# **Problem D. Scoring Subsequences**

**Time limit** 2500 ms **Mem limit** 262144 kB

The score of a sequence  $[s_1, s_2, \ldots, s_d]$  is defined as  $\frac{s_1 \cdot s_2 \cdot \ldots \cdot s_d}{d!}$ , where  $d! = 1 \cdot 2 \cdot \ldots \cdot d$ . In particular, the score of an empty sequence is 1.

For a sequence  $[s_1, s_2, \ldots, s_d]$ , let m be the maximum score among all its subsequences. Its *cost* is defined as the maximum length of a subsequence with a score of m.

You are given a **non-decreasing** sequence  $[a_1, a_2, \ldots, a_n]$  of integers of length n. In other words, the condition  $a_1 \le a_2 \le \ldots \le a_n$  is satisfied. For each  $k = 1, 2, \ldots, n$ , find the cost of the sequence  $[a_1, a_2, \ldots, a_k]$ .

A sequence x is a subsequence of a sequence y if x can be obtained from y by deletion of several (possibly, zero or all) elements.

## Input

Each test contains multiple test cases. The first line contains the number of test cases t ( $1 \le t < 10^4$ ). The description of the test cases follows.

The first line of each test case contains an integer n ( $1 \le n \le 10^5$ ) — the length of the given sequence.

The second line of each test case contains n integers  $a_1, a_2, \ldots, a_n$  ( $1 \le a_i \le n$ ) — the given sequence. It is guaranteed that its elements are in non-decreasing order.

It is guaranteed that the sum of n over all test cases does not exceed  $5 \cdot 10^5$ .

### Output

For each test case, output n integers — the costs of sequences  $[a_1, a_2, \ldots, a_k]$  in ascending order of k.

### Sample 1

Lista 2 - Soma acumulada, Two pointers e STL Mar 29, 2023

Input	Output
3	1 1 2
3	1 1
1 2 3	1 2 3 4 5
2	
1 1	
5	
5 5 5 5 5	

### Note

In the first test case:

- The maximum score among the subsequences of [1] is 1. The subsequences [1] and [] (the empty sequence) are the only ones with this score. Thus, the cost of [1] is 1.
- The maximum score among the subsequences of [1,2] is 2. The only subsequence with this score is [2]. Thus, the cost of [1,2] is 1.
- The maximum score among the subsequences of [1, 2, 3] is 3. The subsequences [2, 3] and [3] are the only ones with this score. Thus, the cost of [1, 2, 3] is 2.

Therefore, the answer to this case is  $1\ 1\ 2$ , which are the costs of [1],[1,2] and [1,2,3] in this order.