

CAMBRIDGE ACADEMY FOR SCIENCE AND  
TECHNOLOGY

AQA COMPUTER SCIENCE  
PRACTICAL COMPUTING PROJECT

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## CRYPTOGRAPHY ONLINE

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# **Chapter 1**

## **Analysis**

### **1.1 What is Cryptography**

Cryptography is idea of allowing 2 parties to communicate securely and not allowing an adversary to listen in on the communications. In a general sense it is the art of building secure protocols that allow us to communicate securely. This idea has been around for centuries and is constantly evolving with the increase in demand for technology in our everyday lives and the need make certain that everything that is in the public domain is secure.

#### **1.1.1 Quick History**

##### **1.1.1.1 Ancient History**

One of the first recorded instances of cryptography is from the Roman Empire when *Julius Caesar* created what is now known as the Caesar Cipher. This cipher works by shifting the letters of the alphabet a given number of times. According to *Gaius Suetonius Tranquillus*, Julius Caesar used a shift of +3 places to protect messages of military importance. Even though it is unknown how effective the cipher was at the time it can be assumed that it was reasonably secure. Not least because most of Caesars enemies would have been illiterate and others would have just presumed that the messages were written in an unknown foreign language.

At the time there was no recorded way to break these ciphers. The earliest records of attacks that could be used to break the cipher are from the 9<sup>th</sup> century, with the work of *Al-Kindi* in the Arab world with the discovery of frequency analysis.

##### **1.1.1.2 Recent History**

**WW1:** One of the most notable events during WW1 would be the British interception and decryption of the Zimmermann Telegram. Room 40, the section in British admiralty most identified with cryptanalysis effort during WW1, heavily contributed to the decryption of the Zimmermann Telegram.

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This decryption is often referred to as the most significant triumph in signals intelligence for Britain in the First World War, and one of the first times in which a single piece of signals intelligence directly influenced world events. In this case the United States of America joined the War on 6<sup>th</sup> April 1917.

**WW2:** During World War 2, cryptography was used extensively with a plethora of ciphers systems fielded by the nations involved during the war. In addition to the advancements of cipher systems, the theoretical and practical aspects of cryptanalysis was much more advanced.

Probably the most important codebreaking event during WW2 was the breaking and decryption of the *Enigma* Cipher. The first 'full' break of the enigma cipher was in 1932 by Poland, with the techniques and insights were passed on to the British and French Allies just before the start of the War in 1939. These were improved significantly by the British efforts at the Bletchley Park research station during the War. The decryption of the Enigma Cipher allowed the allies to read important parts of the German Radio networks and it provided an invaluable source of military intelligence throughout the war. Intelligence from this source (including other high level sources, including the Fish Ciphers), was eventually called *Ultra*.

A similar break into an important Japanese cipher (PURPLE) by the US Army Signals Intelligence started before the US entered the War. The product of this effort was given the codename *MAGIC*, it was the highest security Japanese diplomatic cipher.

### 1.1.2 Modern Day Cryptography

#### 1.1.2.1 Symmetric

Symmetric-Key Algorithms are algorithms for cryptography that use the same Key for encryption and decryption of the plaintext and ciphertext respectively. These *Keys* are a representation of a shared secret between 2 or more parties, that can be used to maintain a confidential link of communication. The main drawback of this system is that all the parties communicating need to know the secret key in order to communicate with each other.

There are 2 main types of Symmetric Cryptography Algorithms:

- Stream Ciphers

Stream ciphers will go through each bit of the plaintext and encrypt it one at a time

- Block Ciphers

Block Ciphers will divide the plaintext into groups of bits and will encrypt each of those *Blocks* at once, padding the plaintext if the length of the plaintext does not equally divide the block size of the cipher. Blocks of 64-bits were commonly used but now a days a block size of 128-bits is more common. The Advanced Encryption Standard (approved by NIST in 2001) and the GCM Block cipher both use block sizes of 128-bits.

### 1.1.2.2 Asymmetric

Public Key Cryptography or Asymmetric Cryptography is any cryptographic system that instead of using a single secret key, uses pairs of keys:

- Public Keys

These could be known widely to the public domain

- Private Keys

These are only known to the Owner

This accomplishes 2 things: Authentication, where the public key verifies that the holder of the paired private keys sent the message, and encryption, where only the paired private key holder can decrypt the message encrypted with the public key.

Public Key systems are often based on complex mathematical systems that currently have no reasonable solution to them. Some of these include certain integer factorization, discrete logarithm and elliptic curve problems. Unlike symmetric key algorithms, asymmetric algorithms do not require a secure channel of communication for the initial exchange of one or more of the secret keys between the parties.

Because of the computational complexity of asymmetric cryptography, it is usually only used for small blocks of data. This is typically the transfer of a symmetric encryption key or *Session Key*. This session key is used to encrypt the rest of the potentially longer message. This symmetric encryption/decryption is based on simpler algorithms and is much faster.

In a public key signature system a person can combine their message with a private key to create a short digital signature on the message. Anyone with the corresponding public key can combine a message, a digital signature and the known public key to verify if the signature is valid or not. Therefore this provides authentication of a message provided that the owner of the private key keeps the private key secret.

These public key algorithms play fundamental roles in cryptosystems, applications and protocols. They are heavily involved in internet standards such as TLS (Transport Layer Security), S/MIME, PGP and GPG. Some public key algorithms provide key distribution and secrecy. Examples include the Diffie-Hellman Key Exchange. Some algorithms provide digital signatures. Examples include the Digital Signature Algorithm and some provide both, e.g. RSA.

Public Key Cryptography finds applications in the Information Security Discipline. Information Security (IS) is concerned with all aspects of protecting electronic information assets against security threats. Public Key cryptography is used as a method of assuring the confidentiality, authenticity and non-reputability of electronic communications.

### 1.1.2.3 Cryptanalysis

Cryptanalysis is the study of information systems working towards the goal of unveiling the hidden aspects of the system. This knowledge is then used

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to break the information system and gain access to the contents of encrypted information.

In addition to mathematical analysis of cryptographic algorithms, cryptanalysis also involves looking at side-channel attacks. These attacks don't specifically look for weaknesses in the algorithm itself but for a weakness in the implementation of algorithm.

Considering the end goal has been the same, the specific ways in which we get there have evolved and developed drastically of the past few decades. We have gone from the pen-and-papers methods of the past, to the machines like the British bombes and colossus supercomputer at Bletchley part to the mathematically advanced computerized schemes of the present. Most cryptanalysis of modern day algorithms involves solving complex pure mathematical problems, including the integer-factorization problem and the discrete logarithm problem.

### 1.1.2.4 Protocols

A security protocol is an abstract protocol that performs a security function and applies cryptographic methods, often grouped together as sequences of cryptographic primitives. The protocol defines how the algorithms should be used.

Cryptographic protocols are widely used for application-level data transport. A cryptographic protocol usually incorporates at least a few of the following features

- Key Agreement / Establishment
- Entity Authentication
- Symmetric Encryption and message material construction
- Secure Application-level data transport
- Non-repudiation methods
- Secret Sharing Methods
- Secure Multi-party computation

**Example: Transport Layer Security** An example of one of these algorithms could be the Transport Layer Security, or TLS, protocol. TLS is used to secure web (HTTP/HTTPS) connections. It has an entity authentication mechanism based on the X.509 system; a key setup phase, where a symmetric key is formed by employing public-key cryptography; and a secure application-level data transport system. These 3 functions have very important interconnections. Standard TLS does not however implement Non-repudiation methods.

There are other types of cryptographic protocols as well, and even the spelling has multiple meanings. Cryptographic Application Protocols, often

use one or more underlying key agreement methods, which are sometimes themselves referred to as cryptographic protocols. For example, TLS employs the Diffie-Hellman Key Exchange, which although is only a part of the TLS protocol, could be seen as a completely independent cryptographic protocol in itself for other applications.

### **1.1.3 Applications of Modern Cryptography in Everyday Life**

Cryptography is present in nearly every single electronic device that has been produced in the past decade. This ranges from your new ePassport to your new mobile phone to your smart fridge. It is everywhere and because of this it has become even more important.

For the most part Cryptography provides security to a service that we use in our daily lives. Examples of these services could be:

- ATM Cash Withdraw
- File Storage
- Emails
- TV
- Text Messaging
- Web Browsing
- Payment Systems like PayPal

## **1.2 Important Cryptographic Algorithms**

### **1.2.1 DES**

#### **1.2.1.1 What is DES?**

DES, or the Data Encryption Standard, is a symmetric block cipher used for the encryption and decryption of electronic data. Even though it has now been proven that DES is insecure it was a major keystone in the development of modern cryptography.

Developed in the early 1970's by IBM, based on an earlier design by *Horst Feistel*, the algorithm was submitted to the National Bureau of Standards (NBS) following the agency's invitation to propose a candidate for the protection of unclassified, sensitive electronic government data. In 1976, after consultation with the National Security Agency (NSA), the NBS eventually selected a modified version of DES which was published as a Federal Information Processing Standard (FIPS) for the United States in 1977. It should be noted that this modified version helped protect against differential cryptanalysis but weakened it significantly against brute-force attacks, the attack that

would eventually make NIST (National Institute for Standards and Technology, the new NBS) ask for the newer Advanced Encryption Standard (AES).

### 1.2.1.2 Overview of DES

DES is a Block Cipher. It takes a fixed-length amount of plaintext bits and transforms it through a series of complicated operations which results in ciphertext bits. In the case of DES, its block-size is 64-bits, this means that you would split up your plaintext into 64-bit blocks and pass them through the algorithm one at a time. In the case that your plaintext does not fully divide into 64-bits you would use padding to increase the size of the plaintext until it fully divided into 64-bits. DES also uses a Key that heavily effects the transformation, so decryption can only be done if the user has the Key. DES uses a Key size of 64-bits. However it should be noted that 8 of these bits are used solely for parity checks so the effective Key size of DES is 56-bits. The Key is stored or transferred as 8 bytes with odd parity. According to *ANSI INCITS 92-1981*, section 3.5:

*One bit in every byte of the KEY may be utilized for error detection in key generation, distribution and storage. Bits 8,16,...,64 are for use in ensuring that each byte is of odd parity.*

Like all Block Ciphers, DES on its own is not inherently secure, it must be used in a mode of operation to achieve this. FIPS-81 specifies several modes to be used with DES.

Decryption works the same way as encryption, but the keys are used in reverse order. This gives the advantage that you can use the same hardware/software for both encryption and decryption.

**Overview of Internal Structure:** DES uses 16 rounds, this means that the core blocks of the cipher are repeated 16 times on each block of plaintext. There is also an Initial Permutation and a Final Permutation, name IP and FP respectively. These have no significant cryptographic impact on the cipher but were added to allow the loading of blocks in and out of mid-1970s 8-bit based hardware.

Before the main rounds the block is divided into two 32-bit halves, being processes alternatively. This structure is known as a Feistel Network. This way of constructing a block cipher ensures that decryption and encryption are very similar processes, the only difference being that the subkeys are applied in reverse for decryption. Figure 1.1 shows this.

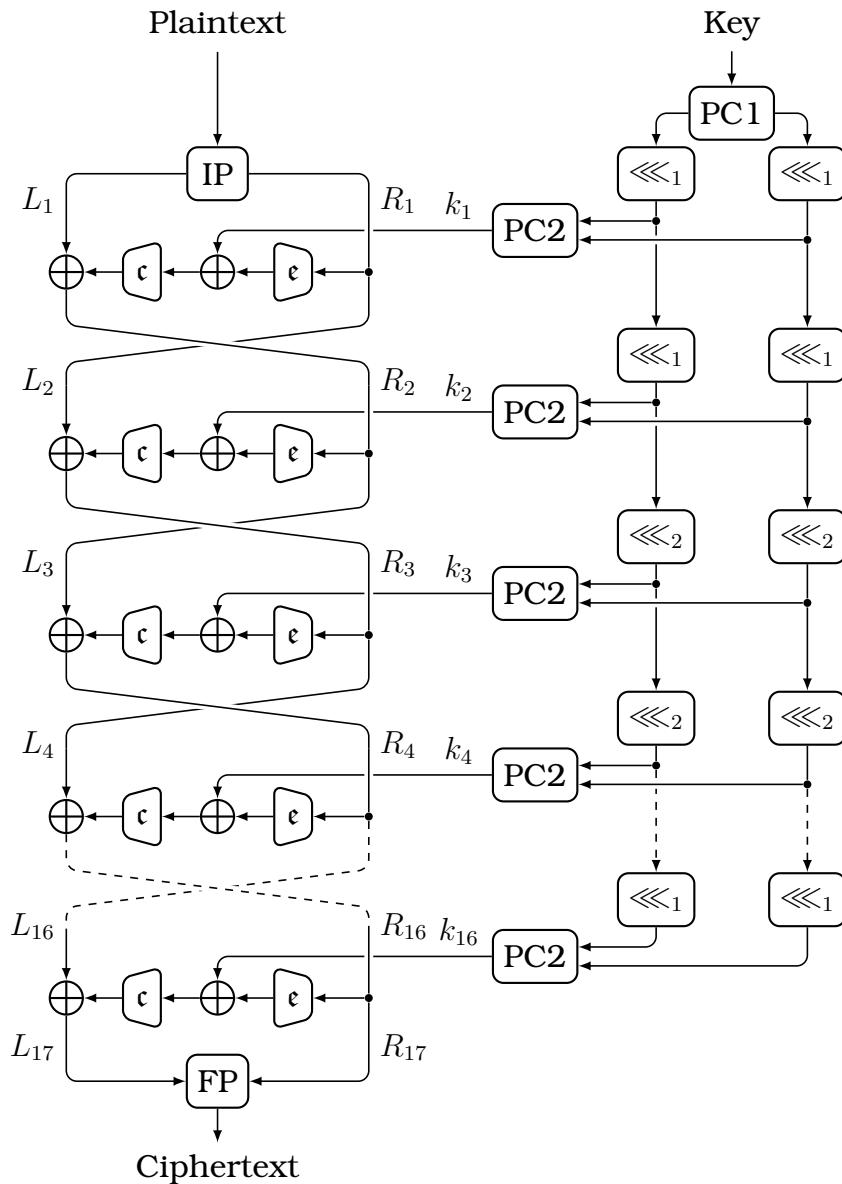


Figure 1.1: High Level Overview of the DES Block Cipher

## 1.2.2 AES

### 1.2.2.1 What is AES?

AES, or the Advanced Encryption Standard, is a specification for the encryption of electronic data established by the National Institute for Standards and Technology (NIST) in 2001. AES is a subset of the Rijndael Cipher, developed by 2 Belgian cryptographers. *Vincent Rijmen* and *Joan Daemen*, who submitted the cipher during the AES selection phase. Rijndael is a family of Block Ciphers which support multiple block sizes and key lengths.

For AES, NIST selected only 3 members of the Rijndael cipher. Each using

a block size of 128-bits and supports using key lengths of 128, 192, 256 bits.

AES was first adopted by the US Government and nowadays is used worldwide. It has become the defacto standard for securing electronic data. It has replaced the Data Encryption Standard which was first published in 1977. AES was first announced by NIST on *November 26, 2001* as a FIPS PUB 197 (FIPS 197). This announcement followed a five year standardization process on which fifteen competing designs were presented and evaluated, before the Rijndael Cipher was accepted as the most suitable.

AES became effective as a federal government standard on *May 26, 2002*, after its approval by the state of commerce. AES is included in ISO/IEC 18033-3 Standard. AES is available in multiple encryption packages and is the first(and only) cipher approved by the National Security Agency (NSA) for top secret information when used in an NSA cryptographic module.

### **1.2.2.2 Overview of AES**

AES is based on what is known as a substitution-permutation network, and is very fast in both hardware and software. Unlike its predecessor DES, AES is not build on a Feistal Network. Since AES is a variant of the Rijndael Cipher using a Block size of 128-bits and supporting key sizes of 128, 192, 256 bits.

AES operates on a 4 x 4 column major order matrix of bytes, known as the state of the cipher. The calculations of this Cipher are performed in the Galios Field of  $2^8$ ,  $GF(2^8)$ , this is covered in detail in *Section 2.4.1*. The byte ordering in the matrix is shown in Figure 1.2.

$b_0$	$b_4$	$b_8$	$b_{12}$
$b_1$	$b_5$	$b_9$	$b_{13}$
$b_2$	$b_6$	$b_{10}$	$b_{14}$
$b_3$	$b_7$	$b_{11}$	$b_{15}$

Figure 1.2: AES Byte Ordering

The Key size used for the AES cipher specifies the number of rounds the used to convert the plaintext block into the ciphertext block.

- 128-bits : 10 Rounds
- 192-bits : 12 Rounds
- 256-bits : 14 Rounds

Each round consists of several processing steps, each containing 4 steps including one that depends on the key supplied to the algorithm. A set of

reverse rounds are applied to transform the ciphertext back into the plaintext using the same key. A High Level description of the algorithm is given below in Figure 1.3:

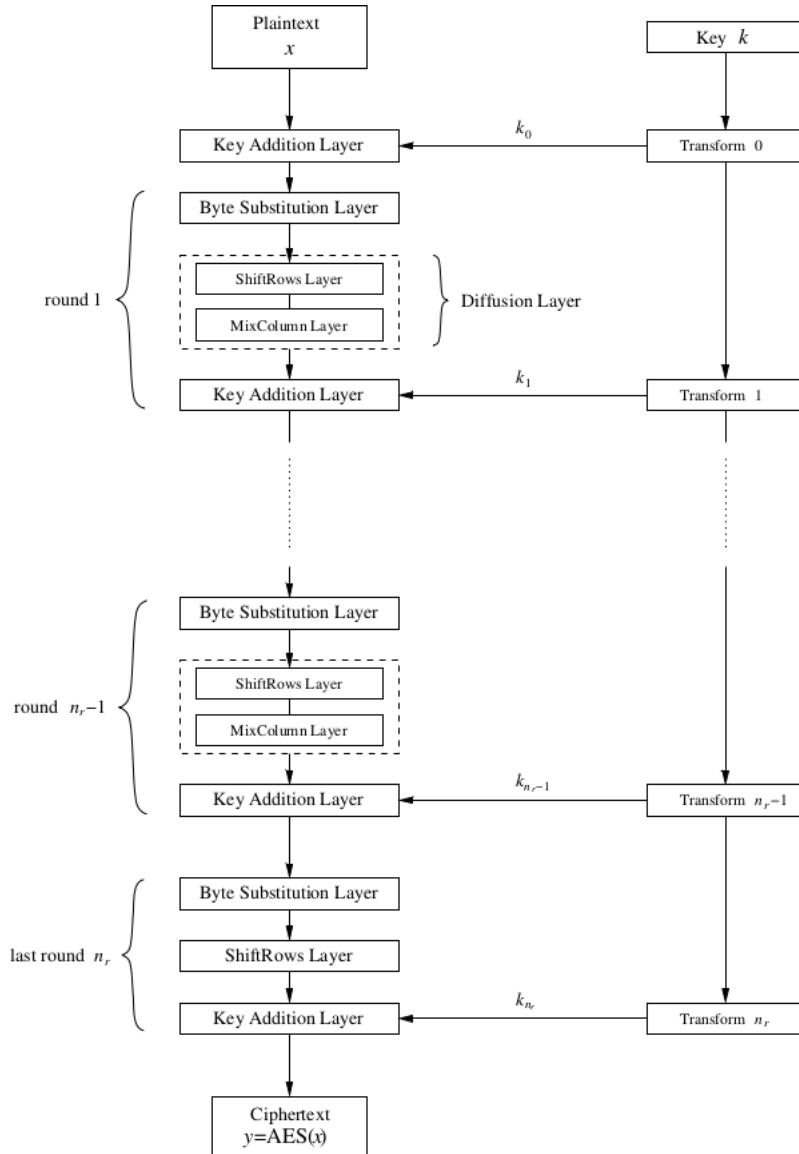


Figure 1.3: AES High Level Overview

## 1.3 Why is this important?

### 1.3.1 The Importance of Cryptography in the Modern day

In the modern era, the amount of reliance we have on technology has exponentially increased over the past few decades. With this dramatic increase, we

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have started using this new technology to complete tasks that use very important and critical information about us, like online banking. This has opened a new opportunity for criminals to gain access to your critical accounts and now, rather than having to rob a bank, steal your credit cards, mug you, they only need to be in the same coffee shop connected to the same public Wifi as you. This is a very bad situation.

