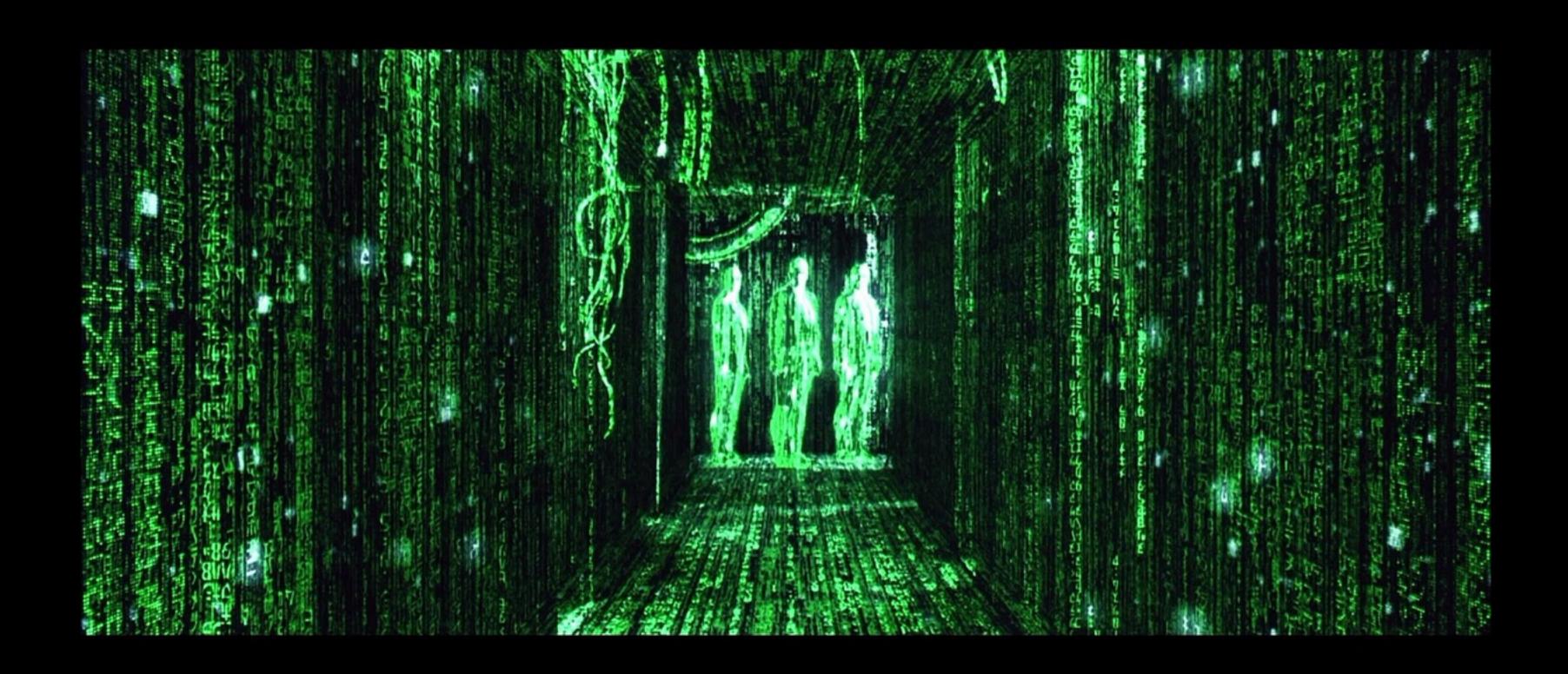
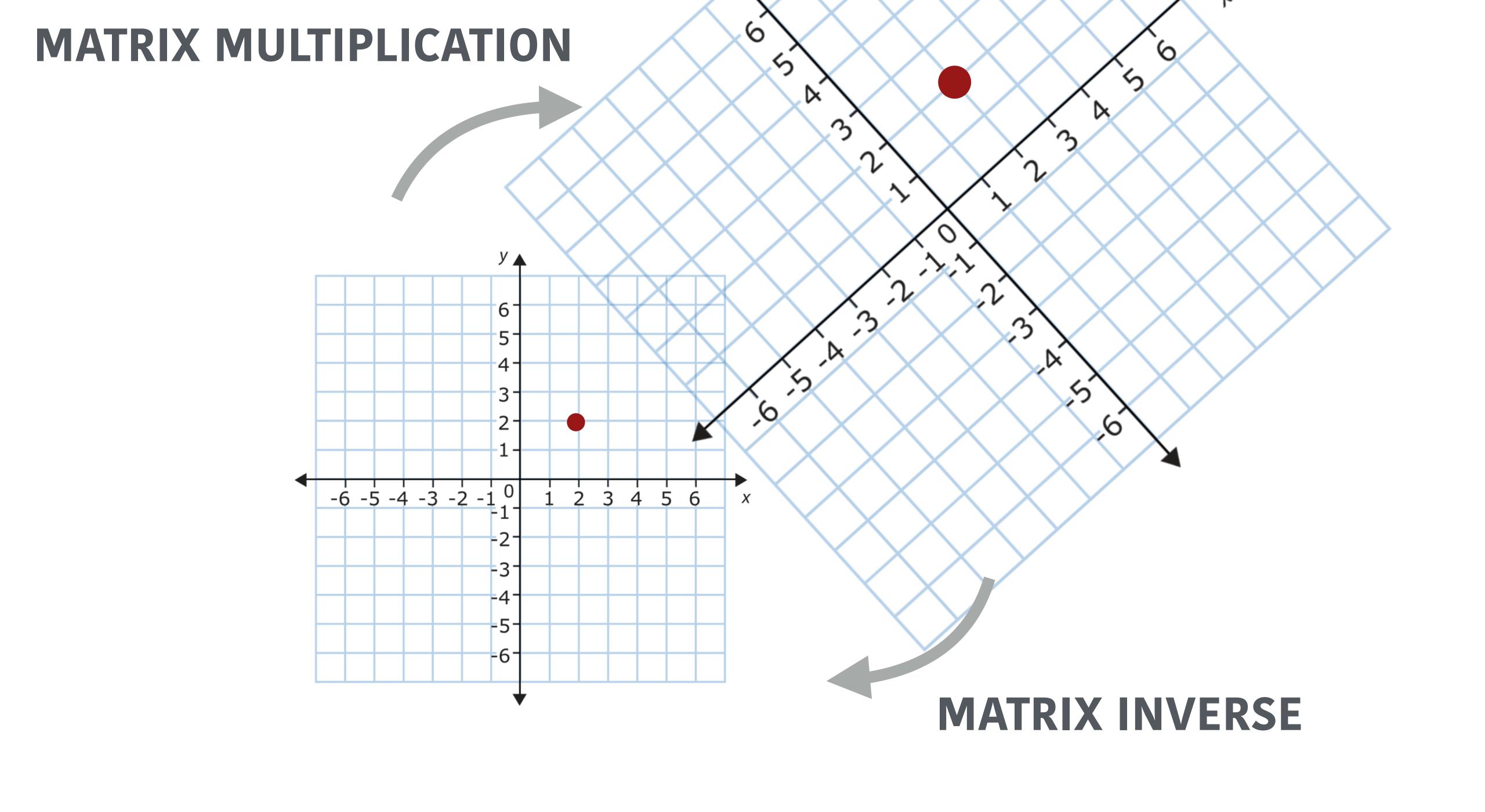
### Matrix transformations.

#### Part 2

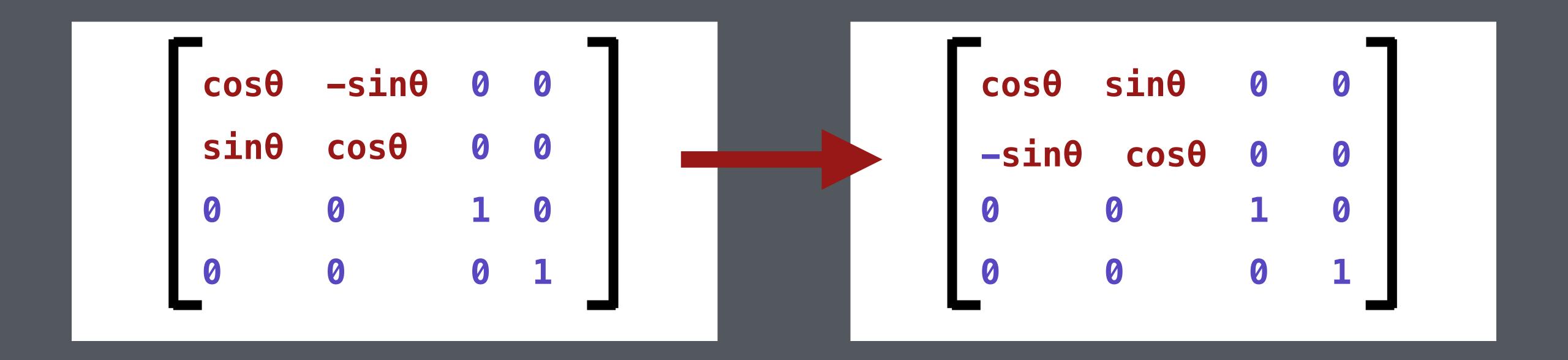


A **matrix** that "undoes" the transformation of the original matrix.



- Scaled by 1/scale

- Scaled by 1/scale
- Rotated by the transpose of the linear part of the matrix.



- Scaled by 1/scale
- Rotated by the transpose of the rotation.
- Translated by the translation \* -1

## The Inverse

```
Matrix Matrix::inverse() {
    float m00 = m[0][0], m01 = m[0][1], m02 = m[0][2], m03 = m[0][3];
    float m10 = m[1][0], m11 = m[1][1], m12 = m[1][2], m13 = m[1][3];
   float m20 = m[2][0], m21 = m[2][1], m22 = m[2][2], m23 = m[2][3];
   float m30 = m[3][0], m31 = m[3][1], m32 = m[3][2], m33 = m[3][3];
   float v0 = m20 * m31 - m21 * m30;
   float v1 = m20 * m32 - m22 * m30;
   float v2 = m20 * m33 - m23 * m30;
   float v3 = m21 * m32 - m22 * m31;
   float v4 = m21 * m33 - m23 * m31;
   float v5 = m22 * m33 - m23 * m32;
   float t00 = + (v5 * m11 - v4 * m12 + v3 * m13);
   float t10 = - (v5 * m10 - v2 * m12 + v1 * m13);
   float t20 = + (v4 * m10 - v2 * m11 + v0 * m13);
   float t30 = - (v3 * m10 - v1 * m11 + v0 * m12);
   float invDet = 1 / (t00 * m00 + t10 * m01 + t20 * m02 + t30 * m03);
   float d00 = t00 * invDet:
   float d10 = t10 * invDet;
   float d20 = t20 * invDet;
   float d30 = t30 * invDet;
   float d01 = - (v5 * m01 - v4 * m02 + v3 * m03) * invDet;
   float d11 = + (v5 * m00 - v2 * m02 + v1 * m03) * invDet;
   float d21 = - (v4 * m00 - v2 * m01 + v0 * m03) * invDet;
   float d31 = + (v3 * m00 - v1 * m01 + v0 * m02) * invDet;
   v0 = m10 * m31 - m11 * m30;
   v1 = m10 * m32 - m12 * m30;
   v2 = m10 * m33 - m13 * m30;
   v3 = m11 * m32 - m12 * m31;
   v4 = m11 * m33 - m13 * m31;
   v5 = m12 * m33 - m13 * m32;
    float d02 = + (v5 * m01 - v4 * m02 + v3 * m03) * invDet;
   float d12 = - (v5 * m00 - v2 * m02 + v1 * m03) * invDet;
   float d22 = + (v4 * m00 - v2 * m01 + v0 * m03) * invDet;
   float d32 = -(v3 * m00 - v1 * m01 + v0 * m02) * invDet;
   v0 = m21 * m10 - m20 * m11;
   v1 = m22 * m10 - m20 * m12;
   v2 = m23 * m10 - m20 * m13;
   v3 = m22 * m11 - m21 * m12;
   v4 = m23 * m11 - m21 * m13;
   v5 = m23 * m12 - m22 * m13;
   float d03 = - (v5 * m01 - v4 * m02 + v3 * m03) * invDet;
   float d13 = + (v5 * m00 - v2 * m02 + v1 * m03) * invDet;
   float d23 = -(v4 * m00 - v2 * m01 + v0 * m03) * invDet;
   float d33 = + (v3 * m00 - v1 * m01 + v0 * m02) * invDet;
   Matrix m2;
   m2.m[0][0] = d00;
   m2.m[0][1] = d01;
   m2.m[0][2] = d02;
   m2.m[0][3] = d03;
   m2.m[1][0] = d10;
   m2.m[1][1] = d11;
   m2.m[1][2] = d12;
   m2.m[1][3] = d13;
   m2.m[2][0] = d20;
   m2.m[2][1] = d21;
   m2.m[2][2] = d22;
   m2.m[2][3] = d23;
   m2.m[3][0] = d30;
   m2.m[3][1] = d31;
   m2.m[3][2] = d32;
   m2.m[3][3] = d33;
   return m2;
```

