 \times I_o} = \frac{100}{40 \times 0.1mA} = 25k\Omega$$

$1/g_{m1} \sim 5\Omega$ and **So $r_{be2} \gg 1/g_{m1}$!**

The schematic circuit is re-drawn.

We have managed to reduce the original circuit to quite a simple one.

drop the subscript '2' for simplicity.



Now find R_o

RHS →

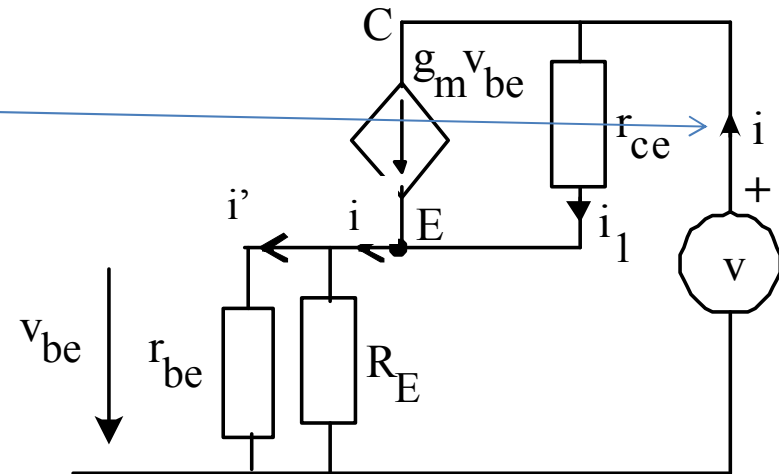
we can write

$$i = g_m v_{be} + \frac{v - (-v_{be})}{r_{ce}}$$

$$i = \left(g_m + \frac{1}{r_{ce}} \right) v_{be} + \frac{v}{r_{ce}}$$

current through r_{ce}

(1)



Need to find v_{be} : consider current division at 'E'

$$i' = i \frac{R_E}{r_{be} + R_E} = -\frac{v_{be}}{r_{be}} \quad \text{That is, } v_{be} = -i R_E // r_{be}$$

substitute $v_{be} = -i R_E // r_{be}$ into Eqn.1 to get: $i = -\left(g_m + \frac{1}{r_{ce}} \right) i R_E // r_{be} + \frac{v}{r_{ce}}$

$$R_O = \frac{v}{i} = r_{ce} \left[1 + \left(g_m + \frac{1}{r_{ce}} \right) R_E // r_{be} \right] \quad \text{...complicated expression!}$$

But we can also say $g_{m2} \gg 1/r_{ce2}$ ($4\text{m} \gg 0.1\text{m}/150 \sim 10^{-6}$) giving $R_O \sim r_{ce} \left[1 + \frac{R_E r_{be} g_m}{R_E + r_{be}} \right]$

Finally....

$$R_O \sim r_{ce} \left[1 + \frac{R_E \times r_{be} \times g_m}{R_E + r_{be}} \right]$$

if $R_E \ll r_{be2}$ ($1k < 25k$)

OUTPUT RESISTANCE IS SIMPLY

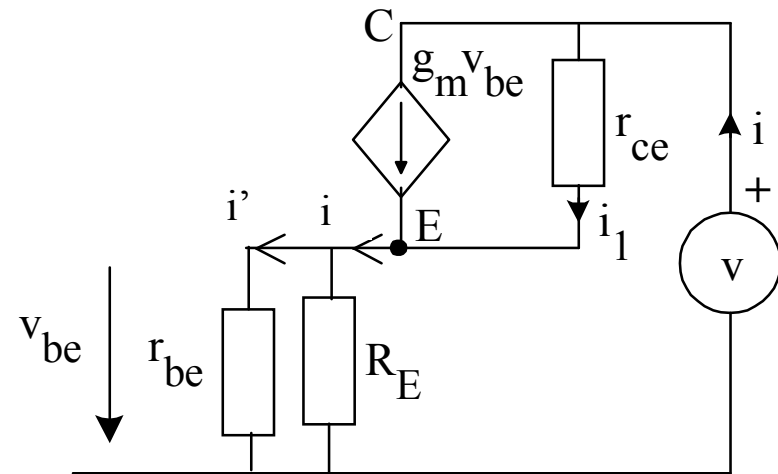
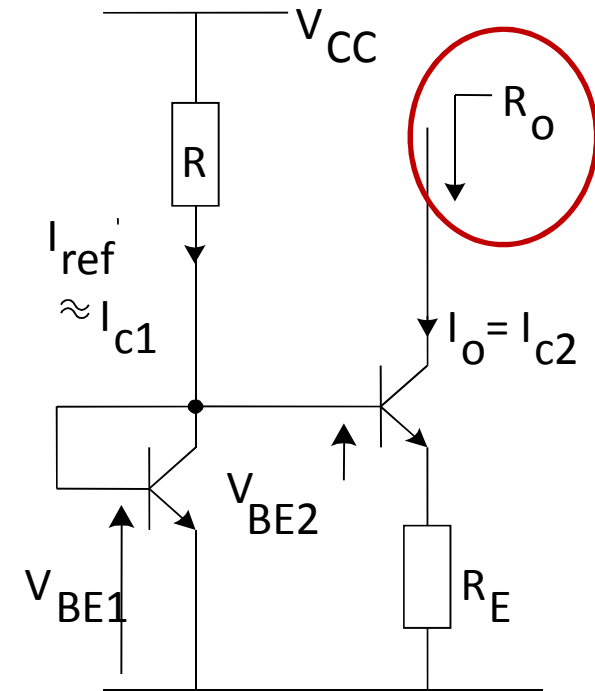
$$R_O \sim r_{ce} [1 + g_m R_E]$$

Now
$$g_m R_E = \frac{I_O}{V_T} R_E$$

and $R_E I_O$ is the voltage drop across R_E !