Cryptography plays a key role in this as it is the only thing that stops attackers from being able to access all of our critical information. As long our data is encrypted securely, it doesn't matter whether or not they can see what we are doing by being connected to the same public Wifi, all they will see is jiberish that makes no sense. And as long as the algorithms we use are secure and we make sure they don't get access to our private cryptographic keys they will never be able to access our critical data.

This is why Cryptography is very very important in the Modern Day. Cryptography is the only defense we have against attackers who have access to our data. The counter argument could be made that as long as they never get access to our data we will be fine. But, recent cyber attacks against corporate companies have proven that even the most secure facilities are not 100% secure. So preventing the attackers from getting the data in the first place is important, but it is equally important to make sure that when they get the data, that data is useless to them.

### 1.3.2 Analysis of Current Solutions

Now we know that cryptography is possible one of the most important concepts in our digital age we need to make sure that it stays that way. This means we need to educate and train the next generation of cryptographers so that in 100 years time, we don't run out of people that can develop, test, maintain the next wave of cryptographic algorithms. So, what are the current ways that an individual can learn the ways of the cryptographers.

#### 1.3.2.1 1. Academia

The most traditional way to break into a given industry, you enroll at a institution that allows you to study cryptography. You will learn everything, from the basics of cryptography all the way up to why specifically the designers of certain algorithms did it that way rather than another way.

- Advantages

With this method being the most traditional way of learning a given subject, it has been tried and tested for many many years and works pretty much every time. With the additional bonus of having staff who will provide you any assistance you require over your few years of study, whether that would be on understanding a given topic or just to answer some of your questions. You also have ability to use any on-site facilities that the institute provide for you and this can be a massive help as it means you

don't have to go out and spend money on specialist equipment to test something. You can just use the institutes.

- Disadvantages

Even though this is the most traditional way to learn something in depth, like everything it does have flaws. For some people, learning this way just doesn't work well. You will spend most of your time learning about the theoretical side of the subject and will only look at the practical side on a few occasions. Couple this along with the fact that this route is very very expensive it makes it pointless for somebody that learns best by doing practical work.

### **1.3.2.2 2. Self Taught**

Becoming a more and more popular way to learn about cryptography is to just teach yourself, its the route it took. This way allows you to quickly focus in on exactly the aspect of cryptography that you find interesting and learn about it in depth.

- Advantages

With the internet becoming more and more accessible to the average person it has made an abundance of learning resources available to anyone with a browser from the last decade. This given us an opportunity to learn more things than ever before and it is all completely free. There is plenty of information on cryptography that you can learn from, this includes YouTube series on every aspect of modern cryptography to research papers about an up and coming area of cryptography, like Quantum Cryptography. Combine this with the fact that you can learn at exactly the right pace for you and it is a very good option.

- Disadvantages

The main drawback of this option is that you will need a device that allows you to connect to the internet, and you will need internet which does cost a fair amount. You also need the commitment to stick to it. Because you can go at your own pace, it does mean there is no one that will make you stick to learning about it. The entire responsibility of learning about the subject is in your own hands and for some this could be to much and they will just give up after about a week.

### **1.3.2.3 3. Learning on the Job**

This option mixes the aspects of both the previously mentioned options. Some people will have already gotten a job in the technology industry before realizing how important cryptography is and will want to learn it so they know that they are doing there job right.

- Advantages

With already working, you will be moved away from the theoretical and more the practical. This is great for some people. You will also be able to see exactly how these highly complicated concepts directly affect the way we use the internet. You may also have the opportunity through your employer to attend various courses and conferences that allow you to gain various certifications in cryptography and maybe even the broader InfoSec industry.

- Disadvantages

The main disadvantage here is that you will need a job in a somewhat relevant area in the industry and in order to get the job in the first place you will probably have gone through options 1 and 2 anyway.

## **1.4 My Proposed Solution**

### **1.4.1 End Goal**

The end goal of my project is to provide a website that combines the best parts of Options 1 and 2 from the above list. It will teach the users everything from the core concepts of cryptography all the way to the very complicated systems that implement modern cryptography. This way people have the ability to learn as much as they would while in academia while getting the same freedom as if they were teaching themselves.

### **1.4.2 Proposed End Users**

In the short term there my End Users will be a few students from the Computer Science class. Over the past few weeks while I have been learning Cryptography they have noticed and thought it was pretty cool and wanted to learn as well. But most of them just don't have the commitment to sit through hours of lectures like I did to learn the content so I thought that I should build something that they can use.

Due to the content in this project, I will also be making it available to the public so anyone that really wants to learn about Cryptography will have the option to. This allows for a much larger range of people who will have the option to learn about Cryptography which everyone can see as being a good thing.

### **1.4.3 How the User will interact with the system**

The main way that users will interact with my system is quite simple. First they will need to create an account so they can record and keep track of their progress. They will then select a specific area to study. This is completely up to the user, they can work their way through chronologically going through

each section or just jump to the middle and crack on with the hard stuff. Once in the selected section, they will read through the information content displayed on the screen. Once the user feels confident they understand that content, they can attempt to answer the sample questions at the bottom of the page. These questions will cover all content shown on that given page and will vary in difficulty. Once they have answered the questions they can check if they are right, this information will be shown in the report section, any questions they get wrong will be shown and the provided solutions as well so the user can see where they went wrong and learn from the mistakes made. Once they are happy with how they have performed in that given section they can move on to the next section repeating this process.

#### **1.4.4 Technical Analysis of my System**

##### **1.4.4.1 Option 1: Classical Approach**

My first idea about how I was going to attempt to build this system was arguably the 'classical' approach. By using the 3 core web technologies, (HTML CSS JS), I would have all the features that would be needed to fully achieve my goal.

- Advantages

The biggest advantage of choosing this option would be that it has been around for decades. It is truly a tried and tested method. This means that not only does it have the flexibility that I would require, but if I were to run across any problems then I would just have to use the internet and chances are someone else has had that problem before and they would know how I could fix it and make it work. This is a massive perk over the other 2 choices as it means that even if I come across an abundance of problems, I will definitely be able to find a solution in a timely manner.

An another advantage is that Javascript, that main language I would be using to 'code' the website, has many frameworks and extensions that I would be able to use freely. This allows me the ability to be a lot more ambitious about what I want to do as I wouldn't have to develop the majority of the core complex functions. I would just have to know how I need to implement them.

- Disadvantages

The main disadvantage of this option for me is that personally I tend to stay away from this kind of work. I personally am much more of a back-end type developer. So I would definitely go for one of the other options.

I also have much more experience with the back-end type languages and feel I would be spending the majority of my time learning the concepts and syntax of this option, whereas if I were to choose one of the other options I already know the syntax so could start working straight away.

#### **1.4.4.2 Option 2: Modern Approach**

This Option is the most 'modern' approach I could think of. This option considers all options with similarities to ASP.NET. I consider this the 'modern' approach as we are not using specific web technologies to create our website. We are just using a standard High Level language to do it, the main 2 contenders here are clearly C-Sharp and Java.

- Advantages

The main advantage here is that by using a normal programming language, you have lots of flexibility. Because this is a normal programming language you are not bound by the paradigms of normal web development. You can effectively create a Desktop application and with very little modifications, it will be possible to turn it into a Web application. Another advantage is that it is very easy to incorporate previously coded modules into your web application.

This also has the advantage that it suits my needs better as well. Since I have lots more experience with these types of languages, I would have much more time to spend on the actual web application rather than learning the language. This means I can get more done and have a better, more complete end result.

This option is also new technology, not so new that there is no documentation and help but not so old there is the same amount of help that Option 1 provides. Since it is in this mid-stage area, it will only be used more and more so looking at it in terms of what industry might need in a few years, this would give me a good opportunity to learn a technology that will make me more employable than the average person.

- Disadvantages

The main disadvantage of this option is that since it revolves around fairly new technology, it will not be streamlined to the point of Option 1. What I mean by this is that it may take more effort to create the same thing from Option 1 using this method. This method may provide the best solution, but it may take a far longer time to get to the 'best' solution when compared to a 'client ready' solution from Option 1. The solution from Option 1 may not be as good as this one, but on a scale of 'first conception' to 'ready to ship', this Option is not the one to choose.

#### **1.4.4.3 Option 3: The Hybrid**

The final option is a sort of combination of the other Options but with a sort of twist. It will be using the C++ language, which is by no means the go to for creating web applications. It also includes using a 3rd party library which will provide the necessary core web technology functionality.

- Advantages

The clear advantage of this option is that because it uses a 'mid' level language, that allows us to write very fast code. Rather than having to go through a framework and converting from source to bytecode to asm, we can go directly from the source to the asm. This is a very important factor as the the whole purpose of this project is to teach Cryptography and in a lot of situations, the key algorithms need to be fast. So, in that aspect there is no other option.

This option is also my preferred option as C++ is a pure back-end language. I also have the most experience with this language therefore I would be most comfortable working with it. This also removes the need to learn a completely new language to continue with the project. Thus eliminating a massive bottleneck in the process of development.

I would also consider this a very good option to make myself more employable in the future as lots of the older systems are written in C++ and in order to keep them running you need someone who is familiar with the language.

- Disadvantages

The key disadvantage with this option is that it uses a not-so friendly language. Meaning that it takes much more effort to do the same task when compared to the other options. It also has the disadvantage that you need to learn a completely new library to do anything which can be very daunting to consider.

## **1.5 Requirements / Objectives / Limitations**

This whole section is going to serve a check list of the requirements, objectives and limitations of my project. The requirements serve as a detailed check list for me to go over and use to see if my project has all the content I want it to have. The objectives serve as a more 'is my project complete' check list and that is what will be used when checking as to whether or not my project is complete per say. And finally, limitations are similar to objectives but are things that I would like to achieve but couldn't due a variety of reasons including but not limited to time constraints and complexity of the problem.

There are 2 main sections here relating to the User and System. Anything that relates the the User is about how the platform is designed and orientated around the user. When it comes to the System it is mainly about my implementation for the solution.

### **1.5.1 User Requirements**

- Easy to read font
- Intuitive user interface

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- Good flow through out the entirety of the website
- Content explained makes sense
- Hard / Complex areas explained simply
- Content should be easy to follow

### **1.5.2 System Requirements**

#### **1.5.2.1 Platform Requirements**

**A High Level look at what I want the platform to cover.**

- Cryptography
  - Basic information about Cryptography
    - \* Private-Key Cryptography
    - \* Introduction to Public-Key Cryptography
      - Security Mechanisms
      - Authenticity of Public Keys
      - Important Public-Key Algorithms
      - Key Lengths and Security Levels
    - \* Explain the simple protocols
  - Overview of the types of Ciphers
    - \* Block Cipher
    - \* Stream Cipher
    - \* Encryption and Decryption using both types of ciphers
  - Overview of Hashing Functions
  - Brief History on Cryptography
    - \* Caesar Cipher
    - \* Vernam Machine
- Cryptanalysis
  - Very Basic overview of what Cryptanalysis involves
  - Brief History on Cryptanalysis

**Going into more detail about what I want to teach specifically.**

- Cryptography
  - Public-Key Cryptography
    - \* Cryptosystems based of the Discrete Logarithm Problem
      - Diffie-Hellman Key Exchange

- The Discrete Logarithm Problem
- The Elgamal Encryption Scheme
- \* RSA Cryptosystem
- \* Elliptic Curve
- \* Digital Signatures
  - RSA Signature Scheme
  - Elgamal Digital Signature Scheme
  - Digital Signature Scheme (DSA)
  - Elliptic Curve Digital Signature Scheme (ELDSC)
- \* Key Establishment
- \* Message Authentication Codes (MACs)
  - MACs from Hash Functions
  - MACS from Block Ciphers CBC-MAC
  - Galois Counter Message Authentication Code (GMAC)
- More detailed look into the common algorithms
  - \* Block Ciphers
    - Data Encryption Standard (DES)
    - Advanced Encryption Standard (AES)
  - \* Talk about the modes of operation for Block Ciphers
    - Electronic Codebook Mode (ECB)
    - Cipher Block Chaining (CBC)
    - Output Feedback Mode (OFB)
    - Cipher Feedback Mode (CFB)
    - Counter Mode (CTR)
    - Galois Counter Mode (GCM)
  - \* Stream Ciphers
    - Stream ciphers based off Linear Feedback Shift Register (LFSR)
  - \* Hashing Functions
    - MD5
    - SHA-1
    - SHA-2
    - SHA-3
- Implementations of the AES Cipher
- Create theory questions that require the user to demonstrate their understanding of the various Cryptography sections

**Additional Content that I would like to add if possible but not critical to the completion of the project**

- Cryptography

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- Build a simulator for the enigma machine and show graphically how it works
- Coding Problems
  - \* Design Custom coding problems that test the users cryptology knowledge
  - \* Create a custom development environment so the user can enter the solution to the problem on the website and it will be able to tell you if the answer is correct or not
- Cryptanalysis
  - Explain some of the common techniques used in cryptanalysis
  - Provide come example ciphers for the users to practice their cryptanalysis on

### **1.5.2.2 AES Implementation Requirements**

- Key Expansion Implemented
- AddRoundKey Function Implemented
- SubstituteBytes Function Implemented
- ShiftRows Function Implemented
- MixColumns Function Implemented
- Key Schedule Implemented

## **1.5.3 System Objectives**

### **1.5.3.1 Platform Objectives**

I have split up this section into 3 different areas, Website Management, Website Content, User Interaction to make it easier to understand. It is also organized from most important to least important for each section. E.g. the higher up in the list the more important the item is.

1. Website Management
  - (a) Website that I can launch and connect to from my Computer
  - (b) Buying a Domain for the Website
  - (c) Renting a VM for my Website to live in so it can be accessible to anyone
  - (d) Renting a SSL Certificate so I have HTTPS enabled for secure communication between the client and the server
2. Website Content

- (a) Contains content on Symmetric Cryptography
- (b) Contains theoretical questions on Symmetric Cryptography
- (c) Contains content on Asymmetric Cryptography
- (d) Contains theoretical questions on Asymmetric Cryptography
- (e) Create online code-editor with standard code-editor features. E.g. Auto-complete, re factoring, a home made 'intellisense'
- (f) Create questions that require the need to write code in order to solve them
- (g) Review the Coded solutions and suggest improvements
- (h) Create Visual simulation of various algorithms and cryptographic systems
  - i. AES and DES
  - ii. The Engima Machine

### 3. User Interaction

- (a) Login system is implemented
- (b) Authentication for users is implemented
- (c) Relevant user information is stored in local database
- (d) Email verification for accounts is implemented
- (e) Store answers to questions into local database
- (f) Analyse the users answers to questions and produce report on what they need to work on
- (g)

#### **1.5.3.2 AES Implementation Objectives**

1. Key sizes supported
  - (a) 128-bit
  - (b) 192-bit
  - (c) 256-bit
2. Different Modes of Operation
  - (a) ECB (Electronic Code Book)
  - (b) CBC (Cipher Block Chaining)
  - (c) OFB (Output Feedback Mode)
  - (d) CFB (Cipher Feedback Mode)
  - (e) CTR (Counter Mode)
  - (f) GCM (Galois Counter Mode)

### **1.5.4 Acceptable Limitations**

#### **1.5.4.1 Platform Limitations**

1. Website Management
  - (a) Limit to concurrent connections to the website
  - (b) Making the website live to the public
  - (c) Getting SSL/HTTPS setup for the website
2. Website Content
  - (a) Online Code-editor does not support all the modern features
  - (b) Visual simulations are not implemented
3. User Interaction
  - (a) Analysis of user answers not fully finished

#### **1.5.4.2 AES Implementation Limitations**

1. Only 128-bit Key size is supported
2. Only configure ECB Mode of operation
3. Padding is not implemented

## **1.6 Data Usage in the System**

### **1.6.1 Data Security Overview**

This will be covered more in depth in the Documented Design section but I feel it is important to briefly go over it here.

So for all important user critical information stored in the local database, the appropriate security measures will be implemented. Since the only critical user information is the passwords to the users account, before storing the password it will be hashed using a secure hashing algorithm, such as bcrypt, SHA2, SHA3, etc. The reason we hash it rather than encrypt it is that a hash is known as a 1-way function. You can never get the plaintext back from the ciphertext, in this case our plaintext is the password and the ciphertext is the password hash or digest.

### **1.6.2 Data Sources**

The main data sources for my project will be for the users answers to the questions on the various sections provided. I will also receive data from the user as an input for the AES algorithm. For the answers to the questions, the data will be processed and stored in a local database. The input into the AES algorithm will not be stored and will only be processed by the algorithm itself.

### **1.6.3 Data Destinations**

The main data destination for my project will be the back end database in use. This is where the majority of the key information like the authentication information and user data will be stored. All appropriate security measures will also be taken to ensure confidentiality, integrity and availability of the data.

### **1.6.4 Data Analysis**

#### **1.6.4.1 User Data**

All user data will be stored in the database table db\_user. This data will only be able to be accessed through my systems database api.

#### **1.6.4.2 System Data**

All system data will be stored in custom built data structures. Important information like authentication information will be stored in the following database tables:

- auth\_information
- auth\_identity
- auth\_token

Information regarding question data will be stored in a table called questions.

#### **1.6.4.3 Temporary Data**

Temporary data will be stored in a data structure from the web application and then when it is no longer needed the data will be disposed of.

# Chapter 2

## Documented Design

### 2.1 High-Level Overview of System

### 2.2 Project Versioning

#### 2.2.1 File Structure

This section will talk about the general file structure I will be using and the style that I will be coding against. We will be using an example file, file\_structure.cc, which is shown below.

```
1 /**
2 * @file file_structure.cc
3 * @date 21/02/2018
4 * @version 0.01
5 *
6 * @brief A brief explanation of what is contained in this file and what ←
7 *       the purpose of the file is
8 *
9 */
10
11 /**
12 * @class A
13 * @version 0.01
14 *
15 * @brief A brief explanation of what the purpose of the class is and ←
16 *       what it does
17 */
18 class A
19 {
20
21 };
22
23 /**
24 * @class TestClass
25 * @version 0.01
```

```
26 * @implements TestClass
27 *
28 * @brief A brief explanation of what the purpose of the class is and ←
29 * what it does
30 */
31 class B : A
32 {
33 public:
34     /**
35      * @brief A brief explanation of what the function does
36      *
37      * More detailed explanation below
38      */
39     TestClass() = default;
40
41     /**
42      * @brief A brief explanation of what the function does
43      *
44      * @param f A description of the parameters is given here
45      * @param e
46      * @return Describes what the function returns
47      *
48      * More detailed explanation below
49      */
50     int C(int f, bool e);
51
52 private:
53     int f; /*< Detailed information on a member of the class */
54 }
```

---

### 2.2.1.1 File Header

Firstly we will be looking at the generic file header for the .h and .cc files used in my project. The file header is given below:

```
1 /**
2  * @file file_structure.cc
3  * @date 21/02/2018
4  * @version 0.01
5  *
6  * @brief A brief explanation of what is contained in this file and what ←
7  * the purpose of the file is
8  *
9  * @author Jacob Powell
10 */
```

---

There are 5 key sections included in the file header,

- @file - this declared the name of the file, including its extension
- @date - this is the date of creation of the file

- @version - this documents what the version of the file is. It will change when there are small changes and when there are large changes. The significance of the change is shown by which number is changed, e.g. changing from version 0.01 to 0.1 is a more significant change than going from version 0.01 to 0.02
- @brief - this is where a brief description of what the files purpose is and what it contains
- @author - this is where the author of the files name is given

The reason I am including a header block is because when browsing through my project most people will not be able to meticulously go through all the code working out what it does exactly. The header block serves for the purpose of explaining what the code in the file does, giving the reader any key information like version, date of creation and author as soon as they look at the file. This way the reader doesn't have to read all the code, they can just read the header block and they will understand, on a high level, what that section of the code does.

### 2.2.1.2 File Commenting

Throughout the project I will be sticking to a particular commenting style, which applies rules to how document my code. This section explains how I comment and what style I use for each scenario.