### The matrix class.

# Row major vs. column major.

$$egin{bmatrix} {
m Row\ major} & {
m Column\ major} \ 1 & 2 & 3 \ 4 & 5 & 6 \ 7 & 8 & 9 \end{bmatrix} & \begin{bmatrix} 1 & 4 & 7 \ 2 & 5 & 8 \ 3 & 6 & 9 \end{bmatrix}$$

We will use column major order as our standard.

### A vector class.

```
class Vector {
    public:

        Vector();
        Vector(float x, float y, float z);

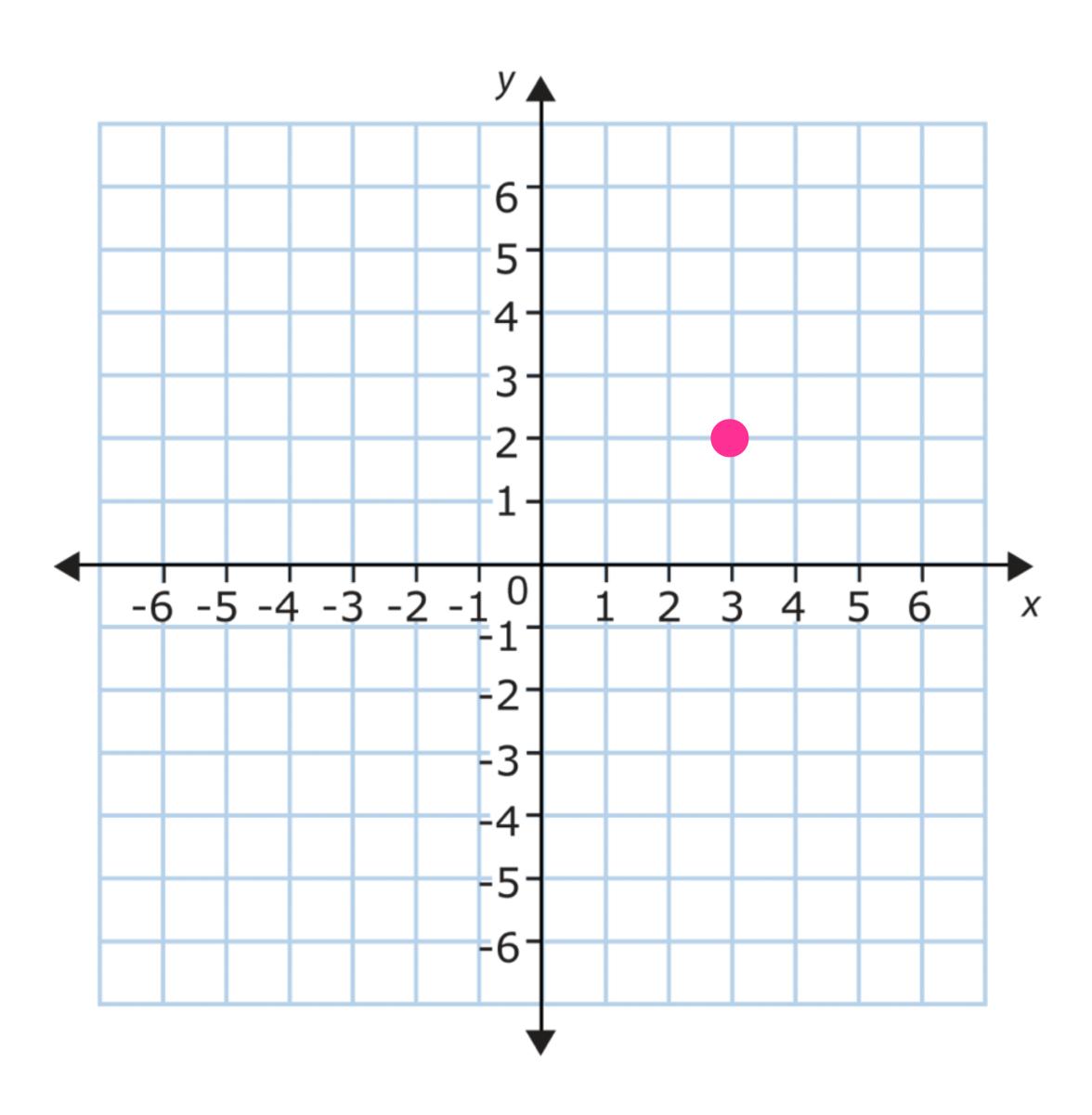
        float length();
        void normalize();

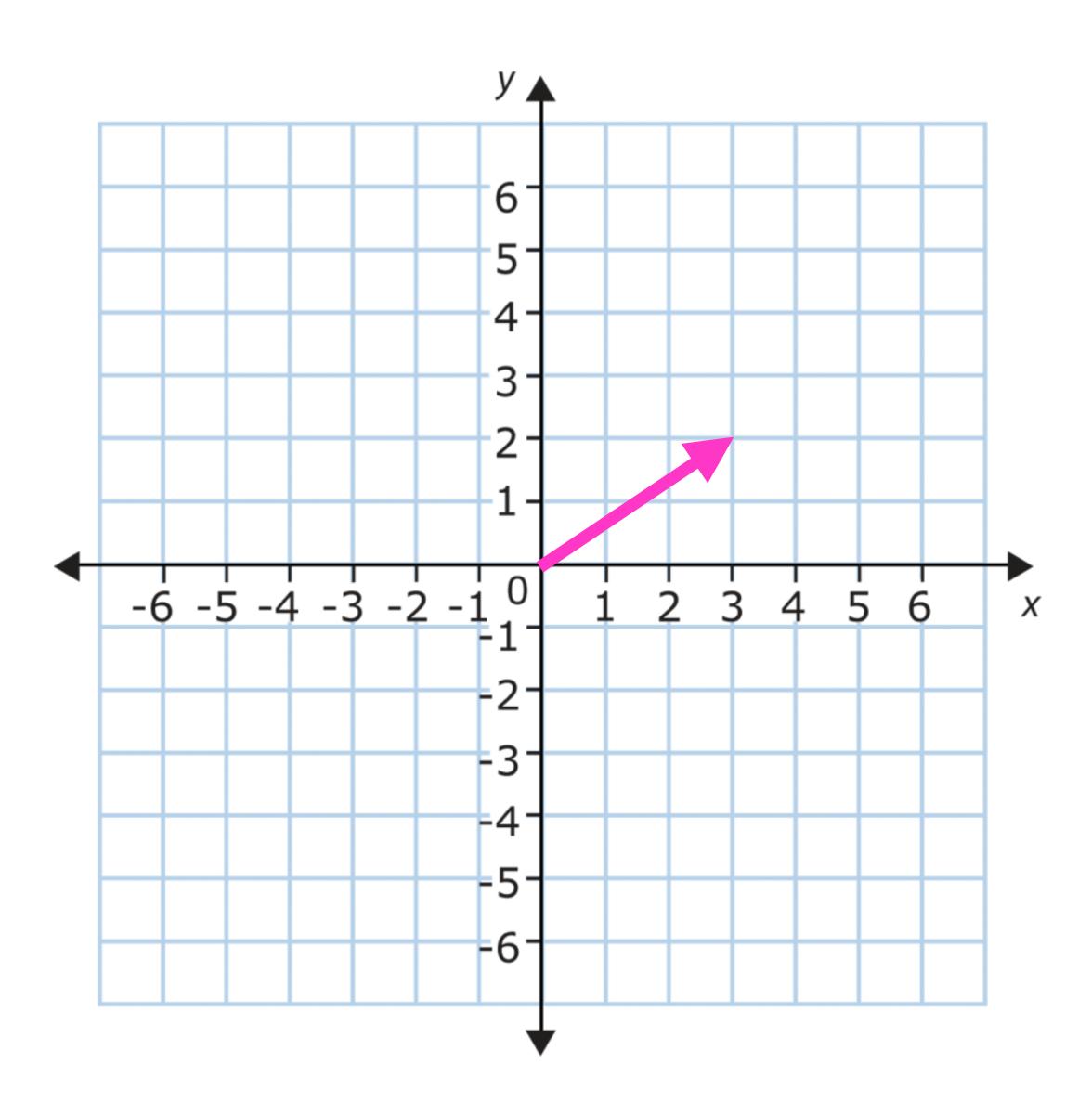
        float x;
        float y;
        float z;
};
```

