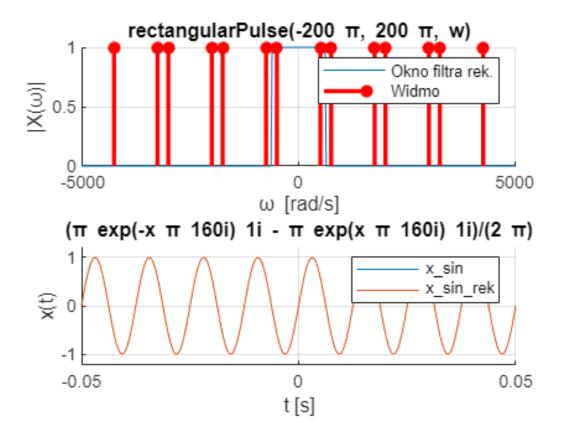
Laboratorium 6 – Próbkowanie i rekonstrukcja sygnałów

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1.1 Ćwiczenie 1

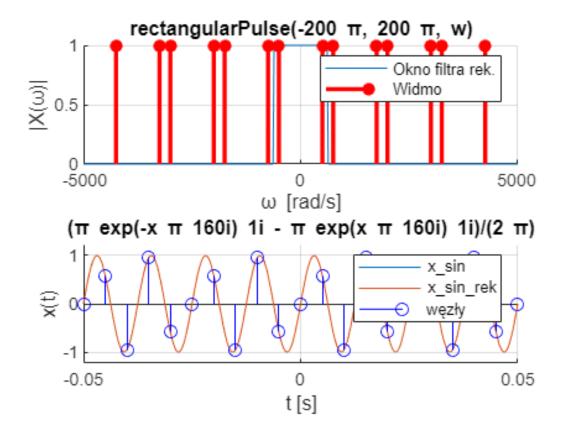
```
clear all; close all;
syms t x w K
fp = 200; fg = fp/2; %Hz
wp = 2*pi*fp; wg = 2*pi*fg;
s = 4/5; ws = s*wg;
x \sin = \sin(ws*t);
X_FT_sin_org = fourier(x_sin);
X_FT_sin = X_FT_sin_org + ... % oryginal widma
symsum((subs(X FT sin org, w, w - K*wp ) + ...% 3 aliasy lewe
subs(X_{FT_sin_org}, w, w + K^*wp)), K , 1, 3); % 3 aliasy prawe
FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x sin rek = ifourier(X FT sin*FILT FT); % odwr. tarnsf. Fouriera
BND t = [-10/fp; 10/fp];
%t SMP = [BND t(1):1/(10*fp):BND t(2)];
BND w = [-4*wp;4*wp];
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT FT,BND w); %okno filtru rek.
%ezplot(X FT sin,BND w)
v_num = abs(double(subs(X_FT_sin, w, w_SMP)));
n = find(abs(v num) == Inf);
stem(w SMP(n),sign(v num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
subplot(2,1,2); hold on; grid on;
ezplot(x sin, BND t); % syg. próbkowany
ezplot(x_sin_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
legend('x\_sin','x\_sin\_rek');
```



1.2 Zadanie 2

Do powyższego przykładu została dodana funkcjonalność, która zaznacza węzły próbkowania na oryginalnym przebiegu czasowym:

```
wezly = BND_t(1) : 1/fp : BND_t(2);
wezly_val = subs(x_sin_rek, x, wezly);
% subplot(2,1,2) ...
stem(wezly, wezly_val, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```



1.3 Zadanie 3

Podpunkt a) s = 1/5

```
clear all; close all;
syms t x w K

fp = 200; fg = fp/2; %Hz
wp = 2*pi*fp; wg = 2*pi*fg;

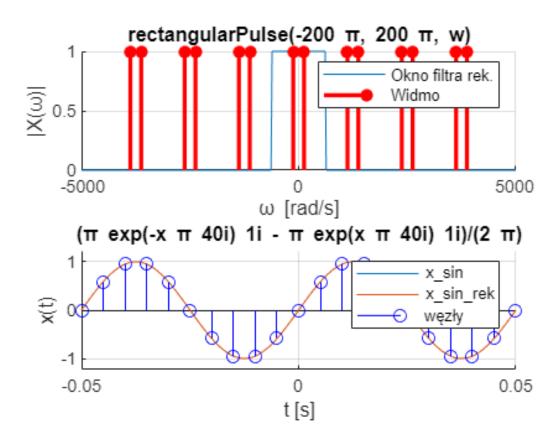
s = 1/5; ws = s*wg;
x_sin = sin(ws*t);
X_FT_sin_org = fourier(x_sin);

X_FT_sin = X_FT_sin_org + ... % oryginal widma
symsum((subs(X_FT_sin_org, w, w - K*wp ) + ...% 3 aliasy lewe
subs(X_FT_sin_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe

FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_sin_rek = ifourier(X_FT_sin*FILT_FT); % odwr. tarnsf. Fouriera