The first area we will look at is how we document classes, their members and their methods. We will look at the example class B and in our file structure.cc example file. The class extract is shown below.

**Classes** An extract of our example classes is given below:

```
1 /**
2 * @class A
3 * @version 0.01
4 *
5 * @brief A brief explanation of what the purpose of the class is and ←
6 *       what it does
7 */
8 class A
9 {
10 };
11
12 /**
13 * @class TestClass
14 * @version 0.01
15 * @implements TestClass
16 *
17 * @brief A brief explanation of what the purpose of the class is and ←
18 *       what it does
```

```
18 */  
19 class B : A  
20 {  
21 };  
22 }
```

A class will contain 4 sections:

- @class - The name of the class, the name should also always use Camel-Casing
- @version - The current version of the class
- @implements - If the class inherits from another class then the name of the inherited class is given here
- @brief - This provides a short explanation of what the class does and what its purpose is

**Methods** An extract of class method documentation is given below:

```
1 class B : A  
2 {  
3 public:  
4     /**  
5      * @brief A brief explanation of what the function does  
6      *  
7      * More detailed explanation below  
8      */  
9     TestClass() = default;  
10  
11    /**  
12     * @brief A brief explanation of what the function does  
13     *  
14     * @param f A description of the parameters is given here  
15     * @param e  
16     * @return Describes what the function returns  
17     *  
18     * More detailed explanation below  
19     */  
20     int C(int f, bool e);
```

- @brief - Explains what the method does
- @param - If the method takes parameters then these will be declared and explained here
- @return - If the method returns something this explains what that is
- Then after these tags a more detailed explanation of what happens in the method will be given below

**Members** An extract of class member documentation is given below

```
1 class B : A
2 {
3     private:
4         int f; /*< Detailed information on a member of the class */
5
6 };
```

- Next to the member use the style `/*< */` to describe what its purpose in the class is

## 2.2.2 Version Changelog

Lets look at the file header again, it is given below:

```
1 /**
2  * @file file_structure.cc
3  * @date 21/02/2018
4  * @version 0.01
5  *
6  * @brief A brief explanation of what is contained in this file and what ←
7  *       the purpose of the file is
8  *
9  * @author Jacob Powell
*/
```

As you can see there is a `@version` tag. For every data structure and file in the project there will be a `@version` tag which will contain the most up to date version of the file / data structure. This allows me to easily keep track of how each element of my project is progressing and evolving. The behavior of this tag is explained in *Section 2.2.1.1*.

## 2.2.3 Off-Site Backups

When developing a project of this scale it is crucial that you don't just *keep all your eggs in one basket* per say. What I mean by this is that you don't want a single point of failure, if I finished my project and then a week before the submission date my laptop died and I couldn't recover the data from my hard-drive then I would not be able to submit my project and I would fail.

For this reason I will be using Github to store daily backups of my projects code and documentation. This way, even if my laptop dies and I have no way of recovering the data I would have only lost a days worth of work, rather than a few months of work.

This will not actually affect the end result of my project but I do feel it is important to talk about it as it is probably the most important step of all since if something goes wrong, you can recover, if you don't you cant.

## 2.3 Bespoke Algorithm Design

### 2.3.1 Question/Answer Algorithm

Since one of the main aspects of this project is to teach a user a new concept and then get them to answer various questions about that topic. There are ? stages to this process, these processes are listen below.

- Stage 1:  
Get the answer selected by the user
- Stage 2:  
Send information based on the users answer to the Database API.
- Stage 3:  
The Database API will then load this information into the db.user.questions record for the currently logged in user.
- Stage 4:  
The Web Application then queries the Database API for the answer of the question in the questions table.
- Stage 5:  
The Web Application then compares both answers to see if the user is correct.
- Stage 6:  
The Web Application then shows the user whether or not the question is right.

#### 2.3.1.1 Algorithm Block Diagram

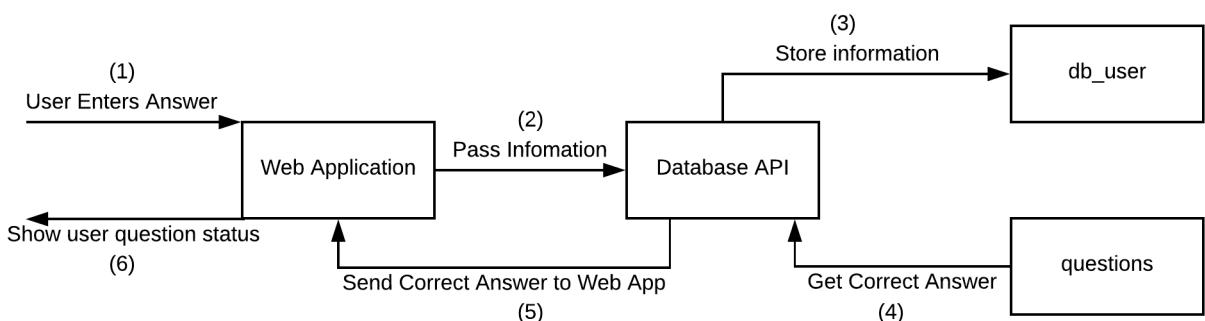


Figure 2.1: The Questions/Answer Algorithm Process

### 2.3.2 Cryptographic

## 2.4 Cryptographic Algorithm Design

### 2.4.1 Galois Fields for AES

In AES, every single operation that is used is based on Finite Fields. This section will give you a brief introduction to what Finite Fields are and how they are used.

#### 2.4.1.1 Introduction to Finite Fields

It should be stated now that the term *Finite Field* means the same thing as the term *Galois Field*. In Abstract Algebra there are 3 basic structures, the group, the ring, and the finite field.

**Groups Definition** A group is a set of elements  $G$  together with an operation  $\cdot$  which contains 2 elements of  $G$ . A group has the following properties:

1. The group operator  $\cdot$  is closed. That is for all  $a, b \in G$ , it holds that  $a \cdot b = c \in G$
2. The group operation is associative. That is,  $a \cdot (b \cdot c) \equiv (a \cdot b) \cdot c$  for all  $a, b, c \in G$
3. There is an identity element  $1 \in G$  such that  $a \cdot 1 = 1 \cdot a = a$  for  $a \in G$
4. There is an inverse element for all elements in  $G$ . That is for  $a \in G$ , there must be a element  $a^{-1} \in G$  such that  $a \cdot a^{-1} = a^{-1} \cdot a = 1$
5. A group is Abelian (or commutative) if,  $a, b \in G$ ,  $a \cdot b \equiv b \cdot a$

Roughly speaking a group is set with one operation and its corresponding inverse operation. If this operation is addition then the inverse operation will be subtraction, if the operation is multiplication then the inverse will be division. If we need a structure that can hold all 4 operations, that is where we will use Finite Fields (Galois Fields). It should be noted that it is common to denote a Finite Field as FF and a Galois Field as GF.

**Finite Field Definition** A field  $F$  is a set of elements with the following properties:

1. All elements of  $F$  for an additive group with the group operation "+" and the identity element 0.
2. All elements of  $F$ , except the identity element 0, form a multiplicative group with the group operation "×" and the identity element 1.

3. When the two group operations are mixed, the distributivity law holds, e.g. for all  $a, b, c \in F : a(b + c) = (ab) + (ac)$

In cryptography we are almost always interested in fields with a finite number of elements which we intuitively name Finite Fields or Galois fields. The number of elements in the field is called the *order* or *cardinality* of the field. It should be noted that a field with order  $m$  only exists if  $m$  is a prime power, e.g.  $m = p^n$  where  $n$  is a positive integer and  $p$  is a prime number.  $p$  is called the characteristic of the finite field. This implies that there are finite fields with 11 elements or 81 elements, since  $81 = 3^4$  or with 256 elements (since  $256 = 2^8$  and 2 is a prime). There is no finite fields with 12 elements since  $12 = 2^2 \cdot 3$  and 12, meaning 12 is not a prime power.

**Prime Fields** The most intuitive examples of FF are fields of prime order, fields with  $n = 1$ . Elements of the  $GF(p)$  can be represented by the integers  $0, 1, \dots, p - 1$ . The two operations are modular integer addition and multiplication modulo  $p$ . This means that if we consider the integer ring  $\mathbb{Z}_m$  and  $m$  happens to be prime then  $\mathbb{Z}_m$  is not only a ring but also a finite field.

In order to do arithmetic in a prime field we have to follow the rules for integer rings: Addition and multiplication are done modulo  $p$ , the additive inverse of any element  $a$  is given by  $a + (-a) = 0 \bmod p$ , and the multiplicative inverse of any non-zero element  $a$  is defined as  $a \cdot a^{-1} = 1$

We can look at the example of the prime field  $GF(2) = \{0, 1\}$ , which is the smallest finite field that can exist. The additive and multiplicative tables for the GF are listed below.

+	0	1
0	0	1
1	1	0

Table 2.1: Additive Table for  $GF(2)$

$\times$	0	1
0	0	0
1	0	1

Table 2.2: Multiplicative Table for  $GF(2)$

This is quite cool as it shows that addition in  $GF(2)$ , modulo 2 addition, is equivalent to and XOR Gate. It also shows us that multiplication in  $GF(2)$  is equivalent to the logical AND Gate. This field,  $GF(2)$  is very important for AES.

### 2.4.1.2 Extention Fields $GF(2^m)$

AES uses a FF of 256 elements and is denoted as  $GF(2^8)$ . This field was chosen as each of the elements in this field can be represented as exactly one byte. It becomes increasing important as the S-Box and MixColumn transformations treat every byte of the internal data path as an element of the field  $GF(2^8)$  and manipulates the data by performing arithmetic in this finite field.

As we said before if the order of a FF is not prime, which is clearly the case here ( $2^8$  is clearly not a prime number) the addition and multiplication operators can not be represented by addition and multiplication of integers modulo  $2^8$ . Fields with  $m > 1$  are called *extension fields*. In order for us to have the ability of working with these fields we need the following:

1. A different notation for the field elements
2. Different rules for when we perform arithmetic operations with the elements

So for the elements of these finite fields, we represent them as *polynomials* with coefficients and that when we compute with these we perform a certain type of *polynomial arithmetic*. The polynomials have a maximum degree of  $m - 1$ , so that there are  $m$  coefficients in total for every element. In the field  $GF(2^8)$ , which is the AES FF, each element  $A \in GF(2^8)$  is represented as:

$$A(x) = a_7x^7 + a_6x^6 + \dots + a_1x + a_0 \text{ where } a_i \in GF(2) = \{0, 1\}$$

It is very important to realise that every element of  $GF(2^8)$  can also be stored as an 8 – bit vector:

$$A = (a_7, a_6, a_5, a_4, a_3, a_2, a_1, a_0)$$

This means we do not have to store the factors  $x^7, x^5, etc$  as it is clear from the bit positions to which power  $x^i$  each coefficients belongs.

### 2.4.1.3 Addition and Subtraction in $GF(2^m)$

This is actually really easy as we just follow the basic polynomial rules of addition and subtraction, we just add or subtract coefficients with equal powers of  $x$ . This is mathematically shown below, Let  $A(x), B(x) \in GF(2^m)$ . The sum of the two elements is then computed as the following:

$$C(x) = A(x) + B(x) = \sum_{i=1}^{m-1} c_i x^i$$

where  $c_i \equiv a_i + b_i \bmod 2$

and the difference between the 2 pairs is computed as the following:

$$C(x) = A(x) - B(x) = \sum_{i=1}^{m-1} c_i x^i$$

where  $c_i \equiv a_i - b_i \equiv a_i + b_i \pmod{2}$

Since we perform modulo 2 addition with the coefficients, addition and subtraction are the same thing. An example of this is given below:

$$\begin{aligned} A(x) &= x^7 + x^6 + x^4 + 1 \\ B(x) &= x^4 + x^2 + 1 \\ C(x) &= A(x) + B(x) = x^7 + x^6 + x^2 \end{aligned}$$

Note if we were to work out the difference between the two polynomials  $A(x)$  and  $B(x)$  it would be the same as  $C(x)$ .

#### 2.4.1.4 Multiplication in $GF(2^m)$

Multiplication in  $GF(2^8)$  is the core operation in the MixColumn transformation in AES. Firstly, 2 elements of  $GF(2^8)$  are multiplied using standard polynomial rules:

$$\begin{aligned} A(x) \cdot B(x) &= (a_{m-1}x^{m-1} + \dots + a_0) \cdot (b_{m-1}x^{-1} + \dots + b_0) \\ C'(x) &= c'_{2m-2}x^{2m-1} + \dots + c'_0 \end{aligned}$$

Where:

$$\begin{aligned} c'_0 &= a_0 b_0 \pmod{2} \\ c'_1 &= a_0 b_1 + a_1 b_0 \pmod{2} \end{aligned}$$

.

.

.

$$c'_{2m-2} = a_{m-1} b_{m-1} \pmod{2}$$

Realize that all coefficients  $a_i$ ,  $b_i$  and  $c_i$  are elements of  $GF(2)$  and that coefficients arithmetic is performed in  $GF(2)$ . In general the product polynomial,  $C(x)$ , will have a degree higher than  $m - 1$  and will thus have to be reduced. The idea is similar to what we would do in prime fields: in  $GF(p)$ , we multiply the two integers, divide the result by a prime and consider only

the remainder. In extension fields the product polynomial  $C(x)$  is divided by a special polynomial and we consider only the remainder after the polynomial division. The special polynomials are called irreducible polynomials and we need them for the module reduction. These polynomials are roughly comparable to prime numbers, basically their only factors are 1 and the polynomial itself. A mathematical description of Extension Field multiplication is given below:

Let  $A(x), B(x) \in GF(2^m)$  and let

$$P(x) \equiv \sum_{i=0}^m p_i x^i, p_i \in GF(2)$$

be an irreducible polynomial. Multiplication of the two elements  $A(x), B(x)$  is given as

$$C(x) \equiv A(x) \cdot B(x) \bmod P(x)$$

This means that we need a irreducible polynomial  $P(x)$ , of degree  $m$  and with coefficients from  $GF(2)$ , for every field  $GF(2^m)$ . Not all polynomials are reducible much like not every number is a prime. We only need to know the irreducible polynomial for AES; it is given below

$$P(x) = x^8 + x^4 + x^3 + x + 1$$

This polynomial is a part of the specification for AES.

Putting this all together, lets say that we have the 2 polynomials  $A(x)$  and  $B(x)$  where  $A(x) = x^3 + x^2 + 1$  and  $B(x) = x^2 + x$  and we want to multiply them in the  $GF(2^4)$ . The irreducible polynomial for this GF is given as  $P(x) = x^4 + x + 1$ .

First we have to work out the plain polynomial multiplication,

$$C'(x) = A(x) \cdot B(x) = x^5 + x^3 + x^2 + x$$

We can now reduce  $C'(x)$  using the standard polynomial division method, but it can sometimes be easier to reduce each of the leading terms  $x^4$  and  $x^5$  individually.

$$\begin{aligned} x^4 &= 1 \cdot P(x) + (x + 1) \\ x^4 &\equiv x + 1 \bmod P(x) \\ x^5 &\equiv x^2 + x \bmod P(x) \end{aligned}$$

Now we just substitute that back into our  $C'(x)$  expression and we will get our result for the multiplication of  $A(x)$  and  $B(x)$

$$C(x) \equiv x^5 + x^3 + x^2 + x \bmod P(x)$$

$$C(x) \equiv (x^2 + x) + (x^3 + x^2 + x) = X63$$

$$A(x) \cdot B(x) \equiv x^3$$

We need to make sure we do not confuse multiplication in  $GF(2^m)$  with integer multiplication, especially if we are concerned with software implementations of Galois fields.

#### 2.4.1.5 Inversion in $GF(2^m)$

Inversion in  $GF(2^8)$  is the core operation in the Byte Substitution Layer of AES which contains the S-Boxes. For a given FF  $GF(2^m)$  and the corresponding irreducible polynomial  $P(x)$ , the inverse  $A^{-1}$  of a nonzero element  $A \in GF(2^m)$  is defined as:

$$A^{-1} \cdot A(x) = 1 \bmod P(x)$$

For small fields, in practice fields with  $2^16$  or fewer elements, look-up tables which contain the precomputed inverses of all finite elements are often used. Figure 2.2 shows the multiplicative inverse for  $GF(2^8)$  used in AES.

		<b>Y</b>															
		0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
<b>X</b>	0	00	01	8D	F6	CB	52	7B	D1	E8	4F	29	C0	B0	E1	E5	C7
	1	74	B4	AA	4B	99	2B	60	5F	58	3F	FD	CC	FF	40	EE	B2
	2	3A	6E	5A	F1	55	4D	A8	C9	C1	0A	98	15	30	44	A2	C2
	3	2C	45	92	6C	F3	39	66	42	F2	35	20	6F	77	BB	59	19
	4	1D	FE	37	67	2D	31	F5	69	A7	64	AB	13	54	25	E9	09
	5	ED	5C	05	CA	4C	24	87	BF	18	3E	22	F0	51	EC	61	17
	6	16	5E	AF	D3	49	A6	36	43	F4	47	91	DF	33	93	21	3B
	7	79	B7	97	85	10	B5	BA	3C	B6	70	D0	06	A1	FA	81	82
	8	83	7E	7F	80	96	73	BE	56	9B	9E	95	D9	F7	02	B9	A4
	9	DE	6A	32	6D	D8	8A	84	72	2A	14	9F	88	F9	DC	89	9A
	A	FB	7C	2E	C3	8F	B8	65	48	26	C8	12	4A	CE	E7	D2	62
	B	0C	E0	1F	EF	11	75	78	71	A5	8E	76	3D	BD	BC	86	57
	C	0B	28	2F	A3	DA	D4	E4	0F	A9	27	53	04	1B	FC	AC	E6
	D	7A	07	AE	63	C5	DB	E2	EA	94	8B	C4	D5	9D	F8	90	6B
	E	B1	0D	D6	EB	C6	0E	CF	AD	08	4E	D7	E3	5D	50	1E	B3
	F	5B	23	38	34	68	46	03	8C	DD	9C	7D	A0	CD	1A	41	1C

Figure 2.2: The multiplicative inverse table of  $GF(2^8)$  for bytes  $xy$  used within the AES S-Box

As an alternative to using lookup tables, it is possible to compute the inverses of all the elements. The main algorithm uses for this task is the Extended Euclidean Algorithm (EEA).

## 2.4.2 AES Internals

### 2.4.2.1 Structure of AES

It should be noted that the 128-bit data path that runs through the algorithm is split up into 16-bytes, this is why many people would consider AES a byte oriented block cipher as it works in pure bytes. So our structure diagram from Figure 1.3 can be adapted to the structure shown in Figure 2.3. We also noted before that the algorithm operates on a  $4 \times 4$  matrix of bytes, Figure 1.2, and this remains true so keep that in mind when performing any operations, this becomes especially important in the ShiftRows and MixColumns steps.