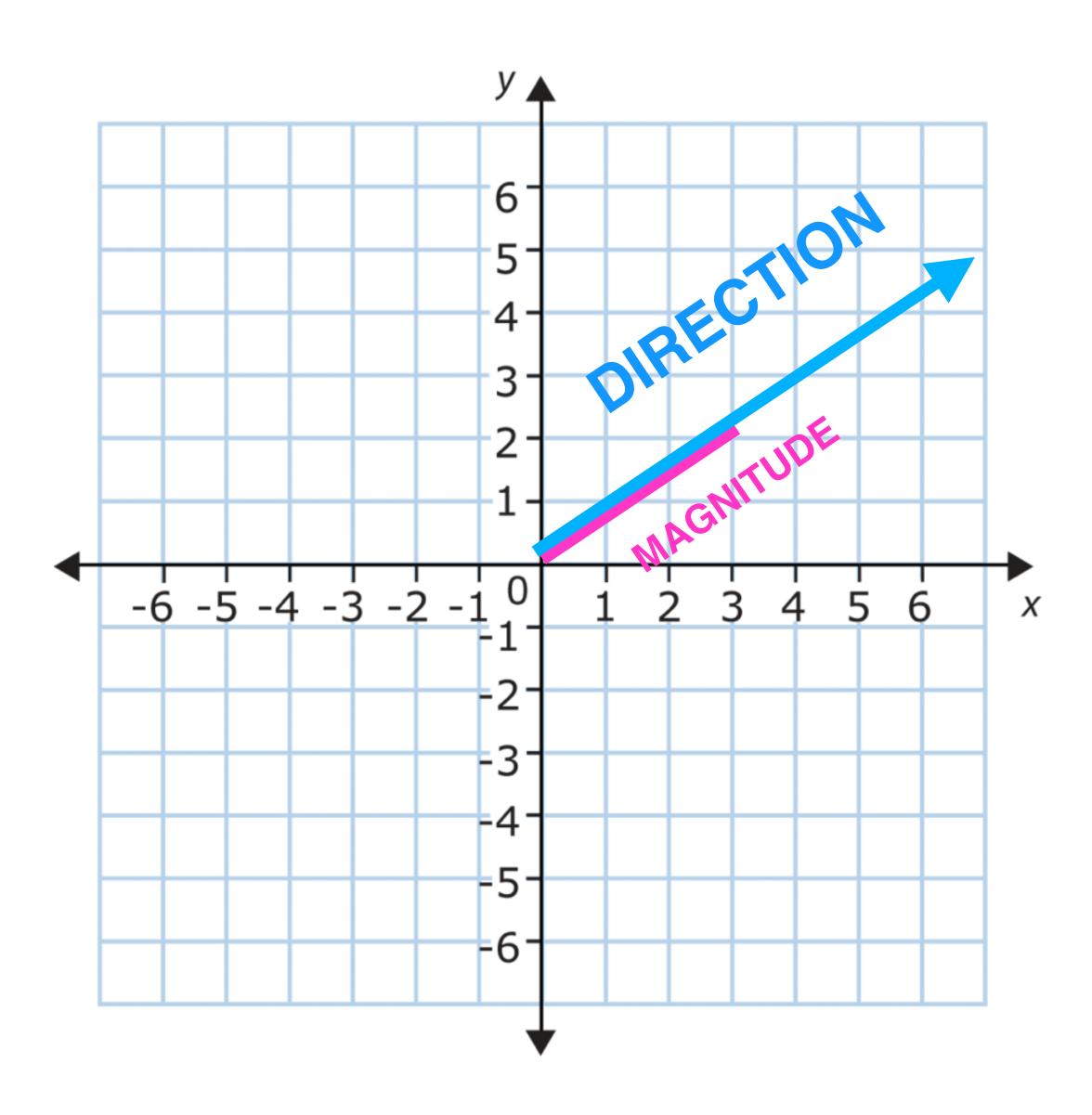
# Vector length.



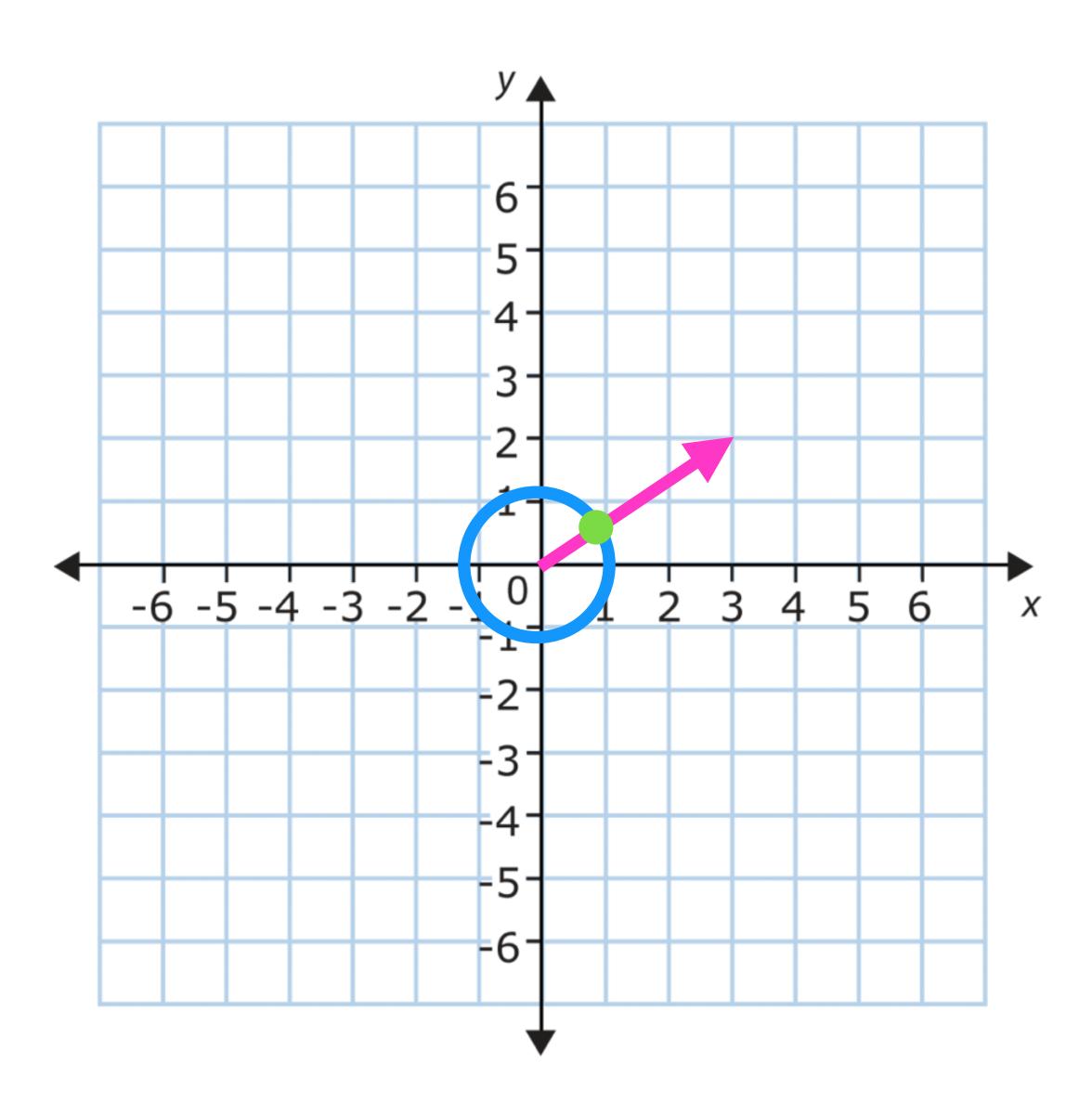
# Normalizing a vector.







# Divide each vector component by the vector length (just be careful if the length is 0!).



# Multiplying matrices and vectors.

```
Vector operator * (const Vector &v);
```

### Creating final entity model matrix.

# Identity matrix.

```
      1
      0
      0
      0

      0
      1
      0
      0

      0
      0
      1
      0

      0
      0
      0
      1
```

#### Scale matrix.

```
Sx 0 0 0 0 0 0 Sy 0 0 0 0 Sz 0 0 0 1
```

#### Translate matrix.

```
      1
      0
      0
      Tx

      0
      1
      0
      Ty

      0
      0
      1
      Tz

      0
      0
      0
      1
```

### Z-axis rotation matrix.

```
      cosθ
      -sinθ
      0

      sinθ
      cosθ
      0

      0
      0
      1

      0
      0
      1
```

# Building the final matrix.

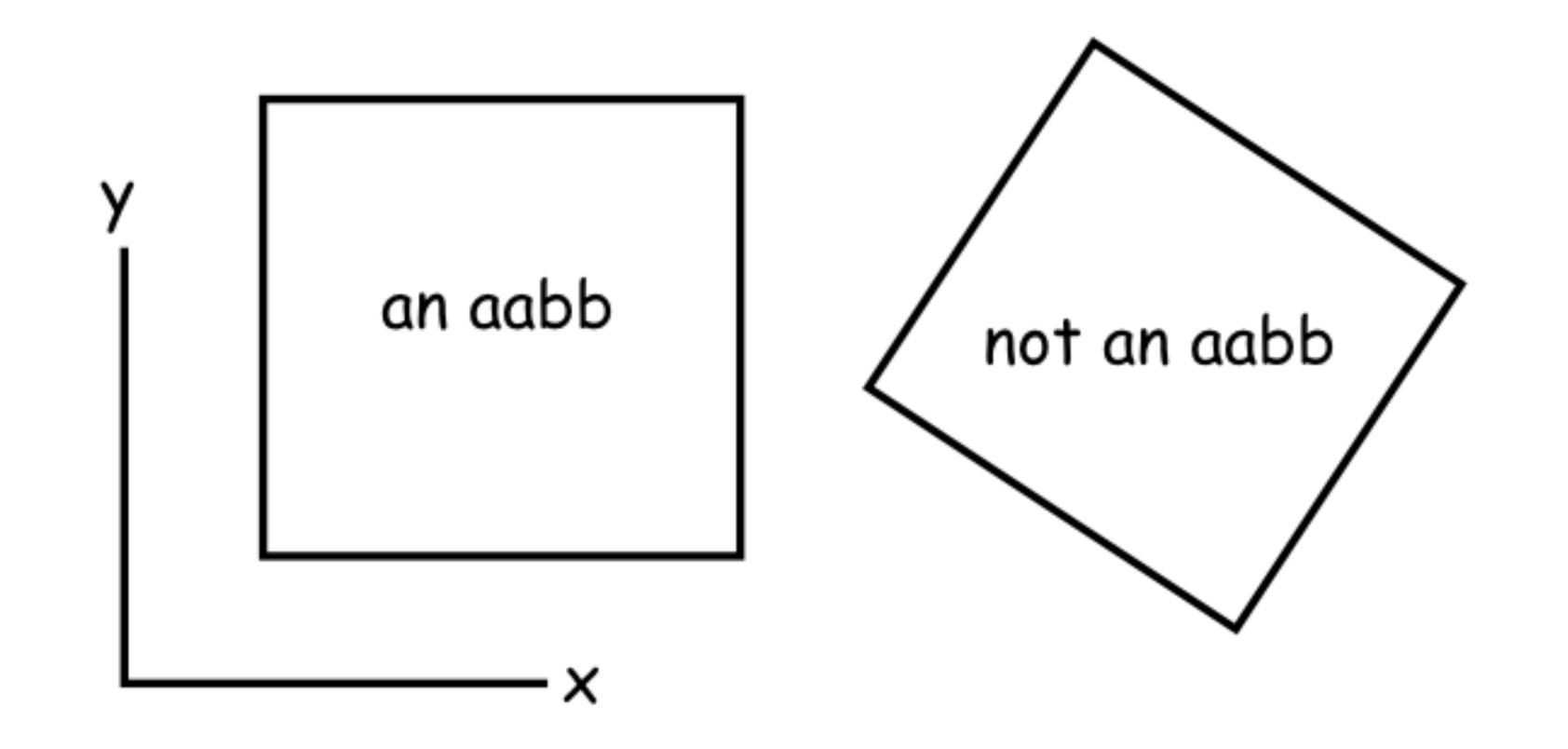


Remember that the order of matrix transform multiplication matters!