BND_t = [-10/fp;10/fp];
```

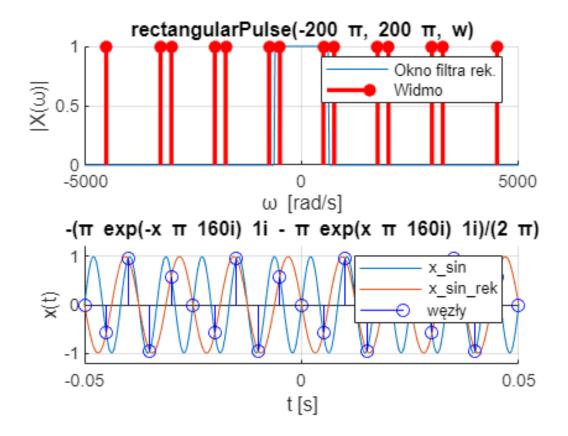
```
%t SMP = [BND t(1):1/(10*fp):BND t(2)];
BND w = [-4*wp;4*wp];
w_{SMP} = [BND_w(1):wp/10:BND_w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
%ezplot(X_FT_sin,BND_w)
v num = abs(double(subs(X FT sin, w, w SMP)));
n = find(abs(v_num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
wezly = BND_t(1) : 1/fp : BND_t(2);
wezly_val = subs(x_sin_rek, x, wezly);
subplot(2,1,2); hold on; grid on;
ezplot(x sin, BND t); % syg. próbkowany
ezplot(x_sin_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(wezly, wezly_val, 'b');
legend('x\sin','x\sin\rek', 'wezły');
```



Podpunkt b) s = 6/5

```
clear all; close all;
syms t x w K
```

```
fp = 200; fg = fp/2; %Hz
wp = 2*pi*fp; wg = 2*pi*fg;
s = 6/5; ws = s*wg;
x \sin = \sin(ws*t);
X_FT_sin_org = fourier(x_sin);
X_FT_sin = X_FT_sin_org + ... % oryginal widma
symsum((subs(X FT sin org, w, w - K*wp ) + ...% 3 aliasy lewe
subs(X_{FT_sin_org}, w, w + K^*wp)), K , 1, 3); % 3 aliasy prawe
FILT FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_sin_rek = ifourier(X_FT_sin*FILT_FT); % odwr. tarnsf. Fouriera
BND_t = [-10/fp;10/fp];
%t SMP = [BND t(1):1/(10*fp):BND t(2)];
BND_w = [-4*wp;4*wp];
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT FT,BND w); %okno filtru rek.
%ezplot(X_FT_sin,BND_w)
v num = abs(double(subs(X FT sin, w, w SMP)));
n = find(abs(v num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
wezly = BND_t(1) : 1/fp : BND_t(2);
wezly_val = subs(x_sin_rek, x, wezly);
subplot(2,1,2); hold on; grid on;
ezplot(x_sin, BND_t); % syg. próbkowany
ezplot(x_sin_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(wezly, wezly_val, 'b');
legend('x = \sin', x=\sin', 'wezły');
```



Podpunkt c) s = 11/5

```
clear all; close all;
syms t x w K

fp = 200; fg = fp/2; %Hz
wp = 2*pi*fp; wg = 2*pi*fg;

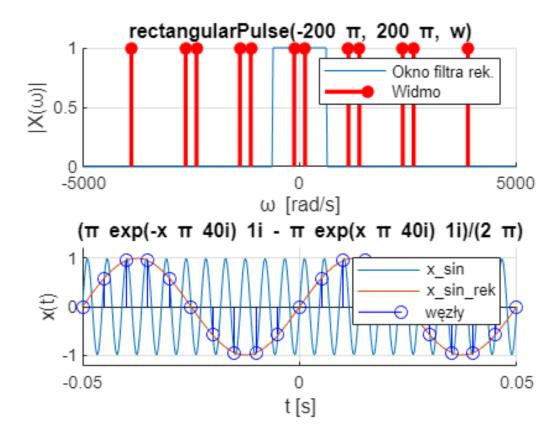
s = 11/5; ws = s*wg;
x_sin = sin(ws*t);
X_FT_sin_org = fourier(x_sin);

X_FT_sin = X_FT_sin_org + ... % oryginal widma
symsum((subs(X_FT_sin_org, w, w - K*wp) + ...% 3 aliasy lewe
subs(X_FT_sin_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe

FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_sin_rek = ifourier(X_FT_sin*FILT_FT); % odwr. tarnsf. Fouriera

BND_t = [-10/fp;10/fp];
%t_SMP = [BND_t(1):1/(10*fp):BND_t(2)];
BND_w = [-4*wp;4*wp];
```

```
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
%ezplot(X_FT_sin,BND_w)
v_num = abs(double(subs(X_FT_sin, w, w_SMP)));
n = find(abs(v_num) == Inf);
stem(w SMP(n),sign(v num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
wezly = BND_t(1) : 1/fp : BND_t(2);
wezly_val = subs(x_sin_rek, x, wezly);
subplot(2,1,2); hold on; grid on;
ezplot(x_sin, BND_t); % syg. próbkowany
ezplot(x_sin_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(wezly, wezly_val, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```

