



✓ Agent is everything that can be viewed as perceiving its environment through 'Sensor' & acting upon that environment through 'Actuators'.

ex -   
   • Human - eyes, ears, ... for sensor.  
    agent    - hand, legs, mouth... for actuators.

• Robotic agent - camera, infrared range finder.  
                  - various motors.

✓ PEAS - Performance measure, Environment, Actuators, Sensors

✓ Agent types - simple reflex: Only current situation  
• Goal based: Reaching until the goal.  
• Utility based: Same as goal based but provides extra component like best way to reach the goal.  
• Learning based: AI  
    ✓ Past experience also have learning capability.

## Searching

- tells agent what to do!
  - to achieve goals or to maximize our utility
  - why not Dijkstra?  $\Rightarrow$  D's algo only works on finite space.
- ✓ A problem defined by 5 states -
- ① initial state.
  - ② Actions .
  - ③ Transition model result
  - ④ Goal test.
  - ⑤ Path Cost .
- ✓ Search strategies -- by picking the order of node expansion. is the soln exist or not!
- . it follows - Completeness, Time Complexity , Optimality , Space ..
- ( least cost ) no of nodes generated  
                        ) max num of nodes  
                        in store.

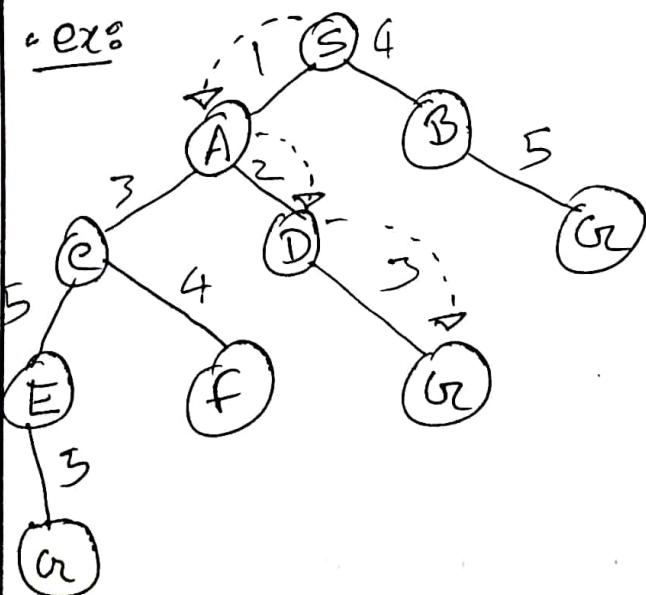
(D) (B)

Types of search algo - ① Blind ② Heuristic Search.

- Blind Strategies - • BFS, Uniform-Cost Search,  
/Uninformed search      DFS, Iterative deepening search,  
                              Bidirectional search.

✓ Uniform Cost Search = used for travelling a weighted tree or graph.

- Goal - find goal node which has lowest cost.
- Priority Queue ② lowest cost ③ BFS.
- Prob: in optimal



LAB : DS : ✓ Dictionary ✓  $\text{Int} \Rightarrow S = [^{\text{Value}}_0, "y"]$

✓ Tuple : • Value cannot be change as set.  
◦ Factor

student = ("n", "y", )

✓ Set : ① Curly braces ② set func

num1 = {1, 2, 3}

num2 = set([4, 5, 6])

num2.add(7)

func : ✓ len()

✓ append("x")

✓ insert(?, "OS")  
    ↓              ↑  
    index      string

✓ remove("OS")

✓ sort()

✓ reverse()

✓ pop() ← last item remove.

✓ copy

✓ count(),

✓ index(?) → position

OOP:

lab

✓ Class Student:

template - can use as,  
+ blue print

roll = ""

gpa = ""

Rahim = Student() ← Class Obj Create.

Rahim.roll = 101 ← value

Rahim.gpa = 3.5

Print(f"Roll: {Rahim.roll}, GPA: {Rahim.gpa}") .

# ✓ function

→ Points to current obj

def display(self):

Print(f"Roll: {self.roll}, GPA: {self.gpa}")

Rahim = Student()

Rahim.roll = 101

Rahim.gpa = 4.7

Rahim.display()

def setValue(self, roll, gpa):  
 self.roll = roll  
 self.gpa = gpa  
Rahim.setValue(101, 3.7)

lab

Constructor: • `-init-(self, roll, gpa)`

↳ self. no need to func to set value  
↳ Obj self का अपने value ही हो जाएँ

⇒ `def -init-(self, roll, gpa):`

`self.roll = roll`

`self.gpa = gpa`

`rahim=student(101, 3.75)`

ex (53)

The One Queue : • Priority queue

Inform Search : we know the goal  
 • heuristic - a func that estimate how close a state  
 is to a goal. (estimation)

✓ Greedy Search : • not optimal

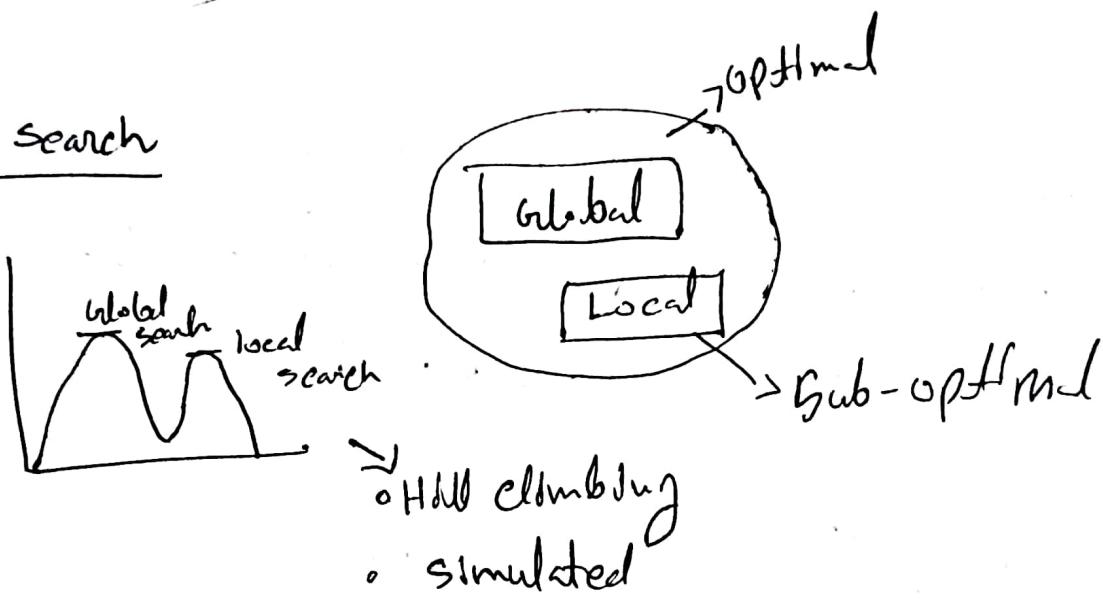
✓ A\* Search : • combination of UCS & Greedy  
 • Uniform-cost order by path cost.  
 •  $f(n) = g(n) + h(n)$   
 • A\* is optimal. \*

• Admissible Heuristics -  
 - in admissible (optimistic)  
 - estimate cost < true cost.

✓ Consistency of Heuristics : ✓

- admissible heuristic, Tree A\* in optimal } TIP
- +  
- consistent " , Graph A\* .. "
- +  
- . with  $h=0$  UCS " "
- (heuristic)

## → Local Search

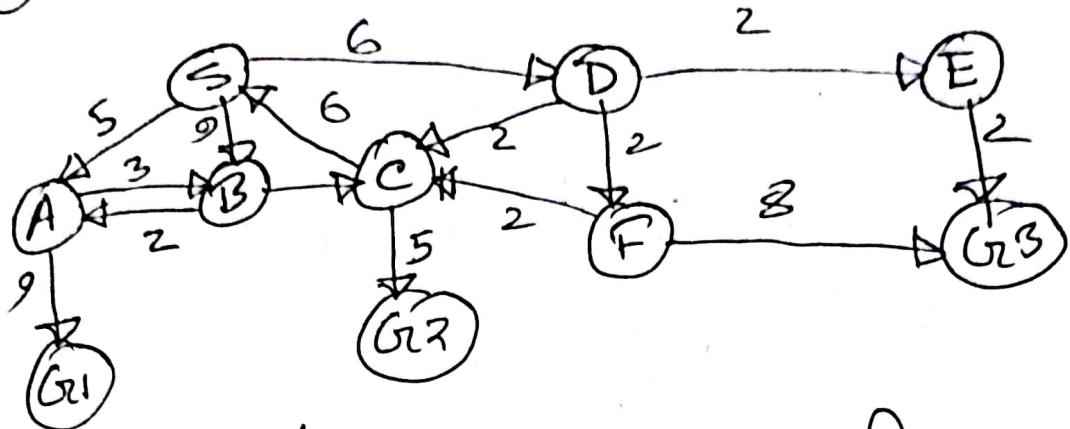


✓ graph - pure dr- obj

- BFS ~~as augt A\*~~ MAZE

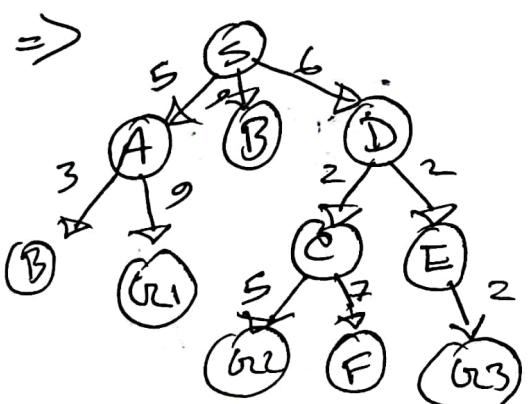
UniformCost Search:

?



We need to reach any one of the destination node ( $G_1, G_2, G_3$ ) starting from  $(S)$ . Find the path from  $S$  to any of these destination node state with the least cumulative cost?