We see therefore that we require at least a few **thermal volts** (25mV) across R_E to 'multiply up' the transistor output Resistance, r_{ce} to give a large R_O for our current source.

$$R_O \sim r_{ce} \left[1 + \frac{\text{voltage drop across } R_E}{25mV} \right]$$



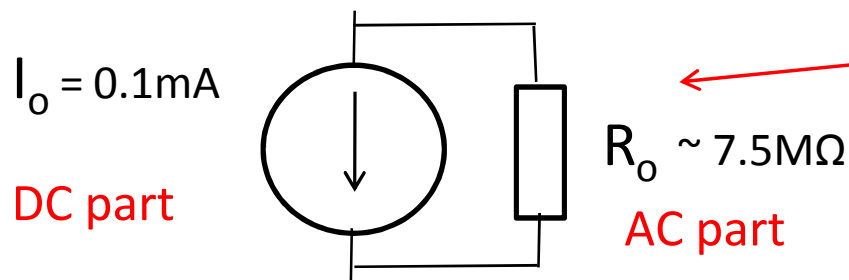
Example

$$I_o = 0.1\text{mA}, R_E = 1\text{k}\Omega$$

$$r_{ce} \sim \frac{V_A}{I_o} = \frac{150}{0.1\text{mA}} = 1.5\text{M}\Omega$$

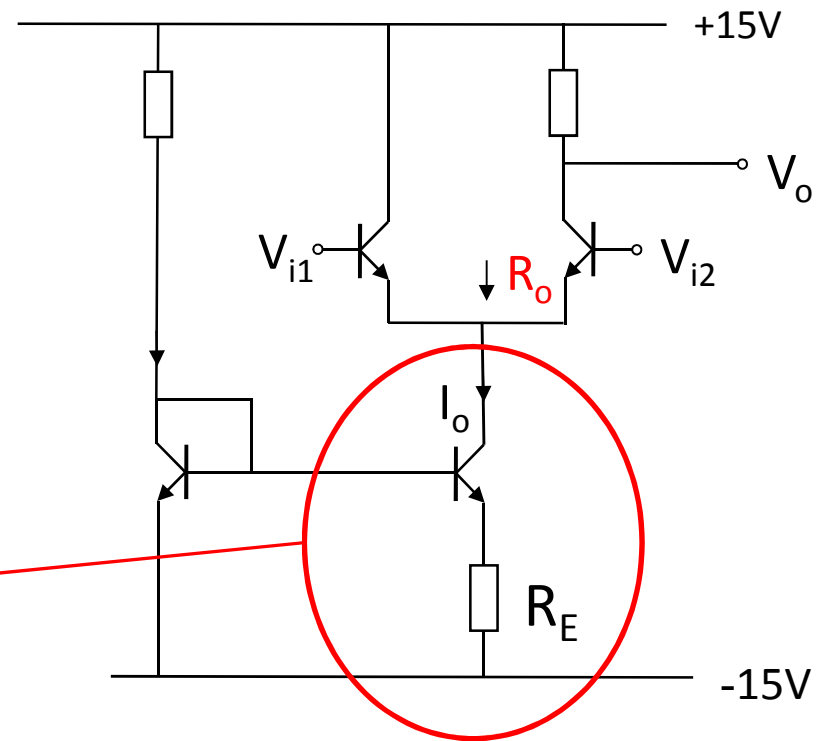
$$R_O \sim r_{ce} [1 + g_m R_E] \\ = 1.5\text{M} [1 + 40 \times 0.1\text{mA} \times 1000]$$