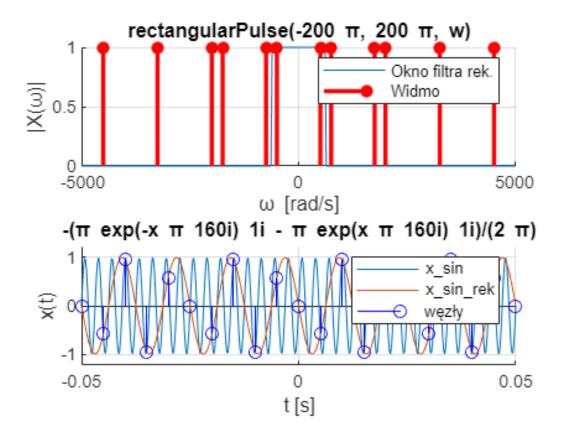


Podpunkt d) s = 16/5

```
clear all; close all;
syms t x w K

fp = 200; fg = fp/2; %Hz
```

```
wp = 2*pi*fp; wg = 2*pi*fg;
s = 16/5; ws = s*wg;
x_{sin} = sin(ws*t);
X_FT_sin_org = fourier(x_sin);
X FT sin = X FT sin org + ... % oryginal widma
symsum((subs(X_FT_sin_org, w, w - K*wp ) + ...% 3 aliasy lewe
subs(X_FT_sin_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe
FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x sin rek = ifourier(X FT sin*FILT FT); % odwr. tarnsf. Fouriera
BND t = [-10/fp; 10/fp];
t_{SMP} = [BND_t(1):1/(10*fp):BND_t(2)];
BND_w = [-4*wp;4*wp];
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
%ezplot(X FT sin,BND w)
v_num = abs(double(subs(X_FT_sin, w, w_SMP)));
n = find(abs(v_num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
wezly = BND_t(1) : 1/fp : BND_t(2);
wezly val = subs(x sin rek, x, wezly);
subplot(2,1,2); hold on; grid on;
ezplot(x_sin, BND_t); % syg. próbkowany
ezplot(x_sin_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(wezly, wezly_val, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```



Podpunkt e) s = 4/5

```
clear all; close all;
syms t x w K

fp = 200; fg = fp/2; %Hz
wp = 2*pi*fp; wg = 2*pi*fg;

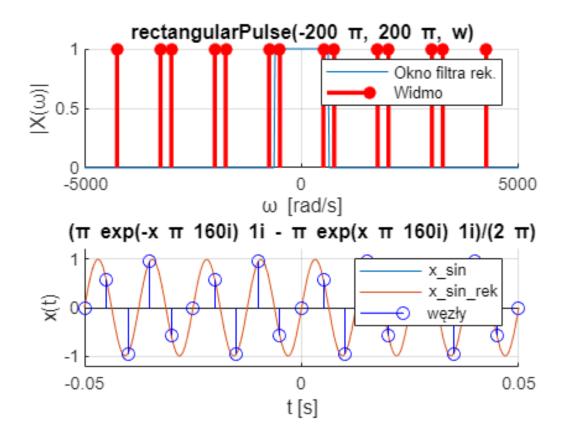
s = 4/5; ws = s*wg;
x_sin = sin(ws*t);
X_FT_sin_org = fourier(x_sin);

X_FT_sin = X_FT_sin_org + ... % oryginal widma
symsum((subs(X_FT_sin_org, w, w - K*wp) + ...% 3 aliasy lewe
subs(X_FT_sin_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe

FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_sin_rek = ifourier(X_FT_sin*FILT_FT); % odwr. tarnsf. Fouriera

BND_t = [-10/fp;10/fp];
%t_SMP = [BND_t(1):1/(10*fp):BND_t(2)];
BND_w = [-4*wp;4*wp];
```

```
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
%ezplot(X_FT_sin,BND_w)
v_num = abs(double(subs(X_FT_sin, w, w_SMP)));
n = find(abs(v_num) == Inf);
stem(w SMP(n),sign(v num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
wezly = BND_t(1) : 1/fp : BND_t(2);
wezly_val = subs(x_sin_rek, x, wezly);
subplot(2,1,2); hold on; grid on;
ezplot(x_sin, BND_t); % syg. próbkowany
ezplot(x_sin_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(wezly, wezly_val, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```

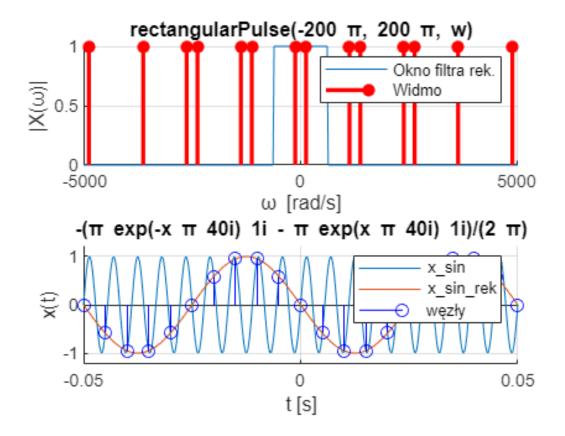


Podpunkt f) s = 9/5

```
clear all; close all;
syms t x w K

fp = 200; fg = fp/2; %Hz
```

```
wp = 2*pi*fp; wg = 2*pi*fg;
s = 9/5; ws = s*wg;
x_{sin} = sin(ws*t);
X_FT_sin_org = fourier(x_sin);
X FT sin = X FT sin org + ... % oryginal widma
symsum((subs(X_FT_sin_org, w, w - K*wp ) + ...% 3 aliasy lewe
subs(X_FT_sin_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe
FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x sin rek = ifourier(X FT sin*FILT FT); % odwr. tarnsf. Fouriera
BND t = [-10/fp; 10/fp];
t_{SMP} = [BND_t(1):1/(10*fp):BND_t(2)];
BND_w = [-4*wp;4*wp];
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
%ezplot(X FT sin,BND w)
v_num = abs(double(subs(X_FT_sin, w, w_SMP)));
n = find(abs(v_num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
wezly = BND_t(1) : 1/fp : BND_t(2);
wezly val = subs(x sin rek, x, wezly);
subplot(2,1,2); hold on; grid on;
ezplot(x_sin, BND_t); % syg. próbkowany
ezplot(x_sin_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(wezly, wezly_val, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```



Podpunkt g) s = 14/5

```
clear all; close all;
syms t x w K

fp = 200; fg = fp/2; %Hz
wp = 2*pi*fp; wg = 2*pi*fg;

s = 14/5; ws = s*wg;
x_sin = sin(ws*t);
X_FT_sin_org = fourier(x_sin);