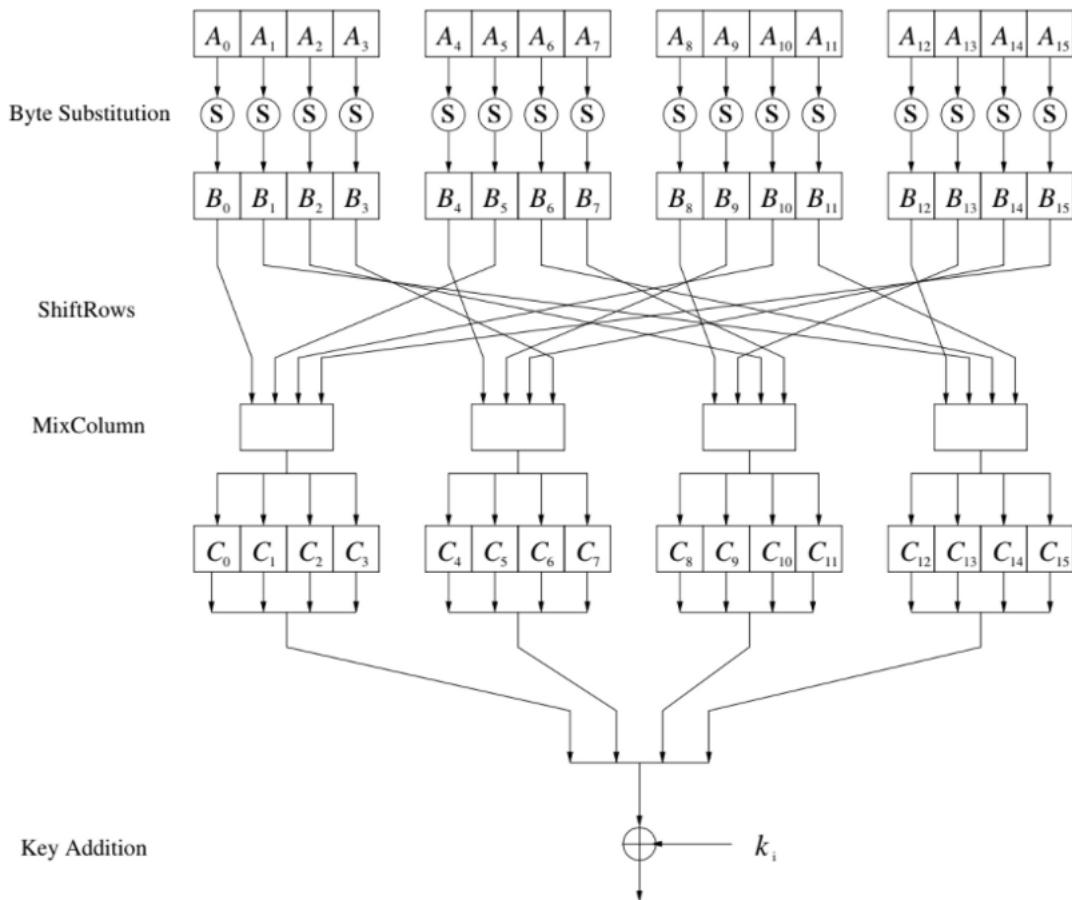


Figure 2.3: AES Byte Level Overview

The rest of this section will be looking into how the different components of each round work, these being the ByteSub Layer, ShiftRows Layer, Mix-Columns Layer and Key Addition Layer.

### 2.4.2.2 Byte Substitution Layer

The first layer in AES is the Byte Substitution Layer. There are 16 parallel S-Box which all take 8-bits as input and 8-bits as output. All 16 S-Box are

identical with is different to DES as that cipher uses 8 unique S-Boxes. Each state Byte  $A_i$  is replaced, substituted, with another Byte,  $B_i$ . The process is shown below:

$$S(A_i) = B_i$$

The S-Box is the only non-linear section of AES. This basically means that

$$S(A) + S(B) \neq S(A + B) \text{ With 2 Byte States } A \text{ and } B.$$

The S-Box substitution is a 1-to-1 mapping, basically all of the  $2^8 = 256$  elements are mapped to one output element. This is good as it allows us to uniquely reverse the S-Box, which is key to the decryption process. In software, the S-Box is usually setup as a 256 Byte lookup table with fixed entries. The AES S-Box is given below for an input byte  $(YX)$ , with  $(YX)$  representing its hexadecimal value in each of its respective columns.

	<b>x0</b>	<b>x1</b>	<b>x2</b>	<b>x3</b>	<b>x4</b>	<b>x5</b>	<b>x6</b>	<b>x7</b>	<b>x8</b>	<b>x9</b>	<b>xa</b>	<b>xb</b>	<b>xc</b>	<b>xd</b>	<b>xe</b>	<b>xf</b>
<b>0x</b>	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
<b>1x</b>	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
<b>2x</b>	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
<b>3x</b>	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
<b>4x</b>	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
<b>5x</b>	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
<b>6x</b>	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
<b>7x</b>	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
<b>8x</b>	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
<b>9x</b>	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
<b>ax</b>	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
<b>bx</b>	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
<b>cx</b>	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
<b>dx</b>	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
<b>ex</b>	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
<b>fx</b>	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

Figure 2.4: The AES S-Box

So lets look at an example, say we have the Byte State  $A_i = (3b)_{hex}$ , then we apply the S-Box and get the following result:

$$S(A_i) \equiv S((3b)_{hex}) \equiv (e2)_{hex}$$

If we were to look at this on a bit level, the point of interest for the cryptography of the cipher, then the substitution becomes:

$$S(A_i) \equiv S(00111011) \equiv (11100010)$$

Even though the S-Box has a 1-to-1 mapping, it does not have any fixed points. This means that there are no input values  $A_i$  that make  $S(A_i) = A_i$ . Even the zero-input state is not a fixed point, i.e  $S((00)_{hex}) = S(00000000) = (01100011)$ .

### Mathematical Description of S-Box

ADD THIS IN LATER

#### 2.4.2.3 ShiftRows Layer

The ShiftRows Layer does exactly what its name implies. It cyclically shifts the rows of the byte matrix, see Figure 1.2. It shifts the first row by 0 bytes, the second row by 1 byte to the left, the third row 2 bytes to the left and the fourth row by 3 bytes to the left. If we take out original byte matrix, also shown in Figure 1.2, shown below:

$b_0$	$b_4$	$b_8$	$b_{12}$
$b_1$	$b_5$	$b_9$	$b_{13}$
$b_2$	$b_6$	$b_{10}$	$b_{14}$
$b_3$	$b_7$	$b_{11}$	$b_{15}$

After the ShiftRows Layer, the matrix would look like this, shown below.

$b_0$	$b_4$	$b_8$	$b_{12}$
$b_5$	$b_9$	$b_{13}$	$b_1$
$b_{10}$	$b_{14}$	$b_2$	$b_6$
$b_{15}$	$b_3$	$b_7$	$b_{11}$

#### 2.4.2.4 MixColumns Layer

The MixColumns Layer is a linear transformation step which mixes the column of the state matrix. The combination of the ShiftRow and MixColumn layers makes it possible that after only three rounds, every byte of the state matrix depends on all 16 plaintext bytes. We denote the MixColumn layer with input matrix B and output matrix C as the following:

$$\text{MixColumn}(B) = C$$

Where B is the state matrix after the ShiftRows layer. Now we take each column as a vector and is then multiplied by a fixed  $4 \times 4$  matrix. This matrix is constant. Multiplication and addition of the coefficients is done in  $GF(2^8)$ . The computation of the first four output bytes is shown below.

$$\begin{pmatrix} C_0 \\ C_1 \\ C_2 \\ C_3 \end{pmatrix} = \begin{pmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{pmatrix} \begin{pmatrix} B_0 \\ B_5 \\ B_{10} \\ B_{15} \end{pmatrix}$$

The second column of  $C$ ,  $(C_4, C_5, C_6, C_7)$  is computed by multiplying the same constant matrix by  $(B_4, B_9, B_{14}, B_3)$ , the third and fourth columns of  $C$  add heed to this as well.

We know that each state byte,  $C_i$  and  $B_i$  are 8-bit values that represent a value in  $GF(2^8)$ . All arithmetic done is performed in this layer is formed in  $GF(2^8)$ . The constants in the matrix are hexadecimal numbers, representing the corresponding values in the Galois Field. So  $01_{hex}$  is  $00000001_{bin}$  which corresponds to the  $GF(2^8)$  element 1,  $02_{hex}$  is  $00000010_{bin}$  corresponds to the  $GF(2^8)$  polynomial  $x$  and  $03_{hex}$  is  $00000011_{bin}$  corresponds to the  $GF(2^8)$  polynomial  $x+1$ .

The additions here are performed in  $GF(2^8)$  so are simple XOR operations with the 2 different bytes. For the multiplications, the constants 01, 02, 03 were chosen as they are very easy to set up in software. Multiplication with 01 is just multiplication by the identity which doesn't require a given operation. Multiplication by 02 and 03 are more complicated, therefore 2 256 byte lookup tables are used. You could do multiplication by 02 as a multiplication by  $x$ , which is just a left shift of 1, and then a modular reduction by the irreducible polynomial of  $GF(2^8)$ ,  $P(x) = x^8 + x^4 + x^3 + x + 1$ . Multiplication by 03 is similar, it is just a left shift of 1 and then adding the original value followed by modular reduction of  $P(x)$  again.

As an example, lets take the input state array,  $B = (25, 25, \dots, 25)$ . Since we are only doing the first column this only involves 2 multiplications, by 02 and 03.

$$\begin{aligned} 02 \cdot 25 &= x \cdot (x^5 + x^2 + 1) \\ &= x^6 + x^3 + x \\ 03 \cdot 25 &= (x + 1) \cdot (x^5 + x^2 + 1) \\ &= (x^6 + x^3 + x) + (x^5 + x^2 + 1) \\ &= x^6 + x^5 + x^3 + x^2 + x + 1 \end{aligned}$$

Since the order of our intermediate values,  $x^6 + x^3 + x$  and  $x^6 + x^5 + x^3 + x^2 + x + 1$ , do not have an order of above 8 we don't need to perform modular reduction with  $P(x)$ , the next step is to add together all the components of the multiplication.

$$\begin{aligned} 02 \cdot 25 &= 1x^6 + 0x^5 + 0x^4 + 1x^3 + 0x^2 + 1x + 0 \\ 03 \cdot 25 &= 1x^6 + 1x^5 + 0x^4 + 1x^3 + 1x^2 + 1x + 1 \\ 01 \cdot 25 &= 0x^6 + 1x^5 + 0x^4 + 0x^3 + 1x^2 + 0x + 1 \\ 01 \cdot 25 &= 0x^6 + 1x^5 + 0x^4 + 0x^3 + 1x^2 + 0x + 1 \end{aligned}$$

---


$$C_i = 0x^6 + 1x^5 + 0x^4 + 0x^3 + 1x^2 + 0x + 1$$

This is where  $i = 0, 1, 2, \dots, 15$ . This means our output state is the value of the  $GF(2^8)$  polynomial  $x^5 + x^2 + 1$  which is 25. So  $C = (25, 25, \dots, 25)$ .

### 2.4.2.5 Key Addition Layer

The key addition layer takes 2 inputs, the current 16-byte state matrix and a sub key which is also 16-bytes. Then the 2 inputs are combined using the XOR operation. The particular sub keys that are derived are explained in the next section, *Section 2.4.2.6*.

### 2.4.2.6 AES Key Schedule

The Key Schedule takes our original 128/192/256 bit key and will then derive the subkeys needed for the algorithm. At the beginning and end of AES a XOR addition is applied to the subkey, this process is sometimes referred to as key-whitening. The number of subkeys required is the number of rounds plus one as we need an extra subkey for the key-whitening. A table with the key lengths, round numbers, and subkeys is shown below.

$N_k(\text{bits})$	$N_r$	$N_{sk}$
128	10	11
192	12	13
256	14	15

Table 2.3: Repsective Key Lengths, Rounds Numbers, Subkey Numbers

The AES Key Schedule is word oriented, where 1 word = 32-bits. Sub keys are stored in an expansion array called  $W$  that consists of words. There are 3 different key schedules for the 3 different key sizes.

**128-bit Key Schedule** The 11 subkeys are computed and stored in an array with elements  $W[0], W[1], \dots, W[43]$ .. Figure 2.5 shows exactly how the subkeys for AES with a 128-bit key are computed.

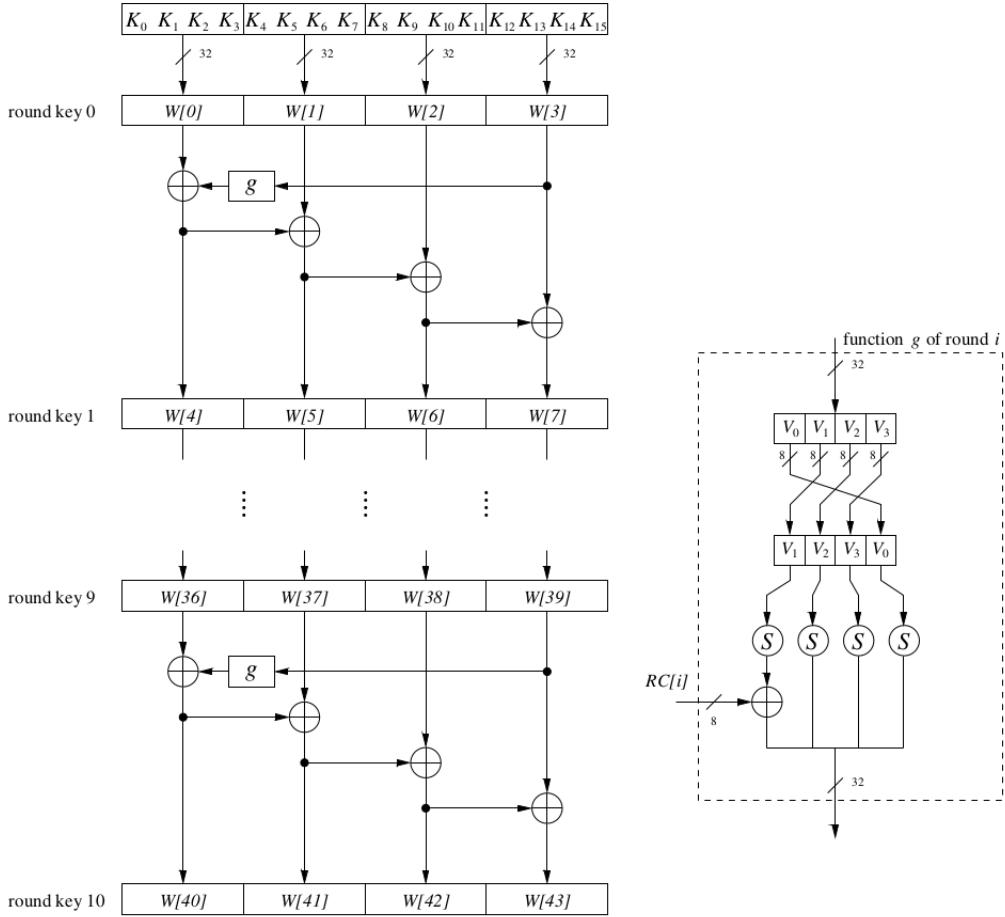


Figure 2.5: 128-bit Key Schedule for AES

The first subkey,  $k_0$ , is just the original key used when initializing the algorithm. So elements  $W[0], \dots, W[3]$  contain our original 128-bit key. Then, the left most word of a subkey  $W[4i]$ , where  $i = 1, 2, \dots, 10$ , is computed using the following formula:

$$W[4i] = W[4(i - 1)] \oplus g(W[4i - 1])$$

With the function  $g$  here being a non-linear function with a 4-byte input and a 4-byte output. The remaining elements of  $W$  are calculated using the following formula:

$$W[4i + j] = W[4i + j - 1] \oplus W[4(i - 1) + j]$$

Where  $i = 1, 2, 3, \dots, 10$  and  $j = 1, 2, 3$ .

The function  $g()$  rotates our 4-byte input, it applies a S-Box substitution and adds a round coefficient,  $RC$ , to it.  $RC$ 's value is an element from  $GF(2^8)$ , i.e. an 8-bit value. This value is only added to the left most byte in the function  $g()$ . The  $RC$  vary from round to round according to the following rule:

$$RC[1] = x^0 = (00000001)_2,$$

$$RC[2] = x^1 = (00000010)_2,$$

$$RC[3] = x^2 = (00000100)_2,$$

$$\dots$$

$$RC[10] = x^9 = (00110110)_2,$$

This function  $g()$  has 2 purposes, its first is to add non-linearity to the key schedule and the second is to remove symmetry from the AES cipher. Both of these are required as it protects from some attacks against block ciphers.

**192-bit Key Schedule** With a 192-bit key, we need 13 subkeys, which means our array  $W$  will have 52 words. The way we compute all of the 13 words, and thus the 52 words, is very similar to the way we compute the subkeys for a 128-bit key, this is shown in Figure 2.6. There are 8 iterations of the Key Schedule, where each iteration computes 6 new words for the subkey array  $W$ . We need 8 round coefficients,  $RC[i]$ , for use in our  $g()$  function. These round constants are computed the same way as in a 128-bit key case.

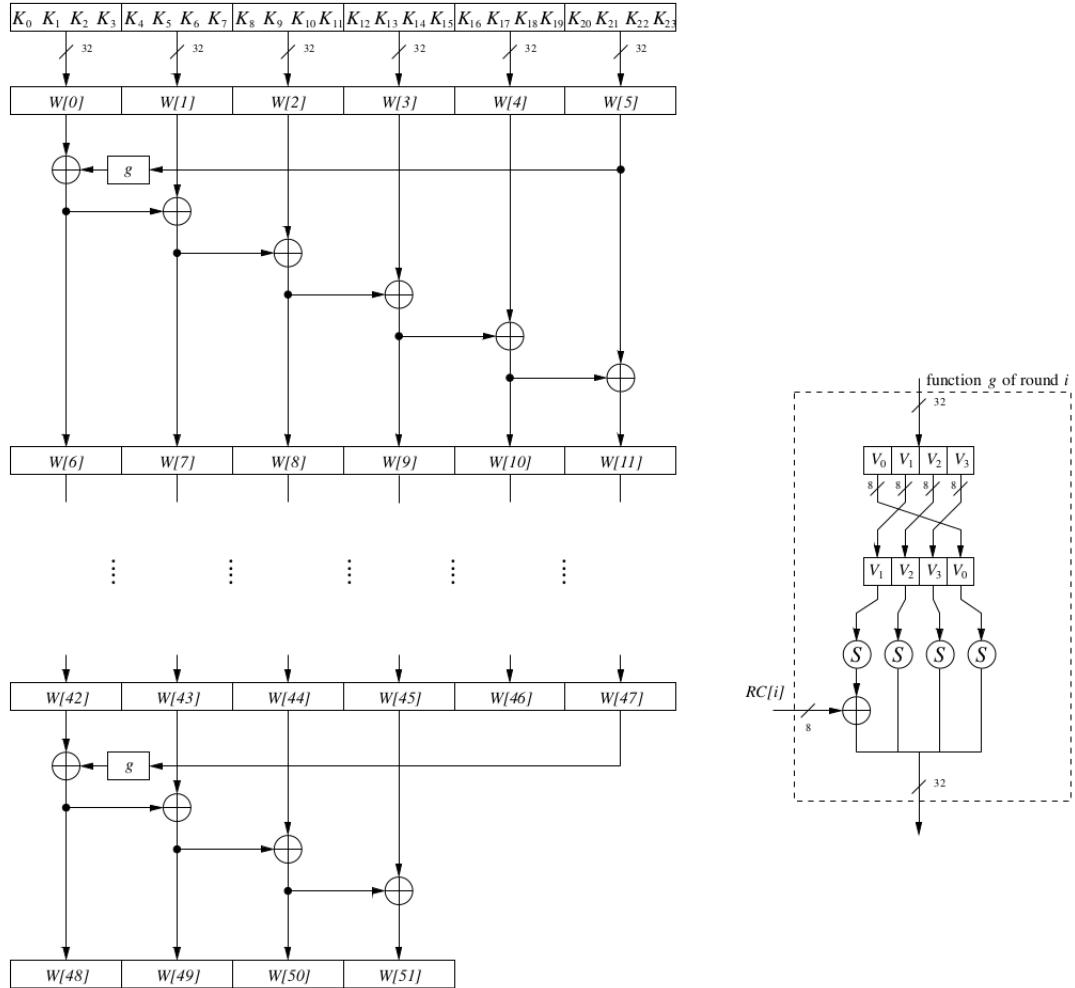


Figure 2.6: 192-bit Key Schedule for AES

**256-bit Key Schedule** With a 256-bit key, we need 15 subkeys, meaning our array  $W$  will contain 60 words. The way we compute all of the 13 words, and thus the 52 words, is very similar to the way we compute the subkeys for a 128-bit key, this is shown in Figure 2.7. There are 7 iterations of the Key Schedule, where each iteration computes 8 new words for the subkey array  $W$ . We need 7 round coefficients,  $RC[i]$ , for use in our  $g()$  function. These round constants are computed the same way as in a 128-bit key case. The key schedule also introduces a new function  $h()$ , which takes a 4-byte input and output.  $h()$  applies the S-Box to each input byte.