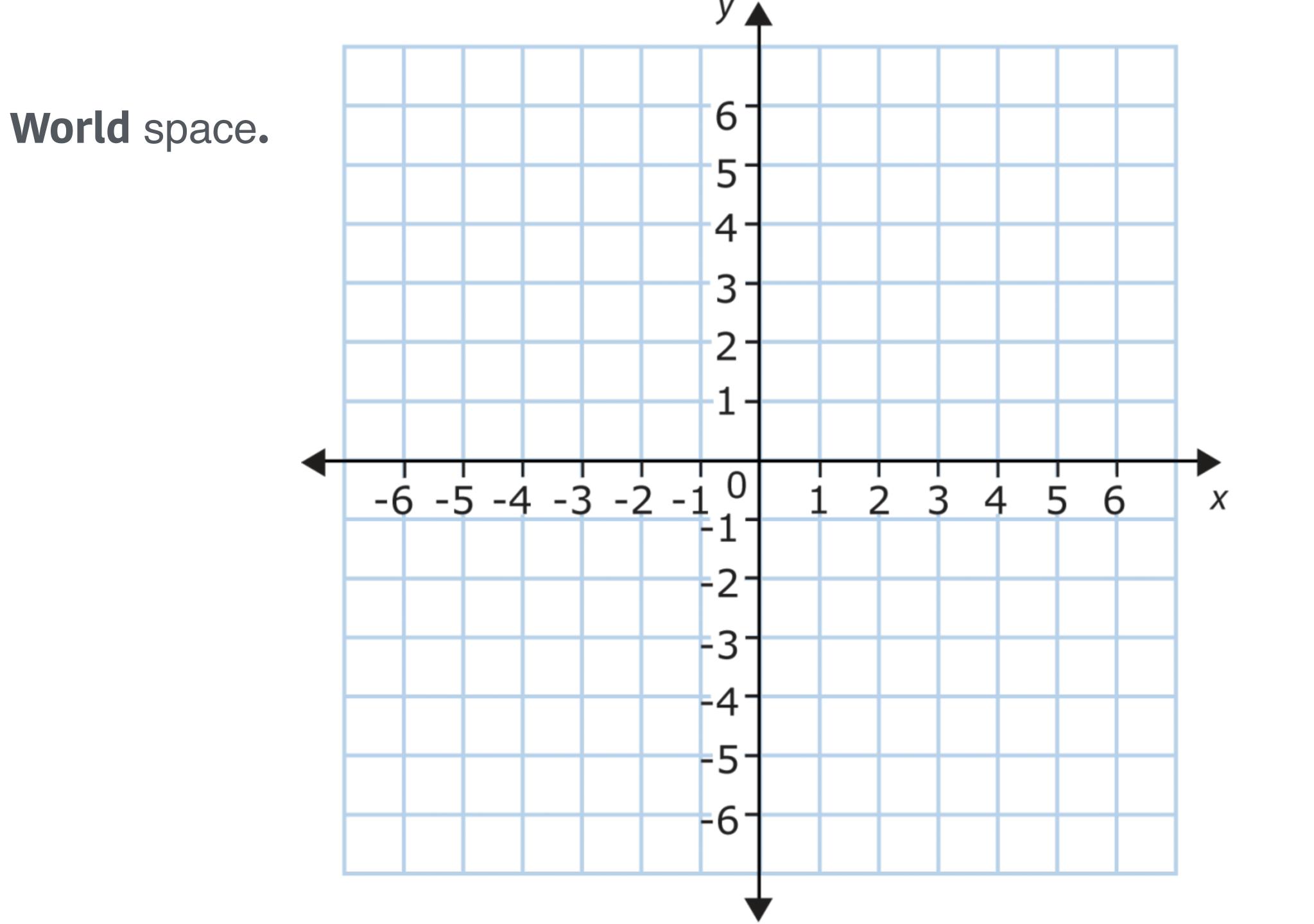
```
class Entity {
public:
    Matrix matrix;
    float x;
    float y;
    float scale_x;
    float scale_y;
    float rotation;
```

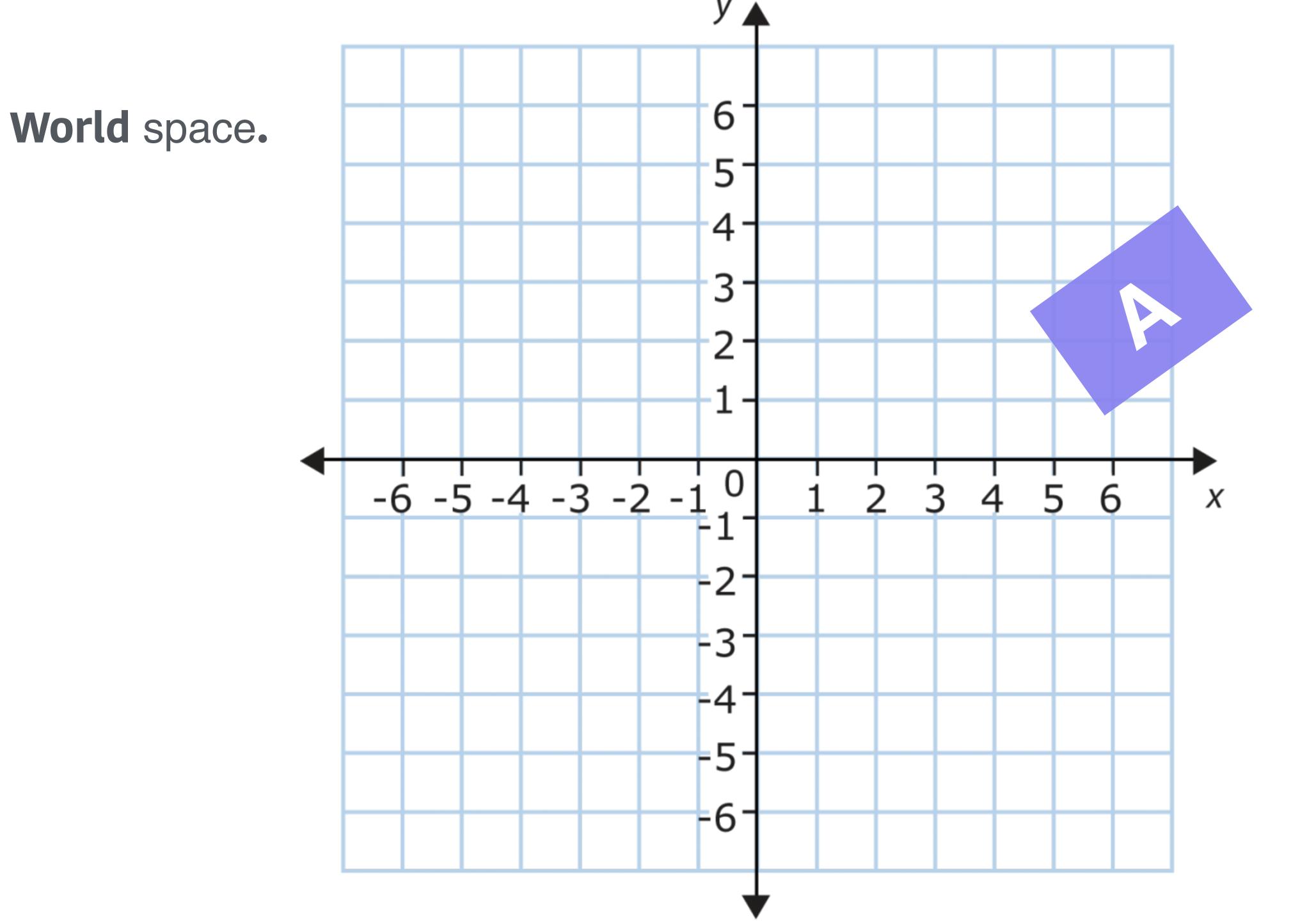
Benefits of storing the transformation matrix.

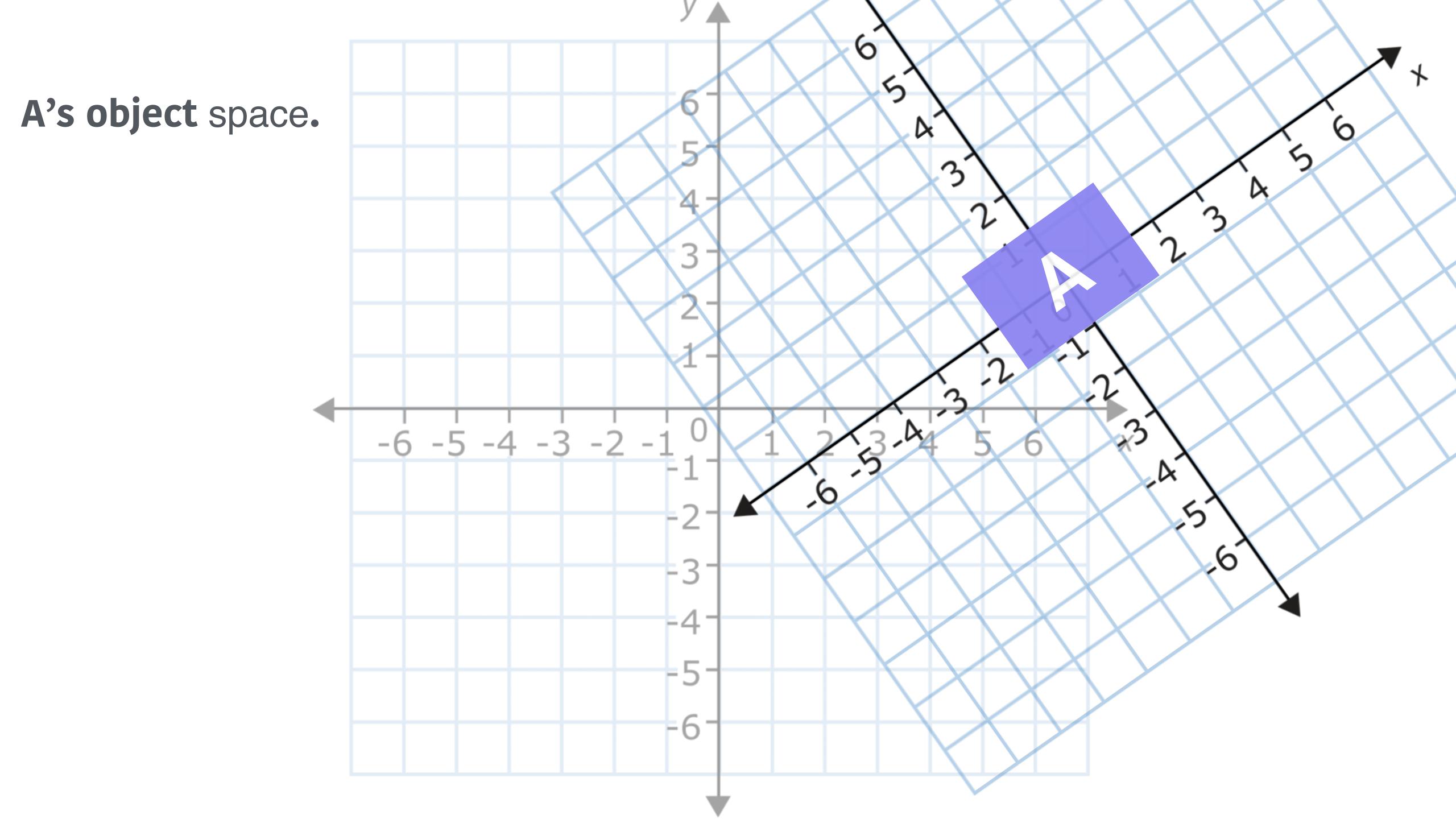
# Non-axis aligned bounding boxes.