$$R_O \sim r_{ce} [1 + 4] \quad R_o = 7.5\text{M}\Omega$$



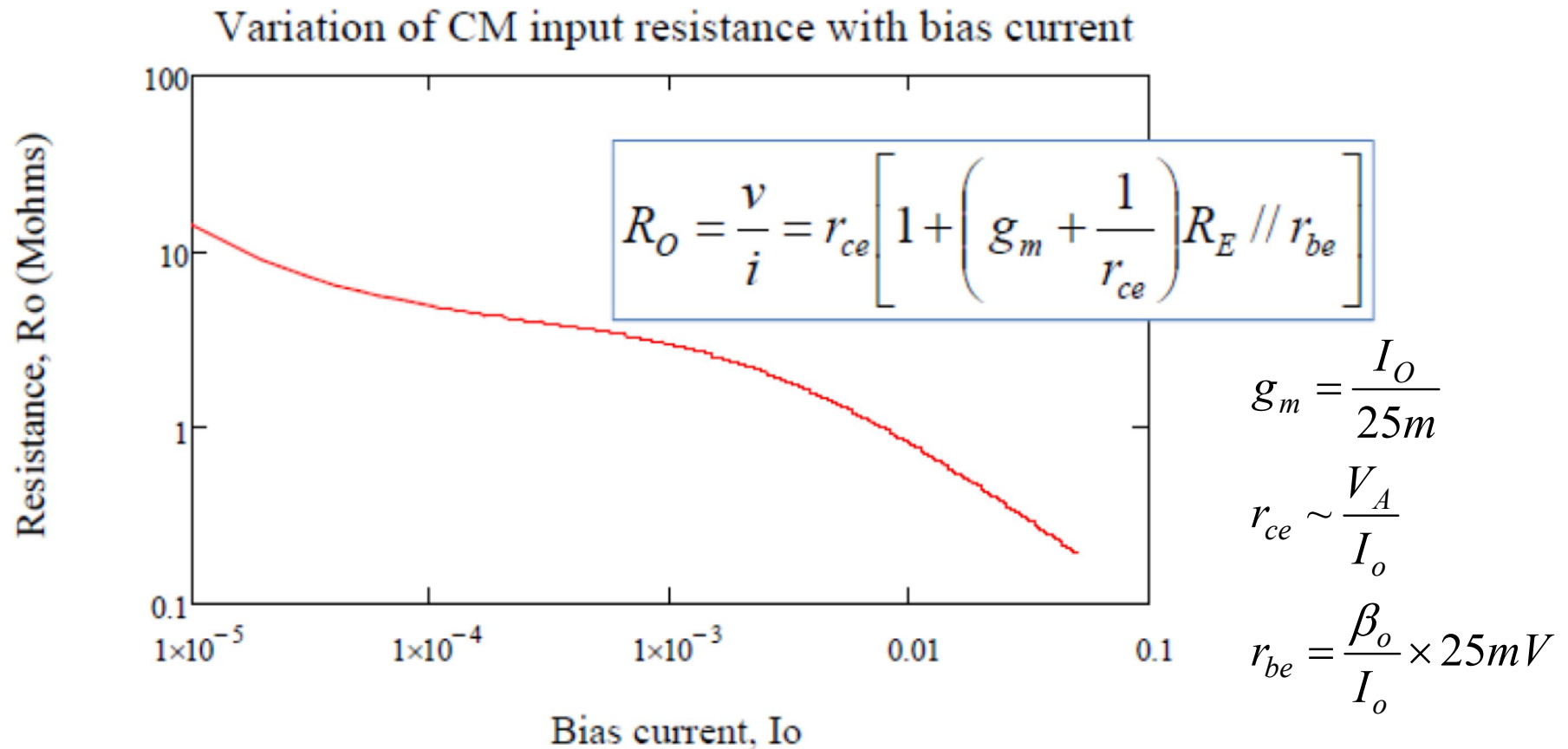
And simple estimate of CMRR is

$$\text{CMRR} \sim \frac{R_o I_o / 2}{25\text{m}} = 15,000$$



An example of the use of a Widlar current mirror to provide the bias current, I_o for a differential amplifier

R_o stays quite large as bias current increases



- Large R_o gives small common-mode gain
- Large I_o gives high differential-mode gain
- Overall, large common-mode rejection ratio with Widlar current source

