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Total Marks:

I D: 242 FC242 H6

Lecture Group: TC1L

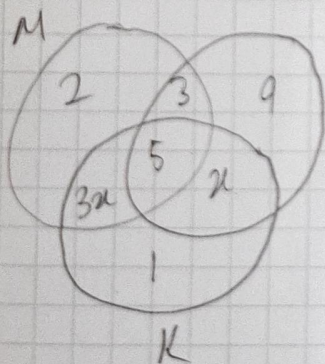
12

i) The Venn diagram shows the number of students in sets M , B , K . Given

$M = \{ \text{Students who like CMT1134 subject} \}$

$B = \{ \text{Students who like CMT1142 subject} \}$

$K = \{ \text{Students who like CMT1114 subject} \}$



If no. of students who like $\overset{(M)}{\text{CMT1134}}$ and $\overset{(K)}{\text{CMT1114}} = 32$,
i) Find value of x .

$$M + K = 32$$

$$3x + 5 = 32$$

$$3x = 27$$

$$x = 9$$

ii) Find the no. of students who like 2 subjects only.

$$3x + 3 + x$$

$$= 3(9) + 9 + 3$$

$$= 39$$

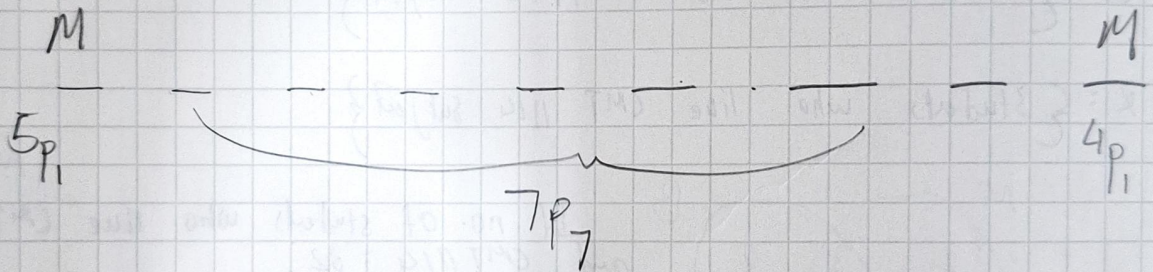
2. There are 4 women and 5 men to be arranged in a row.
Find the number of arrangements that can be found
formed if

i) No restriction

4 women } 9
5 men

$${}^9P_9 = 362880 //$$

ii) Both ends of the rows are men



$$5P_1 \times 7P_7 \times 4P_1 = 100800 //$$

iii) Find the probability that both ends of the rows are men.

$$P(A) = \frac{n(A)}{n(S)}$$

$$= \frac{100800}{362880} = \frac{5}{18} //$$

3. Determine the number of ways of arranging 8 girls of in a circle where 4 girls are always next to each other.

[1 mark]

$$\begin{array}{ccc}
 \begin{array}{c} 4! \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \end{array} & \Rightarrow & \begin{array}{c} \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \\ \cdot \end{array} \\
 \begin{array}{c} \text{1 entity} \\ 4! \\ \downarrow \\ (8-4)+1 = 5 \end{array} & & \begin{array}{c} (n-1)! \\ = (5-1)! \\ = 4! \end{array}
 \end{array}$$

n.o.w for 4 girls = $4!$

= 24

n.o.w for 4 girls always next to each other = $4!$

other

= 24

Total
n.o.a = $4! \times 4!$
= 576 //

4. Study shows that 15% of the population in a country wear Spectacles. Random sample of 20 ~~persons~~ people is selected.

$X \leq 2$

i) Find probability that (at most 2 persons) in this sample wear spectacles

$$P(X \leq 2) = P(X=0) + P(X=1) + P(X=2)$$

$$\begin{aligned}
 &= {}^{20}C_0 (0.15)^0 (0.85)^{20} + {}^{20}C_1 (0.15)^1 (0.85)^{19} + \\
 &{}^{20}C_2 (0.15)^2 (0.85)^{18}
 \end{aligned}$$

$n = 20$

$p = 15\%$

= 0.15

$q = 1 - p$

= 1 - 0.15

= 0.85

= 0.03875953108 + 0.136798345 + 0.2293384019

= 0.404896278

≈ 0.4049 //

$\mu = np$

$\sigma^2 = npq$

ii) what is the mean and S.D of the number of persons who wear spectacles?

$$\begin{aligned}\mu &= np \\ &= 20(0.15) \\ &= 3 //\end{aligned}$$

$$\begin{aligned}\sigma^2 &= npq \\ \sigma &= \sqrt{npq} \\ \sigma &= \sqrt{(20)(0.15)(0.85)} \\ &= 1.5969 //\end{aligned}$$