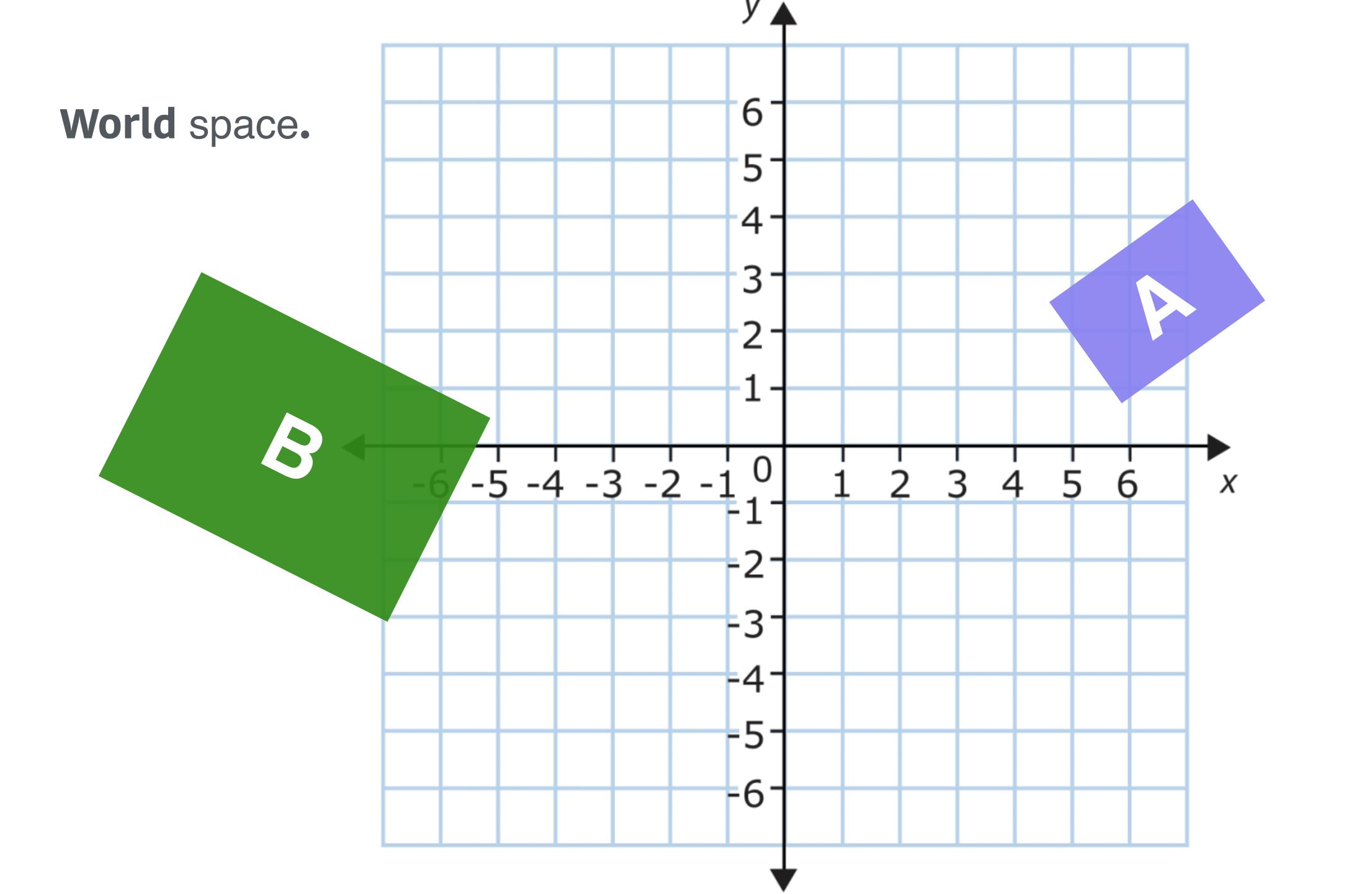


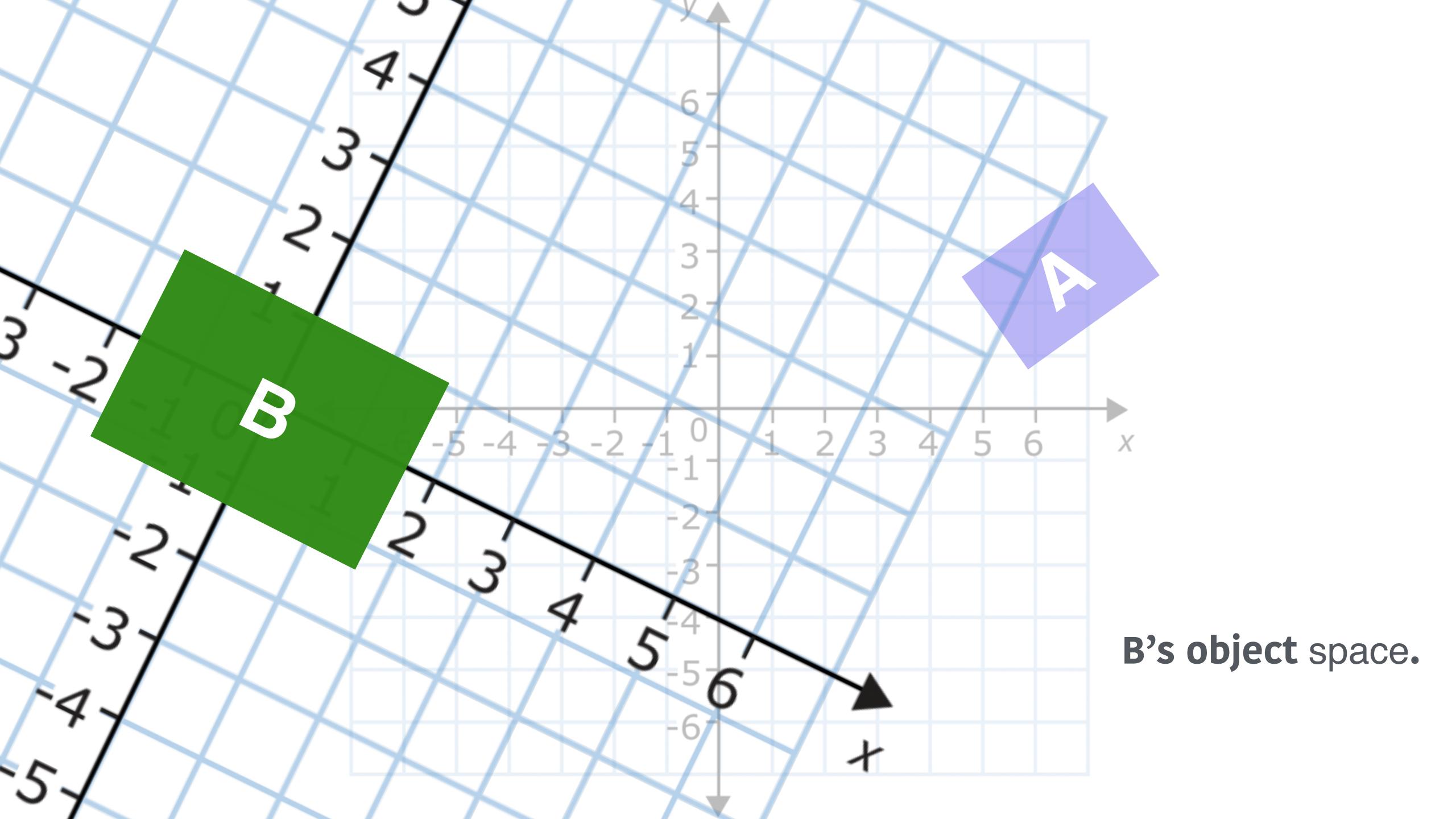
Transforming between coordinate spaces.