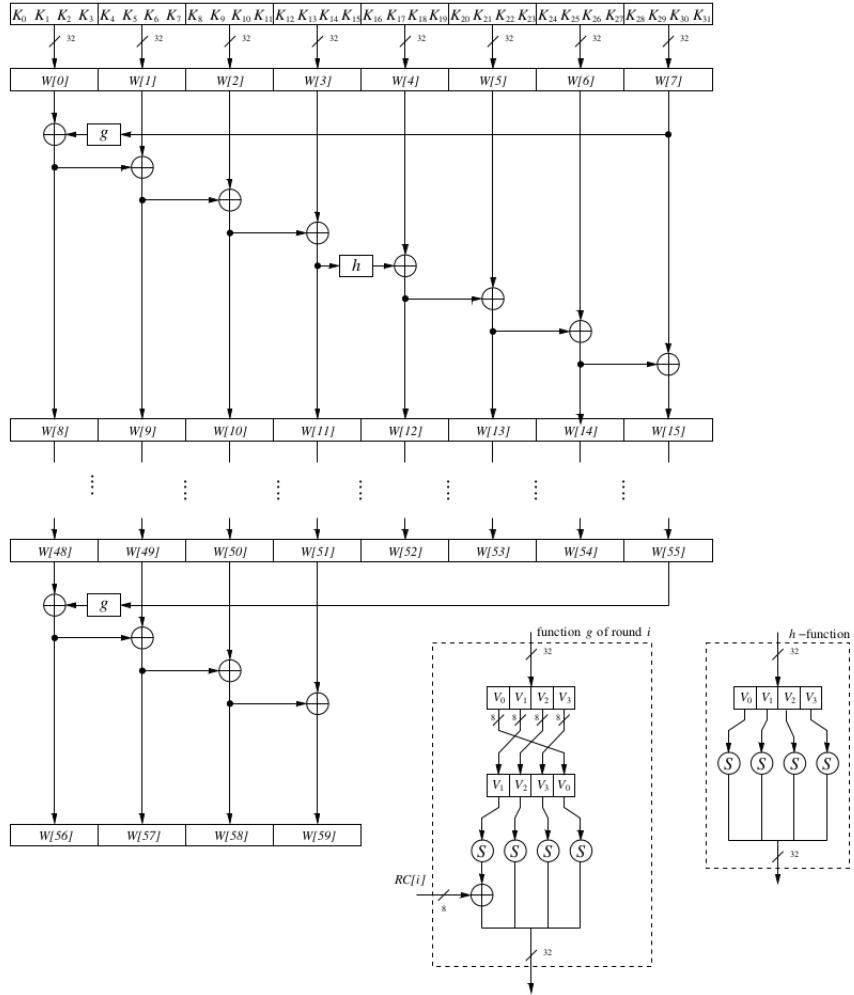


Figure 2.7: 256-bit Key Schedule for AES

### 2.4.3 Decryption in AES

Unlike DES, because AES is not based on a feistal network each layer needs to be inverted in order to decrypt a message that was encrypted using AES. This means that the S-Box, ShiftRows, MixColumns need to be inverted. For the AddRoundKey, this words slightly differently as for this all we need to do is reverse the order of the key schedule. So for the first round we use the last subkey, the second round we use the second-last subkey. The diagram below, Figure 2.8, illustrated this process.

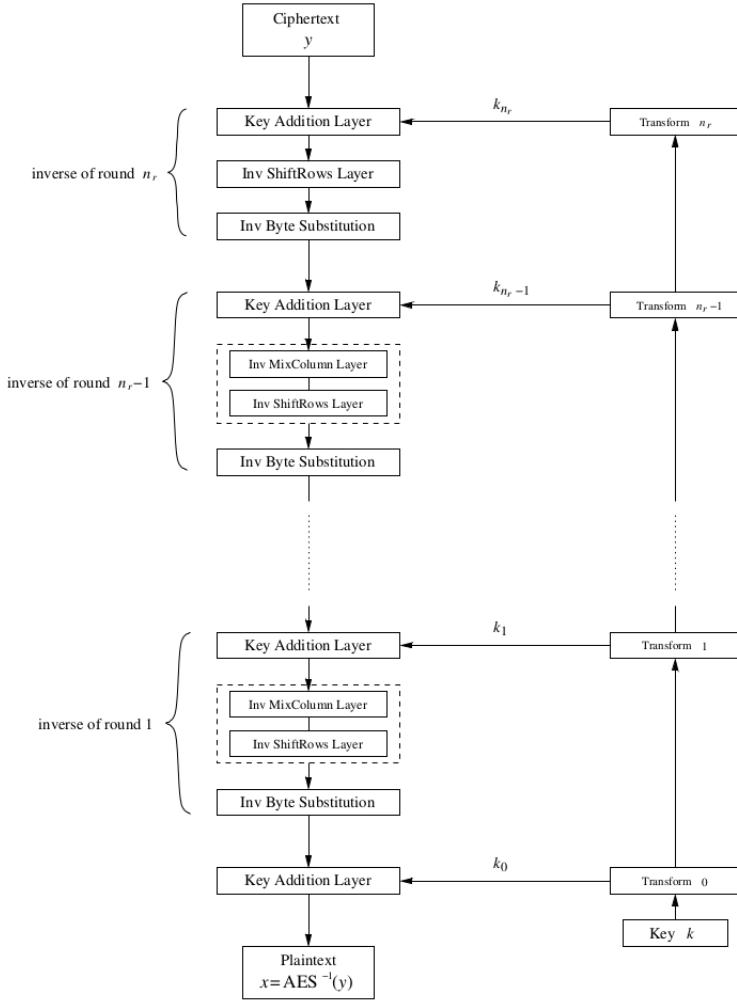


Figure 2.8: The Decryption process for AES

#### 2.4.3.1 Inverse MixColumns Layer

After the addition of the Sub key, the inverse MixColumns step is applied to the state matrix, the exception is on the first decryption round where MixColumns is not applied. We inverse the MixColumn operation by just using the inverse matrix of the MixColumn operation. We have our  $4 \times 4$  input state  $(C_0, C_1, C_2, C_3)$  and we just multiply this by the Inverse Matrix to get our output state  $(B_0, B_1, B_2, B_3)$ .

$$\begin{pmatrix} B_0 \\ B_1 \\ B_2 \\ B_3 \end{pmatrix} = \begin{pmatrix} 0E & 0B & 0D & 09 \\ 09 & 0E & 0B & 0D \\ 0D & 09 & 0E & 0B \\ 0B & 0D & 09 & 0E \end{pmatrix} \begin{pmatrix} C_0 \\ C_1 \\ C_2 \\ C_3 \end{pmatrix}$$

Then in order to calculate  $(B_4, B_5, B_6, B_7)$  we just use the input  $(C_4, C_5, C_6, C_7)$ .  $B_i$  and  $C_i$  are elements from  $GF(2^8)$  and also the constants in our matrix are

elements of  $GF(2^8)$ . It should also be said that additions in the vector-matrix multiplication are bitwise XOR's.

#### 2.4.3.2 Inverse ShiftRows Layer

In order to reverse the Shift Rows Layer all we have to do is shift the elements in the state matrix the opposite direction. The first row is not affected as it is also not affected in the normal ShiftRows layer. With our state matrix  $B = (B_0, B_1, B_2, B_3, \dots, B_{15})$ :

$b_0$	$b_4$	$b_8$	$b_{12}$
$b_1$	$b_5$	$b_9$	$b_{13}$
$b_2$	$b_6$	$b_{10}$	$b_{14}$
$b_3$	$b_7$	$b_{11}$	$b_{15}$

The Inverse Shift Rows operation would give us the following state matrix:

$b_0$	$b_4$	$b_8$	$b_{12}$
$b_{13}$	$b_1$	$b_5$	$b_9$
$b_{10}$	$b_{14}$	$b_2$	$b_6$
$b_7$	$b_{11}$	$b_{15}$	$b_3$

#### 2.4.3.3 Inverse ByteSubstitution Layer

The inverse S-Box is applied when decrypting with AES. Since the AES S-Box is bijective, one-to-one mapping, it is possible to create an inverse S-Box such that:

$$A_i = S^{-1}(B_i) = S^{-1}(S(A_i))$$

The values given in the Inverse S-Box are given in Figure 2.9.

	y																
	0	1	2	3	4	5	6	7	8	9	a	b	c	d	e	f	
x	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	cc	34	a5	e5	f1	71	d8	31	15
	3	04	c7	23	c3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3c	9f	a8
	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
	c	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
	e	e1	f8	98	11	69	d9	8e	94	9b	1e	87	e9	ce	55	28	df
	f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	b0	54	bb	16

Figure 2.9: The AES Inverse S-Box

#### 2.4.3.4 Decryption Key Schedule

Since the first round of the decryption round needs the last subkey, the second round of decryption needs the second-last subkey, etc, etc. So we need to supply the subkeys in reverse order for the decryption rounds. This can generally be done by computing the 11 or 13 or 15 subkeys and storing them. This adds some latency to the decryption of the algorithm when compared to the encryption rounds.

## 2.5 Bespoke Data Structures

## 2.6 Bespoke Database Design

### 2.6.1 User Details

<b>db_user</b>		[table]
<i>id</i>	INTEGER	
	auto-incremented	
version	INTEGER NOT NULL	
user_id	INTEGER NOT NULL	
user_role	INTEGER NOT NULL	
user_identity	TEXT NOT NULL	

Figure 2.10: db.user Database Table

### 2.6.2 User Answered Questions

<b>user_answered_questions</b>		[table]
<i>id</i>	INTEGER	
	auto-incremented	
version	INTEGER NOT NULL	
user_answered_question_id	INTEGER NOT NULL	
user_answered_answer_id	INTEGER NOT NULL	
user_answered_question_text	TEXT NOT NULL	
user_answered_answer_text	TEXT NOT NULL	
user_id	BIGINT	

Figure 2.11: user\_answered\_questions Database Table

### 2.6.3 Authentication Information

<i>auth_info</i>		[table]
<i>id</i>	INTEGER	
	auto-incremented	
version	INTEGER NOT NULL	
user_id	BIGINT	
password_hash	VARCHAR(100) NOT NULL	
password_method	VARCHAR(20) NOT NULL	
password_salt	VARCHAR(20) NOT NULL	
status	INTEGER NOT NULL	
failed_login_attempts	INTEGER NOT NULL	
last_login_attempt	TEXT	
email	VARCHAR(256) NOT NULL	
unverified_email	VARCHAR(256) NOT NULL	
email_token	VARCHAR(64) NOT NULL	
email_token_expires	TEXT	
email_token_role	INTEGER NOT NULL	

Figure 2.12: auth\_information Table

### 2.6.4 Authentication Identity

<i>auth_identity</i>		[table]
<i>id</i>	INTEGER	
	auto-incremented	
version	INTEGER NOT NULL	
auth_info_id	BIGINT	
provider	VARCHAR(64) NOT NULL	
"identity"	VARCHAR(512) NOT NULL	

Figure 2.13: auth\_identity\_table Table

## 2.6.5 Authentication Token

<b>auth_token</b>		[table]
<i>id</i>	INTEGER	
		auto-incremented
version	INTEGER	NOT NULL
auth_info_id	BIGINT	
"value"	VARCHAR(64)	NOT NULL
expires	TEXT	

Figure 2.14: auth\_token Table

## 2.6.6 Question Details

<b>questions</b>		[table]
<i>id</i>	INTEGER	
		auto-incremented
version	INTEGER	NOT NULL
question_text	TEXT	NOT NULL
question_answer	TEXT	NOT NULL
question_option_a	TEXT	NOT NULL
question_option_b	TEXT	NOT NULL
question_option_c	TEXT	NOT NULL

Figure 2.15: questions Table

## 2.6.7 Database Schema Diagram

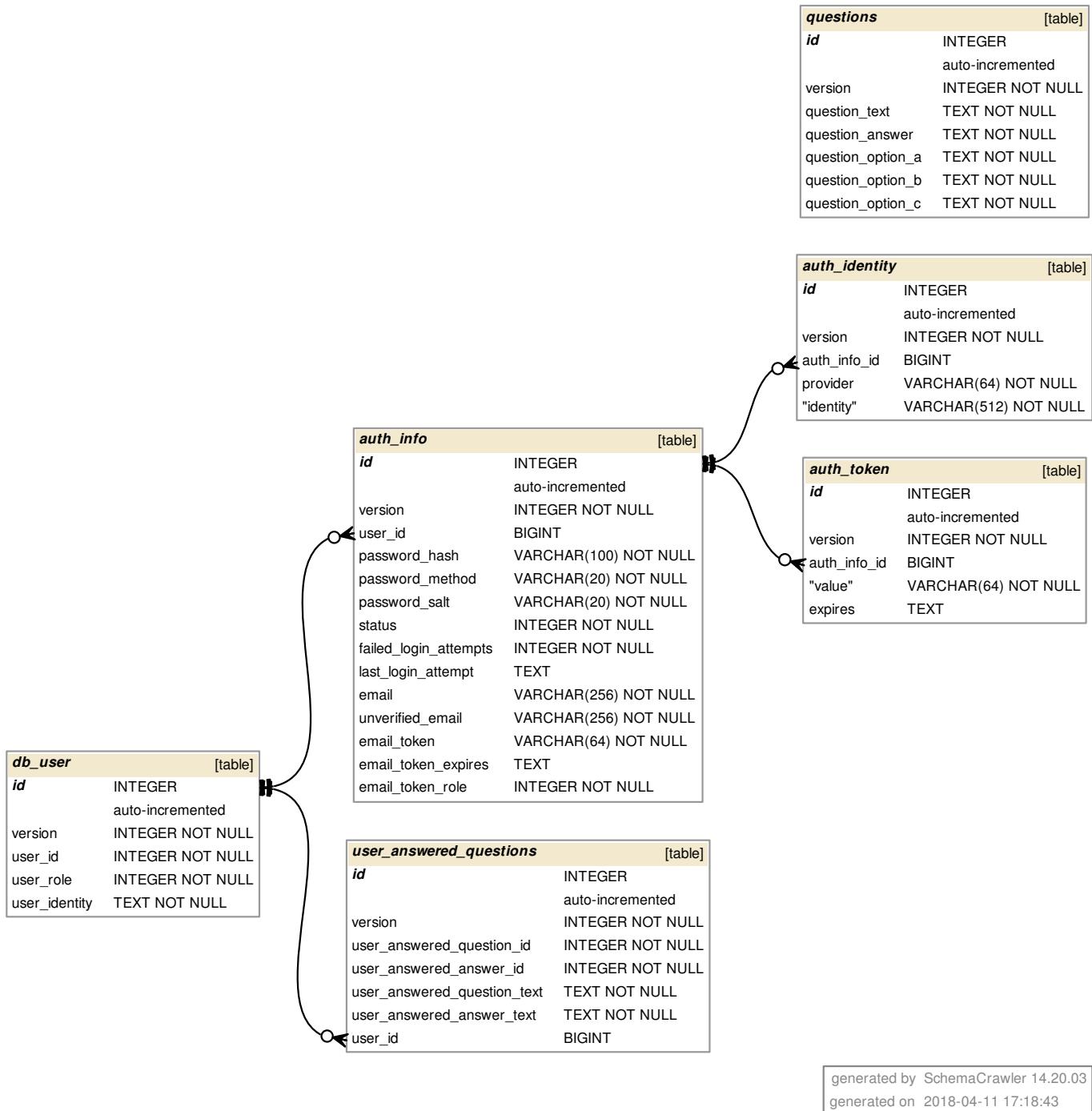


Figure 2.16: data.db schema

## 2.7 User Interface Design

### 2.7.1 Header - User not Logged In

#### 2.7.1.1 Left Side of Header



Figure 2.17: Left Side of the Website Header

#### 2.7.1.2 Right Side of Header



Figure 2.18: Right Side of the Website Header

### 2.7.2 Header - User Logged In

#### 2.7.2.1 Left Side of Header for a Normal User



Figure 2.19: Left Side of the Website Header when a Normal User is logged in

#### 2.7.2.2 Left Side of Header for a Admin User



Figure 2.20: Left Side of the Website Header when an Admin User is logged in

#### 2.7.2.3 Right Side of Header



Figure 2.21: Right Side of the Website Header when a User is logged in

## 2.7.3 Navigation Grid

### 2.7.3.1 Cryptography Basics



Figure 2.22: Cryptography Basics

### 2.7.3.2 Symmetric Cryptography

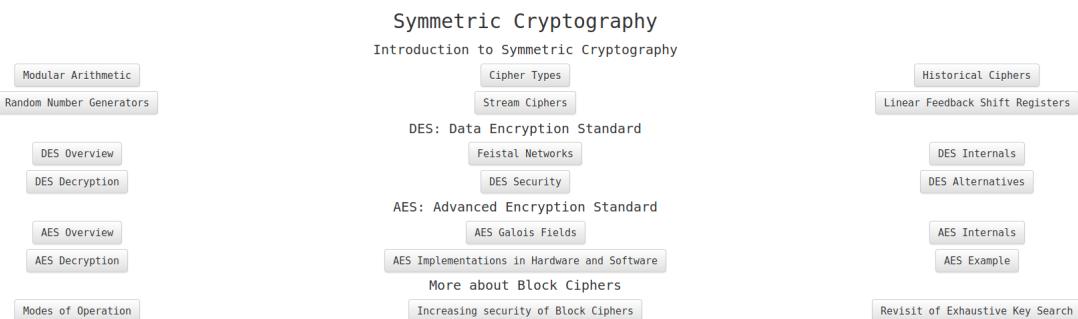


Figure 2.23: Symmetric Cryptography

### 2.7.3.3 Asymmetric Cryptography



Figure 2.24: Asymmetric Cryptography

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### 2.7.3.4 Protocols



Figure 2.25: Protocols

### 2.7.4 Information Content

### 2.7.5 Question Content

### 2.7.6 Login Form

The form is titled "Login". It contains two input fields: "User name" and "Password", each with a placeholder text "Enter your user name" and "Enter your password" respectively. Below these fields is a "Remember me" checkbox with a tooltip "Keeps login for 2 weeks". At the bottom is a blue "Login" button and a link "Lost password | Register".

Figure 2.26: Login Form

### 2.7.7 Register Form

The screenshot shows a registration form titled "Registration". The form is titled "Register using a user name and password:". It contains four input fields: "User name" (with placeholder "Enter your user name"), "Choose Password" (with placeholder "Choose a password"), "Repeat password" (with placeholder "Re-enter your password"), and "Email address" (with placeholder "Enter your email address (optional)"). Below the inputs are two buttons: "Register" (blue) and "Cancel" (gray).

Figure 2.27: Register Form

## 2.8 System Security

Since my project requires users to sign up that means they need to create a password. That means I need to ensure that all users passwords are secured properly so if at any point my database gets leaked onto the internet an attacker can get access to all my users accounts and more importantly user account data.

So all passwords are hashed using the bcrypt hash function. There is normally a lot of debate on which hash function to use but bcrypt has been around for over 10 years and no critical security flaws in its design and implementation have been found making a confident choice for me.

## 2.9 External Library's

### 2.9.1 Wt

Wt, said *Witty*, is a Web framework for the C++ programming language. It provides the basic widgets and building blocks needed to create A Web Application but also has a lot of other really useful features. This include but are not limited to:

- Client Side Optimized

By using a signal-slot system, we don't have to worry about dealing with the AJAX requests. We simply connect a widget to the callback function of the server and its done. It also will use whatever technology is available

for use in the communication, normally AJAX or WebSockets, but it will fall back into full html page reloads if javascript is not available. This allows a Wt Application to be accessible to any browser

- **Built-In Security**

By default, Wt only allows the visible and enable widgets to be interacted with. It also helps prevent CSRF attacks by not storing any of the session information in cookies. Because of the Widget abstraction it discourages the use of raw html in the application which helps to prevent again XSS attacks. SQL Injection attacks are stopped by encouraging the user to use prepared SQL statements when accessing the database. Wt also includes an authentication and registration system with support for OAuth providers like Google and Facebook

- **Object Relational Mapping Library**

This maps C++ classes to tables in my database using Wt::Dbo, a ORM that only requires pure C++. It does not depend on preprocessor magic or code generation.