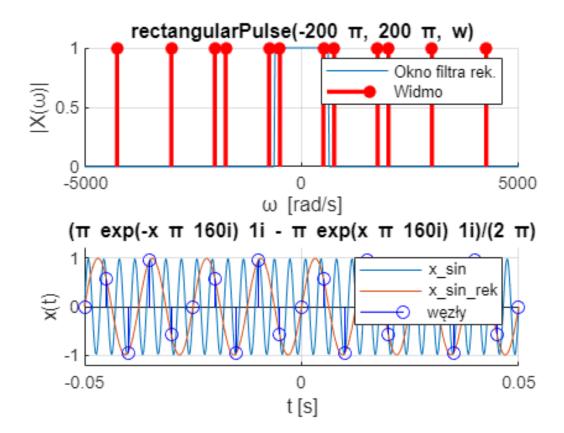
X_FT_sin_org = fourier(x_sin);

X_FT_sin = X_FT_sin_org + ... % oryginal widma
symsum((subs(X_FT_sin_org, w, w - K*wp)) + ...% 3 aliasy lewe
subs(X_FT_sin_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe

FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_sin_rek = ifourier(X_FT_sin*FILT_FT); % odwr. tarnsf. Fouriera

BND_t = [-10/fp;10/fp];
%t_SMP = [BND_t(1):1/(10*fp):BND_t(2)];
BND_w = [-4*wp;4*wp];
```

```
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
%ezplot(X_FT_sin,BND_w)
v_num = abs(double(subs(X_FT_sin, w, w_SMP)));
n = find(abs(v_num) == Inf);
stem(w SMP(n),sign(v num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
wezly = BND_t(1) : 1/fp : BND_t(2);
wezly_val = subs(x_sin_rek, x, wezly);
subplot(2,1,2); hold on; grid on;
ezplot(x_sin, BND_t); % syg. próbkowany
ezplot(x_sin_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(wezly, wezly_val, 'b');
legend('x\leq \sin','x\leq \sin'rek', 'wezy');
```



Dla ułamków mniejszych od 1, sygnał był rekonstruowany poprawnie, zaś dla większych odbiegał od sygnału oryginalnego.

1.4 Zadanie 4

Dla s = 1/5

```
syms t x w K
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
s = 1/5;
ws = s*wg;
x tr = ifourier(triangularPulse(-ws,ws,w));
x_FT_tr_org = triangularPulse(-ws,ws,w);
X_FT_tr = x_FT_tr_org + ... % oryginal widma
symsum((subs(x_FT_tr_org, w, w - K*wp ) + ...% 3 aliasy lewe
subs(x FT tr org, w, w + K^*wp)), K , 1, 3); % 3 aliasy prawe
FILT FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x tr rek = ifourier(X FT tr*FILT FT); % odwr. tarnsf. Fouriera
nodes = BND_t(1) : 1/fp : BND_t(2);
% uniknięcie zera w mianowniku
n = (length(nodes) - 1) / 2;
nodes1 = nodes(1 : n);
nodes2 = nodes(n + 2 : 2 * n + 1);
nodes_values = [subs(x_tr_rek, x, nodes1), ...
limit(x_tr_rek, x, 0), subs(x_tr_rek, x, nodes2)];
BND t = [-10/fp;10/fp];
%t SMP = [BND t(1):1/(10*fp):BND_t(2)];
BND w = [-4*wp;4*wp];
w_{SMP} = [BND_w(1):wp/10:BND_w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
ezplot(X FT tr,BND w)
v_num = abs(double(subs(X_FT_tr, w, w_SMP)));
n = find(abs(v_num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
subplot(2,1,2); hold on; grid on;
ezplot(x tr, BND t); % syg. próbkowany
ezplot(x_tr_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(nodes, nodes_values, 'b');
```

Warning: Using only the real component of complex data.

```
legend('x\_sin','x\_sin\_rek', 'wezty');
```

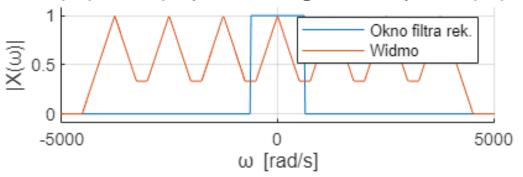
se(-40 π, 0, 40 π, w) + ... + triangularPulse(-40 π, 0, 40 π)Okno filtra rek. 0.4 (3) (3) (0.2) Widmo -5000 5000 ω [rad/s] -(exp(-x π 40i) (exp(x π 40i) - 1)²)/(80 x² π ²) 20 x sin x sin rek ₩₁₀ węzły 0 -0.050.05 t [s]

Dla s = 6/5

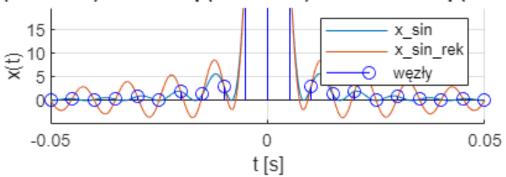
```
syms t x w K
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
s = 6/5;
ws = s*wg;
x_tr = ifourier(triangularPulse(-ws,ws,w));
x_FT_tr_org = triangularPulse(-ws,ws,w);
X_FT_tr = x_FT_tr_org + ... % oryginal widma
symsum((subs(x_FT_tr_org, w, w - K*wp) + ...% 3 aliasy lewe
subs(x_FT_tr_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe
FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_tr_rek = ifourier(X_FT_tr*FILT_FT); % odwr. tarnsf. Fouriera
nodes = BND_t(1) : 1/fp : BND_t(2);
% uniknięcie zera w mianowniku
n = (length(nodes) - 1) / 2;
```