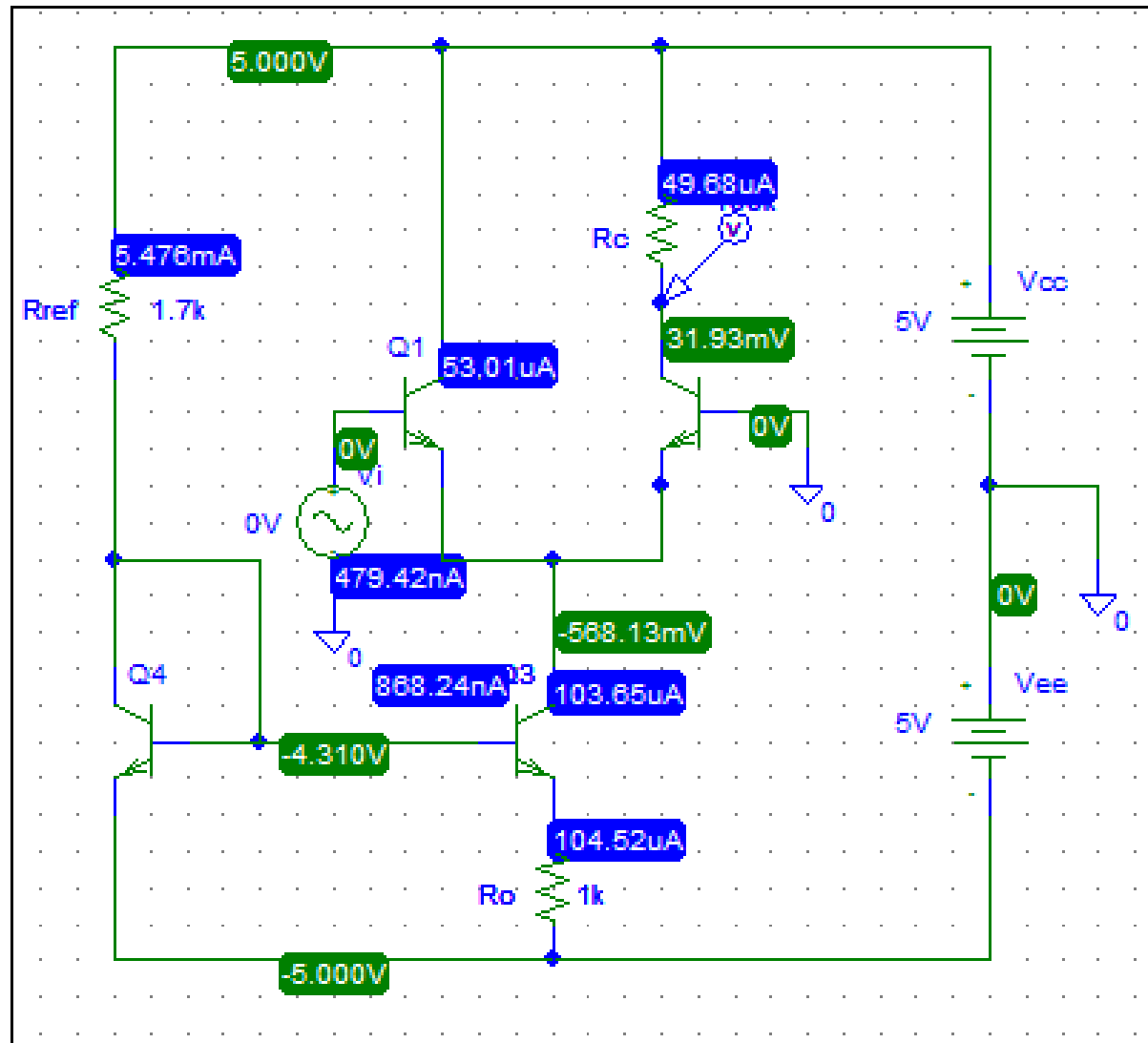
PSPICE DC simulation: V and I

$I_{\text{ref}} = 5.5 \text{ mA}$
Sim: 5.48 mA

$I_o = 100 \text{ mA}$
Sim: 104 mA

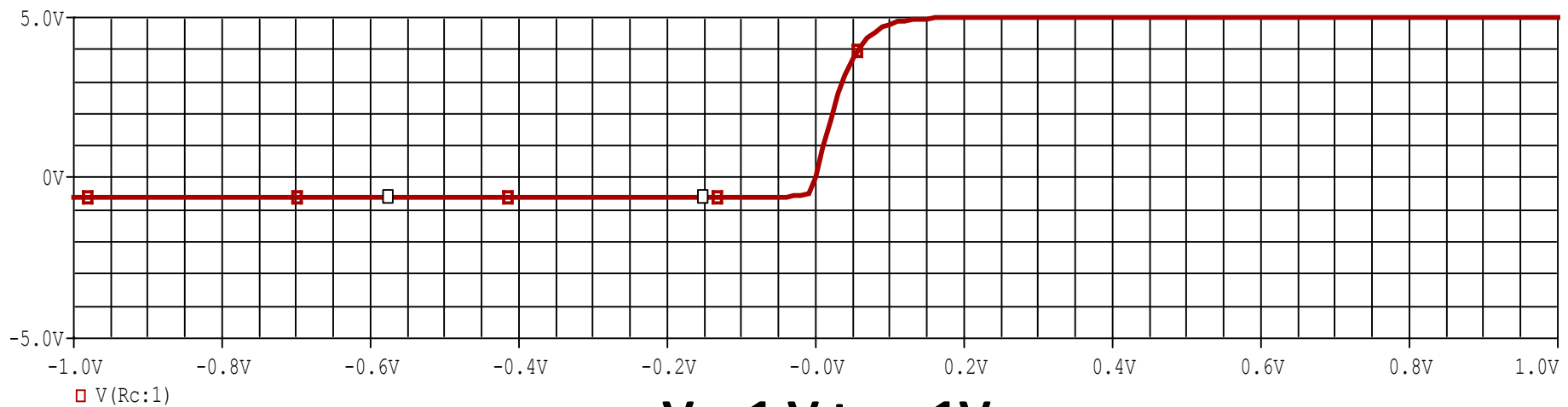
$V_{\text{out}} = 0 \text{ V}$
Sim: 32 mV

Agreement
quite good



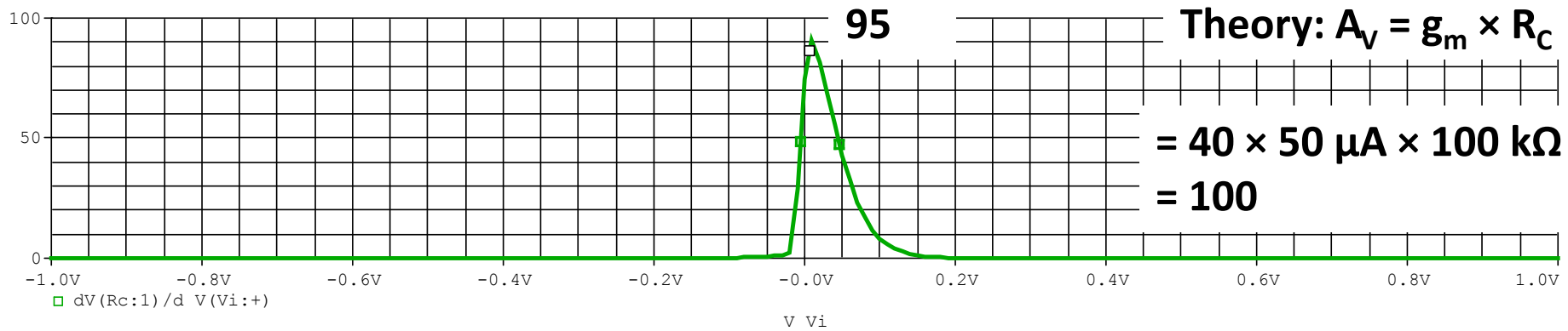
DC Sweep: Diff. gain

$V_{OUT} : -5 \text{ V to } +5 \text{ V}$

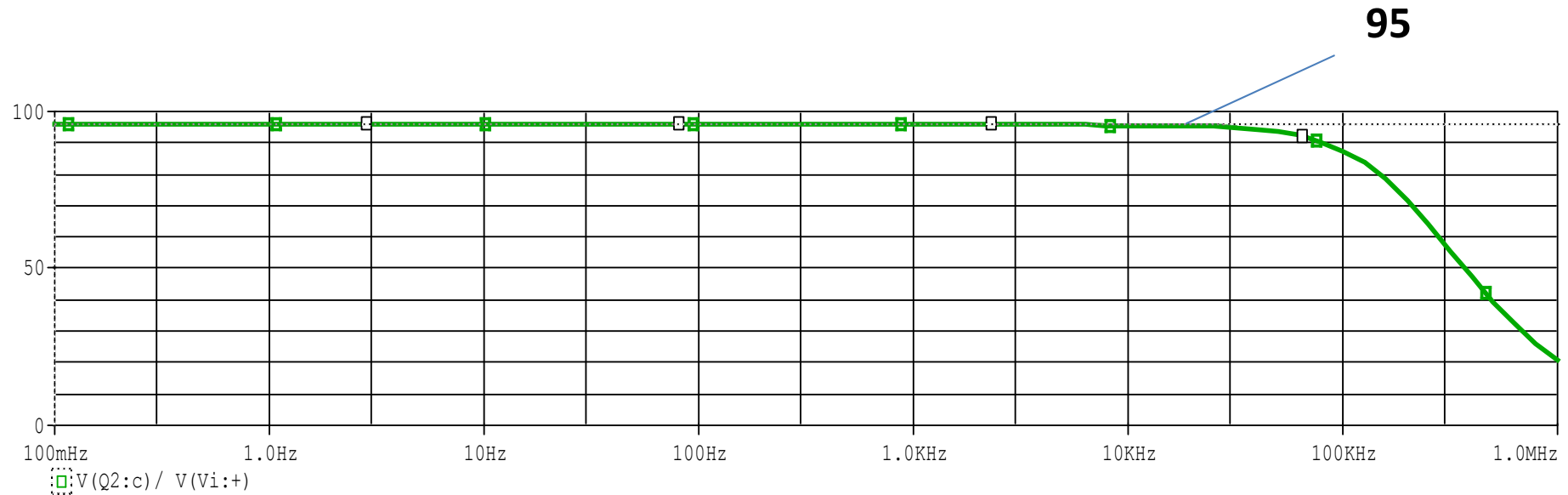


$V_i : -1 \text{ V to } +1 \text{ V}$

A_v



AC Sweep: Voltage gain



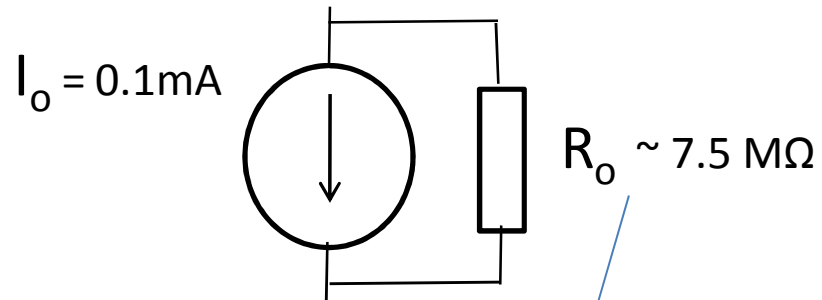
Frequency: 0.1 Hz to 1 MHz

Note: Gain down to DC!