=>



$$S \rightarrow B, \text{cost} = 9$$

$$S \rightarrow D, " = 6$$

$$S \rightarrow A \rightarrow B, " = 5 + 3 = 8$$

$$\cancel{S \rightarrow A \rightarrow G_1}, " = 5 + 9 = 14.$$

$$S \rightarrow D \rightarrow E, " = 6 + 2 = 8 ]$$

$$S \rightarrow D \rightarrow C, " = 6 + 2 = 8 ]$$

$$\cancel{S \rightarrow D \rightarrow C \rightarrow G_2} = 13 ]$$

$$S \rightarrow D \rightarrow C \rightarrow F, " = 15 ]$$

$$S \rightarrow D \rightarrow E \rightarrow G_3, " = 15$$

✓ DFS : LIFO

✓ Iterative deepening search :

• To avoid the infinite dept problem of DFS

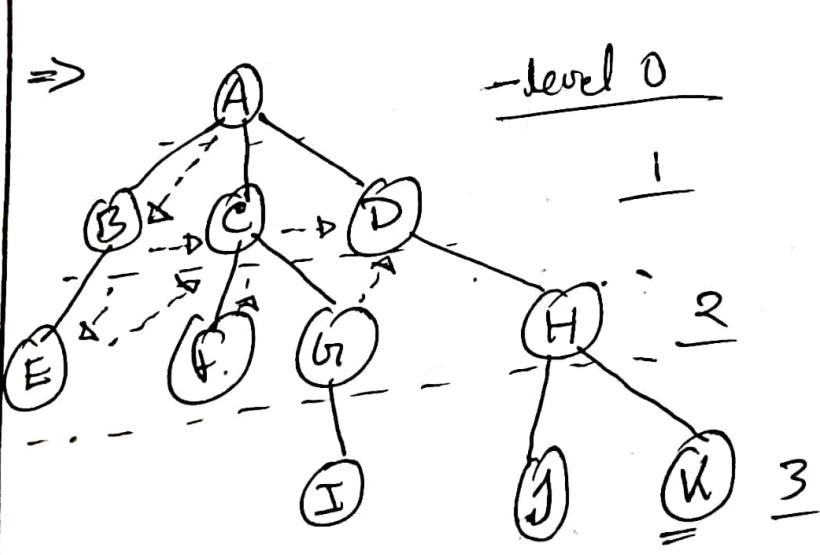
• Combination of BFS & DFS

↓ Pro: less memory.

{  
Pros - it will find goal node at any any  
cons - memory consuming.

so, Iterative finds goals at less memory.

• checks level-wise.



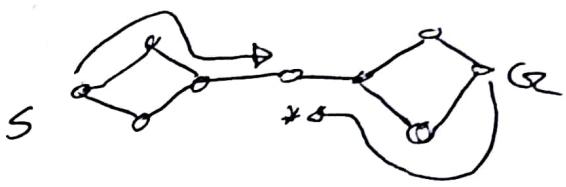
here, goal node = K

Depth level	IDS
0	A
1	A B C D
2	A B E C F G
3	D H
4	A B E C F G
5	I D H J K

NOTE: cons - Same node comes frequently.

## ❖ Bi-Directional Search

- Two simultaneous search from one initial node to goal and backward from goal to initial, stopping when two meet:
    - depth.
  - Time complexity:  $\approx (b^{d/2})$ 
    - breadth
- complete in BFS  
Not in DFS.



## Informed / heuristic search :

✓ Breadth-first, A\*

✓  $f(n) = g(n) + h(n)$

(estimate of total cont)  $\rightarrow$  path cont for n nodes. / estimate of cont to goal from n node.

Heuristics Search : note: a good heuristic can reduce the search process.

ex: 8 puzzle prob.-

1	2	3
4		6
7	5	8

start state

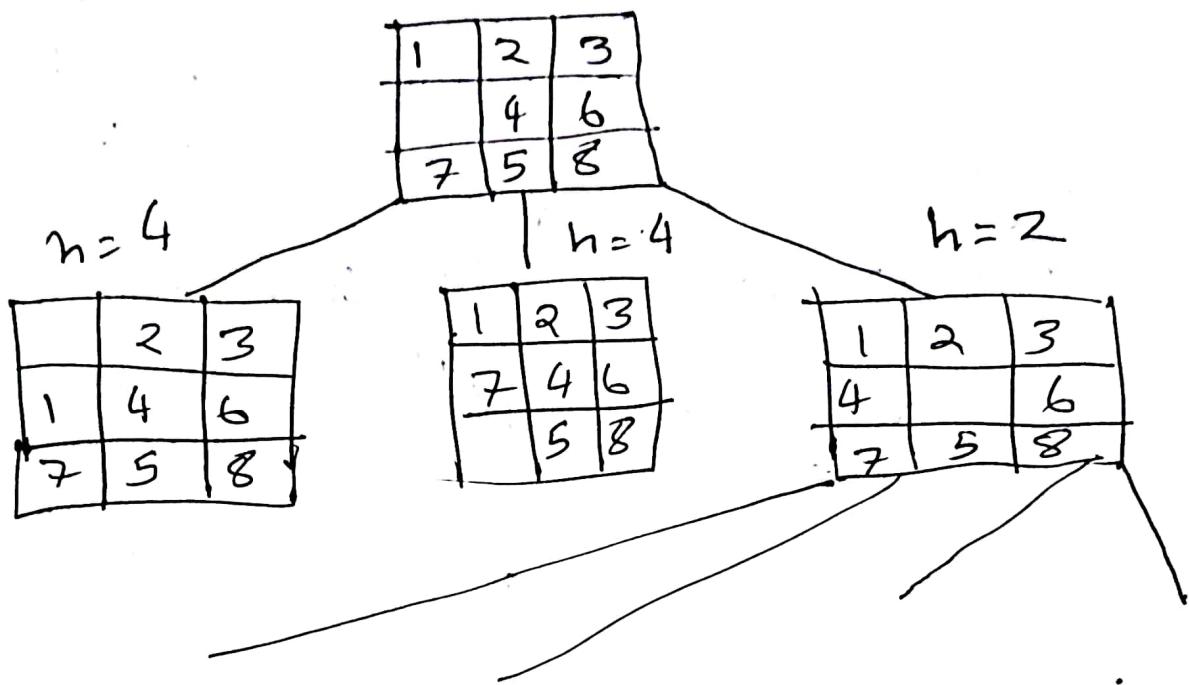
1	2	3
4	5	6
7	8	

goal state

here,  $h_1$  = num of misplaced tiles = 3

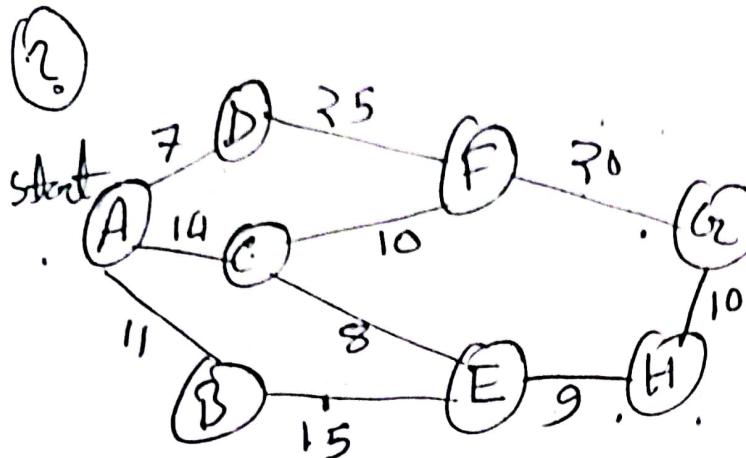
$h_2$  = Manhattan distance .

$$= 0 + 0 + 0 + 1 + 1 + 0 + 0 + 1 + 1$$



$\frac{\text{Nb}^o}{\star}$   
 Greedy approach  
 Best first Search .

## Breadth First Search



heuristic val

$$A \rightarrow h_A = 40$$

$$B \rightarrow h_B = 32$$

$$C \rightarrow h_C = 25$$

$$D \rightarrow h_D = 35$$

$$E \Rightarrow h_E = 19$$

$$F \rightarrow h_F = 17$$

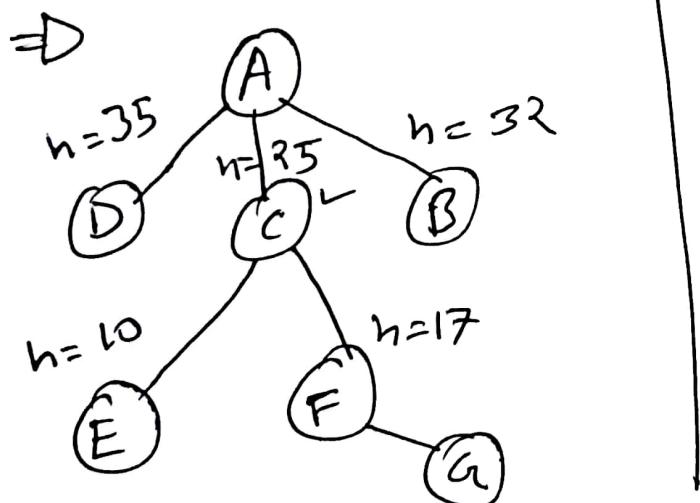
$$H \rightarrow h_H = 10$$

$$G \rightarrow h_G = 0$$

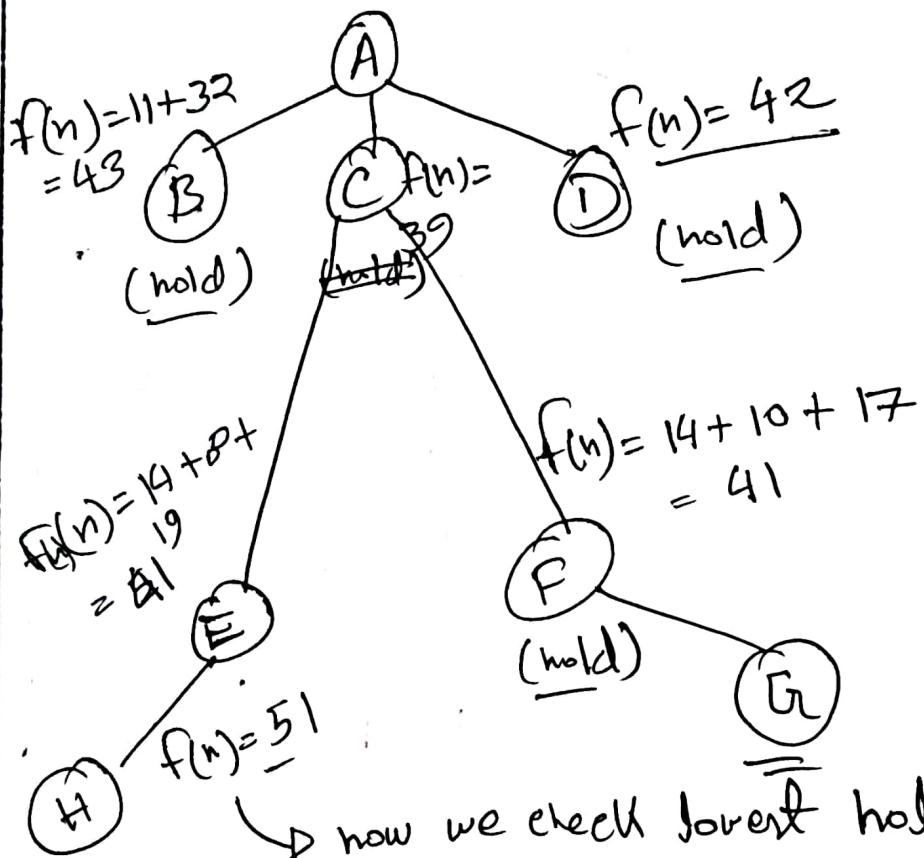
NOTE 2  $h(n) \Rightarrow$  Euclidean distance

$$(x_1, y_1) \& (x_2, y_2)$$

$$\Rightarrow \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



A\* Search  $\circledcirc$  (Same Graph)  $f(n) = g(n) + h(n)$



now we check forest hold, so we go to  $\frac{f}{c}$

it's an optimal solution.