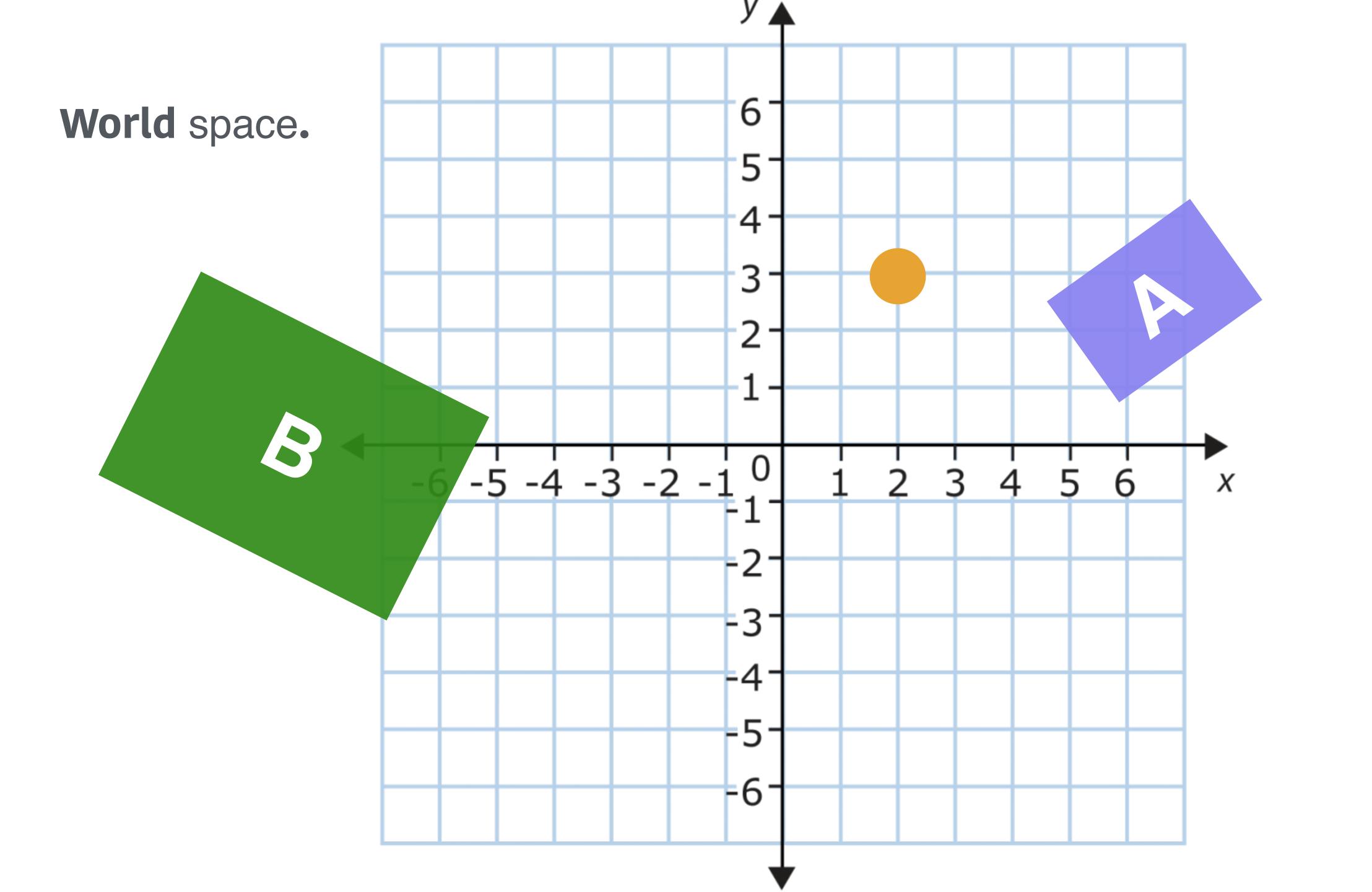


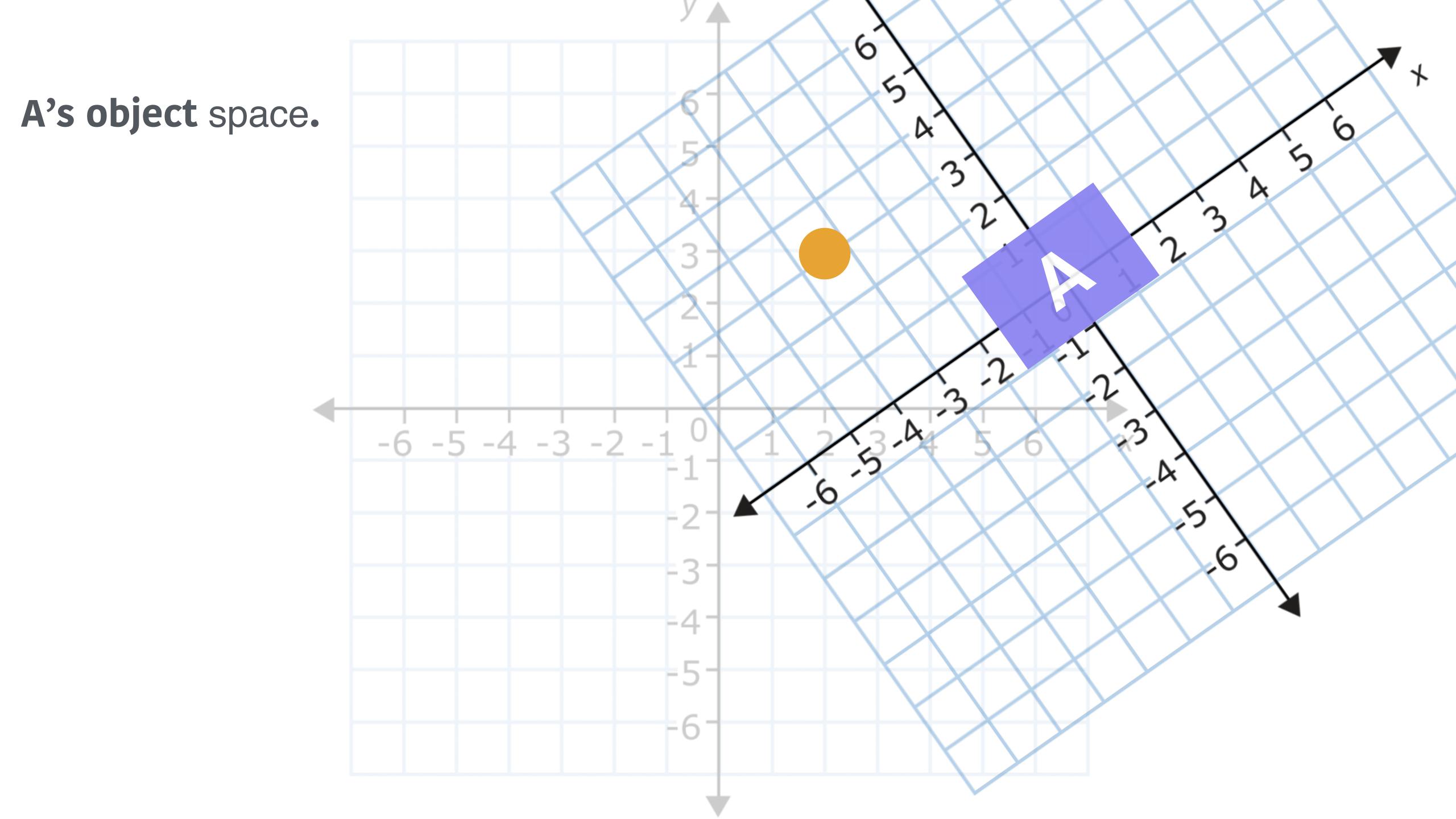


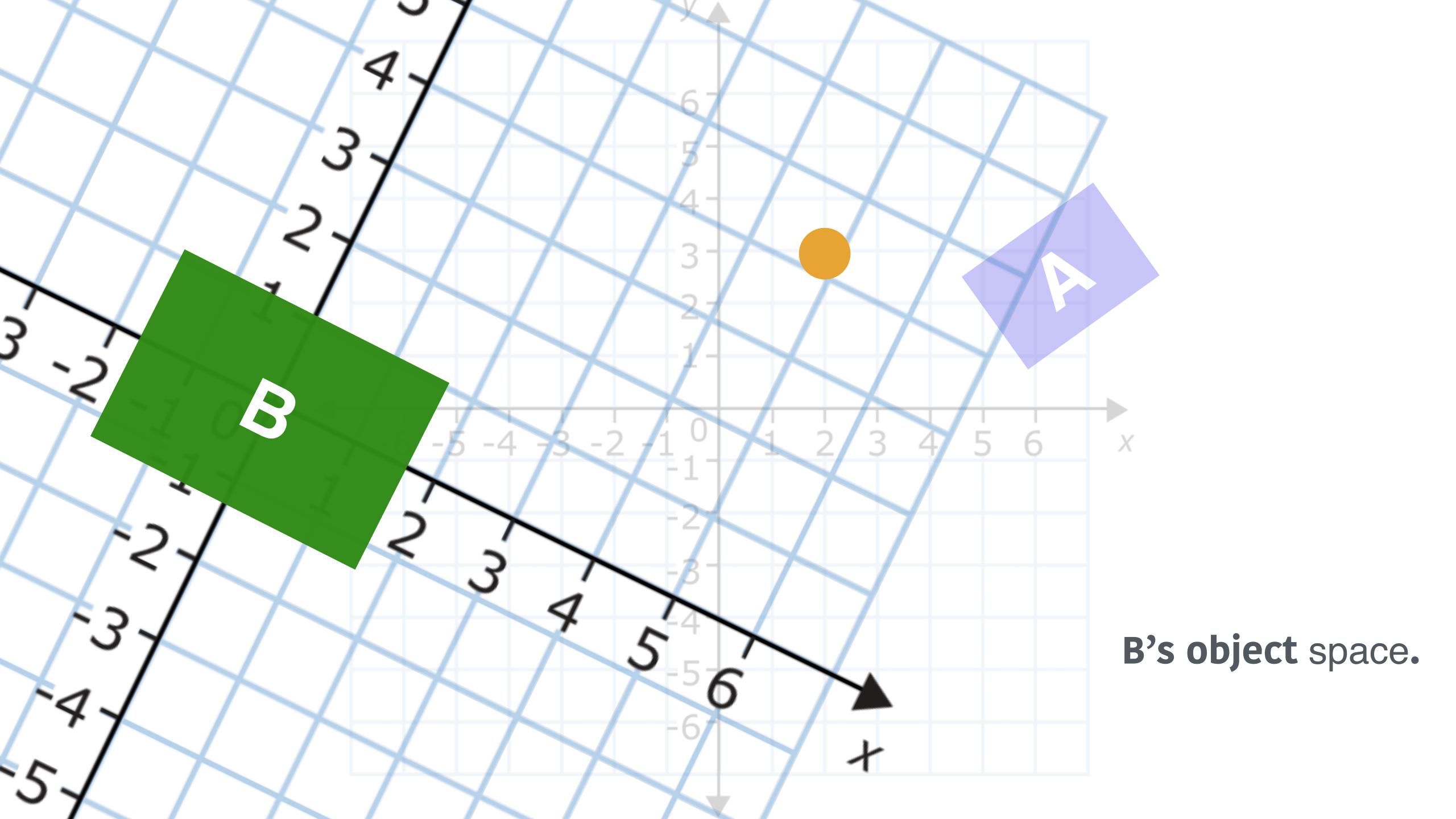


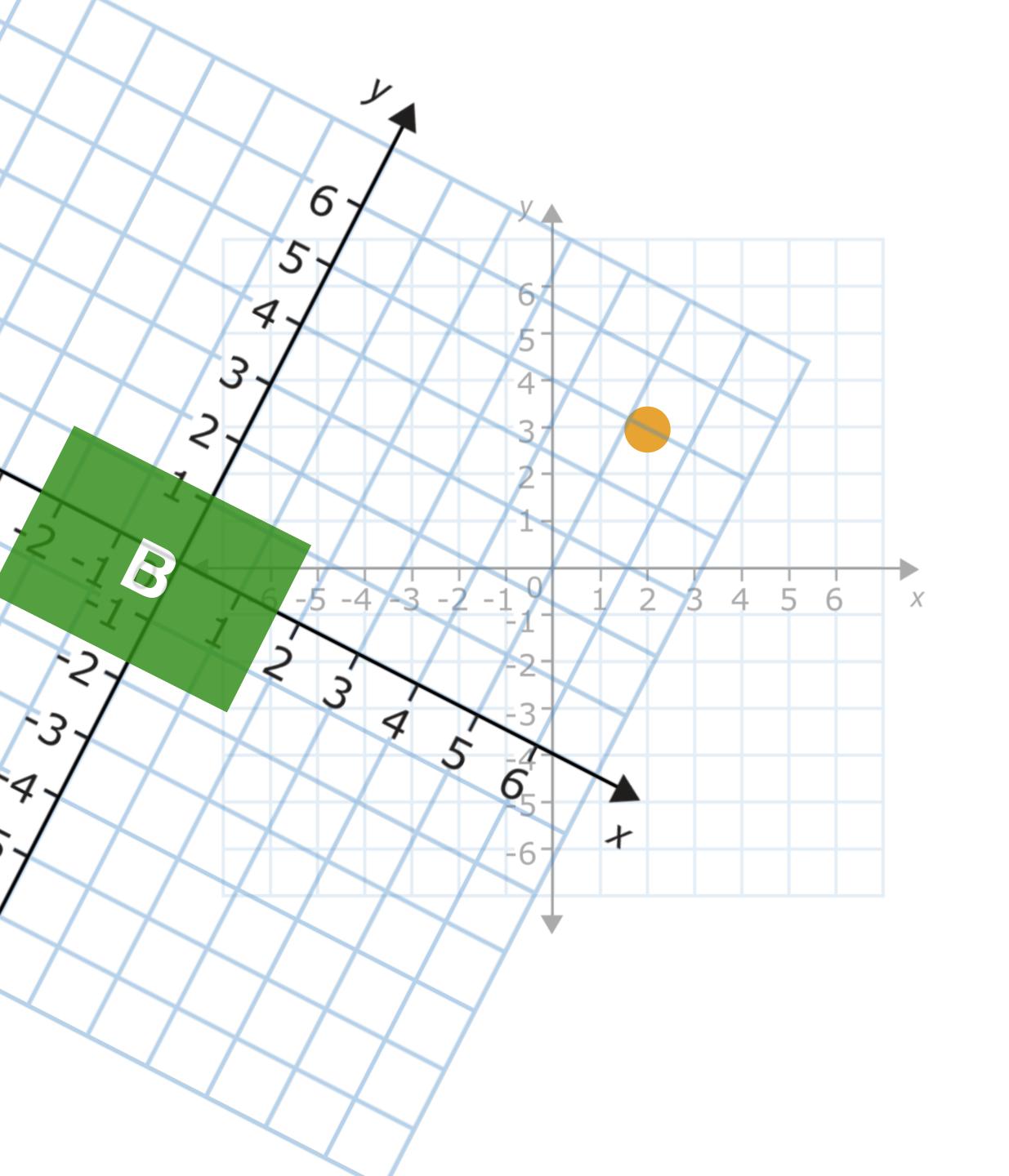




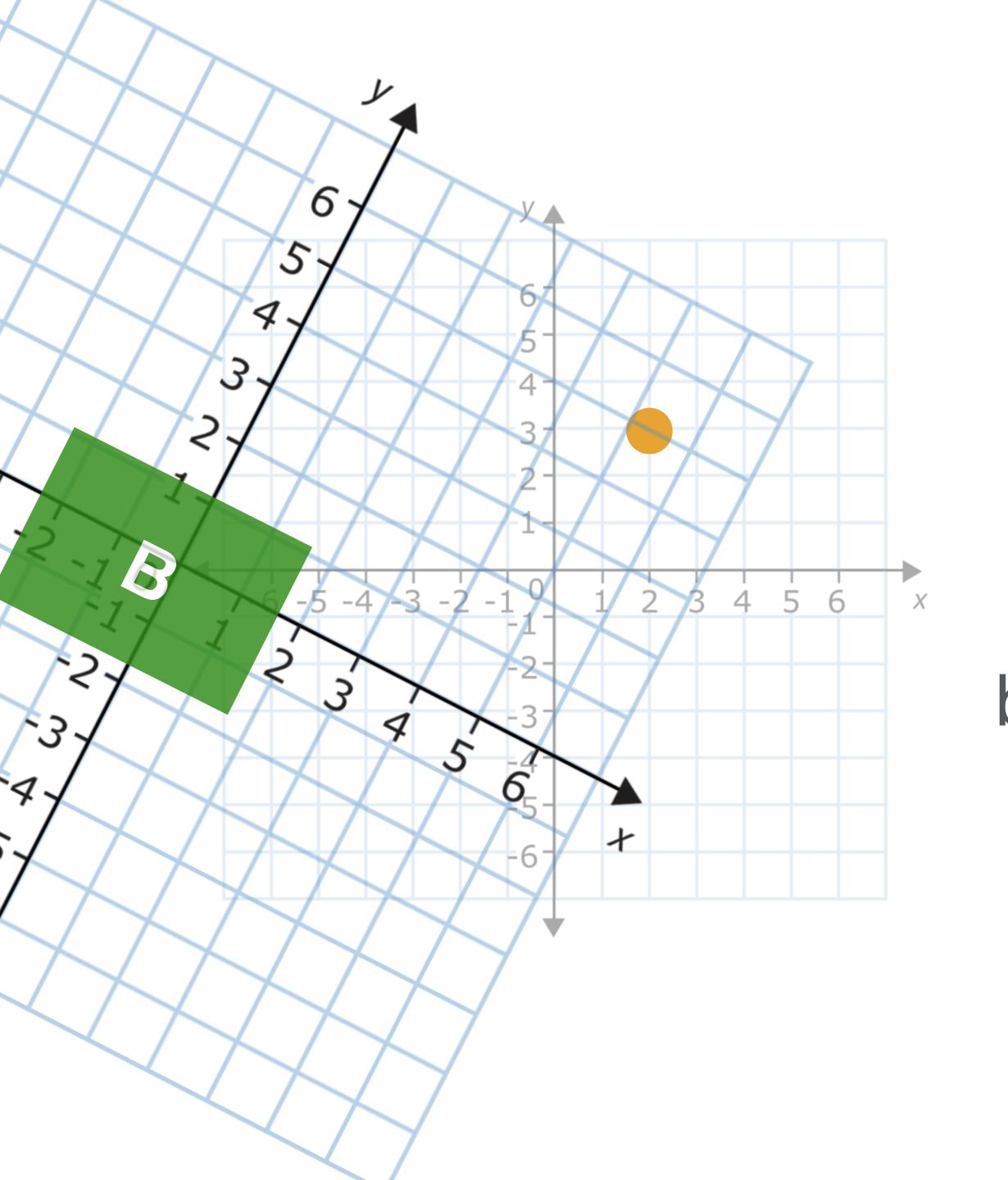




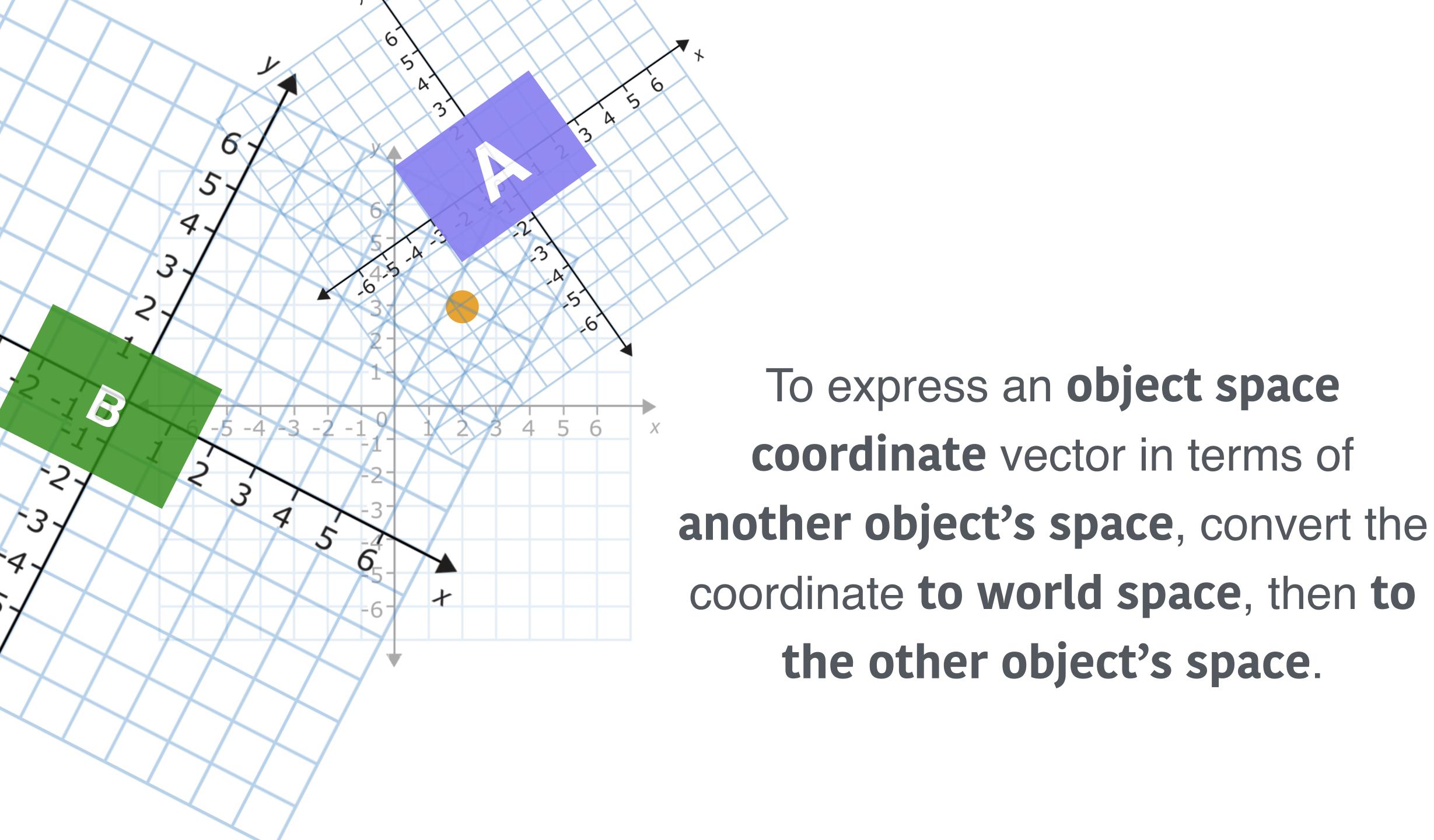