```
nodes1 = nodes(1 : n);
nodes2 = nodes(n + 2 : 2 * n + 1);
nodes values = [subs(x tr rek, x, nodes1), ...
limit(x tr rek, x, 0), subs(x tr rek, x, nodes2)];
BND t = [-10/fp; 10/fp];
%t_SMP = [BND_t(1):1/(10*fp):BND_t(2)];
BND w = [-4*wp;4*wp];
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
ezplot(X_FT_tr,BND_w)
v num = abs(double(subs(X_FT_tr, w, w_SMP)));
n = find(abs(v num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
subplot(2,1,2); hold on; grid on;
ezplot(x_tr, BND_t); % syg. próbkowany
ezplot(x_tr_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(nodes, nodes_values, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```

(-240 m, 0, 240 m, w) + ... + triangularPulse(-240 m, 0, 240)

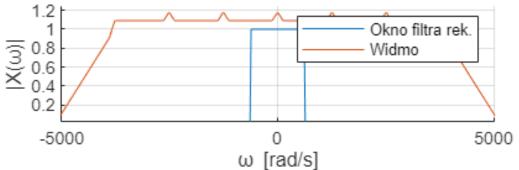


$xp(x \pi 160i) - x \pi exp(-x \pi 200i) 80i + x \pi exp(x \pi 200i)$

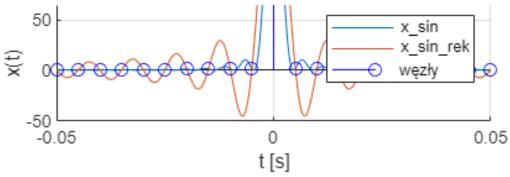


```
syms t x w K
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
s = 11/5;
ws = s*wg;
x tr = ifourier(triangularPulse(-ws,ws,w));
x_FT_tr_org = triangularPulse(-ws,ws,w);
X_FT_tr = x_FT_tr_org + ... % oryginal widma
symsum((subs(x_FT_tr_org, w, w - K*wp ) + ...% 3 aliasy lewe
subs(x_FT_tr_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe
FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x tr rek = ifourier(X FT tr*FILT FT); % odwr. tarnsf. Fouriera
nodes = BND t(1) : 1/fp : BND t(2);
% uniknięcie zera w mianowniku
n = (length(nodes) - 1) / 2;
nodes1 = nodes(1 : n);
nodes2 = nodes(n + 2 : 2 * n + 1);
nodes_values = [subs(x_tr_rek, x, nodes1), ...
limit(x_tr_rek, x, 0), subs(x_tr_rek, x, nodes2)];
BND t = [-10/fp;10/fp];
%t SMP = [BND t(1):1/(10*fp):BND t(2)];
BND w = [-4*wp;4*wp];
w_{SMP} = [BND_w(1):wp/10:BND_w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
ezplot(X FT tr,BND w)
v num = abs(double(subs(X FT tr, w, w SMP)));
n = find(abs(v_num) == Inf);
stem(w SMP(n),sign(v num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
subplot(2,1,2); hold on; grid on;
ezplot(x tr, BND t); % syg. próbkowany
ezplot(x_tr_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(nodes, nodes_values, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```

+(-440 m, 0, 440 m, w) + ... + triangularPulse(-440 m, 0, 440)



p(x π 40i) - x π exp(-x π 200i) 480i + x π exp(x π 200i

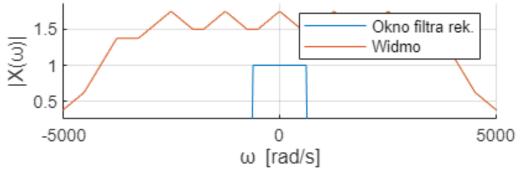


Dla s = 16/5

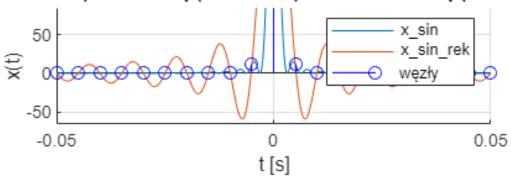
```
syms t x w K
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
s = 16/5;
ws = s*wg;
x_tr = ifourier(triangularPulse(-ws,ws,w));
x_FT_tr_org = triangularPulse(-ws,ws,w);
X_FT_tr = x_FT_tr_org + ... % oryginal widma
symsum((subs(x_FT_tr_org, w, w - K*wp) + ...% 3 aliasy lewe
subs(x_FT_tr_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe
FILT FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_tr_rek = ifourier(X_FT_tr*FILT_FT); % odwr. tarnsf. Fouriera
nodes = BND_t(1) : 1/fp : BND_t(2);
% uniknięcie zera w mianowniku
n = (length(nodes) - 1) / 2;
```

```
nodes1 = nodes(1 : n);
nodes2 = nodes(n + 2 : 2 * n + 1);
nodes values = [subs(x tr rek, x, nodes1), ...
limit(x tr rek, x, 0), subs(x tr rek, x, nodes2)];
BND t = [-10/fp; 10/fp];
%t_SMP = [BND_t(1):1/(10*fp):BND_t(2)];
BND w = [-4*wp;4*wp];
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
ezplot(X_FT_tr,BND_w)
v num = abs(double(subs(X_FT_tr, w, w_SMP)));
n = find(abs(v num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
subplot(2,1,2); hold on; grid on;
ezplot(x_tr, BND_t); % syg. próbkowany
ezplot(x_tr_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(nodes, nodes_values, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```