A - c - f - G

( $* * *$   
+ char 5)

A\* algo: (admissible  $\rightarrow$  optimal)

✓ optimality of A\* Search:

optimal & i)  $h(n) >$  actual cost

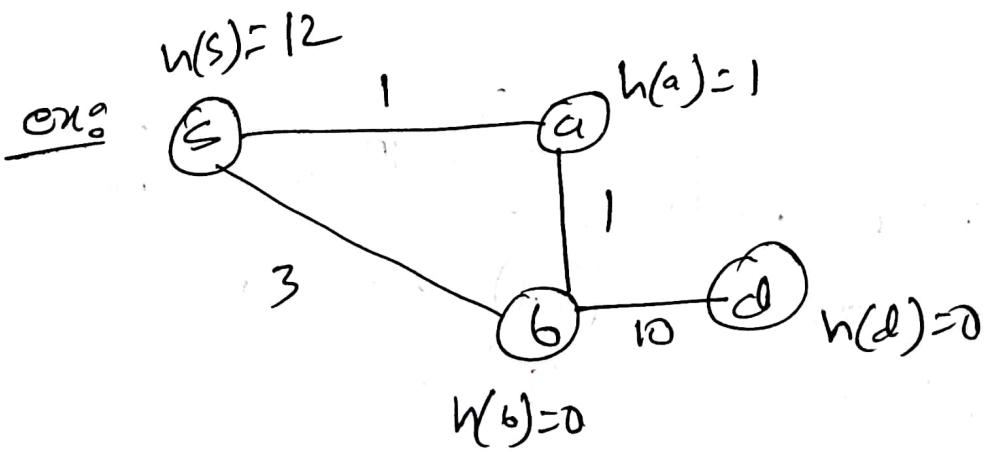
not optimal ii)  $h(n) = \text{actual cost}$

iii)  $h(n) \leq \text{actual cost}$

→ admissible heuristic

✓ consistent heuristic

$$h(n) \leq c(n, n') + h(n')$$



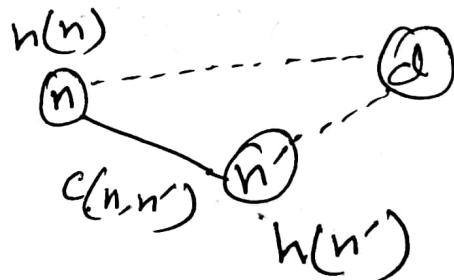
NOTE:

$$f(n) = g(n) + h(n)$$

$g(n)$        $=$        $h(n)$   
 estimated           actual  
 $h(n) \leq h^*(n) = \text{actual cost}$

Underestimation

$$h(n) \geq h^*(n) = \text{over-estimation}$$



$\therefore$  if  $h$  an admissible heuristic

cuz it follows  $h(n) < \text{actual cost}$ .

$\therefore$  ~~it's~~ check consistency  $\Rightarrow h(n) \leq c(n, n') + h(n')$

$$\therefore \text{so it's not consistent.} \quad \begin{aligned} s-a & 12 \leq 1 + 11 \\ s-b & 12 \geq 3 + 0 \quad (X) \end{aligned}$$

estimate val    actual val

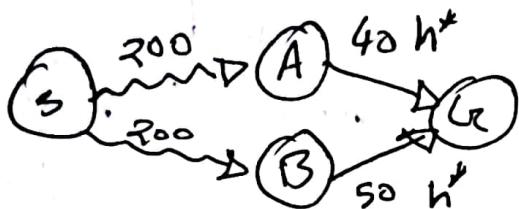
overestimate }  
↳ consistency }

\*  $h(n) \leq h^*(n) \Rightarrow$  Underestimation }

$h(n) \geq h^*(n) \Rightarrow$  Overestimation }

\*  $f(n) = g(n) + h(n)$

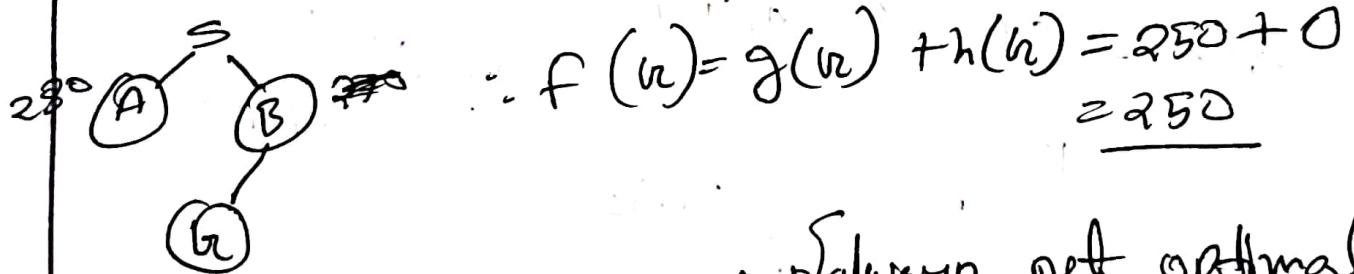
How to make A\* admissible :



here,  $g(A) = 200$  } actual cost  
 $g(B) = 200$  } Value

case 1 : (Overestimation)

let,  $h(A) = 80 \} > h^*$      $\therefore f(A) = 200 + 80 = 280$   
 $h(B) = 70 \} > h^*$      $f(B) = 200 + 70 = 270$



case 2 : (Underestimation)  $\rightarrow$  [always get optimal sol.]

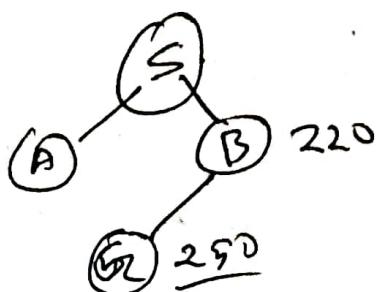
let,  $h(A) = 30$

$h(B) = 20$

$\therefore f(A) = 200 + 30 = 230$

$f(B) = 200 + 20 = 220$

$f(G) = 200 + 50 = \underline{250}$



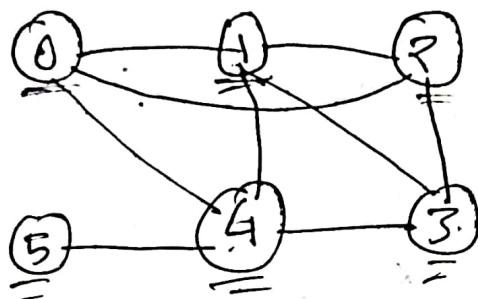
here, it will Backtrack and go to (A),

$\therefore f(G) = g(G) + h(G)$

[N: so we get optimal ans]     $= 200 + 40 = \underline{240}$   
 ↳ Inconsistent.    it's optimal.

DFS:

- (i) Stack
- (ii) Back tracking.



$\Rightarrow$

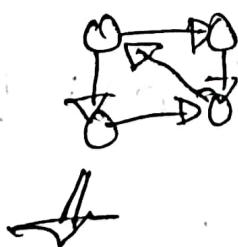


Result: 0, 1, 4, 5, 3, 2

SCC:

- (i) weakly
- (ii) strongly

undirected  $\leftrightarrow$  directed  
edge flip  
replace.



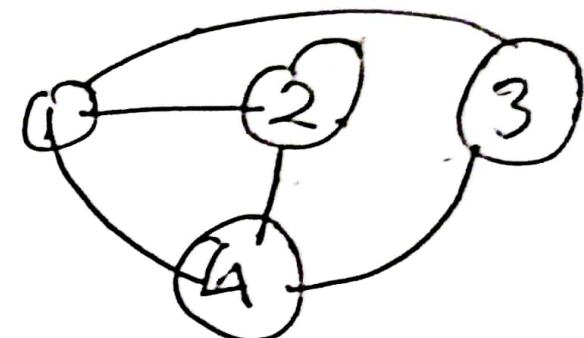
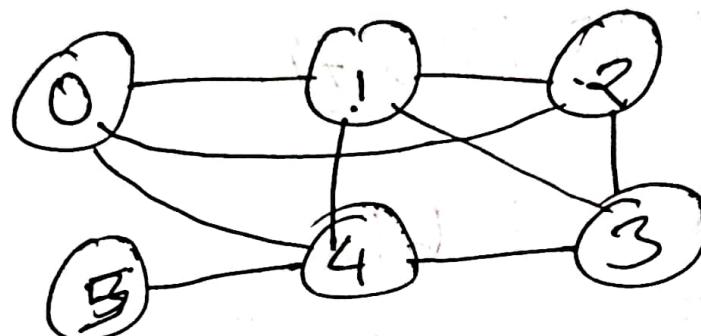
steps:

- 3 (i) Transpose  $G \rightarrow G^T$   $\Leftrightarrow G^T \leftarrow G$ .
- 3 (ii) DFS or component graph.
- 3 (iii)

BFS: ① Queue ② ए वर्टेक्स फिर काम करने वाले अज्य वर्टेक्स

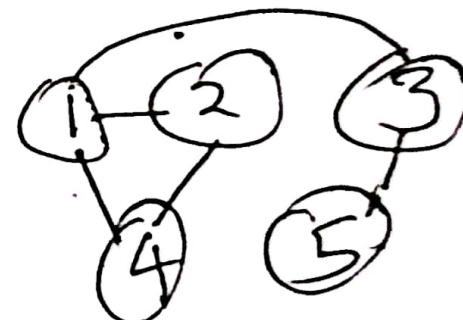
Queue पर insert ③ Visited vertices ~~कहा था~~ insert होगा.

