## Lecture 3 How to minimize cost

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#### Acknowledgement

- Andrew Ng's ML class
  - https://class.coursera.org/ml-003/lecture
  - http://www.holehouse.org/mlclass/ (note)
- Convolutional Neural Networks for Visual Recognition.
  - http://cs23 I n.github.io/
- Tensorflow
  - https://www.tensorflow.org
  - https://github.com/aymericdamien/TensorFlow-Examples

#### Hypothesis and Cost

$$H(x) = Wx + b$$

$$cost(W, b) = \frac{1}{m} \sum_{i=1}^{m} (H(x^{(i)}) - y^{(i)})^2$$

### Simplified hypothesis

$$H(x) = Wx$$

$$cost(W) = \frac{1}{m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})^2$$

#### What cost(W) looks like?

$$cost(W) = \frac{1}{m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})^2$$

X	Y
1	1
2	2
3	3

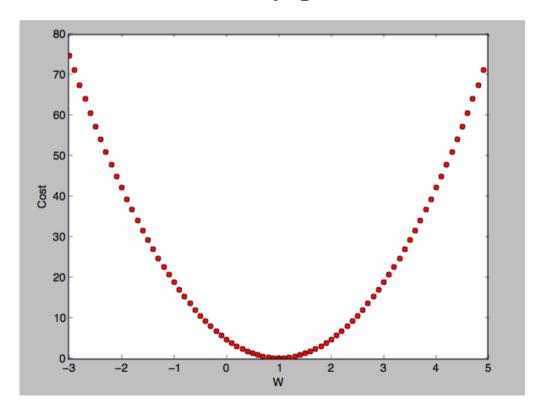
• W=I, cost(W)=0

$$\frac{1}{3}((1*1-1)^2 + (1*2-2)^2 + (1*3-3)^2)$$

• W=0, cost(W)=4.67  $\frac{1}{3}((0*1-1)^2 + (0*2-2)^2 + (0*3-3)^2)$ 

#### What cost(W) looks like?

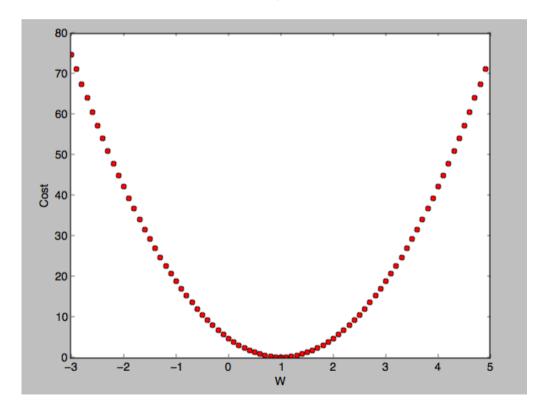
$$cost(W) = \frac{1}{m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})^2$$



Otality Woth,
Deep Learning -> FORM
=> FIZE

#### How to minimize cost?

$$cost(W) = \frac{1}{m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})^2$$

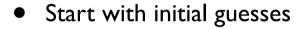


#### Gradient descent algorithm

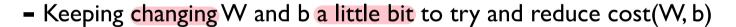
- Minimize cost function
- Gradient descent is used many minimization problems
- For a given cost function, cost (W, b), it will find W, b to minimize cost
- It can be applied to more general function: cost (w1, w2, ...)

 $\rightarrow$   $\omega = \omega = 0.7$ 

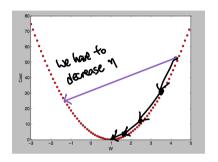
#### How it works?



- Start at 0,0 (or any other value)



- Each time you change the parameters, you select the gradient which reduces cost(W, b) the most possible
- Repeat
- Do so until you converge to a local minimum
- Has an interesting property
  - Where you start can determine which minimum you end up



#### Formal definition

$$cost(W) = \frac{1}{m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})^2$$



$$cost(W) = \frac{1}{2m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})^2$$
 তানুম দুখন সমা ক্রান্তার ধ্যাকুর দেবের

#### Formal definition

$$cost(W) = \frac{1}{2m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})^2$$

$$W := W - \alpha \frac{\partial}{\partial W} cost(W)$$

#### Formal definition

$$W := W - \alpha \frac{\partial}{\partial W} \frac{1}{2m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})^2$$

$$W := W - \alpha \frac{1}{2m} \sum_{i=1}^{m} 2(Wx^{(i)} - y^{(i)})x^{(i)}$$

$$W := W - \alpha \frac{1}{m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})x^{(i)}$$



#### **Derivative Calculator**

#### Calculate derivatives online — with steps and graphing!

Also check the <u>Integral Calculator</u>!