# Chapter 3

## Technical Solution

This chapter will cover my coding implementations for my project. I will not be showcasing all the source code here as it would be far to difficult to search through and find the important parts of my solution. I will mainly be showing code snippets. The full source code solution for my project will be available in the appendix of this report.

### 3.1 AES Implementation

#### 3.1.1 AES Key Schedule

```
1 void AESImplementation::KeyExpansion(const byte key[], byte expandedKey[])=>
2     const {
3
4 #if defined(debug) && debug == 1
5     std::cout << "Key Expansion Start" << std::endl;
6 #endif
7     memset(expandedKey, 0, this->_b);
8     memcpy(expandedKey, key, this->_n);
9 #if defined(debug) && debug == 1
10    std::cout << "W[0 3]:";
11    for(byte i = 0; i < this->_n; i++){
12        std::cout << std::hex << std::setfill('0') << std::setw(2) << ←
13            unsigned(expandedKey[i]);
14    }
15    std::cout << std::endl;
16 #endif
17
18
19 byte t[4];
20 byte u[4];
21
22 for(byte rcon = 1; keySizeIterator < this->_b; rcon++){
23     memcpy(t, expandedKey + (keySizeIterator - 4), 4);
```

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---

```
25 #if defined(debug) && debug == 1
26     std::cout << "PRE 4: ";
27     for(byte i = 0; i < 4; i++)
28         std::cout << std::hex << std::setfill('0') << std::setw(2) <<←
29             unsigned(t[i]);
30     std::cout << std::endl;
31 #endif
32
33     this >KeyExpansionCore(rcon, t, u);
34     memcpy(t, expandedKey + (keySizeIterator      this >_n), 4 * sizeof(←
35         byte));
36
36 #if defined(debug) && debug == 1
37     std::cout << "W[i    4]: ";
38     for(byte i = 0; i < 4; i++)
39         std::cout << std::hex << std::setfill('0') << std::setw(2) <<←
40             unsigned(u[i]);
41     std::cout << std::endl;
42
43     for(byte i = 0; i < 4; i++)
44         t[i] ^= u[i];
45
46 #if defined(debug) && debug == 1
47     std::cout << "W[i]: ";
48     for(byte i = 0; i < 4; i++)
49         std::cout << std::hex << std::setfill('0') << std::setw(2) <<←
50             unsigned(t[i]);
51     std::cout << std::endl;
52
53     memcpy(expandedKey + keySizeIterator, t, 4 * sizeof(byte));
54     keySizeIterator += 4;
55
56     for(byte i = 0; i < 3 && (keySizeIterator < this >_b); i++){
57         memcpy(t, expandedKey + (keySizeIterator - 4), 4 * sizeof(←
58             byte));
59
59 #if defined(debug) && debug == 1
60     std::cout << "temp: ";
61 #endif
62     for (byte j = 0; j < 4; j++)
63     {
64         expandedKey[keySizeIterator + j] = t[j] ^ expandedKey[←
65             keySizeIterator      this >_n + j];
66 #if defined(debug) && debug == 1
67         std::cout << (unsigned)expandedKey[keySizeIterator + j];
68 #endif
69     }
70 #if defined(debug) && debug == 1
71     std::cout << std::endl;
72 #endif
73     keySizeIterator += 4;
74 }
```

```

74     if ((this >_key_size == 256) && (keySizeIterator < this >_b)){
75
76         memcpy(t, expandedKey + (keySizeIterator - 4), 4 * sizeof(←
77             byte));
78         for(byte i = 0; i < 4; i++){
79             t[i] = sbox[t[i]];
80         }
81
82         for(byte i = 0; i < 4; i++){
83             expandedKey[keySizeIterator + i] = t[i] ^ expandedKey[←
84                 keySizeIterator - this >_n + i];
85             t[i] ^= expandedKey[keySizeIterator - this >_n - 4 + i];
86         }
87         //memcpy(expandedKey + (keySizeIterator - 3 - 1), t, 4 * ←
88             sizeof(byte));
89         keySizeIterator += 4;
90     }
91
92     for(byte i = 0; (i < this >_m) && (keySizeIterator < this >_b); i++)
93     {
94         memcpy(t, expandedKey + (keySizeIterator - 4), 4 * sizeof(←
95             byte));
96 #if defined(debug) && debug == 1
97         std::cout << "temp: ";
98 #endif
99         for (byte j = 0; j < 4; j++)
100     {
101         expandedKey[keySizeIterator + j] = t[j] ^ expandedKey[←
102             keySizeIterator - this >_n + j];
103 #if defined(debug) && debug == 1
104             std::cout << (unsigned)expandedKey[keySizeIterator + j];
105 #endif
106     }
107
108 }
109
110 #if defined(debug) && debug == 1
111     int count = 0;
112     int roundNumber = 1;
113     std::cout << "Expanded Key: ";
114     for(byte i = 0; i < this >_b; i++){
115         if(count % 16 == 0)
116             std::cout << std::endl;
117
118         std::cout << std::hex << std::setfill('0') << std::setw(2) << ←
119             unsigned(expandedKey[i]);
120         count++;
121         roundNumber++;
122     }

```

```

122     std::cout << std::endl;
123     std::cout << "Key Expansion End" << std::endl;
124 #endif
125 }

```

### 3.1.1.1 AES Key Schedule Core

```

1 void AESImplementation::KeyExpansionCore(byte roundNumber, const byte ←
  keyIn[4], byte keyOut[4]){
2
3 #if defined(debug) && debug == 1
4     std::cout << "Key Expansion Core Start" << std::endl;
5
6     std::cout << "KEY OUT: ";
7
8     for(byte i = 0; i < 4; i++){
9         std::cout << std::hex << std::setfill('0') << std::setw(2) << ←
10        unsigned(keyOut[i]);
11    }
12    std::cout << std::endl;
13
14    std::cout << "KEY IN: ";
15
16    for(byte i = 0; i < 4; i++){
17        std::cout << std::hex << std::setfill('0') << std::setw(2) << ←
18        unsigned(keyIn[i]);
19    }
20    std::cout << std::endl;
21 #endif
22
23 /**
24 * Rotation Step
25 */
26 byte temp = keyOut[0];
27 for(byte i = 0; i < 3; i++){
28     keyOut[i] = keyOut[i+1];
29 }
30 keyOut[3] = temp;
31
32 #if defined(debug) && debug == 1
33     std::cout << "After Rotation: ";
34
35     for(byte i = 0; i < 4; i++){
36         std::cout << std::hex << std::setfill('0') << std::setw(2) << ←
37         unsigned(keyOut[i]);
38     }
39     std::cout << std::endl;
40 #endif

```

```

41 /**
42  * Substitution Step
43 */
44 for(byte i = 0; i < 4; i++){
45     keyOut[i] = sbox[keyOut[i]];
46 }
47
48 #if defined(debug) && debug == 1
49     std::cout << "After Substitution: ";
50     for(byte i = 0; i < 4; i++){
51         std::cout << std::hex << std::setfill('0') << std::setw(2) << ←
52             unsigned(keyOut[i]);
53     }
54     std::cout << std::endl;
55 #endif
56
57     keyOut[0] = keyOut[0] ^ rcon[roundNumber];
58
59 #if defined(debug) && debug == 1
60     std::cout << "After XOR With RCON: ";
61     for(byte i = 0; i < 4; i++){
62         std::cout << std::hex << std::setfill('0') << std::setw(2) << ←
63             unsigned(keyOut[i]);
64     }
65     std::cout << std::endl;
66
67     std::cout << "Key Expansion Core End" << std::endl;
68 #endif
69 }
```

### 3.1.2 AES Add Round Key

```

1 void AESImplementation::AddRoundKey(byte state[4][4], byte roundKey←
2 [4][4]) {
3     for(byte i = 0; i < 4; i++){
4         auto* key = reinterpret_cast<uint32_t *>(roundKey[i]);
5         auto* row_state = reinterpret_cast<uint32_t *>(state[i]);
6         *row_state ^= *key;
7     }
8     this->outputState("After Key Addition: ");
9 }
```

### 3.1.3 AES Substitute Bytes

```

1 void AESImplementation::SubBytes(byte state[4][4]) {
2     for(byte i = 0; i < 4; i++)
3         for(byte j = 0; j < 4; j++)
4             state[i][j] = sbox[state[i][j]];
5     this->outputState("After SubBytes: ");
6 }
```

6 }

### 3.1.4 AES Shift Rows

```
1 void AESImplementation::ShiftRows(byte state[4][4]) {
2     for(byte i = 1; i < 4; i++){
3         byte row[4];
4         for(byte j = 0; j < 4; j++)
5             row[j] = state[i][j];
6         for(byte j = 0; j < 4; j++)
7             state[i][j] = row[(i + j) % 4];
8     }
9     this->outputState("After ShiftRows: ");
10 }
```

### 3.1.5 AES Mix Columns

```
1 void AESImplementation::MixColumns(byte state[4][4]) {
2
3     for(byte i = 0; i < 4; i++){
4         byte column[4] = {state[0][i], state[1][i], state[2][i], state[3][i]};
5
6         state[0][i] = galois_mul_2[column[0]] ^ galois_mul_3[column[1]] ^ ←
7             column[2] ^ column[3];
8         state[1][i] = column[0] ^ galois_mul_2[column[1]] ^ galois_mul_3[←
9             column[2]] ^ column[3];
10        state[2][i] = column[0] ^ column[1] ^ galois_mul_2[column[2]] ^ ←
11            galois_mul_3[column[3]];
12        state[3][i] = galois_mul_3[column[0]] ^ column[1] ^ column[2] ^ ←
13            galois_mul_2[column[3]];
14    }
15    this->outputState("After MixColumns: ");
16 }
```

### 3.1.6 AES Inverse Substitute Bytes

```
1 void AESImplementation::InverseSubBytes(byte state[4][4]) {
2     for(byte i = 0; i < 4; i++)
3         for(byte j = 0; j < 4; j++)
4             state[i][j] = inverse_sbox[state[i][j]];
5     this->outputState("After InverseSubBytes: ");
6 }
```

### 3.1.7 AES Inverse Shift Rows

```

1 void AESImplementation::InverseShiftRows(byte state[4][4]) {
2     for(byte i = 1; i < 4; i++){
3         byte row[4];
4         for(byte j = 0; j < 4; j++){
5             row[j] = state[i][j];
6             for(int k = 3; k >= 0; k--) {
7                 state[i][k] = row[(k + (4 - i)) % 4];
8             }
9         }
10    this->outputState("After InverseShiftRows: ");
11 }
```

### 3.1.8 AES Inverse Mix Columns

```

1 void AESImplementation::InverseMixColumns(byte state[4][4]) {
2     for(byte i = 0; i < 4; i++){
3         byte column[4] = {state[0][i], state[1][i], state[2][i], state[3][i]};
4
5         state[0][i] = galois_mul_14[column[0]] ^ galois_mul_11[column[1]] ^
6             ^ galois_mul_13[column[2]] ^ galois_mul_9[column[3]];
7         state[1][i] = galois_mul_9[column[0]] ^ galois_mul_14[column[1]] ^
8             ^ galois_mul_11[column[2]] ^ galois_mul_13[column[3]];
9         state[2][i] = galois_mul_13[column[0]] ^ galois_mul_9[column[1]] ^
10            ^ galois_mul_14[column[2]] ^ galois_mul_11[column[3]];
11        state[3][i] = galois_mul_11[column[0]] ^ galois_mul_13[column[1]] ^
12            ^ galois_mul_9[column[2]] ^ galois_mul_14[column[3]];
13    }
14    this->outputState("After InverseMixColumns: ");
15 }
```

## 3.2 Web Application Implementation

### 3.2.1 Application Launcher

```

1 /**
2 * @brief This method returns a live instance of the web application
3 *
4 * @param env The current environment that the application is running from.
5 * @return An instance of the starter class which builds the initial running of the web app
6 */
7 std::unique_ptr<WApplication> createApplication(const WEnvironment& env)
```

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---

```
8  {
9      return cpp14::make_unique<CryptoOnlineLauncher>(env);
10 }
11
12 /**
13 * @brief The main function for the project.
14 * It created the server instance and configures it for the requirements ←
15 * of the project. It also handles any errors
16 * that may stop the flow of the program.
17 *
18 * @param argc The number of command line arguments
19 * @param argv The command line arguments that set the http listen ip and←
20 *             the port the server will run on. It also sets
21 *             the current working directory and the links to the necessary ←
22 *             directories that contain the style sheets and resources.
23 * @return
24 */
25 int main(int argc, char **argv)
26 {
27     try {
28         WServer server(argc, argv, WTHTTP_CONFIGURATION);
29
30         server.addEntryPoint(EntryPointType::Application, ←
31             createApplication);
32
33         Session::configureAuth();
34
35         if(server.start()){
36             Wt::WServer::waitForShutdown();
37             server.stop();
38         }
39
40     } catch (WServer::Exception& e) {
41         std::cerr << e.what() << std::endl;
42     } catch (std::exception &e) {
43         std::cerr << "exception: " << e.what() << std::endl;
44     }
45 }
```

### 3.2.1.1 Application Launcher Handling Class

```
1 /**
2 * @brief Constructor for the CryptoOnlineLauncher
3 * It loads the initial state including the theme, css files and message ←
4 * bundles
5 *
6 * @param environment current enviroment that the application is loaded ←
7 *                     with
8 */
9 CryptoOnlineLauncher::CryptoOnlineLauncher(const Wt::WEnvironment &←
10     environment)
11     : WApplication(environment), _session(appRoot() + "data.db") {
```

```

9  /**
10   * This section gets the current environment theme for the project. ←
11   * Then checks if the theme is set to bootstrap3,
12   * if it is then it sets the project theme to bootstrap3. If the ←
13   * environment theme is not set to bootstrap3 then
14   * It check if the theme is set to bootstrap2, if it is it then makes←
15   * that the theme. If the environment theme is
16   * neither then it just creates a shared WCssTheme and sets that to ←
17   * the theme.
18   */
19 const std::string *themePtr = environment.getParameter("theme");
20 std::string theme;
21 if (!themePtr)
22     theme = "bootstrap3";
23 else
24     theme = *themePtr;
25
26 if (theme == "bootstrap3") {
27     auto bootstrapTheme = std::make_shared<Wt::WBootstrapTheme>();
28     bootstrapTheme->setVersion(Wt::BootstrapVersion::v3);
29     bootstrapTheme->setResponsive(true);
30     this->setTheme(bootstrapTheme);
31
32     // load the default bootstrap3 (sub ) theme
33     this->useStyleSheet("resources/themes/bootstrap/3/bootstrap_theme←
34     .min.css");
35 } else if (theme == "bootstrap2") {
36     auto bootstrapTheme = std::make_shared<Wt::WBootstrapTheme>();
37     bootstrapTheme->setResponsive(true);
38     this->setTheme(bootstrapTheme);
39 } else
40     this->setTheme(std::make_shared<Wt::WCssTheme>(theme));
41
42 this->setTitle("Cryptology Online");
43
44 /**
45  * Load the initial settings of the website
46  */
47 this->root()->addWidget(Wt::cpp14::make_unique<CryptoOnlineHome>(<-
48     _session));
49 this->root()->setContentAlignment(Wt::AlignmentFlag::Center);
50 }

```

### 3.2.2 Creating the Header

#### 3.2.2.1 No User Logged in

```

1 /**
2  * @brief This method creates the header for the website when no user is ↵
3   * logged in
4 */
5 void CryptoOnlineHeader::create_navigation_bar() {
6     this >navigation_bar = Wt::cpp14::make_unique<Wt::WNavigationBar>();
7     this >navigation_bar >setTitle("Crypto Online", Wt::WLink(Wt::←
8         LinkType::InternalPath, "/home"));
9     this >navigation_bar >setResponsive(true);
10    this >navigation_bar >setStyleClass("navigation_bar_things");
11    this >navigation_bar >setMaximumSize(Wt::WLength::Auto, 50);
12
13    this >navigation_bar_contents_stack = this >addWidget(Wt::cpp14::←
14        make_unique<Wt::WStackedWidget>());
15    navigation_bar_contents_stack >addStyleClass("contents");
16
17    this >left_menu = Wt::cpp14::make_unique<Wt::WMenu>(this >←
18        navigation_bar_contents_stack);
19    auto left_menu_ = this >navigation_bar >addMenu(std::move(this >←
20        left_menu));
21    left_menu_ >addItem("Home") >setLink(Wt::WLink(Wt::LinkType::←
22        InternalPath, "/home"));
23    left_menu_ >addItem("Symmetric");
24    left_menu_ >addItem("Asymmetric");
25
26    this >right_menu = Wt::cpp14::make_unique<Wt::WMenu>();
27    auto right_menu_ = this >navigation_bar >addMenu(std::move(this >←
28        right_menu), Wt::AlignmentFlag::Right);
29    right_menu_ >addItem("Login / Register") >setLink(Wt::WLink(Wt::←
30        LinkType::InternalPath, "/login"));
31
32    this >addWidget(std::move(this >navigation_bar), 1);
33}

```

#### 3.2.2.2 A User is Logged in

```

1 /**
2  * @brief This method creates a header for when a user is logged in.
3  * It also handles whether or not the user is an admin and if that←
4   * user is then it gives them the
5   * option to go to admin settings.
6 */
7 void CryptoOnlineHeader::create_user_navigation_bar() {
8     this >navigation_bar = Wt::cpp14::make_unique<Wt::WNavigationBar>();
9     this >navigation_bar >setTitle("Crypto Online", Wt::WLink(Wt::←
10        LinkType::InternalPath, "/home"));
11    this >navigation_bar >setResponsive(true);
12
13    this >navigation_bar_contents_stack = this >addWidget(Wt::cpp14::←
14        make_unique<Wt::WStackedWidget>());
15    navigation_bar_contents_stack >addStyleClass("contents");
16
17    this >left_menu = Wt::cpp14::make_unique<Wt::WMenu>(this >←
18        navigation_bar_contents_stack);
19    auto left_menu_ = this >navigation_bar >addMenu(std::move(this >←
20        left_menu));
21    left_menu_ >addItem("Home") >setLink(Wt::WLink(Wt::LinkType::←
22        InternalPath, "/home"));
23    left_menu_ >addItem("Symmetric");
24    left_menu_ >addItem("Asymmetric");
25
26    this >right_menu = Wt::cpp14::make_unique<Wt::WMenu>();
27    auto right_menu_ = this >navigation_bar >addMenu(std::move(this >←
28        right_menu), Wt::AlignmentFlag::Right);
29    right_menu_ >addItem("Logout") >setLink(Wt::WLink(Wt::←
30        LinkType::InternalPath, "/logout"));
31
32    this >addWidget(std::move(this >navigation_bar), 1);
33}

```

```

10    this >navigation_bar >setStyleClass("navigation_bar_things");
11    this >navigation_bar >setMaximumSize(Wt::WLength::Auto, 50);
12
13    this >navigation_bar_contents_stack = this >addWidget(Wt::cpp14::make_unique<Wt::WStackedWidget>());
14    navigation_bar_contents_stack >addStyleClass("contents");
15
16    this >left_menu = Wt::cpp14::make_unique<Wt::WMENU>(this >navigation_bar_contents_stack);
17    auto left_menu_ = this >navigation_bar >addMenu(std::move(this >left_menu));
18    left_menu_ >addItem("Home") >setLink(Wt::WLink(Wt::LinkType::InternalPath, "/home"));
19
20    // Getting information on the current logged in user
21    const Wt::Auth::User& u = _current_session.login().user();
22    auto current_user = database_interface.get_user(u.id());
23
24    if(current_user >user_role == Role::Admin)
25        left_menu_ >addItem("Admin Settings") >setLink(Wt::WLink(Wt::LinkType::InternalPath, "admin"));
26
27    Wt::Dbo::Transaction transaction(_current_session);
28    auto username = left_menu_ >addItem("User Logged In: " + this >_current_session.user() >identity(Wt::Auth::Identity::LoginName));
29    username >disable();
30
31    this >right_menu = Wt::cpp14::make_unique<Wt::WMENU>();
32    auto right_menu_ = this >navigation_bar >addMenu(std::move(this >right_menu), Wt::AlignmentFlag::Right);
33    right_menu_ >addItem("Profile") >setLink(Wt::WLink(Wt::LinkType::InternalPath, "/profile"));
34    right_menu_ >addItem("Sign Out") >setLink(Wt::WLink(Wt::LinkType::InternalPath, "/signout"));
35
36    this >addWidget(std::move(this >navigation_bar), 1);
37 }