\pm (-640 π , 0, 640 π , w) +...+ triangularPulse(-640 π , 0, 640

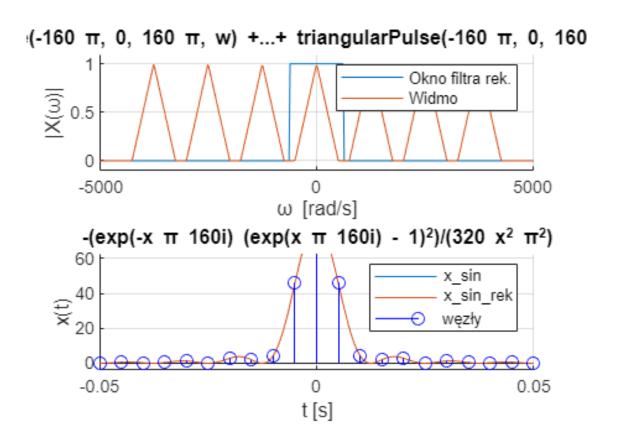


$p(x \pi 160i) - x \pi exp(-x \pi 200i) 960i + x \pi exp(x \pi 200i)$



```
syms t x w K
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
s = 4/5;
ws = s*wg;
x tr = ifourier(triangularPulse(-ws,ws,w));
x_FT_tr_org = triangularPulse(-ws,ws,w);
X_FT_tr = x_FT_tr_org + ... % oryginal widma
symsum((subs(x_FT_tr_org, w, w - K*wp ) + ...% 3 aliasy lewe
subs(x_FT_tr_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe
FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x tr rek = ifourier(X FT tr*FILT FT); % odwr. tarnsf. Fouriera
nodes = BND t(1) : 1/fp : BND t(2);
% uniknięcie zera w mianowniku
n = (length(nodes) - 1) / 2;
nodes1 = nodes(1 : n);
nodes2 = nodes(n + 2 : 2 * n + 1);
nodes_values = [subs(x_tr_rek, x, nodes1), ...
limit(x_tr_rek, x, 0), subs(x_tr_rek, x, nodes2)];
BND_t = [-10/fp;10/fp];
%t SMP = [BND t(1):1/(10*fp):BND t(2)];
BND w = [-4*wp;4*wp];
w_{SMP} = [BND_w(1):wp/10:BND_w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
ezplot(X_FT_tr,BND_w)
v num = abs(double(subs(X FT tr, w, w SMP)));
n = find(abs(v_num) == Inf);
stem(w SMP(n),sign(v num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
subplot(2,1,2); hold on; grid on;
ezplot(x tr, BND t); % syg. próbkowany
ezplot(x_tr_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(nodes, nodes values, 'b');
```

```
legend('x\_sin','x\_sin\_rek', 'wexty');
```



Dla s = 9/5

```
syms t x w K
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
s = 9/5;
ws = s*wg;

x_tr = ifourier(triangularPulse(-ws,ws,w));
x_FT_tr_org = triangularPulse(-ws,ws,w);

X_FT_tr = x_FT_tr_org + ... % oryginal widma
symsum((subs(x_FT_tr_org, w, w - K*wp)) + ...% 3 aliasy lewe
subs(x_FT_tr_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe

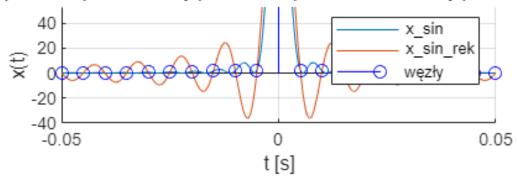
FILT_FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_tr_rek = ifourier(X_FT_tr*FILT_FT); % odwr. tarnsf. Fouriera
```

```
nodes = BND_t(1) : 1/fp : BND_t(2);
% uniknięcie zera w mianowniku
n = (length(nodes) - 1) / 2;
nodes1 = nodes(1 : n);
nodes2 = nodes(n + 2 : 2 * n + 1);
nodes_values = [subs(x_tr_rek, x, nodes1), ...
limit(x_tr_rek, x, 0), subs(x_tr_rek, x, nodes2)];
BND_t = [-10/fp;10/fp];
%t SMP = [BND t(1):1/(10*fp):BND t(2)];
BND w = [-4*wp;4*wp];
w_{SMP} = [BND_w(1):wp/10:BND_w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
ezplot(X FT tr,BND w)
v_num = abs(double(subs(X_FT_tr, w, w_SMP)));
n = find(abs(v_num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
subplot(2,1,2); hold on; grid on;
ezplot(x tr, BND t); % syg. próbkowany
ezplot(x_tr_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(nodes, nodes_values, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```

(-360 π, 0, 360 π, w) +...+ triangularPulse(-360 π, 0, 360 Okno filtra rek. Widmo -5000 0 5000

р(х т 40і) - х т ехр(-х т 200і) 320і + х т ехр(х т 200і

ω [rad/s]

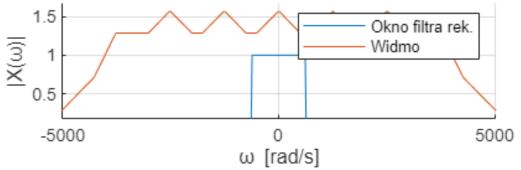


Dla s = 14/5

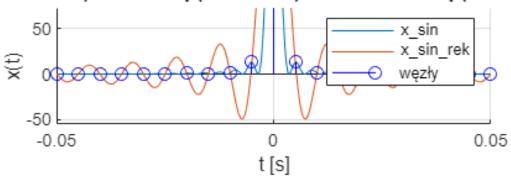
```
syms t x w K
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
s = 14/5;
ws = s*wg;
x_tr = ifourier(triangularPulse(-ws,ws,w));
x_FT_tr_org = triangularPulse(-ws,ws,w);
X_FT_tr = x_FT_tr_org + ... % oryginal widma
symsum((subs(x_FT_tr_org, w, w - K*wp) + ...% 3 aliasy lewe
subs(x_FT_tr_org, w, w + K*wp)), K , 1, 3); % 3 aliasy prawe
FILT FT = rectangularPulse(-wg,wg,w); % filtr rekonstruuj;cy
x_tr_rek = ifourier(X_FT_tr*FILT_FT); % odwr. tarnsf. Fouriera
nodes = BND_t(1) : 1/fp : BND_t(2);
% uniknięcie zera w mianowniku
n = (length(nodes) - 1) / 2;
```