④ Inserted vertices repeat होते हैं।



Queue: 0 → 1 → 2 → 3 → 5

Visited: 0 1 2 4 3 5



### Chap-4

AI:

local search  $\rightarrow$

- Hill climb.

- Simulate annealing.

- Gradient Descent.

- Local beam

- Genetic alg.

### Chap-5

Adversarial Search  $\rightarrow$

- game plan

- $\alpha-\beta$  pruning.

- Min/Max

### Chap-6

CSP  $\rightarrow$

- graph coloring.

- Crypto, Anthmatics.

(hypothesis  $\rightarrow$  heuristic func.)

### local Search:

④ 4 queens. ⑤ Hill Climbing.

→ local search algo are designed to explore search space systematically.

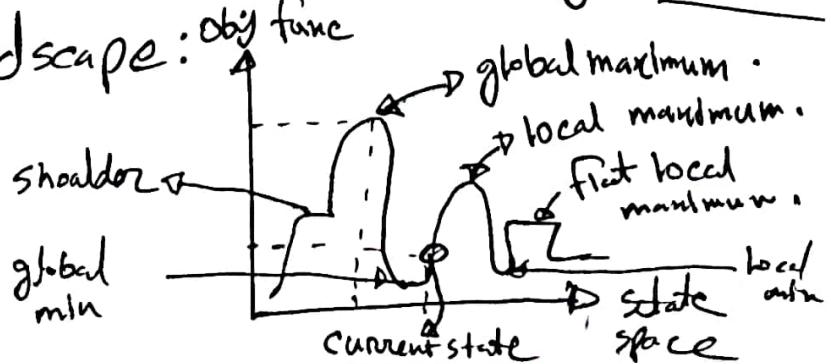
→ local search operate using a single current node (rather than multiple paths) and generally move only to neighbors of that node. The followed by the search are not retained Advantages -

① They are very little memory.

② They can often find reasonable solution in large or infinite (continuous) state spaces for which systematic algo's are unviable

NOTE: ✓ goal state  $\exists$ , object  $\exists$ , ✓ Obj  $\rightarrow$  optimize

✓ state-space  $\Rightarrow$  landscape:  $\begin{matrix} \text{Obj func} \\ \uparrow \end{matrix}$



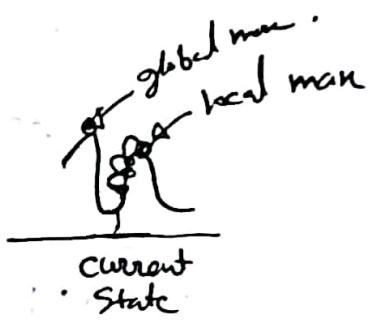
- - location - defined by state.
  - elevation - defined by the value of the heuristic cost function or objective function.
    - if elevation corresponds to cost, then the aim is to find the lowest valley - a global minimum.
    - if elevation corresponds to an objective function, then the aim is to find the height peak - global max.

## Hill Climb Search:

function hill climbing (problem) return a state  
that is a local maximum:

{ inputs: problem, a

local variable: current, a node  
neighbor, a node



current  $\leftarrow$  MAKE-NODE (INITIAL-STATE [problem])

loop do

neighbor  $\leftarrow$  a height- valued successor of current

if value [neighbor]  $\leq$  value [current] then

return STATE [current]

current  $\leftarrow$  neighbor.

}

✓ Hill climbing algo problems:

- local min
- flat max
- Ridge min

↳ To solve this issue -

• simulated annealing algo

## Simulated annealing search

- Idea: escape local maximum by allowing some "bad" moves but gradually decrease their frequency.

function:

- search function SIMULATED-ANNEALING(problem, schedule) returns a solution state
  - { inputs: problem, a problem schedule, a mapping from the time to 'temperature'

local variable: current, a node  
next, a node

T, a "temperature" controlling

problem of downward steps

current  $\leftarrow$  MAKE NODE (INITIAL-STATE [problem])

for  $t \leftarrow 1$  to  $\infty$  do

$T \leftarrow$  Schedule [ $t$ ]



if  $T=0$  then return current

next  $\leftarrow$  a randomly selected successor of current

$$\Delta E \leftarrow \text{VALUE}[\text{next}] - \text{VALUE}[\text{current}]$$

if  $\Delta E > 0$  then current  $\leftarrow$  next

else

current  $\leftarrow$  next only with probability  $e^{\frac{\Delta E}{T}}$

3

## Gradient Descent:

Assume we have cost function  $c(x_1, \dots, x_n)$

Target:

We want to minimize over continuous variable  $x_1, x_2, x_3, \dots, x_n$

Algorithm

Step 1: Compute the gradient:  $\frac{\partial c(x_1, \dots, x_n)}{\partial x_i}, \forall i$

Step 2: Take small step downhill in the

direction of the gradient:

$$x_i \rightarrow x'_i = x_i - \gamma \frac{\partial c(x_1, \dots, x_n)}{\partial x_i}, \forall i$$

where,  $\gamma$  is learning rate (hyper parameter)

Step 3: Check if  $c(x_1, \dots, x'_i, \dots, x_n) < c(x_1, \dots, x_i, \dots, x_n)$

If true then accept, if not reject.

Step 4: Repeat.

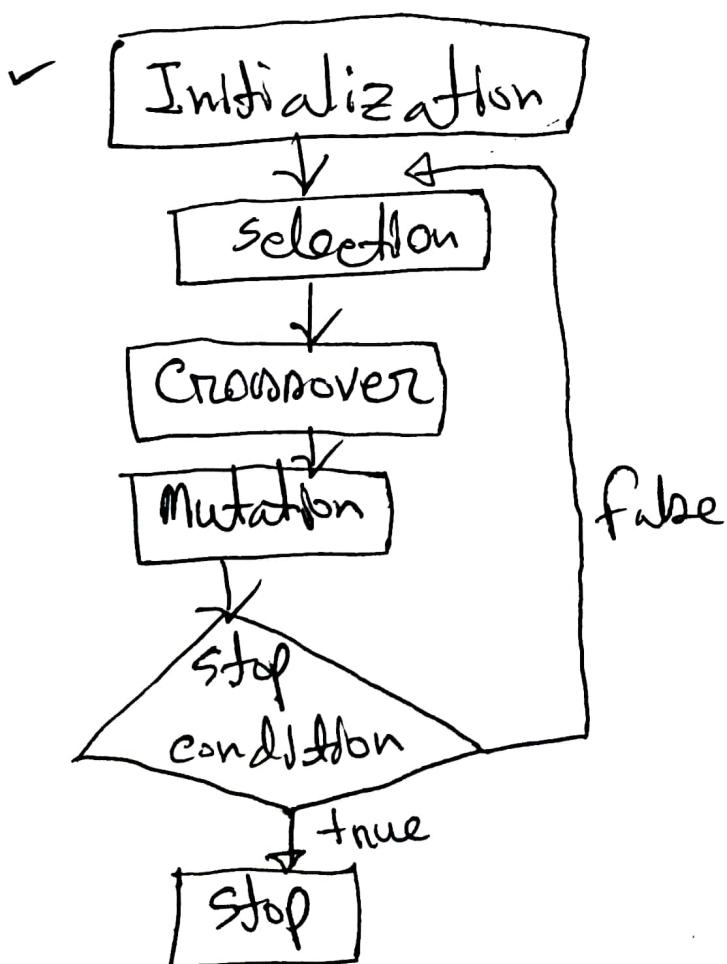
## Local beam Search :

- Take care of space complexity.
- Beam width ( $\beta$ ) is given.
  - how many choice / what / many path.
- If not complete



## Genetic algorithm

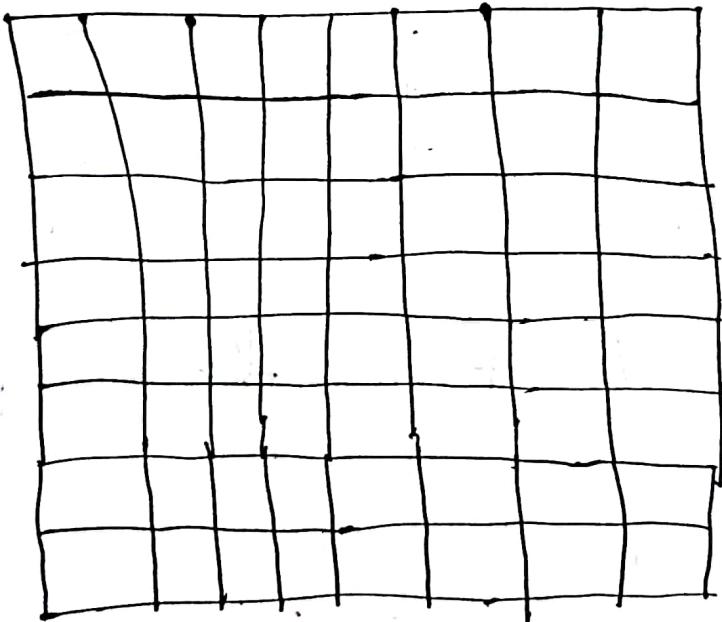
- Step 1: Initialize population.
- Step 2: Select according to fitness.
- Step 3: Crossover between selected chromosome.
- Step 4: Perform mutation.
- Step 5: Repeat output till the column condition of stop true.



fitness function: evaluates how given solution is to the optimal solution of the problem.

A function should return higher values for better state.

exercise: ⑧ queen's - solve with genetic algo!