No coupling capacitors

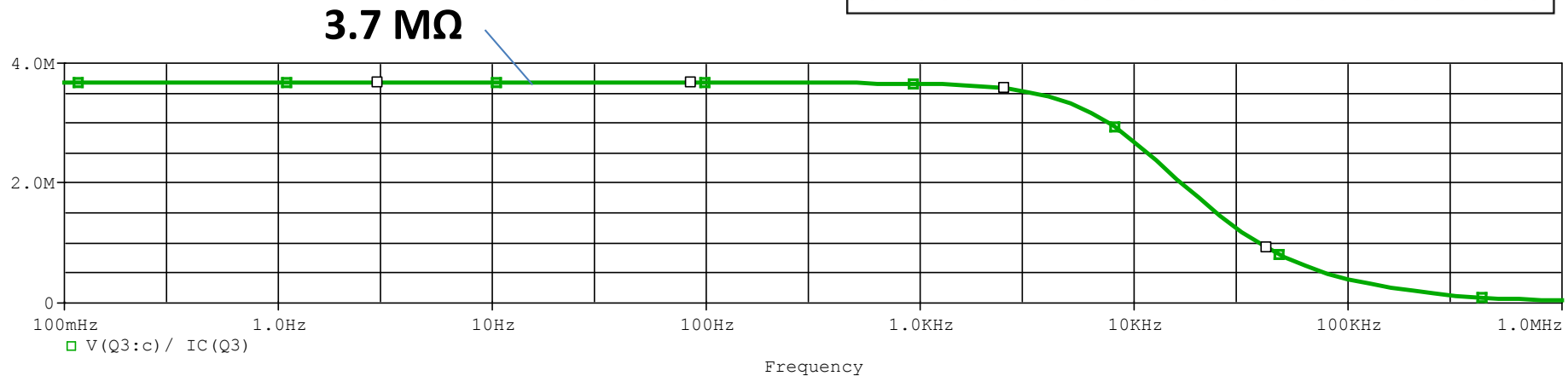
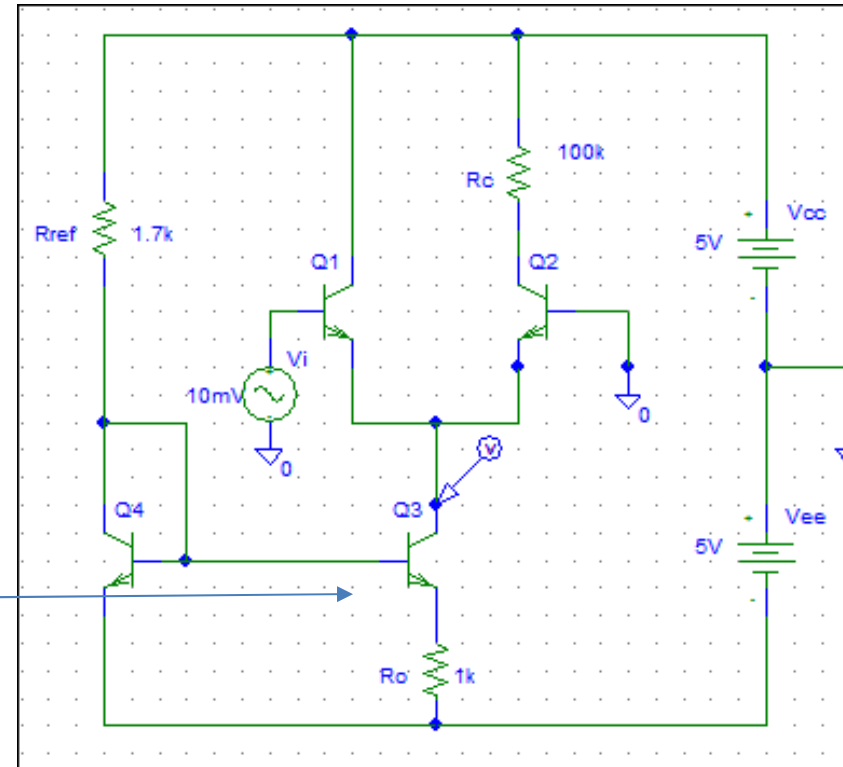
Ro value

