

Mathematical Model

Parameters

- N : Number of different illuminations (constant)
- M : Number of lamp powers (constant)
- $Coefficients_{ij}$: Coefficients relating lamp powers to illumination, where $i \in \{1, \dots, N\}$ and $j \in \{1, \dots, M\}$
- $DesiredIlluminations_i$: Desired level of illuminations for $i \in \{1, \dots, N\}$

Decision Variables

- P_j : Power of lamp j for $j \in \{1, \dots, M\}$
- E_i : Absolute error for illumination i for $i \in \{1, \dots, N\}$

Objective

Minimize the absolute error between the actual illumination levels and the desired illumination levels:

$$\min \sum_{i=1}^N E_i$$

Constraints

$$\sum_{j=1}^M Coefficients_{ij} \cdot P_j - DesiredIlluminations_i \leq E_i, \quad \forall i \in \{1, \dots, N\} \quad (1)$$

$$DesiredIlluminations_i - \sum_{j=1}^M Coefficients_{ij} \cdot P_j \leq E_i, \quad \forall i \in \{1, \dots, N\} \quad (2)$$

$$P_j \geq 0, \quad \forall j \in \{1, \dots, M\} \quad (3)$$