To express a world space coordinate vector in terms of an entity's **object space**, multiply the vector by the **inverse** of that entity's transform matrix.



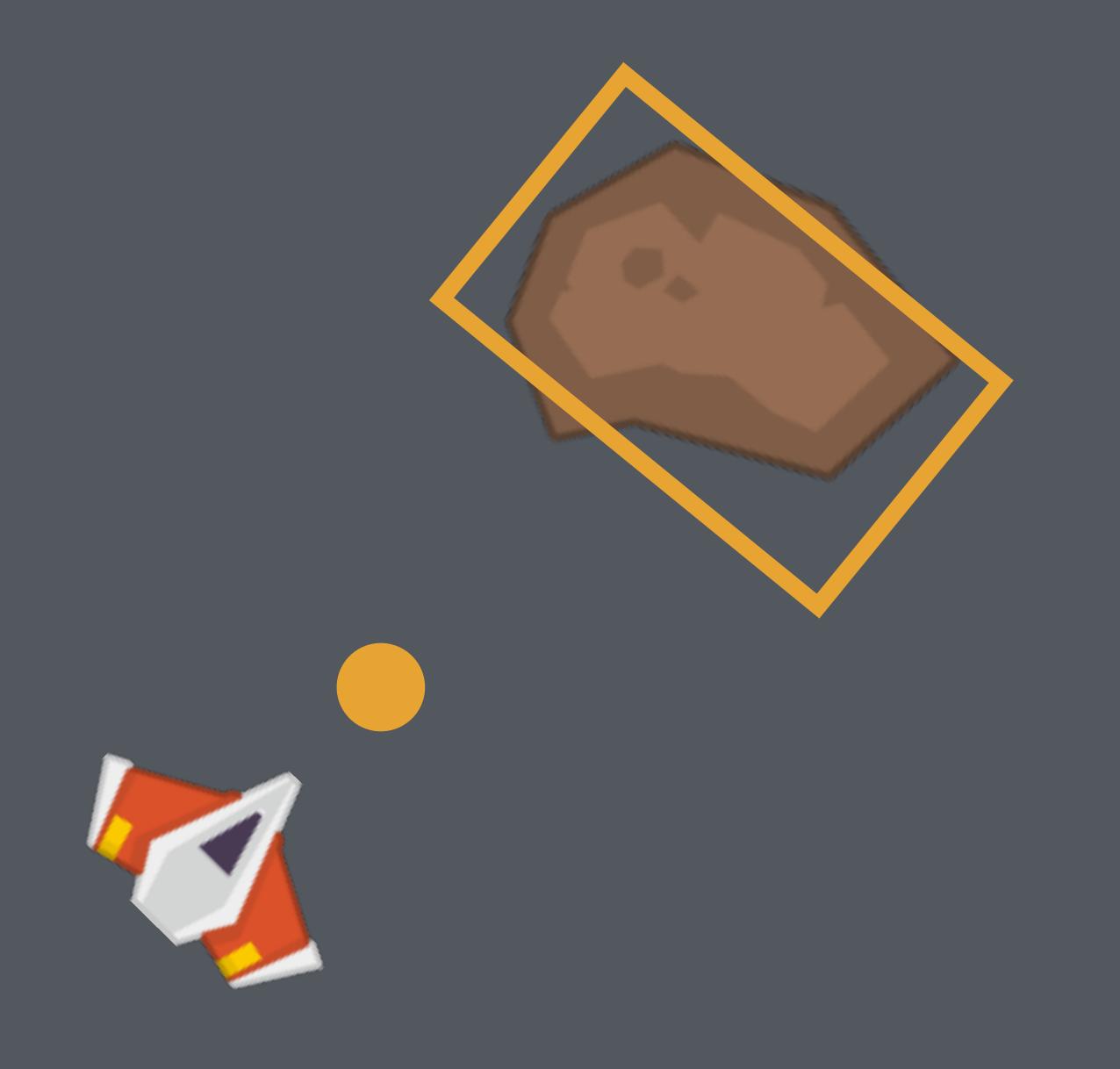
To express an **object space** coordinate vector in terms of **world space**, multiply the vector by that entity's **transform matrix**.