```
nodes1 = nodes(1 : n);
nodes2 = nodes(n + 2 : 2 * n + 1);
nodes values = [subs(x tr rek, x, nodes1), ...
limit(x tr rek, x, 0), subs(x tr rek, x, nodes2)];
BND t = [-10/fp; 10/fp];
%t_SMP = [BND_t(1):1/(10*fp):BND_t(2)];
BND w = [-4*wp;4*wp];
w SMP = [BND w(1):wp/10:BND w(2)];
figure; subplot(2,1,1); hold on; grid on;
ezplot(FILT_FT,BND_w); %okno filtru rek.
ezplot(X_FT_tr,BND_w)
v num = abs(double(subs(X_FT_tr, w, w_SMP)));
n = find(abs(v num) == Inf);
stem(w_SMP(n),sign(v_num(n)),'r*', 'LineWidth', 2);
xlabel('\omega [rad/s]'); ylabel('|X(\omega)|')
legend('Okno filtra rek.','Widmo');
subplot(2,1,2); hold on; grid on;
ezplot(x_tr, BND_t); % syg. próbkowany
ezplot(x_tr_rek, BND_t) % syg. odtworzony
xlabel('t [s]'); ylabel('x(t)')
stem(nodes, nodes_values, 'b');
legend('x\_sin','x\_sin\_rek', 'wezly');
```

(-560 m, 0, 560 m, w) +...+ triangularPulse(-560 m, 0, 560



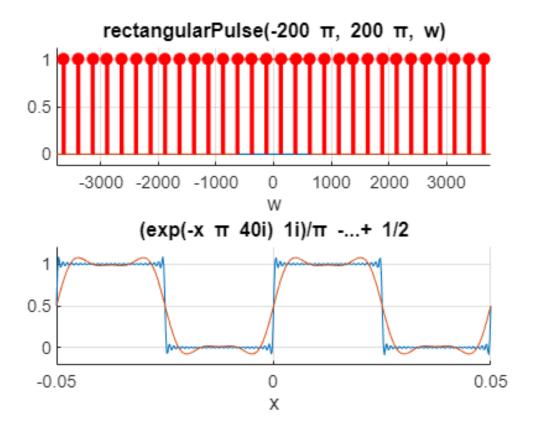
$p(x \pi 160i) - x \pi exp(-x \pi 200i) 720i + x \pi exp(x \pi 200i)$



1.5 Zadanie 5

Dla s = 1/5

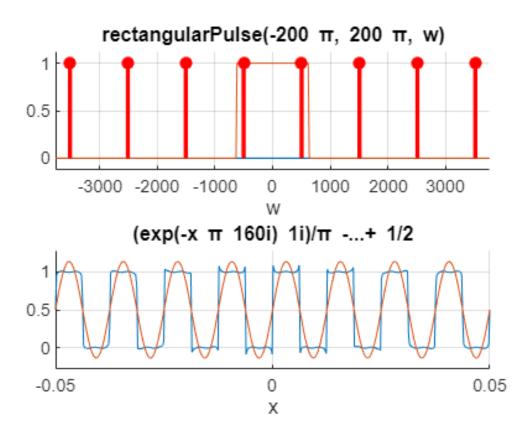
```
syms t x w K
s = 1/5;
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
ws = s*wg;
fs = s*fg;
T = 1/fs;
x = rectangularPulse(0,T/2,t);
NT = 50;
sumX = 0;
ind = -NT:NT;
BND = [-T/2 \ T/2];
for n=ind
   Xn = 1/T*int(x*exp(-1i*ws*n*t),t,BND);
    sumX = sumX + Xn * dirac(w-n*ws);
end
X FT oryg = 2*pi*sumX;
FILT_FT = rectangularPulse(-wg,wg,w);
x_tr_rek = ifourier(X_FT_oryg*FILT_FT);
BND t = [-10/fp;10/fp];
t_SMP = [BND_t(1):1/(10*fp):BND_t(2);];
BND_w = [-3*wp; 3*wp];
w_{SMP} = [BND_w(1):wp/10:BND_w(2);];
figure;
subplot(2,1,1); hold on; grid on;
ezplot(X_FT_oryg,BND_w);
ezplot(FILT_FT, BND_w);
v num = subs(imag(X FT oryg),w,w SMP);
n = find(abs(v_num) == inf);
stem(w_SMP(n),abs(sign(v_num(n))),'r*', 'LineWidth', 2);
w_num = subs(real(X_FT_oryg),w,w_SMP);
n = find(abs(v num) == inf);
stem(w_SMP(n),abs(sign(v_num(n))),'r*', 'LineWidth', 2)
subplot(2,1,2); hold on; grid on;
ezplot(ifourier(X_FT_oryg),BND_t);
ezplot(x tr rek, BND t);
```



Dla s = 4/5