Consider the following individual states for 8 queen problem. Perform genetic algorithm with the threshold of selection 16:

## W Adversarial Search:

Types of games:

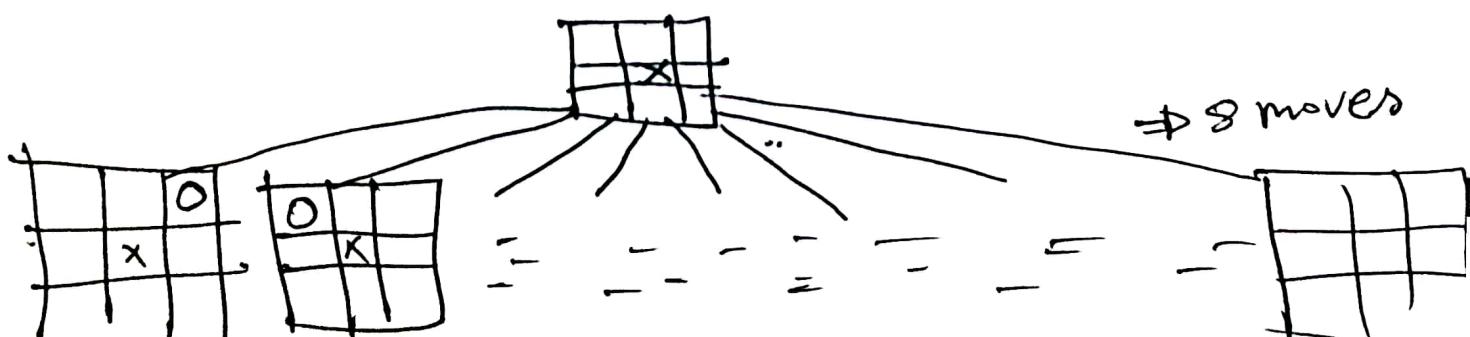
Perfect information	deterministic	chance
-On	even checkers,	monopoly, backgammon
Imperfect information	Battle-n-hp	budget poker

Typical assumption: □ Two agents whose action

alternate. Utility values for each agent; are opposite of the other.

- Fully observable environment.
- Generalize to stochastic games, multiple players, non-zero-sum etc.

Game tree (2 player deterministic turns)



here, how we search this tree to find the optimal move?

Games - adversary

solution in strategy.

\* strategy specify move for every possible opponent reply.

- Minimax search, an approx. solution.

- Evaluation function: evaluate "goodness" of game position.

example: chess, checkers, go etc.

## Games as Search

Two players: Max and MIN

+ Max moves first and they take turns

Until game is over.

- Winner gets reward and looser gets penalty.
- "Zero-Sum" = sum of reward and penalty is constant.
- Formal definition as a search problem:
  - ° Initial state: setup specified by the rules  
eg. initial board configuration of chess.

- ° Player(s): Defines which player has the move in a state.
- ° Action(s): Returns the set of legal moves in a state
- ° Result: transition model defines the result of a move
- ° Terminal test: Is the game finished?

True if finished.

- Utility function: Gives numerical values of terminal state  $s$  for player  $p$ .

for example:  $\text{win}(+1)$ ;  $\text{lose}(-1)$  and  $\text{draw}(0)$

as shown in the tac toe.

{ Backtracking - Best Move Strategy - Min-Max }

D  
• Max  $\Rightarrow$  Utility will be max (Best Move) • Min  $\Rightarrow$  Worse Move

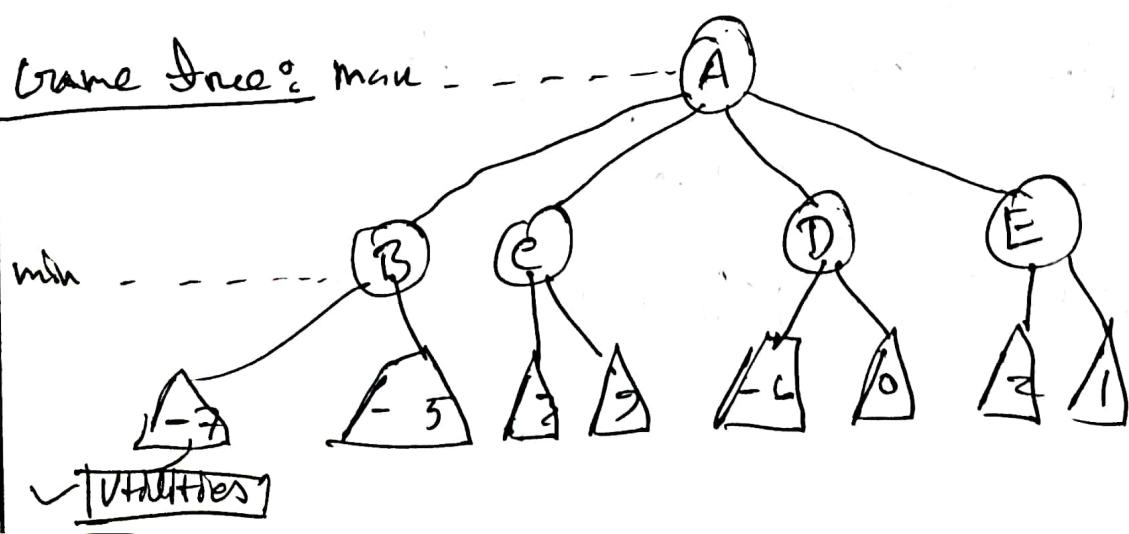
C-3

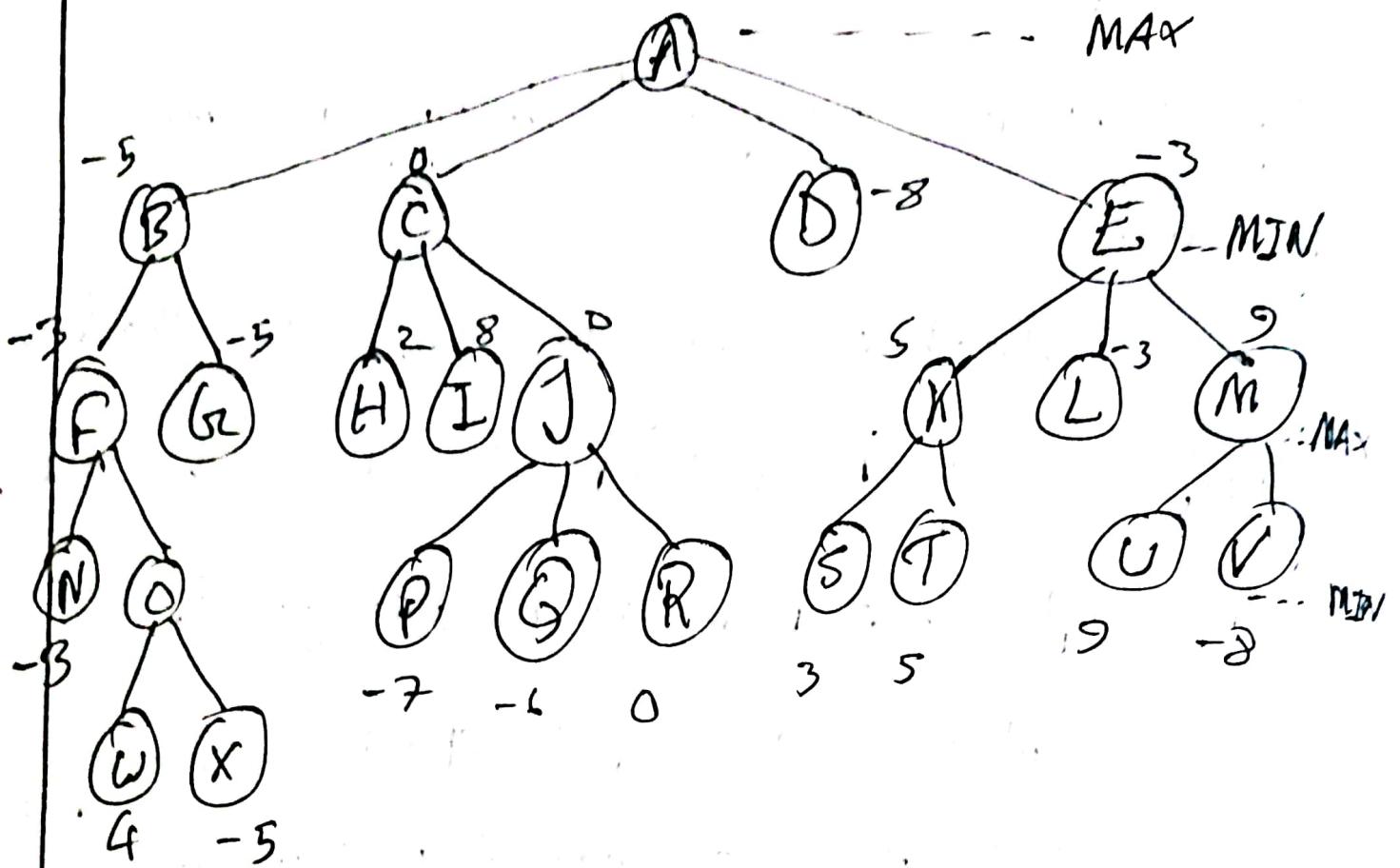
### Min-Max procedure:

Designed to find the optimal strategy for max and find best move:

- i) Generate the whole game tree, down to the leaves.
- ii) Apply utility (Payoff) function to each leaf.
- iii) Back-up values from leaves through branch nodes.
  - a Max node computes the max of its child
  - a Min node computes the min of its child values.
- iv) At root: choose the move leading to the child of highest value.

Game Tree: Max - - -





$A \rightarrow C \rightarrow J \rightarrow R \circlearrowleft$

Po position of minimax

- Complete? Yes.
- Optimal? Yes. :  $\underbrace{\text{num of node}}$ .
- Time complexity?  $(b^m)$
- Space complexity?  $O(bm)$

## Static (Heuristic) Evaluation function:

An Evaluation function:

- Estimate how good the current board configuration is for a player.
- Chen: Value of all white pieces.
  - value of all black pieces.