```

### 3.2.3 Initializing the Home Page

```

1 /**
2 * @brief Constructor for the CryptoOnlineHome class.
3 * The constructor handles the initial loading of the home page. It first calls the home page which contains the
4 * navigation grid to all the internal pages plus the profile stats and user information.
5 *
6 * It also handles the behaviour of the website when the internal path changes and correctly navigates to the
7 * appropriate page that the user has requested to navigate to.
8 */

```

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---

```
9 CryptoOnlineHome::CryptoOnlineHome(Session& session) : _current_session(↔
10   session),
11   database_interface(↔
12     session) {
13
14   load_home_page();
15   load_database();
16
17   this >handleInternalPath(Wt::WApplication::instance() >internalPath() ↔
18     );
19
20   Wt::WApplication::instance() >internalPathChanged()
21     .connect(this, &CryptoOnlineHome::handleInternalPath);
22 }
```

### 3.2.4 Handling Internal Path Changes

```
1 /**
2  * @brief This method handles any internal path changes to the ←
3  * application.
4  * It monitors for any change in the internal path and when it does ←
5  * change it calls the appropriate method to deal with
6  * internal path change.
7  *
8  * @param path The new internal path the application has changed to
9  */
10 void CryptoOnlineHome::handleInternalPath(const std::string &path) {
11
12   Wt::WApplication *app = Wt::WApplication::instance();
13
14   std::cout << "PATH CHANGED: " + path << std::endl;
15
16   if (path == "/home") {
17     load_home_page();
18   } else if (path == "/signout") {
19     _current_session.login().logout();
20     load_home_page();
21     app >setInternalPath("/home", true);
22   } else if (path == "/profile") {
23     load_profile_page();
24   } else if (path == "/login") {
25     load_login_page();
26     app >setInternalPath("/login", true);
27   } else if (path == "/symmetric/modular arithmetic") {
28     load_modular_arithmetic_page();
29   } else if (path == "/basics/concepts") {
30     load_intro_to_cryptography_page();
31   }
32   /*
33    * TODO: Add navigation to all parts of the website
34    */
35 }
```

```

34     Wt::WApplication::instance() >setInternalPath( "/home" , true );
35 }
```

### 3.2.5 Session Management

#### 3.2.5.1 Initialzing Session on Start-up of Application

```

1 /**
2  * @brief This method connects to the database file and maps the various ←
3   database classes to tables. It then checks if
4   *           the table exists and if it doesnt then it creates it. If it does←
5   then it just uses the existing database.
6  * @param sqliteDb
7  */
8 Session::Session(const std::string &sqliteDb) {
9     auto connection = Wt::cpp14::make_unique<Wt::Dbo::backend::Sqlite3>(←
10    sqliteDb);
11    connection >setProperty("show queries" , "true");
12    this >setConnection(std::move(connection));
13
14    this >mapClass<DbUser>"db_user");
15    this >mapClass<DbUserAnsweredQuestion>"user_answered_questions");
16    this >mapClass<DbQuestions>"questions");
17    this >mapClass<Wt::Auth::Dbo::AuthInfo<DbUser>>"auth_info");
18    this >mapClass<Wt::Auth::Dbo::AuthInfo<DbUser>>::AuthIdentityType>"←
19      auth_identity");
20    this >mapClass<Wt::Auth::Dbo::AuthInfo<DbUser>>::AuthTokenType>"←
21      auth_token");
22
23    std::cout << "Checking the Database Contents" << std::endl;
24    try {
25        this >createTables();
26        std::cerr << "Created Database" << std::endl;
27    }catch(Wt::Dbo::Exception &e){
28        std::cerr << e.what() << std::endl;
29        std::cerr << "Using Existing Database" << std::endl;
30    }
31    this >_users = Wt::cpp14::make_unique<Wt::Auth::Dbo::UserDatabase<Wt←
32      ::Auth::Dbo::AuthInfo<DbUser>>>(*this);
33 }
```

#### 3.2.5.2 Configuration of Authentication Services

```

1 /**
2  * @brief Setup the authentication for users to login through. This ←
3   includes setting passwords strength validators.
4  *           Adding throttlers to stop brute force attacks on password ←
5   attempts. Adding hashing to user passwords. It also
6  *           adds OAuth services like Google and Facebook 2.
```

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```
5 *           It also determines whether or not a user needs to provide an ←
6 *               email address and whether or not they need to
7 *                   prove they are real by activating their account by clicking an ←
8 *               authentication email.
9 */
10 void Session::configureAuth() {
11     myAuthService.setAuthTokensEnabled(true, "logincookie");
12     myAuthService.setEmailVerificationEnabled(true);
13     myAuthService.setEmailVerificationRequired(false);
14
15     std::unique_ptr<Wt::Auth::PasswordVerifier> verifier =
16         Wt::cpp14::make_unique<Wt::Auth::PasswordVerifier>();
17     verifier >addHashFunction(Wt::cpp14::make_unique<Wt::Auth::←
18         BCryptHashFunction>(7));
19     myPasswordService.setVerifier(std::move(verifier));
20     myPasswordService.setAttemptThrottlingEnabled(true);
21     myPasswordService.setStrengthValidator(Wt::cpp14::make_unique<Wt::←
22         Auth::PasswordStrengthValidator>());
23
24     if (Wt::Auth::GoogleService::configured()) {
25         std::cout << "GOOGLE SERVICE CONFIGURED" << std::endl;
26         myOAuth.push_back(Wt::cpp14::make_unique<Wt::Auth::GoogleService←
27             >(myAuthService));
28     }
29
30     if (Wt::Auth::FacebookService::configured())
31         myOAuth.push_back(Wt::cpp14::make_unique<Wt::Auth::←
32             FacebookService>(myAuthService));
33
34     for (unsigned i = 0; i < myOAuth.size(); i++)
35         myOAuth[i] >generateRedirectEndpoint();
36 }
```

### 3.2.5.3 Getting Auth Information on Logged in User

```
1 /**
2  * @return The AuthInfo about the current user logged in
3 */
4 Wt::Dbo::ptr<AuthInfo> Session::user() {
5     if (_login.loggedIn()){
6         Wt::Dbo::ptr<AuthInfo> authInfo = _users >find(_login.user());
7         return authInfo;
8     }else{
9         return Wt::Dbo::ptr<AuthInfo>();
10    }
11 }
```

### 3.2.5.4 Registering a New User

```

1 /**
2 * @brief This method handles the registration of a new user
3 *       It is called during a transaction
4 *
5 * @param user The new user that just registered on the site
6 */
7 void Session::new_registered_user(Wt::Auth::User &user) {
8     auto authInfo{_users >find(user)};
9     auto foundUser{authInfo >user()};
10
11    if (!foundUser){
12        foundUser = this >add(Wt::cpp14::make_unique<DbUser>());
13        authInfo.modify() >setUser(foundUser);
14    }
15}

```

### 3.2.5.5 Linking Logged in User to User Database

```

1 /**
2 * First we check if the user exists in the db_user table and if not we ←
3 * then
4 * add to the table. If they do already exist this method exits
5 *
6 * @param user The user we are linking to the user database
7 */
8 void Session::link_account_to_database(const Wt::Auth::User& user) {
9     std::cout << "Link Account Called" << std::endl;
10    if (!this >does_user_exist_in_dbuser(user)){
11        std::cout << "Adding user to the db_user database" << std::endl;
12        Wt::Dbo::Transaction transaction(*this);
13
14        std::unique_ptr<DbUser> new_user{new DbUser()};
15        new_user >user_id = std::stoi(user.id());
16        new_user >user_identity = user.identity(Wt::Auth::Identity::←
17            LoginName);
18        new_user >user_role = Role::User;
19
20        Wt::Dbo::ptr<DbUser> userPtr = (*this).add(std::move(new_user));
21    }

```

### 3.2.5.6 Checking if a User already exists in the User Database

```

1 /**
2 * @brief This methods gets given a User and then goes through the ←
3 *       db_user table to check to see if that user
4 *       already exists and does not need to be added.

```

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---

```
5 * @param user The user we are looking for in the db_user table
6 * @return True if the user exists in the db_user table. False if the user
7 does not
8 */
9 bool Session::does_user_exist_in_dbuser(const Wt::Auth::User &user) {
10
11     Wt::Dbo::Transaction transaction(*this);
12     const std::string& looking_for_this_id = user.id();
13
14     std::cout << "Checking for a User with ID: " << looking_for_this_id <<
15         std::endl;
16
17     Wt::Dbo::collection< Wt::Dbo::ptr<DbUser> > all_users = this->find<<
18         DbUser>();
19
20     if (!all_users.empty()) {
21         for(const Wt::Dbo::ptr<DbUser>& current_user : all_users){
22             long long int id = current_user.id();
23             std::cout << "Identity: " << id << std::endl;
24             if(std::to_string(id) == looking_for_this_id) {
25                 std::cout << "User already exists in Database" << std::endl;
26                 return true;
27             }
28         }
29     }
30 }
```

### 3.2.6 Database API

#### 3.2.6.1 Getting User Information from the Database

```
1 /**
2 * @brief This method gets given an id for a user and then searches
3 through the DbUser table for the user with that id.
4 * If it finds a user with that id then it returns a Wt::Dbo::ptr<<
5     DbUser> object containing all the information
6 * on that user. If it does not find the user it does nothing.
7 *
8 * @param looking_for_id The id of the user we are looking for
9 * @return The user in db_user with id == looking for id
10 */
11 Wt::Dbo::ptr<DbUser> db_interface::get_user(std::string looking_for_id) {
12
13     std::cerr << "Getting Information for User with ID(" <<
14         looking_for_id << ")" << std::endl;
15
16     Wt::Dbo::Transaction transaction(current_session);
```