$$R_O \sim r_{ce} [1 + g_m R_E]$$



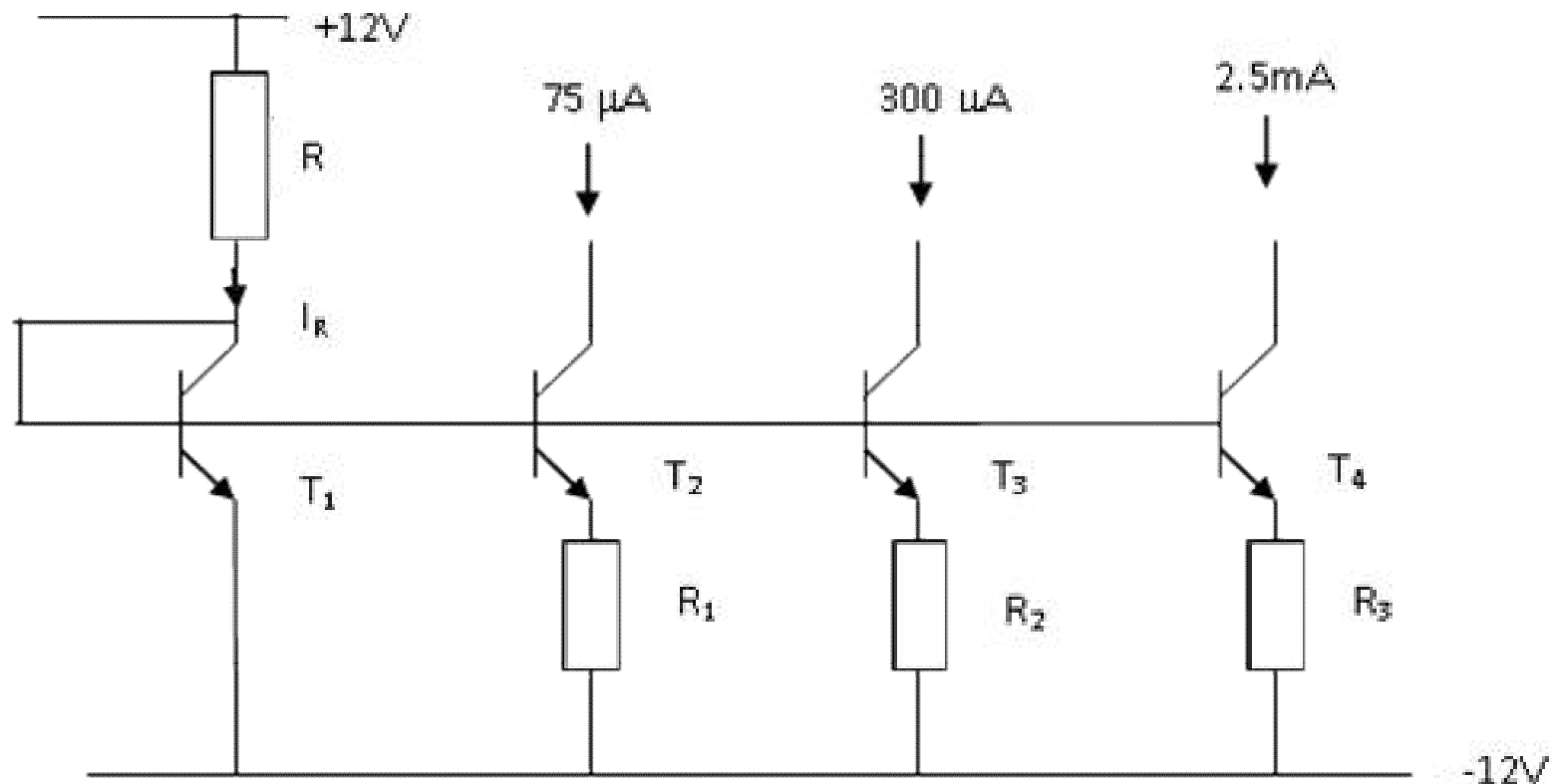
Using Early voltage of 150 V

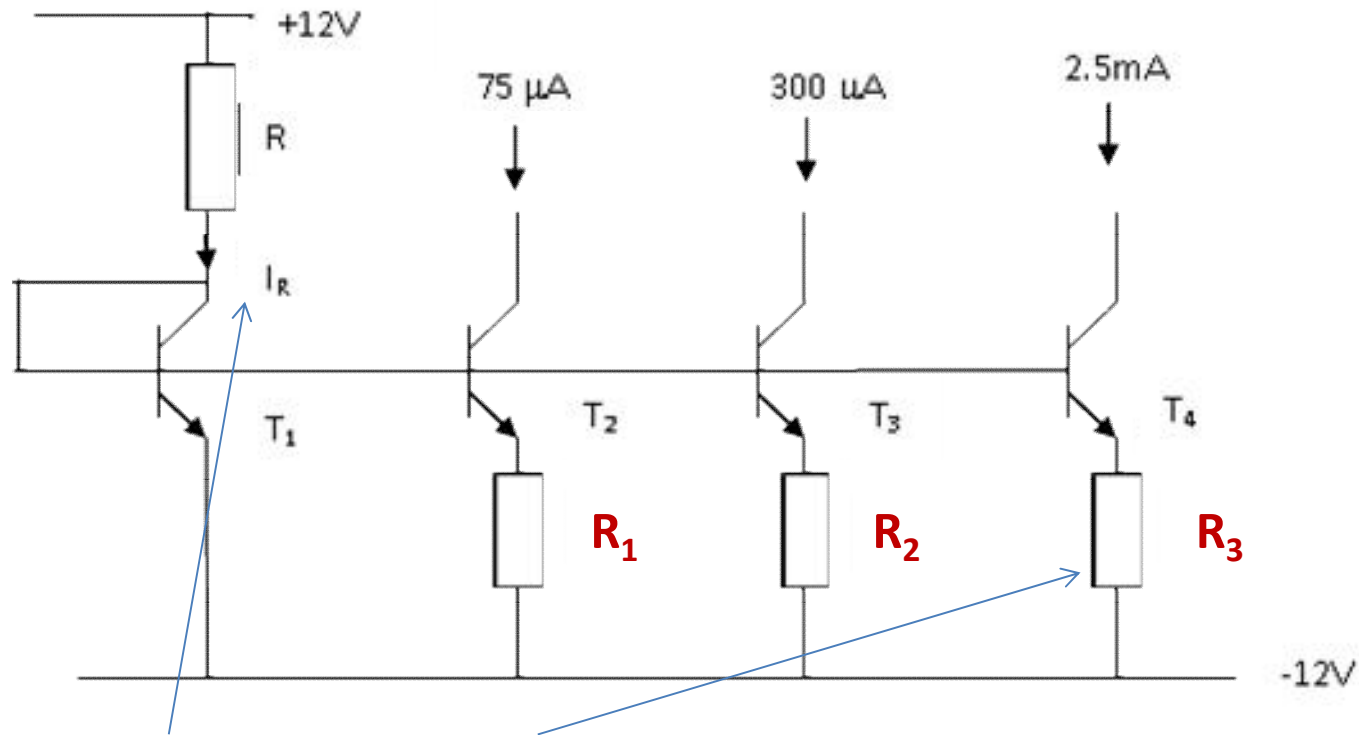
$R_o = 3.7\text{ M}\Omega$ using $V_A = 74\text{ V}$ (2N2222)



Worked Example

An operational amplifier comprises three stages with bias requirements of $75\ \mu\text{A}$, $300\ \mu\text{A}$ and $2.5\ \text{mA}$. Sketch the circuit and design the current mirror arrangement to provide these bias currents. Assume power supplies of $\pm 12\text{V}$, identical transistors with Early voltages, $V_A = 100\ \text{V}$, $V_T = 25\ \text{mV}$ and $V_{BE} = 0.7\text{V}$. Take $r_{ce} = V_A/I_C$.