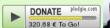
<u>Ableitungsrechner</u> auf Deutsch



Hello there!

X

Was this calculator helpful to you? Then I would highly appreciate **small donations** via PayPal:



... or use this link for shopping on Amazon, without affecting your order.

Thank you!

Calculate the Derivative of ...

(xa-y)^2

Go!

This will be calculated:

$$rac{\mathrm{d}}{\mathrm{d}x}\Big[\left(xa-y
ight)^2\Big]$$

Not what you mean? *Use parentheses!* Set differentiation variable and order in "*Options*".

About Help Examples Options

The Derivative Calculator lets you calculate derivatives of functions online — for free!

Our calculator allows you to check your solutions to calculus exercises. It helps you practice by showing you the full working (step by step differentiation).

The Derivative Calculator supports computing first, second, ..., fifth derivatives as well as differentiating functions with many variables (partial derivatives), implicit differentiation and calculating roots/zeros. Interactive graphs/plots help visualize and better understand the functions.

For more about how to use the Derivative Calculator, go to "Help" or take a look at the examples.

And now: Happy differentiating!

Recommend this Website

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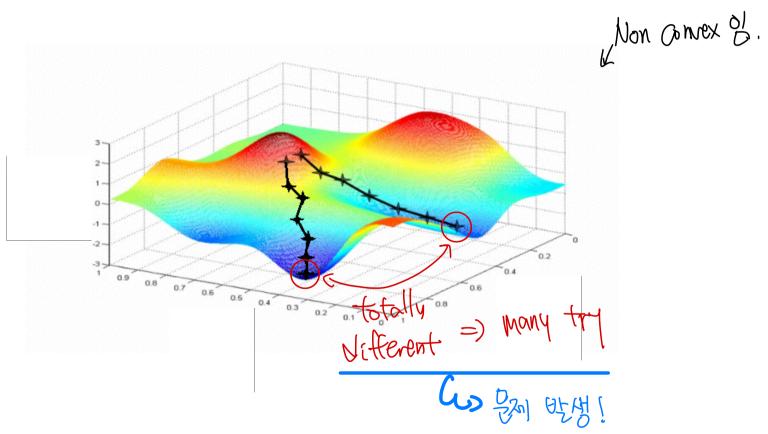
Result

Done! See the result further below.

#### Gradient descent algorithm

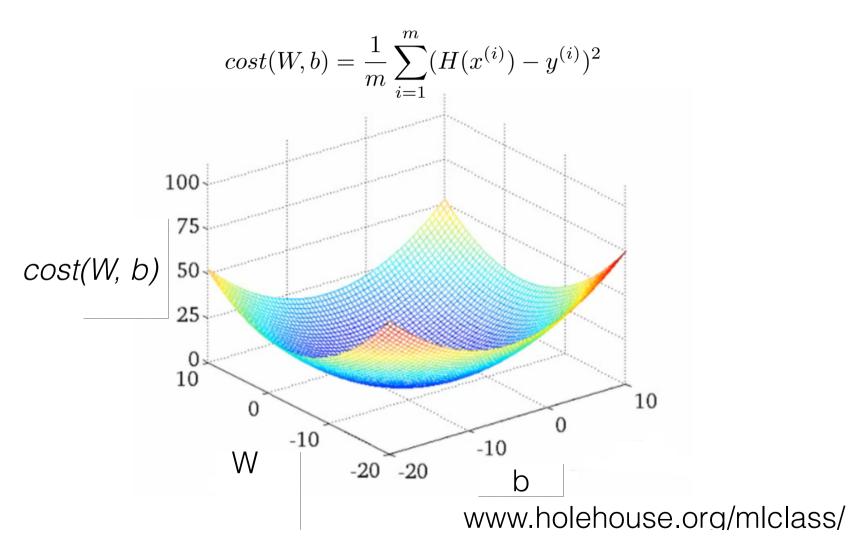
$$W := W - \alpha \frac{1}{m} \sum_{i=1}^{m} (Wx^{(i)} - y^{(i)})x^{(i)}$$

#### Convex function



www.holehouse.org/mlclass/

#### Convex function



# Next Multivariable logistic regression