```
15     std::cerr << "Getting all user data from the DbUser table" << std::endl;
16     Wt::Dbo::collection< Wt::Dbo::ptr<DbUser> > all_users = ↵
17         current_session.find<DbUser>();
18
19     if (!all_users.empty()){
20         std::cerr << "DbUser Table is not Empty" << std::endl;
21         for(const Wt::Dbo::ptr<DbUser>& current_user : all_users){
22             long long int id = current_user.id();
23             std::cout << "Identity: " << id << std::endl;
24             if(std::to_string(id) == looking_for_id)
25                 return current_user;
26         }
27 }
```

---

# **Chapter 4**

## **Testing**

### **4.1 The Web Application**

### **4.2 AES Implementation**

My AES Implementation has been tested against the Federal Information Processing Standard Publication 197 (FIPS 197) test vectors. All test vectors use hexadecimal notation.

#### **4.2.1 AES-128**

$Nk=4$ ,  $Nr=10$

Plaintext = 00112233445566778899aabcccddeeff

Key = 000102030405060708090a0b0c0d0e0f

##### **4.2.1.1 Cipher (ENCRYPT)**

round[ 0].input	00112233445566778899aabcccddeeff
round[ 0].k_sch	000102030405060708090a0b0c0d0e0f
round[ 1].start	00102030405060708090a0b0c0d0e0f0
round[ 1].s_box	63cab7040953d051cd60e0e7ba70e18c
round[ 1].s_row	6353e08c0960e104cd70b751bacad0e7
round[ 1].m_col	5f72641557f5bc92f7be3b291db9f91a
round[ 1].k_sch	d6aa74fdd2af72fadaa678f1d6ab76fe
round[ 2].start	89d810e8855ace682d1843d8cb128fe4
round[ 2].s_box	a761ca9b97be8b45d8ad1a611fc97369
round[ 2].s_row	a7be1a6997ad739bd8c9ca451f618b61
round[ 2].m_col	ff87968431d86a51645151fa773ad009
round[ 2].k_sch	b692cf0b643dbdf1be9bc5006830b3fe
round[ 3].start	4915598f55e5d7a0daca94fa1f0a63f7
round[ 3].s_box	b59cb73fcd90ee05774222dc067fb68
round[ 3].s_row	3bd92268fc74fb735767cbe0c0590e2d

round[ 3].m_col	4c9c1e66f771f0762c3f868e534df256
round[ 3].k_sch	b6ff744ed2c2c9bf6c590cbf0469bf41
round[ 4].start	fa636a2825b339c940668a3157244d17
round[ 4].s_box	2dfb02343f6d12dd09337ec75b36e3f0
round[ 4].s_row	2d6d7ef03f33e334093602dd5bfb12c7
round[ 4].m_col	6385b79ffc538df997be478e7547d691
round[ 4].k_sch	47f7f7bc95353e03f96c32bcfd058dfd
round[ 5].start	247240236966b3fa6ed2753288425b6c
round[ 5].s_box	36400926f9336d2d9fb59d23c42c3950
round[ 5].s_row	36339d50f9b539269f2c092dc4406d23
round[ 5].m_col	f4bcd45432e554d075f1d6c51dd03b3c
round[ 5].k_sch	3caaa3e8a99f9deb50f3af57adf622aa
round[ 6].start	c81677bc9b7ac93b25027992b0261996
round[ 6].s_box	e847f56514dadde23f77b64fe7f7d490
round[ 6].s_row	e8dab6901477d4653ff7f5e2e747dd4f
round[ 6].m_col	9816ee7400f87f556b2c049c8e5ad036
round[ 6].k_sch	5e390f7df7a69296a7553dc10aa31f6b
round[ 7].start	c62fe109f75eedc3cc79395d84f9cf5d
round[ 7].s_box	b415f8016858552e4bb6124c5f998a4c
round[ 7].s_row	b458124c68b68a014b99f82e5f15554c
round[ 7].m_col	c57e1c159a9bd286f05f4be098c63439
round[ 7].k_sch	14f9701ae35fe28c440adf4d4ea9c026
round[ 8].start	d1876c0f79c4300ab45594add66ff41f
round[ 8].s_box	3e175076b61c04678dfc2295f6a8bfc0
round[ 8].s_row	3e1c22c0b6fcbf768da85067f6170495
round[ 8].m_col	baa03de7a1f9b56ed5512cba5f414d23
round[ 8].k_sch	47438735a41c65b9e016baf4aebf7ad2
round[ 9].start	fde3bad205e5d0d73547964ef1fe37f1
round[ 9].s_box	5411f4b56bd9700e96a0902fa1bb9aa1
round[ 9].s_row	54d990a16ba09ab596bbf40ea111702f
round[ 9].m_col	e9f74eec023020f61bf2ccf2353c21c7
round[ 9].k_sch	549932d1f08557681093ed9cbe2c974e
round[10].start	bd6e7c3df2b5779e0b61216e8b10b689
round[10].s_box	7a9f102789d5f50b2beffd9f3dca4ea7
round[10].s_row	7ad5fda789ef4e272bca100b3d9ff59f
round[10].k_sch	13111d7fe3944a17f307a78b4d2b30c5
round[10].output	69c4e0d86a7b0430d8cdb78070b4c55a

#### 4.2.1.2 Inverse Cipher (DECRYPT)

round[ 0].iinput	69c4e0d86a7b0430d8cdb78070b4c55a
round[ 0].ik_sch	13111d7fe3944a17f307a78b4d2b30c5

round[ 1].istart	7ad5fda789ef4e272bca100b3d9ff59f
round[ 1].is_box	bdb52189f261b63d0b107c9e8b6e776e
round[ 1].is_row	bd6e7c3df2b5779e0b61216e8b10b689
round[ 1].im_col	4773b91ff72f354361cb018ea1e6cf2c
round[ 1].ik_sch	13aa29be9c8faff6f770f58000f7bf03
round[ 2].istart	54d990a16ba09ab596bbf40ea111702f
round[ 2].is_box	fde596f1054737d235febad7f1e3d04e
round[ 2].is_row	fde3bad205e5d0d73547964ef1fe37f1
round[ 2].im_col	2d7e86a339d9393ee6570a1101904e16
round[ 2].ik_sch	1362a4638f2586486bff5a76f7874a83
round[ 3].istart	3e1c22c0b6fcfb768da85067f6170495
round[ 3].is_box	d1c4941f7955f40fb46f6c0ad68730ad
round[ 3].is_row	d1876c0f79c4300ab45594add66ff41f
round[ 3].im_col	39daee38f4f1a82aab432410c36d45b9
round[ 3].ik_sch	8d82fc749c47222be4dadc3e9c7810f5
round[ 4].istart	b458124c68b68a014b99f82e5f15554c
round[ 4].is_box	c65e395df779cf09ccf9e1c3842fed5d
round[ 4].is_row	c62fe109f75eedc3cc79395d84f9cf5d
round[ 4].im_col	9a39bf1d05b20a3a476a0bf79fe51184
round[ 4].ik_sch	72e3098d11c5de5f789dfe1578a2ccb
round[ 5].istart	e8dab6901477d4653ff7f5e2e747dd4f
round[ 5].is_box	c87a79969b0219bc2526773bb016c992
round[ 5].is_row	c81677bc9b7ac93b25027992b0261996
round[ 5].im_col	18f78d779a93eef4f6742967c47f5fd
round[ 5].ik_sch	2ec410276326d7d26958204a003f32de
round[ 6].istart	36339d50f9b539269f2c092dc4406d23
round[ 6].is_box	2466756c69d25b236e4240fa8872b332
round[ 6].is_row	247240236966b3fa6ed2753288425b6c
round[ 6].im_col	85cf8bf472d124c10348f545329c0053
round[ 6].ik_sch	a8a2f5044de2c7f50a7ef79869671294
round[ 7].istart	2d6d7ef03f33e334093602dd5bfb12c7
round[ 7].is_box	fab38a1725664d2840246ac957633931
round[ 7].is_row	fa636a2825b339c940668a3157244d17
round[ 7].im_col	fc1fc1f91934c98210fbfb8da340eb21
round[ 7].ik_sch	c7c6e391e54032f1479c306d6319e50c
round[ 8].istart	3bd92268fc74fb735767cbe0c0590e2d
round[ 8].is_box	49e594f755ca638fda0a59a01f15d7fa
round[ 8].is_row	4915598f55e5d7a0dac94fa1f0a63f7
round[ 8].im_col	076518f0b52ba2fb7a15c8d93be45e00
round[ 8].ik_sch	a0db02992286d160a2dc029c2485d561
round[ 9].istart	a7be1a6997ad739bd8c9ca451f618b61
round[ 9].is_box	895a43e485188fe82d121068cbd8ced8
round[ 9].is_row	89d810e8855ace682d1843d8cb128fe4
round[ 9].im_col	ef053f7c8b3d32fd4d2a64ad3c93071a

round[ 9].ik_sch	8c56dff0825dd3f9805ad3fc8659d7fd
round[10].istart	6353e08c0960e104cd70b751bacad0e7
round[10].is_box	0050a0f04090e03080d02070c01060b0
round[10].is_row	00102030405060708090a0b0c0d0e0f0
round[10].ik_sch	000102030405060708090a0b0c0d0e0f
round[10].ioutput	00112233445566778899aabbccddeeff

## 4.2.2 AES-192

$Nk=6, Nr=12$

Plaintext = 00112233445566778899aabccddeeff

Key = 000102030405060708090a0b0c0d0e0f1011121314151617

### 4.2.2.1 Cipher (ENCRYPT)

round[ 0].input	00112233445566778899aabccddeeff
round[ 0].k_sch	000102030405060708090a0b0c0d0e0f
round[ 1].start	00102030405060708090a0b0c0d0e0f0
round[ 1].s_box	63cab7040953d051cd60e0e7ba70e18c
round[ 1].s_row	6353e08c0960e104cd70b751bacad0e7
round[ 1].m_col	5f72641557f5bc92f7be3b291db9f91a
round[ 1].k_sch	10111213141516175846f2f95c43f4fe
round[ 2].start	4f63760643e0aa85aff8c9d041fa0de4
round[ 2].s_box	84fb386f1ae1ac977941dd70832dd769
round[ 2].s_row	84e1dd691a41d76f792d389783fbac70
round[ 2].m_col	9f487f794f955f662afc86abd7f1ab29
round[ 2].k_sch	544afef55847f0fa4856e2e95c43f4fe
round[ 3].start	cb02818c17d2af9c62aa64428bb25fd7
round[ 3].s_box	1f770c64f0b579deaaac432c3d37cf0e
round[ 3].s_row	1fb5430ef0accf64aa370cde3d77792c
round[ 3].m_col	b7a53ecbbf9d75a0c40efc79b674cc11
round[ 3].k_sch	40f949b31cbabd4d48f043b810b7b342
round[ 4].start	f75c7778a327c8ed8cfefc1a6c37f53
round[ 4].s_box	684af5bc0acce85564bb0878242ed2ed
round[ 4].s_row	68cc08ed0abbd2bc642ef555244ae878
round[ 4].m_col	7a1e98bdacb6d1141a6944dd06eb2d3e
round[ 4].k_sch	58e151ab04a2a5557effb5416245080c
round[ 5].start	22ffc916a81474416496f19c64ae2532
round[ 5].s_box	9316dd47c2fa92834390a1de43e43f23
round[ 5].s_row	93faa123c2903f4743e4dd83431692de
round[ 5].m_col	aaa755b34cff57cef6f98e1f01c13e6
round[ 5].k_sch	2ab54bb43a02f8f662e3a95d66410c08
round[ 6].start	80121e0776fd1d8a8d8c31bc965d1fee
round[ 6].s_box	cdc972c53854a47e5d64c765904cc028
round[ 6].s_row	cd54c7283864c0c55d4c727e90c9a465
round[ 6].m_col	921f748fd96e937d622d7725ba8ba50c
round[ 6].k_sch	f501857297448d7ebdf1c6ca87f33e3c
round[ 7].start	671ef1fd4e2a1e03dfdcb1ef3d789b30
round[ 7].s_box	8572a1542fe5727b9e86c8df27bc1404
round[ 7].s_row	85e5c8042f8614549ebca17b277272df
round[ 7].m_col	e913e7b18f507d4b227ef652758acbcc
round[ 7].k_sch	e510976183519b6934157c9ea351f1e0

round[ 8].start	0c0370d00c01e622166b8accd6db3a2c
round[ 8].s_box	fe7b5170fe7c8e93477f7e4bf6b98071
round[ 8].s_row	fe7c7e71fe7f807047b95193f67b8e4b
round[ 8].m_col	6cf5edf996eb0a069c4ef21cbfc25762
round[ 8].k_sch	1ea0372a995309167c439e77ff12051e
round[ 9].start	7255dad30fb80310e00d6c6b40d0527c
round[ 9].s_box	40fc5766766c7bcae1d7507f09700010
round[ 9].s_row	406c501076d70066e17057ca09fc7b7f
round[ 9].m_col	7478bcdce8a50b81d4327a9009188262
round[ 9].k_sch	dd7e0e887e2fff68608fc842f9dcc154
round[10].start	a906b254968af4e9b4bdb2d2f0c44336
round[10].s_box	d36f3720907ebf1e8d7a37b58c1c1a05
round[10].s_row	d37e3705907a1a208d1c371e8c6fbfb5
round[10].m_col	0d73cc2d8f6abe8b0cf2dd9bb83d422e
round[10].k_sch	859f5f237a8d5a3dc0c02952beefd63a
round[11].start	88ec930ef5e7e4b6cc32f4c906d29414
round[11].s_box	c4cedcab694694e4b23bfdd6fb522fa
round[11].s_row	c494bffae62322ab4bb5dc4e6fce69dd
round[11].m_col	71d720933b6d677dc00b8f28238e0fb7
round[11].k_sch	de601e7827bcdf2ca223800fd8aeda32
round[12].start	afb73eeb1cd1b85162280f27fb20d585
round[12].s_box	79a9b2e99c3e6cd1aa3476cc0fb70397
round[12].s_row	793e76979c3403e9aab7b2d10fa96ccc

#### 4.2.2.2 Inverse Cipher (DECRYPTION)

round[ 0].iinput	dda97ca4864cdfe06eaf70a0ec0d7191
round[ 0].ik_sch	a4970a331a78dc09c418c271e3a41d5d
round[ 1].istart	793e76979c3403e9aab7b2d10fa96ccc
round[ 1].is_box	afd10f851c28d5eb62203e51fb7b827
round[ 1].is_row	afb73eeb1cd1b85162280f27fb20d585
round[ 1].im_col	122a02f7242ac8e20605afce51cc7264
round[ 1].ik_sch	d6beb0dc209ea494db073803e021bb9
round[ 2].istart	c494bffae62322ab4bb5dc4e6fce69dd
round[ 2].is_box	88e7f414f532940eccd293b606ece4c9
round[ 2].is_row	88ec930ef5e7e4b6cc32f4c906d29414
round[ 2].im_col	5cc7aecce3c872194ae5ef8309a933c7
round[ 2].ik_sch	8fb999c973b26839c7f9d89d85c68c72
round[ 3].istart	d37e3705907a1a208d1c371e8c6fbfb5
round[ 3].is_box	a98ab23696bd4354b4c4b2e9f006f4d2
round[ 3].is_row	a906b254968af4e9b4bdb2d2f0c44336
round[ 3].im_col	b7113ed134e85489b20866b51d4b2c3b

round[ 3].ik_sch	f77d6ec1423f54ef5378317f14b75744
round[ 4].istart	406c501076d70066e17057ca09fc7b7f
round[ 4].is_box	72b86c7c0f0d52d3e0d0da104055036b
round[ 4].is_row	7255dad30fb80310e00d6c6b40d0527c
round[ 4].im_col	ef3b1be1b9b0e64bdcb79f1e0a707fb
round[ 4].ik_sch	1147659047cf663b9b0ece8dfc0bf1f0
round[ 5].istart	fe7c7e71fe7f807047b95193f67b8e4b
round[ 5].is_box	0c018a2c0c6b3ad016db7022d603e6cc
round[ 5].is_row	0c0370d00c01e622166b8accd6db3a2c
round[ 5].im_col	592460b248832b2952e0b831923048f1
round[ 5].ik_sch	dcc1a8b667053f7dcc5c194ab5423a2e
round[ 6].istart	85e5c8042f8614549ebca17b277272df
round[ 6].is_box	672ab1304edc9bfdd78f1033d1e1ee
round[ 6].is_row	671ef1fd4e2a1e03dfdc1ef3d789b30
round[ 6].im_col	0b8a7783417ae3a1f9492dc0c641a7ce
round[ 6].ik_sch	c6deb0ab791e2364a4055fbe568803ab
round[ 7].istart	cd54c7283864c0c55d4c727e90c9a465
round[ 7].is_box	80fd31ee768c1f078d5d1e8a96121dbc
round[ 7].is_row	80121e0776fd1d8a8d8c31bc965d1fee
round[ 7].im_col	4ee1ddf9301d6352c9ad769ef8d20515
round[ 7].ik_sch	dd1b7cdaf28d5c158a49ab1dbbc497cb
round[ 8].istart	93faa123c2903f4743e4dd83431692de
round[ 8].is_box	2214f132a896251664aec94164ff749c
round[ 8].is_row	22ffc916a81474416496f19c64ae2532
round[ 8].im_col	1008ffe53b36ee6af27b42549b8a7bb7
round[ 8].ik_sch	78c4f708318d3cd69655b701bfc093cf
round[ 9].istart	68cc08ed0abbd2bc642ef555244ae878
round[ 9].is_box	f727bf53a3fe7f788cc377eda65cc8c1
round[ 9].is_row	f75c7778a327c8ed8cfebfc1a6c37f53
round[ 9].im_col	7f69ac1ed939ebaac8ece3cb12e159e3
round[ 9].ik_sch	60dcef10299524ce62dbef152f9620cf
round[10].istart	1fb5430ef0accf64aa370cde3d77792c
round[10].is_box	cbd264d717aa5f8c62b2819c8b02af42
round[10].is_row	cb02818c17d2af9c62aa64428bb25fd7
round[10].im_col	cfaf16b2570c18b52e7fef50cab267ae
round[10].ik_sch	4b4ecbdb4d4dcfda5752d7c74949cbde
round[11].istart	84e1dd691a41d76f792d389783fbac70
round[11].is_box	4fe0c9e443f80d06affa76854163aad0
round[11].is_row	4f63760643e0aa85aff8c9d041fa0de4
round[11].im_col	794cf891177bfd1d8a327086f3831b39
round[11].ik_sch	1a1f181d1e1b1c194742c7d74949cbde
round[12].istart	6353e08c0960e104cd70b751bacad0e7
round[12].is_box	0050a0f04090e03080d02070c01060b0
round[12].is_row	00102030405060708090a0b0c0d0e0f0

round[12].ik_sch	000102030405060708090a0b0c0d0e0f
round[12].ioutput	00112233445566778899aabbccddeeff

### 4.2.3 AES-256

$Nk=8$ ,  $Nr=14$

Plaintext = 00112233445566778899aabcccddeeff

Key = 000102030405060708090a0b0c0d0e0f101112131415161718191a1b1c1d1e1f

#### 4.2.3.1 Cipher (ENCRYPT)

round[ 0].input	00112233445566778899aabcccddeeff
round[ 0].k_sch	000102030405060708090a0b0c0d0e0f
round[ 1].start	00102030405060708090a0b0c0d0e0f0
round[ 1].s_box	63cab7040953d051cd60e0e7ba70e18c
round[ 1].s_row	6353e08c0960e104cd70b751bacad0e7
round[ 1].m_col	5f72641557f5bc92f7be3b291db9f91a
round[ 1].k_sch	101112131415161718191a1b1c1d1e1f
round[ 2].start	4f63760643e0aa85efa7213201a4e705
round[ 2].s_box	84fb386f1ae1ac97df5cf237c49946b
round[ 2].s_row	84e1fd6b1a5c946fdf4938977cfbac23
round[ 2].m_col	bd2a395d2b6ac438d192443e615da195
round[ 2].k_sch	a573c29fa176c498a97fce93a572c09c
round[ 3].start	1859fbc28a1c00a078ed8aadc42f6109
round[ 3].s_box	adcb0f257e9c63e0bc557e951c15ef01
round[ 3].s_row	ad9c7e017e55ef25bc150fe01ccb6395
round[ 3].m_col	810dce0cc9db8172b3678c1e88a1b5bd
round[ 3].k_sch	1651a8cd0244beda1a5da4c10640bade
round[ 4].start	975c66c1cb9f3fa8a93a28df8ee10f63
round[ 4].s_box	884a33781fdb75c2d380349e19f876fb
round[ 4].s_row	88db34fb1f807678d3f833c2194a759e
round[ 4].m_col	b2822d81abe6fb275faf103a078c0033
round[ 4].k_sch	ae87dff00ff11b68a68ed5fb03fc1567
round[ 5].start	1c05f271a417e04ff921c5c104701554
round[ 5].s_box	9c6b89a349f0e18499fda678f2515920
round[ 5].s_row	9cf0a62049fd59a399518984f26be178
round[ 5].m_col	aeb65ba974e0f822d73f567bdb64c877
round[ 5].k_sch	6de1f1486fa54f9275f8eb5373b8518d
round[ 6].start	c357aae11b45b7b0a2c7bd28a8dc99fa
round[ 6].s_box	2e5bacf8af6ea9e73ac67a34c286ee2d
round[ 6].s_row	2e6e7a2dafc6eef83a86ace7c25ba934
round[ 6].m_col	b951c33c02e9bd29ae25cdb1efa08cc7
round[ 6].k_sch	c656827fc9a799176f294cec6cd5598b
round[ 7].start	7f074143cb4e243ec10c815d8375d54c
round[ 7].s_box	d2c5831a1f2f36b278fe0c4cec9d0329
round[ 7].s_row	d22f0c291ffe031a789d83b2ecc5364c
round[ 7].m_col	ebb19e1c3ee7c9e87d7535e9ed6b9144
round[ 7].k_sch	3de23a75524775e727bf9eb45407cf39

round[ 8].start	d653a4696ca0bc0f5acaab5db96c5e7d
round[ 8].s_box	f6ed49f950e06576be74624c565058ff
round[ 8].s_row	f6e062ff507458f9be50497656ed654c
round[ 8].m_col	5174c8669da98435a8b3e62ca974a5ea
round[ 8].k_sch	0bdc905fc27b0948ad5245a4c1871c2f
round[ 9].start	5aa858395fd28d7d05e1a38868f3b9c5
round[ 9].s_box	bec26a12cfb55dff6bf80ac4450d56a6
round[ 9].s_row	beb50aa6cff856126b0d6aff45c25dc4
round[ 9].m_col	0f77ee31d2ccadc05430a83f4ef96ac3
round[ 9].k_sch	45f5a66017b2d387300d4d33640a820a
round[10].start	4a824851c57e7e47643de50c2af3e8c9
round[10].s_box	d61352d1a6f3f3a04327d9fee50d9bdd
round[10].s_row	d6f3d9dda6279bd1430d52a0e513f3fe
round[10].m_col	bd86f0ea748fc4f4630f11c1e9331233
round[10].k_sch	7ccff71cbeb4fe5413e6bbf0d261a7df
round[11].start	c14907f6ca3b3aa070e9aa313b52b5ec
round[11].s_box	783bc54274e280e0511eacc7e200d5ce
round[11].s_row	78e2acce741ed5425100c5e0e23b80c7
round[11].m_col	af8690415d6e1dd387e5fbedd5c89013
round[11].k_sch	f01afafee7a82979d7a5644ab3afe640
round[12].start	5f9c6abfbac634aa50409fa766677653
round[12].s_box	cfde0208f4b418ac5309db5c338538ed
round[12].s_row	cfb4dbedf4093808538502ac33de185c
round[12].m_col	7427fae4d8a695269ce83d315be0392b
round[12].k_sch	2541fe719bf500258813bbd55a721c0a
round[13].start	516604954353950314fb86e401922521
round[13].s_box	d133f22a1aed2a7bfa0f44697c4f3ffd
round[13].s_row	d1ed44fd1a0f3f2afa4ff27b7c332a69
round[13].m_col	2c21a820306f154ab712c75eee0da04f
round[13].k_sch	4e5a6699a9f24fe07e572baacdf8cdea
round[14].start	627bceb9999d5aaac945ecf423f56da5
round[14].s_box	aa218b56ee5ebeacdd6ecebf26e63c06
round[14].s_row	aa5ece06ee6e3c56dde68bac2621bebf
round[14].k_sch	24fc79ccbf0979e9371ac23c6d68de36
round[14].output	8ea2b7ca516745bfeafc49904b496089

#### 4.2.3.2 Inverse Cipher (DECRYPT)

round[ 0].iinput	8ea2b7ca516745bfeafc49904b496089
round[ 0].ik_sch	24fc79ccbf0979e9371ac23c6d68de36
round[ 1].istart	aa5ece06ee6e3c56dde68bac2621bebf
round[ 1].is_box	629deca599456db9c9f5ceaa237b5af4

round[ 1].is_row	627bceb9999d5aaac945ecf423f56da5
round[ 1].im_col	e51c9502a5c1950506a61024596b2b07
round[ 1].ik_sch	34f1d1ffbfceaa2ffce9e25f2558016e
round[ 2].istart	d1ed44fd1a0f3f2afa4ff27b7c332a69
round[ 2].is_box	5153862143fb259514920403016695e4
round[ 2].is_row	516604954353950314fb86e401922521
round[ 2].im_col	91a29306cc450d0226f4b5eaef5efed8
round[ 2].ik_sch	5e1648eb384c350a7571b746dc80e684
round[ 3].istart	cfb4dbedf4093808538502ac33de185c
round[ 3].is_box	5fc69f53ba4076bf50676aaa669c34a7
round[ 3].is_row	5f9c6abfbac634aa50409fa766677653
round[ 3].im_col	b041a94eff21ae9212278d903b8a63f6
round[ 3].ik_sch	c8a305808b3f7bd043274870d9b1e331
round[ 4].istart	78e2acce741ed5425100c5e0e23b80c7
round[ 4].is_box	c13baaeccae9b5f6705207a03b493a31
round[ 4].is_row	c14907f6ca3b3aa070e9aa313b52b5ec
round[ 4].im_col	638357cec07de6300e30d0ec4ce2a23c
round[ 4].ik_sch	b5708e13665a7de14d3d824ca9f151c2
round[ 5].istart	d6f3d9dda6279bd1430d52a0e513f3fe
round[ 5].is_box	4a7ee5c9c53de85164f348472a827e0c
round[ 5].is_row	4a824851c57e7e47643de50c2af3e8c9
round[ 5].im_col	ca6f71058c642842a315595fdf54f685
round[ 5].ik_sch	74da7ba3439c7e50c81833a09a96ab41
round[ 6].istart	beb50aa6cff856126b0d6aff45c25dc4
round[ 6].is_box	5ad2a3c55fe1b93905f3587d68a88d88
round[ 6].is_row	5aa858395fd28d7d05e1a38868f3b9c5
round[ 6].im_col	ca46f5ea835eab0b9537b6dbb221b6c2
round[ 6].ik_sch	3ca69715d32af3f22b67ffade4ccd38e
round[ 7].istart	f6e062ff507458f9be50497656ed654c
round[ 7].is_box	d6a0ab7d6cca5e695a6ca40fb953bc5d
round[ 7].is_row	d653a4696ca0bc0f5acaab5db96c5e7d
round[ 7].im_col	2a70c8da28b806e9f319ce42be4baead
round[ 7].ik_sch	f85fc4f3374605f38b844df0528e98e1
round[ 8].istart	d22f0c291ffe031a789d83b2ecc5364c
round[ 8].is_box	7f4e814ccb0cd543c175413e8307245d
round[ 8].is_row	7f074143cb4e243ec10c815d8375d54c
round[ 8].im_col	f0073ab7404a8a1fc2cba0b80df08517
round[ 8].ik_sch	de69409aef8c64e7f84d0c5fcfab2c23
round[ 9].istart	2e6e7a2dafc6eef83a86ace7c25ba934
round[ 9].is_box	c345bdffa1bc799e1a2dcaab0a857b728
round[ 9].is_row	c357aae11b45b7b0a2c7bd28a8dc99fa
round[ 9].im_col	3225fe3686e498a32593c1872b613469
round[ 9].ik_sch	aed55816cf19c100bcc24803d90ad511
round[10].istart	9cf0a62049fd59a399518984f26be178

round[10].is_box	1c17c554a4211571f970f24f0405e0c1
round[10].is_row	1c05f271a417e04ff921c5c104701554
round[10].im_col	9d1d5c462e655205c4395b7a2eac55e2
round[10].ik_sch	15c668bd31e5247d17c168b837e6207c
round[11].istart	88db34fb1f807678d3f833c2194a759e
round[11].is_box	979f2863cb3a0fc1a9e166a88e5c3fdf
round[11].is_row	975c66c1cb9f3fa8a93a28df8ee10f63
round[11].im_col	d24bfb0e1f997633cfce86e37903fe87
round[11].ik_sch	7fd7850f61cc991673db890365c89d12
round[12].istart	ad9c7e017e55ef25bc150fe01ccb6395
round[12].is_box	181c8a098aed61c2782ffba0c45900ad
round[12].is_row	1859fbc28a1c00a078ed8aadc42f6109
round[12].im_col	aec9bda23e7fd8aff96d74525cdce4e7
round[12].ik_sch	2a2840c924234cc026244cc5202748c4
round[13].istart	84e1fd6b1a5c946fdf4938977cfbac23
round[13].is_box	4fe0210543a7e706efa476850163aa32
round[13].is_row	4f63760643e0aa85efa7213201a4e705
round[13].im_col	794cf891177bfd1ddf67a744acd9c4f6
round[13].ik_sch	1a1f181d1e1b1c191217101516131411
round[14].istart	6353e08c0960e104cd70b751bacad0e7
round[14].is_box	0050a0f04090e03080d02070c01060b0
round[14].is_row	00102030405060708090a0b0c0d0e0f0
round[14].ik_sch	000102030405060708090a0b0c0d0e0f
round[14].ioutput	00112233445566778899aabccddeeff

# **Chapter 5**

## **Evaluation**

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