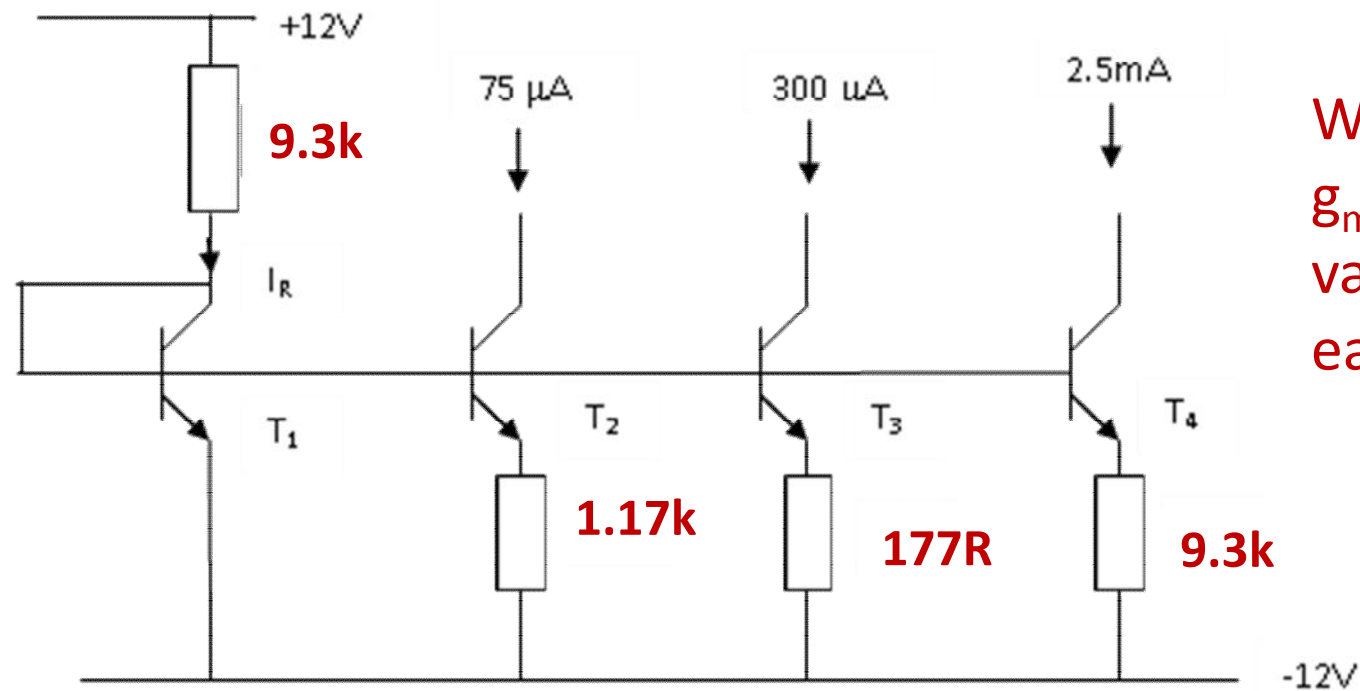


Choose $I_R = 2.5\text{mA}$ then $R_3 = 0$ (simple current mirror)

$$R = \frac{V_{CC} - (-V_{EE} + V_{BE})}{I_R} = \frac{V_{CC} + |V_{EE}| - V_{BE}}{I_R} = \frac{24 - 0.7}{2.5 \times 10^{-3}} = 9.3\text{k}\Omega$$

$$R_1 = \frac{V_T}{I_{O1}} \ln \left(\frac{I_R}{I_{O1}} \right) = \frac{2.5 \times 10^{-3}}{75 \times 10^{-6}} \ln \left(\frac{2.5\text{mA}}{75\mu\text{A}} \right) = 1.17\text{k}\Omega$$

$$R_2 = \frac{V_T}{I_{O2}} \ln \left(\frac{I_R}{I_{O2}} \right) = \frac{2.5 \times 10^{-3}}{300 \times 10^{-6}} \ln \left(\frac{2.5\text{mA}}{300\mu\text{A}} \right) = 177\Omega$$



Work out g_m and r_{ce} values for each transistor

$$R_{o2} \sim r_{ce2} [1 + g_{m2} \times R_1] = 1.3 \times 10^6 [1 + 3 \times 10^{-3} \times 1.17 \times 10^3] = 5.86 M\Omega$$

$$R_{o3} \sim r_{ce3} [1 + g_{m3} \times R_2] = 333 \times 10^3 [1 + 12 \times 10^{-3} \times 177] = 1.04 M\Omega$$

$$R_{o4} \sim r_{ce4} [1 + g_{m4} \times 0] = 40 \times 10^3 = 40 k\Omega$$

MCQ

Current sources are used for the following purpose:

- a) Provide more gain
- b) To provide the DC bias for circuits
- c) Reduce power consumption
- d) Increase amplifier output resistance

MCQ

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- a) Provide more gain
- b) To provide the DC bias for circuits**
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MCQ

For the differential amplifier, use of a current source has the benefit of:

- a) Increasing the differential gain
- b) Increasing the common-mode gain
- c) Decreasing the common-mode rejection ratio
- d) Increasing the common-mode rejection ratio

MCQ

For the differential amplifier, use of a current source has the benefit of:

- a) Increasing the differential gain
- b) Increasing the common-mode gain
- c) Decreasing the common-mode rejection ratio
- d) Increasing the common-mode rejection ratio

Milestone...