For Chen, typically linear weight sum of features

$$\text{Eval}(s) = w_1 f_1(s) + w_2 f_2(s) + \dots + w_n f_n(s)$$

Heuristic in  $E(n) = M(n) - O(n)$

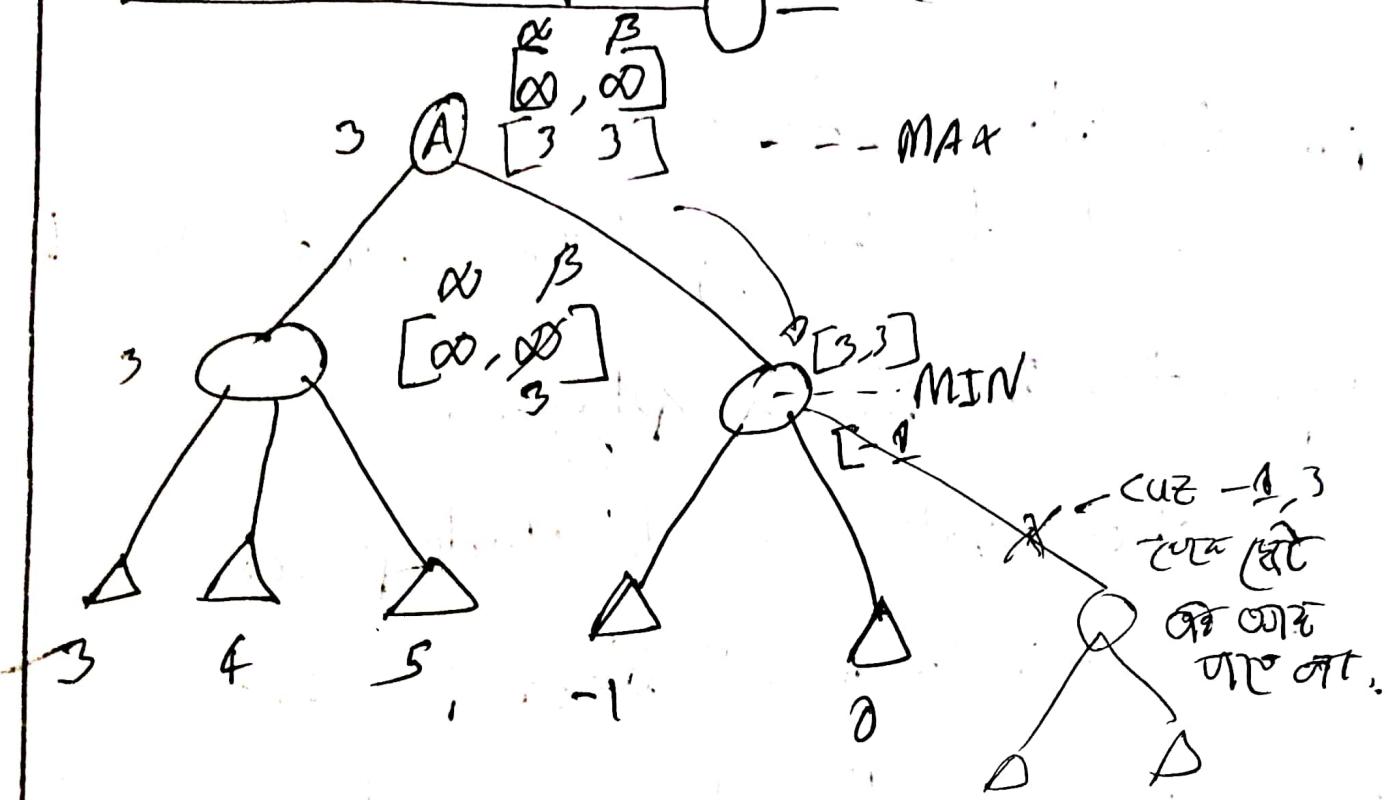
Where,  $M(n)$  in the total of my possible winning line.

$O(n)$  in total of opponent possible winning line,

$E(n)$  in the total Evaluation for state  $n$ .

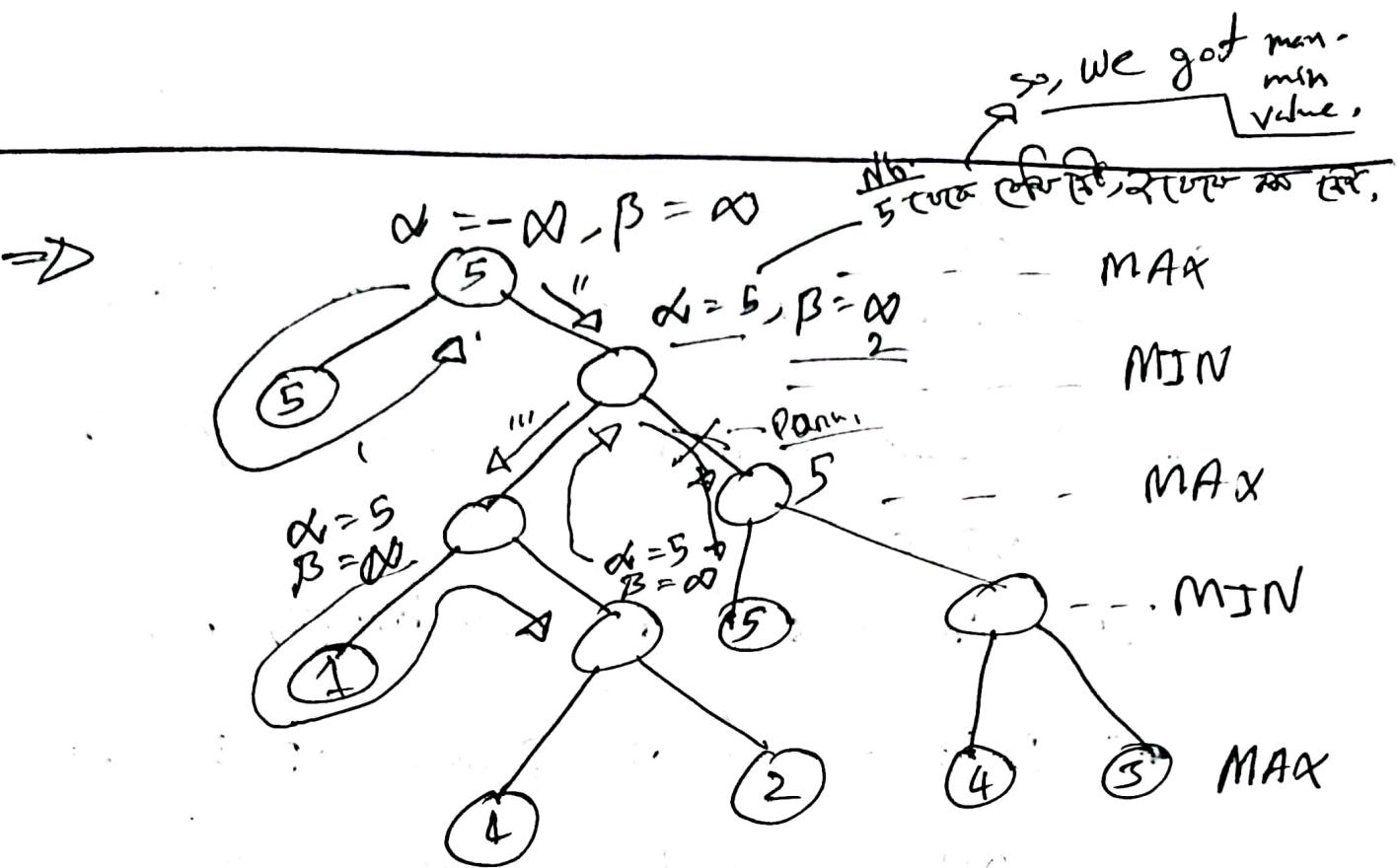
← Update version of min-max algo.  
- DFS

④ Alpha-Beta pruning :- (DFS).



□ What is the min-max value of the root node for the game tree below?

Annotating that if performs a DFS that always generates the left most child node first and a  $\text{lo}(\text{and } \text{hi})$  of  $\text{Max}(\text{and } \text{Min})$  corresponds to a value of  $-\infty$  ( $\text{and } \infty$ , respectively) determines the alpha and beta values of the remaining node(s).



the minimum value is 5.

NOTE: In minimax we have to explore every nodes  
the time complexity will be  $O(b^d)$ ; So we can  
cut off the search by exploring less no. of nodes

# condition  $\Rightarrow$   $\boxed{\alpha \geq \beta}$   $\rightarrow$  then we will Prun. ✓

- Max  $\Rightarrow \alpha$
- Min  $\Rightarrow \beta$

~~W~~ constraint

## Constraint Satisfaction Problem (CSP)

\* CSP ~~consist~~ consists of three components

V, D, C

→ V is a set of variables  $\{V_1, V_2, \dots, V_n\}$

→ D is a set of Domains  $\{D_1, D_2, \dots, D_n\}$   
one for each variable <sup>(types)</sup>.

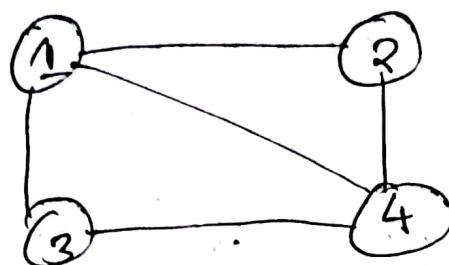
→ C is set of constraints that  
specifies combination of values,  
 $c_i = (\text{Scope}, \text{Rel})$

Where, Scope is set of variables that  
participate in constraint.

Rel is relation that defines the  
value that variable can take.

(Chap - 15 - 7)

Graph coloring problem: • Backtracking in intelligent way.



$$V = \{1, 2, 3, 4\}$$

$$D = \{\text{Red, Green, Blue}\}$$

$$C = \{1 \neq 2, 1 \neq 3, 1 \neq 4, 2 \neq 3, 2 \neq 4, 3 \neq 4\}$$

$$\{2 \neq 4, 3 \neq 4\}$$

↓ initial step

	1	2	3	4
Initial Domain	R, G, B	R, G, B	R, G, B	R, G, B
1 = R	R	G, B	G, B	G, B
2 = G	R	G	B	B
3 = B	R	G	B	B
4 = G	R	G	G	B

Note: Here,  $1 \neq 2, 1 \neq 3, 1 \neq 4$   
so, the color in intell 2, 3, 4  
will be GB, GB, GB.