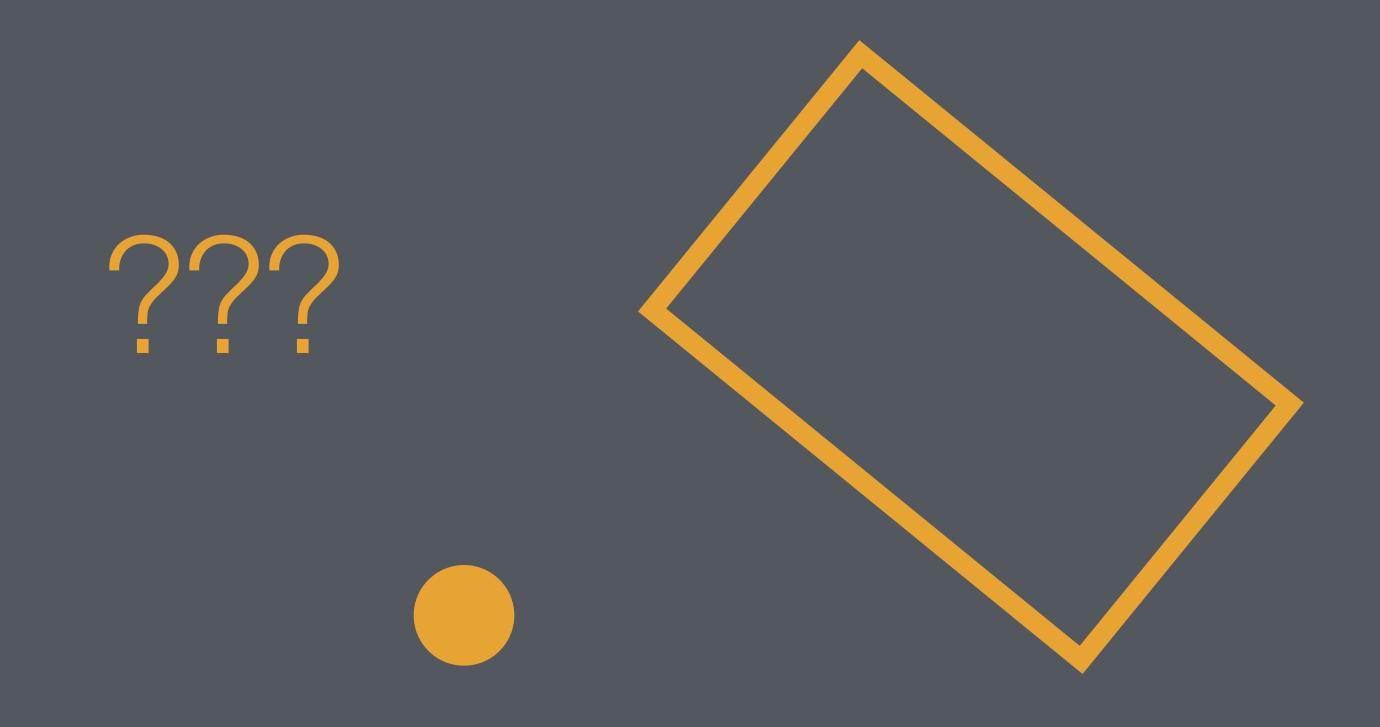


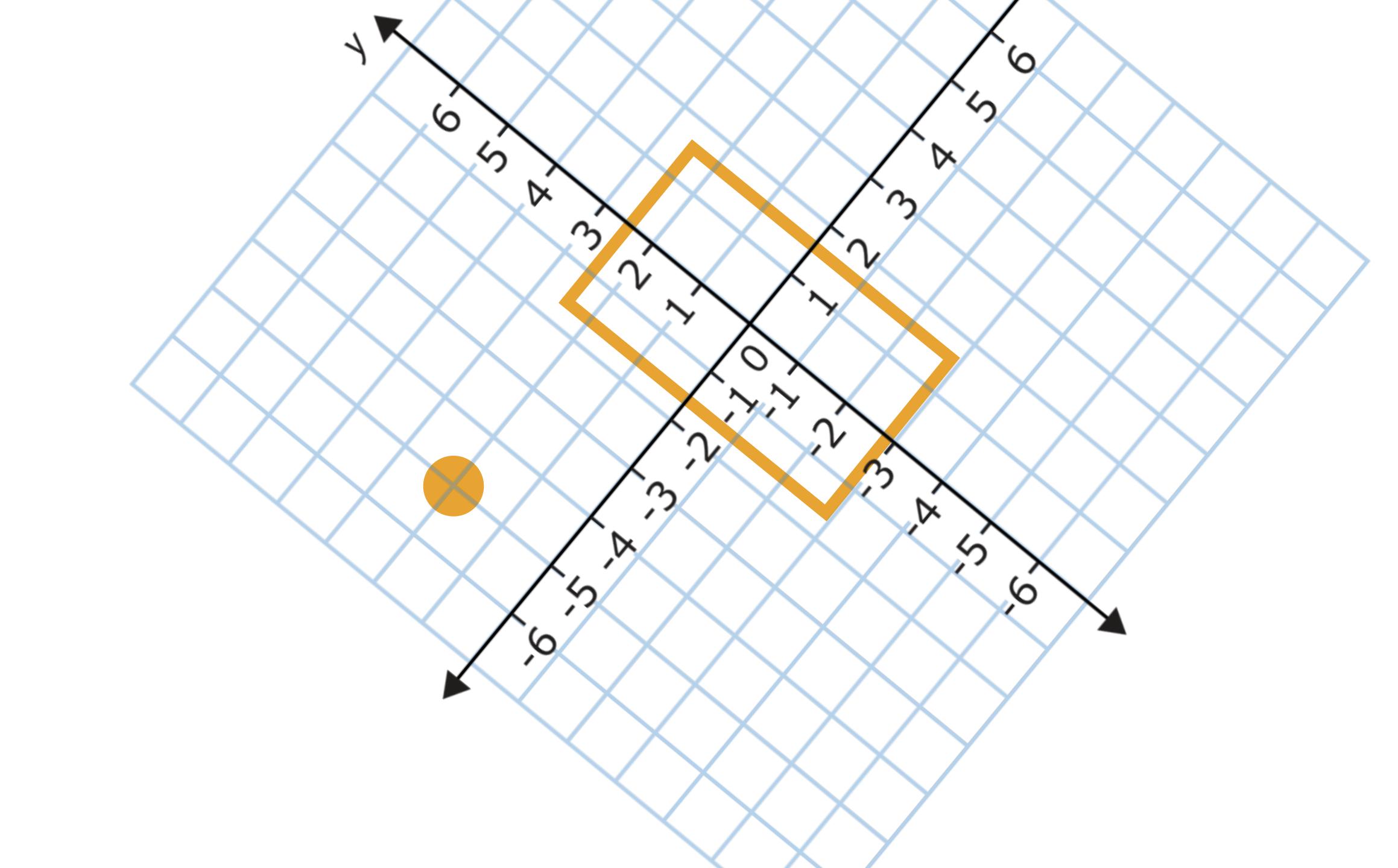
## Point / rotated rectangle collision.

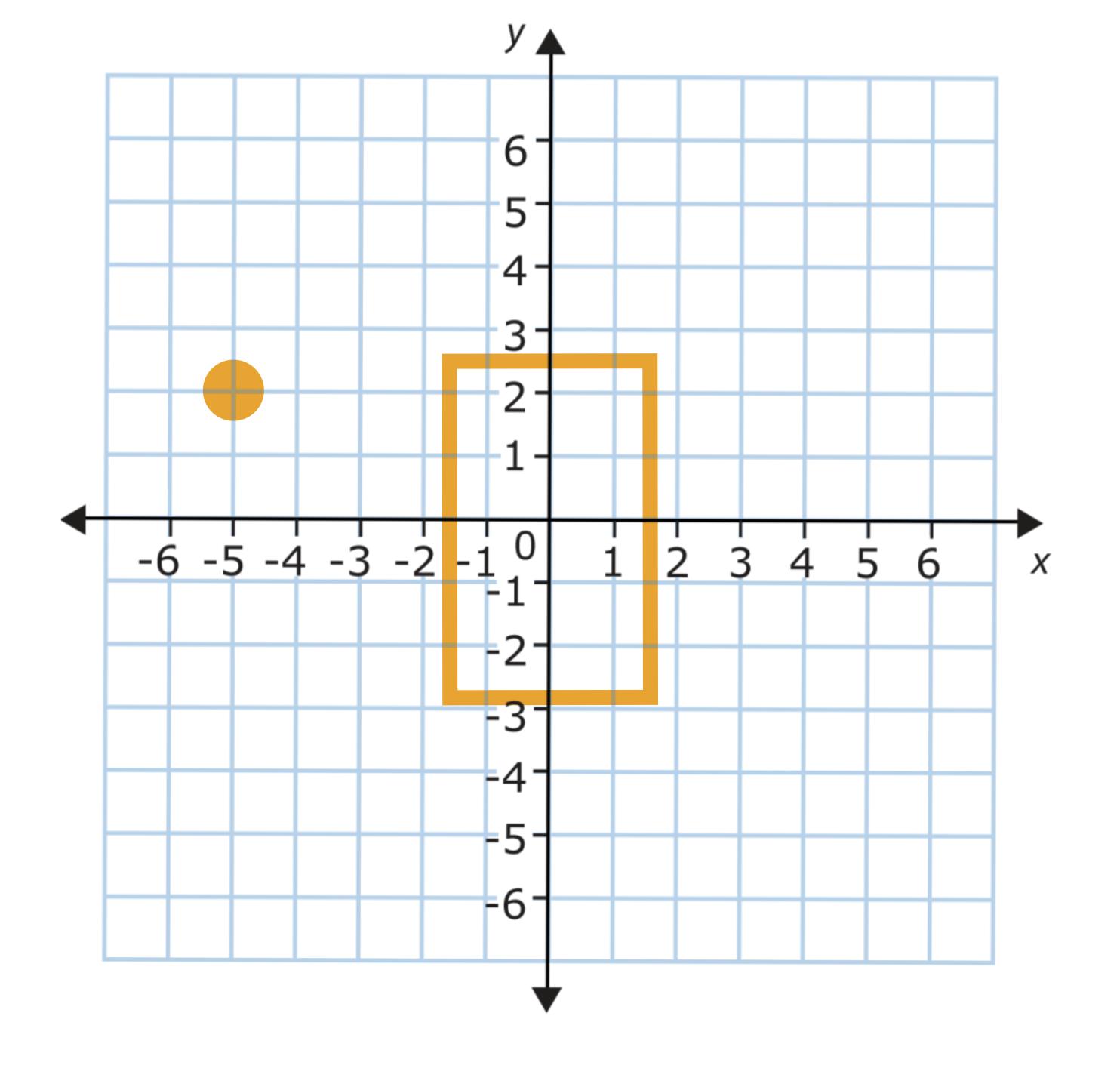












## Point / rotated rectangle collision.

- 1. Multiply the point vector by the inverse of the entity's transform matrix.
- 2. Do regular point / rectangle check with the resulting coordinates.

Rotated rectangle / rotated rectangle collision.







## Separating axis theorem collision.