```
syms t x w K
s = 4/5;
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
ws = s*wg;
fs = s*fg;
T = 1/fs;
x = rectangularPulse(0,T/2,t);
NT = 50;
sumX = 0;
ind = -NT:NT;
BND = [-T/2 T/2];
for n=ind
    Xn = 1/T*int(x*exp(-1i*ws*n*t),t,BND);
    sumX = sumX + Xn * dirac(w-n*ws);
end
X_FT_oryg = 2*pi*sumX;
FILT_FT = rectangularPulse(-wg,wg,w);
```

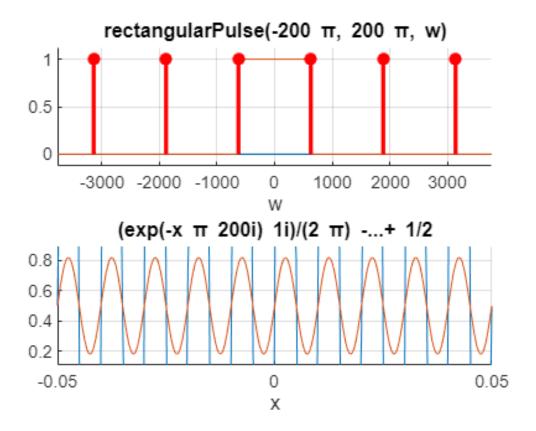
```
x tr rek = ifourier(X FT oryg*FILT FT);
BND_t = [-10/fp;10/fp];
t_SMP = [BND_t(1):1/(10*fp):BND_t(2);];
BND w = [-3*wp; 3*wp];
w_{SMP} = [BND_w(1):wp/10:BND_w(2);];
figure;
subplot(2,1,1); hold on; grid on;
ezplot(X_FT_oryg,BND_w);
ezplot(FILT_FT, BND_w);
v_num = subs(imag(X_FT_oryg),w,w_SMP);
n = find(abs(v_num) == inf);
stem(w_SMP(n),abs(sign(v_num(n))),'r*', 'LineWidth', 2);
w_num = subs(real(X_FT_oryg),w,w_SMP);
n = find(abs(v_num) == inf);
stem(w_SMP(n),abs(sign(v_num(n))),'r*', 'LineWidth', 2)
subplot(2,1,2); hold on; grid on;
ezplot(ifourier(X_FT_oryg),BND_t);
ezplot(x_tr_rek, BND_t);
```



Dla s = 1

```
syms t x w K
s = 1;
```

```
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
ws = s*wg;
fs = s*fg;
T = 1/fs;
x = rectangularPulse(0,T/2,t);
NT = 50;
sumX = 0;
ind = -NT:NT;
BND = [-T/2 \ T/2];
for n=ind
    Xn = 1/T*int(x*exp(-1i*ws*n*t),t,BND);
    sumX = sumX + Xn * dirac(w-n*ws);
end
X_{FT_oryg} = 2*pi*sumX;
FILT_FT = rectangularPulse(-wg,wg,w);
x_tr_rek = ifourier(X_FT_oryg*FILT_FT);
BND_t = [-10/fp;10/fp];
t_SMP = [BND_t(1):1/(10*fp):BND_t(2);];
BND_w = [-3*wp; 3*wp];
w_{SMP} = [BND_w(1):wp/10:BND_w(2);];
figure;
subplot(2,1,1); hold on; grid on;
ezplot(X_FT_oryg,BND_w);
ezplot(FILT_FT, BND_w);
v_num = subs(imag(X_FT_oryg),w,w_SMP);
n = find(abs(v num) == inf);
stem(w_SMP(n),abs(sign(v_num(n))),'r*', 'LineWidth', 2);
w_num = subs(real(X_FT_oryg),w,w_SMP);
n = find(abs(v_num) == inf);
stem(w_SMP(n),abs(sign(v_num(n))),'r*', 'LineWidth', 2)
subplot(2,1,2); hold on; grid on;
ezplot(ifourier(X_FT_oryg),BND_t);
ezplot(x_tr_rek, BND_t);
```



Dla s = 6/5

```
syms t x w K
s = 6/5;
fp = 200;
fg = fp/2; %Hz
wp = 2*pi*fp;
wg = 2*pi*fg;
ws = s*wg;
fs = s*fg;
T = 1/fs;
x = rectangularPulse(0,T/2,t);
NT = 50;
sumX = 0;
ind = -NT:NT;
BND = [-T/2 T/2];
for n=ind
    Xn = 1/T*int(x*exp(-1i*ws*n*t),t,BND);
    sumX = sumX + Xn * dirac(w-n*ws);
end
X_FT_oryg = 2*pi*sumX;
FILT_FT = rectangularPulse(-wg,wg,w);
```

```
x tr rek = ifourier(X FT oryg*FILT FT);
BND_t = [-10/fp;10/fp];
t_SMP = [BND_t(1):1/(10*fp):BND_t(2);];
BND w = [-3*wp; 3*wp];
w\_SMP = [BND_w(1):wp/10:BND_w(2);];
figure;
subplot(2,1,1); hold on; grid on;
ezplot(X_FT_oryg,BND_w);
ezplot(FILT_FT, BND_w);
v_num = subs(imag(X_FT_oryg),w,w_SMP);
n = find(abs(v_num) == inf);
stem(w_SMP(n),abs(sign(v_num(n))),'r*', 'LineWidth', 2);
w_num = subs(real(X_FT_oryg),w,w_SMP);
n = find(abs(v_num) == inf);
stem(w_SMP(n),abs(sign(v_num(n))),'r*', 'LineWidth', 2)
subplot(2,1,2); hold on; grid on;
ezplot(ifourier(X_FT_oryg),BND_t);
ezplot(x_tr_rek, BND_t);
```