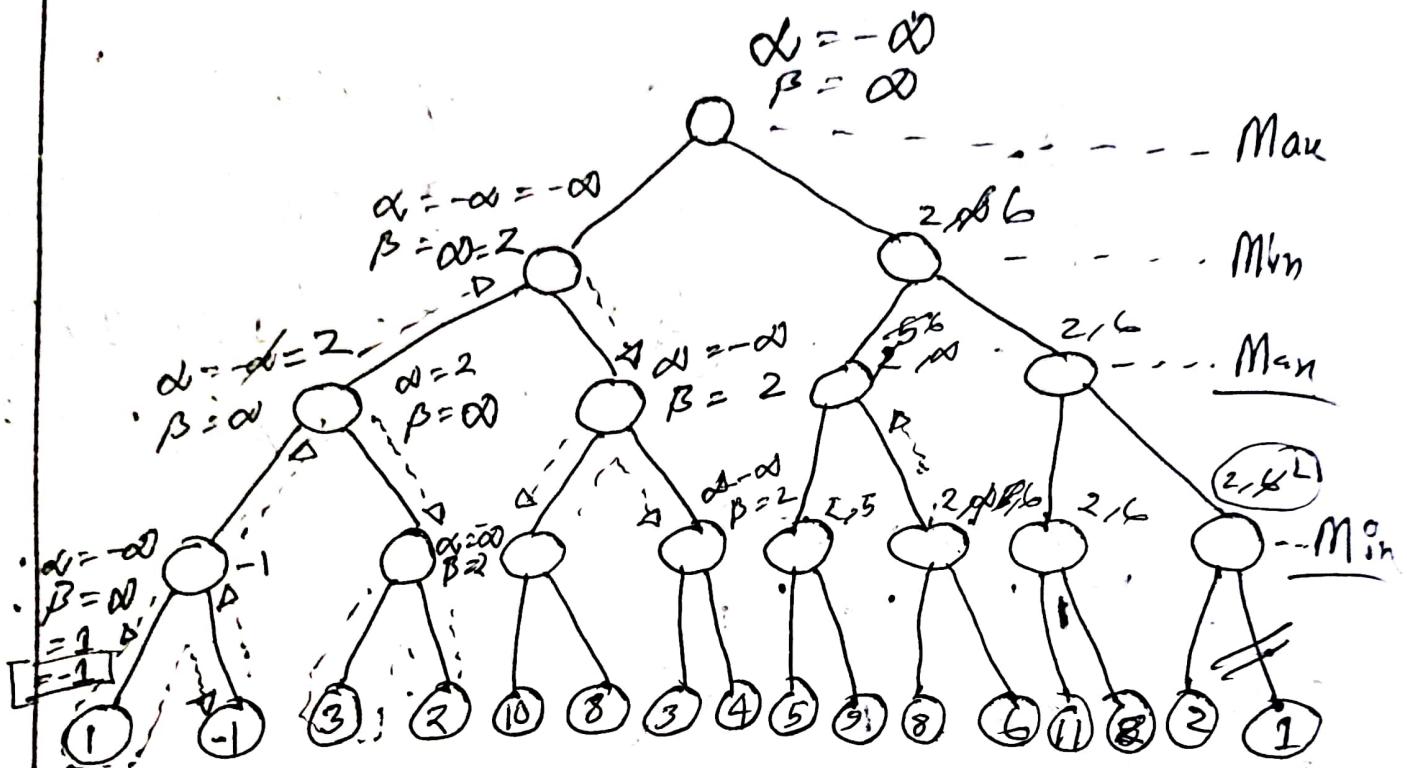
Note: here, 1 is fixed for R

here, in ④ in red  
case back track  
as it's empty.

here, no neighbour colour  
is not same.

Back Track

## αβ<sup>c</sup> (Alpha-Beta pruning)



→ Condition: here,  $\alpha$  = value of best choice so far for Max (right)  
 $\beta$  = value of best choice so far for Min. (left)

Prune when,  $\alpha \geq \beta$ .

✓ (CSP)

## Cryptarithm problems

→ Digits that can be assigned to a wordly alphabet

→ Range - (0-9)

→ Construction :-

\* No two letter have same value

\* sum of digit must be as shown in problem.

\* There should be only one carry-forward.

$$\begin{array}{r} \text{@no } 0 \text{ TO} \\ \text{a0} \\ \hline \text{OUT} \end{array}$$

⇒

$$\boxed{2}_T \quad \boxed{1}_0$$

T → 2

0 → 1

a → 8

v → 0

$$\begin{array}{r} \boxed{8}_a \quad \boxed{1}_v \\ \hline \boxed{1}_0 \quad \boxed{0}_u \quad \boxed{2}_r \end{array}$$

③ SEND

MORE

-----  
MONEY

$$\Rightarrow \begin{array}{r} 2_s \ 5_E \ \underline{\underline{3_N}} \ 7_D \\ + 1_M \ 0_O \ 8_R \ 5_E \\ \hline \end{array}$$

$$\begin{array}{r} 1_M \\ 0_O \ 0_N \ 5_E \ 5_T \\ \hline \text{carry} \end{array}$$

④ SOME

+ TIME

-----  
S P E N T

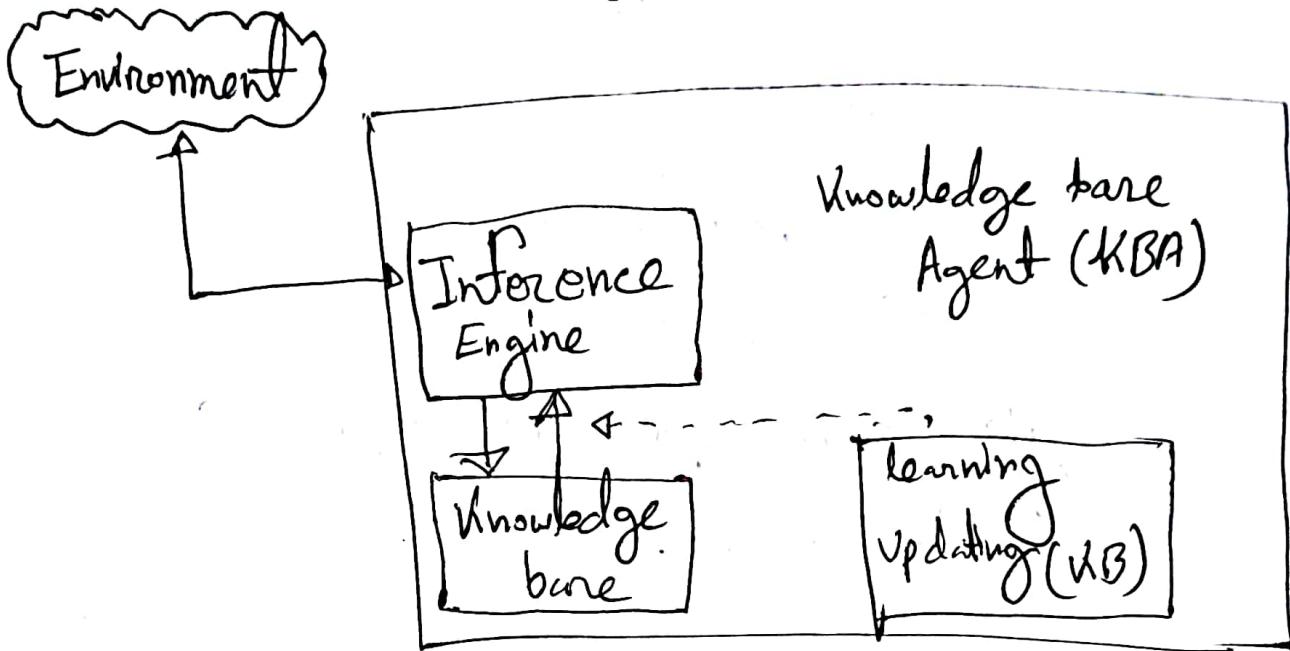
$$\Rightarrow \begin{array}{r} 4_s \ 9_o \ 3_m \ 4_E \\ + 8_T \ 5_I \ 3_m \ 4_E \\ \hline \end{array}$$

$$\begin{array}{r} 1_s \ 0_p \ 4_E \ 6_n \ 8_T \\ \hline \end{array}$$

## Chap-8

Final

⇒ Knowledge base and Agent :-



Operations perform by KBA :-

- (i) Tell : This operation tells KB agent that precise from the environment.
- (ii) ASK : This operation tells → what action it should perform .
- (iii) Perform / Action : If perform the selected ACTION!

Formal Symbol System :

- Ontology.

- Representation.

- Inference.

- symbol correspond to things / ideas  
in the world.

- pattern matching & rewrite corresponds  
to inference.

Ontology → (what exists in world)  
 $(\wedge \vee !)$  → defines meanings of symbol.

→ logic representation ontology.

{  $\wedge$ : and,  $\vee$ : or,  $!$ : not }

Representation : Syntax Vs semantics.

$\subseteq$  : if  $(a > 0) \{ \dots \}$

else  $\{ \dots \}$

## ✓ Inference

Schema vs Mechanism

Proof steps      search strategy

✓ Knowledge base Agent:

- KB = Knowledge Base

- A set of sentences or facts

- A set of statement in a logic language

- Inference

- Deriving new sentences from old.

- A simple model for reasoning

- Agent is told or perceives new evidence.

- Agent then infer new facts to add the KB.

ex:  $A, B \text{ logic} \rightarrow A \vee B \text{ infer}$   
 $A \text{ in } T \wedge B \text{ in } T \rightarrow T$ .

## Approaches to Knowledge Representation:

### i) Inferential Knowledge.

→ EWU is a university, Propositional logic

→ All student curail in CSE,

Predicate logic.

### ii) Inheritable Knowledge:

→ OOP.

### iii) Simple Relational Knowledge:

→ DBMS.

### iv) Procedural Knowledge.

→ USE of small code with If-else condition.

## (1) Logical Representation:

Types of logic:

- \* propositional logic
- \* Predicate logic (first order logic, )

first order predicate calculus )

Predicate:

{ for all  $x : \forall x \{$

for one  $x : \exists x \}$

\* Fuzzy logic

\* Probability

\* Temporal logic.

\* Moral logic .

## Wumpus world PEAS description:

		breeze	PIT
wumpus		PIT	breeze
stink		breeze	
start	Bree-ze	PIT	Bree-ze

### \* Performance measure:

- gold: +1000, death: -1000
- -1 per step, -10 for using the arrow

### \* Environment

- squares adjacent to wumpus are smelly.
- squares adjacent to pit are breezy.

- Gritter iff gold in in-the-name square.
- shooting Killn.wumpone if u are facing it.
- shooting men up only the arrow.
- Gerabing picks up gold if in name square.

\* Sensor: Stench, Breeze, Gritter, Scream

\* Actuators: left turn, Right turn, forward, runb, Release, shoot.

□ We used logical reasoning to find the gold.

Entailment: It means that one thing follows from another:  $KB \models \alpha$ .

e.g. "Mary is Sue's sister and Amy is sue daughter"

entail - "Mary is Amy's aunt!"

## Models:

We say  $m$  is model of a sentence  $\alpha$  if  $\alpha$  is true in  $m$ .  
 $M(\alpha)$  is the set of all model of  $\alpha$ .

Then  $KB \models \alpha$  iff  $M(KB) \subseteq M(\alpha)$ .

e.g. Brazil won the WC in 2002 and Italy won in 2006.

$\alpha = \text{Brazil won}$

think of  $KB$  and  $\alpha$  as collection of constraints and model  $m$  as possible states.

$M(KB)$  are the sol of  $KB$  &

$M(\alpha)$  the sol of  $\alpha$

Then  $KB \models \alpha$  when all sol to  $KB$  are also sol to  $\alpha$ .