Differential amplifier
Two outputs

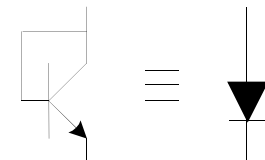
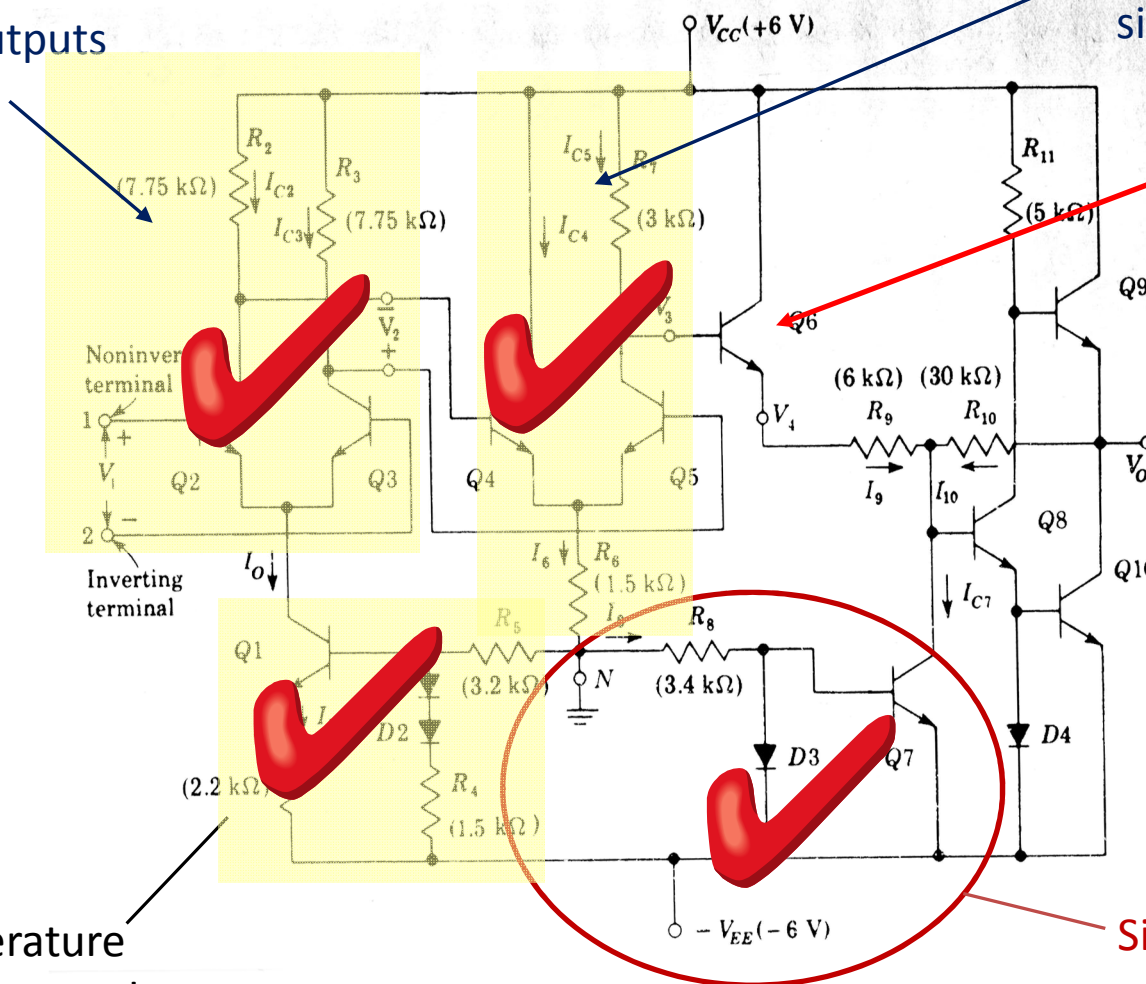
Differential amplifier
single output

Signal goes
into base,
comes out of
emitter
??????

- Identify building blocks
- Perform a d.c. analysis
- Perform an a.c. analysis

Temperature
compensated
current source

Simple current
mirror

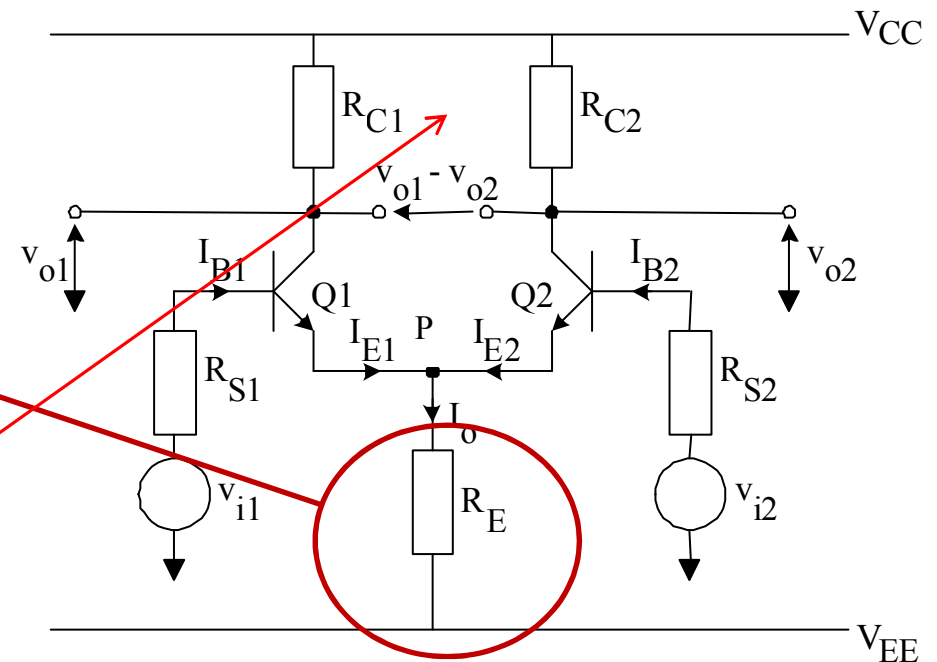


Next lecture

Recall the 'problems' with the Diff Amp

We require

- a better bias circuit to replace R_E , which will allow us to set the current I_o independently of the resistance in the 'tail'
- We would also like such a bias circuit to exhibit a very large dynamic resistance to give high common mode rejection ratio (CMRR).



ACTIVE LOADS:

replace the collector resistors to give a high resistance (for high gain)