Recap:

### # Propositional logic:

Syntax: The propositional symbols  $P_1, P_2$  are sentences -

- ✓ If  $s$  is a sentence,  $\neg s$  is a sentence (negation)
- ✓ If  $s_1$  &  $s_2$  are sentence,  $s_1 \wedge s_2$  is a sentence (conjunction)
- ✓ " " " " ,  $s_1 \vee s_2$  in a sentence (disjunction).
- ✓ " " " " ,  $s_1 \Rightarrow s_2$  in a sentence (implication)
- ✓ " " " " ,  $s_1 \Leftrightarrow s_2$  " " (biconditional).

### Semantics:

Each model/world specifies true or false.

for each proposition symbol.

For example,  $P_1$  or  $P_2$  is false.

with respect to

---

Rules for evaluating truth w.r.t a model, m:

$\neg s$  is true iff  $s$  is false.

$s_1 \wedge s_2$  is true if  $s_1$  is true and  $s_2$  is true. ~~s $\neq$~~

$s_1 \vee s_2$  " " " or " " "

$s_1 \Rightarrow s_2$  " true  $s_1$  is false or  $s_2$  is true

~~$s_1 \leftrightarrow s_2$~~  " <sup>false</sup> iff  $s$  is true and  $s_2$  is false.

$s_1 \leftrightarrow s_2$  is true iff  $s_1 \Rightarrow s_2$  is true and

$s_2 \Rightarrow s_1$  " true.

Suppose,  $P_1 = \text{true}$

$P_2 = \text{true}$

$P_3 = \text{false}$

For arbitrary sentence,

$$\begin{aligned}\neg P_1 \wedge (P_2 \vee P_3) &= \text{false} \wedge (\text{true} \vee \text{false}) \\ &= \text{false} \wedge \text{true} = \text{false}\end{aligned}$$

## Truth Table 2

in always true when premises  
are false  
 $P \rightarrow Q$   
(implication)

P	Q	$\neg P$	$P \wedge Q$	$P \vee Q$	$P \Rightarrow Q$	$P \Leftarrow Q$
F	F	T	F	F	T	T
F	T	T	F	T	T	F
T	F	F	F	T	F	F
T	T	F	T	T	T	T

## logical equivalence:

two sentences are logically equivalent iff they are true in some model.

$$\alpha \equiv \beta \text{ if } \alpha \models \beta \text{ & } \beta \models \alpha$$

$\rightarrow (\alpha \wedge \beta) \equiv (\beta \wedge \alpha)$  commutativity of  $\wedge$

$\rightarrow (\alpha \vee \beta) \equiv (\beta \vee \alpha)$  " of  $\vee$

$\rightarrow ((\alpha \wedge \beta) \wedge \gamma) \equiv (\alpha \wedge (\beta \wedge \gamma))$  associativity of  $\wedge$

$$\rightarrow (\alpha \wedge \beta) \vee \gamma \equiv (\alpha \vee (\beta \vee \gamma)) \text{ .. } \Leftarrow \text{f } \checkmark$$

$$\rightarrow \neg(\neg \alpha) \equiv \alpha \text{ double negation elimination.}$$

$$\rightarrow (\alpha \Rightarrow \beta) \equiv (\neg \beta \Rightarrow \neg \alpha) \text{ contraposition.}$$

$$\rightarrow (\alpha \Rightarrow \beta) \equiv (\neg \alpha \vee \beta) \text{ implication elimination.}$$

$$\rightarrow (\alpha \Leftarrow) \equiv ((\alpha \Rightarrow \beta) \wedge (\beta \Rightarrow \alpha)) \text{ bi-conditional elimination.}$$

$$\rightarrow \neg(\alpha \wedge \beta) \equiv (\neg \alpha \vee \neg \beta) \text{ de morgan}$$

$$\rightarrow \neg(\alpha \vee \beta) \equiv (\neg \alpha \wedge \neg \beta) \text{ de morgan}$$

$$\rightarrow (\alpha \wedge (\beta \vee \gamma)) \equiv ((\alpha \wedge \beta) \vee (\alpha \wedge \gamma))$$

distributivity of  $\wedge$  over  $\vee$

$$\rightarrow (\alpha \vee (\beta \wedge \gamma)) \equiv ((\alpha \vee \beta) \wedge (\alpha \vee \gamma)) \text{ distributivity of } \vee \text{ over } \wedge.$$

Validity and satisfiability:

A sentence is valid if it is true in all models.

e.g.: True,  $A \vee \neg A$ ,  $A \Rightarrow A$ ,  $(A \wedge (A \Rightarrow B)) \Rightarrow B$

Validity is connected to inference via

the deduction theorem  $\mathcal{KB} \models \alpha$  if and only if  $(\mathcal{KB} \Rightarrow \alpha)$  is valid.

A sentence is satisfiable if it is true in some model.

A sentence is unsatisfiable if it is false in all models.

Satisfiability: is connected to inference via following:

$KB \neq \alpha$  iff  $(KB \wedge \neg \alpha)$  is unsatisfiable.

(There is no model for which  $KB = \text{true}$  &  $\alpha = \text{false}$ )

# Problem?

Find whether the meaning of the statement  
is true or false -

"If the earth moves round the sun or the  
~~sun moves~~ sun moves round the earth, then copernicus  
might be a mathematician  $\text{but}$  was ~~not~~ <sup>not</sup> an  
astronomer."

$\Rightarrow P = \text{the earth moves round the sun} = \text{True}(T)$

$q = \text{Sun} \quad \text{"} \quad \text{"} \quad \text{earth} = F$

$R = \text{copernicus might be a mathematician} = T$   
 $S = \text{"} \quad \text{was an astronomer} = T$

~~P~~  $\rightarrow$  Propositional logic  $\Rightarrow$

$$(P \vee Q) \Rightarrow (R \wedge \neg S)$$

$$\vdash (T \vee F) \Rightarrow (T \wedge \neg T)$$

$$\vdash T \Rightarrow (F \wedge F)$$

$$\vdash T \Rightarrow F$$

$$\vdash F$$

In spite of having French nationality,

B. Russel was a critic of imperialism,

then either he was not a bachelor or  
he was a mathematician.

$\Rightarrow P = B.$  Russel has French nationality  $= T$ .

$q = B.$  Russel was a critic of imperialism  $= T$ .

$R = B.$  Russel was a bachelor  $= T$ .

$s = B.$  Russel was a mathematician  $= T$ .

$$(P \wedge Q) \Rightarrow (\neg \neg P \vee \neg Q)$$

$$= (\top \wedge \top) \Rightarrow (\neg \top \vee \top)$$

$$= F \Rightarrow (F \vee \top)$$

$$= \top \Rightarrow \top$$

$$= \top.$$

To Prove that,  $\neg(P \vee (\neg P \wedge Q)) \equiv \neg P \wedge \neg Q$   
 $\equiv \neg(P \vee Q)$

s.t.  $\neg(P \vee (\neg P \wedge Q))$

$$= \neg P \wedge \neg(\neg P \wedge Q) \quad [\text{De morgan}]$$

$$= \neg P \wedge (P \vee \neg Q) \quad [\text{Double negation} \& \\ \text{De morgan}]$$

$$= (\neg P \wedge P) \vee (\neg P \wedge \neg Q) \quad [\text{Distributive} \\ \text{property}]$$

$$= F \vee (\neg P \wedge \neg Q)$$

$$\begin{aligned}
 &= \neg P \wedge \neg Q \\
 &= \neg(P \wedge Q) = 
 \end{aligned}$$

## Inference 2

NOTE: KB Agent

→ Knowledge representation.

- propositional logic

new logic using old logic on evidence

so, generating the conclusion from evidence and facts is termed as inference.

- inference rules are the templates for generating valid arguments. Inference rules are applied to derive proofs at AI, and the proof is a sequence of the conclusion that leads to the goal.

\* implication :  $P \rightarrow Q$

\* converse :  $Q \Rightarrow P$  (opposite of implication)

\* contrapositive :  $\neg Q \Rightarrow \neg P$

\* Inverse :  $\neg P \Rightarrow \neg Q$  (opposite of contrapositive)

P	Q	$P \Rightarrow Q$	$Q \Rightarrow P$	$\neg Q \Rightarrow \neg P$	$\neg P \Rightarrow \neg Q$
T	T	T	T	T	T
T	F	F	T	F	T
F	T	T	F	T	F
F	F	T	T	T	T

From truth table, we can prove

$P \rightarrow Q$  is equivalent to  $Q \Rightarrow \neg P$  and  $Q \Rightarrow P$  is equivalent to  $\neg P \Rightarrow \neg Q$ .

Class - 2

# let  $P, Q$  and  $R$  be the proposition

$P$ : Grizzly bears have been seen in the area.

$Q$ : Hiking is safe on the trail

$R$ : Berries are ripe along the trail.

write - three proposition using  $P, Q$  and logical connection,

(a) Berries are ripe along the trail but grizzly bears have not been seen in the area

$$P. \text{Logic} = R \wedge \neg P$$

(b) Grizzly bears have not been seen in the area and hiking on the trail is safe but berries are ripe along the trail.

$$P. \text{logic} = \neg P \wedge Q \wedge R.$$

② If berries are ripe along the trail, hiking is safe if and only if grizzly bears have not been seen in the area.

$$\text{P. logic: } r \Rightarrow (\neg g \leftrightarrow \neg p)$$

③ It is not safe to hike on the trail but grizzly bear have not been seen in the area and the berries along the trail are ripe.

$$\Rightarrow \neg g \wedge \neg p \wedge r$$

## Types of inference rules -

① Modus ponens: One of the most essential law of inference in the modus ponens rule which asserts that if  $p$  and  $p \Rightarrow q$  are both true, we can infer that  $q$  will be true as well.

Notation of modus ponens =  $\frac{P \Rightarrow Q, P}{Q}$

e.g. "If I am sleepy then I go to bed"

$$P \Rightarrow Q$$

I am sleepy =  $P$  premise

I go to bed =  $q$  conclusion.

Hence, we can say that if  $P \Rightarrow Q$  is true and  $P$  is true then  $q$  will be true

$P$	$Q$	$P \Rightarrow Q$
0	0	0
0	1	1
1	0	0
1	1	1

(6) Modus Tollens: If  $P \Rightarrow Q$  is true and  $\neg Q$  is true then  $\neg P$  will also be true.

Notation modus Tollens =  $\frac{P \Rightarrow Q, \neg Q}{\neg P}$

Premise: I do not go to the bed  $\neg Q$

Conclusion: which infers that I am not sleepy  
 $\neg P$

$\neg P$	$\neg Q$	$P \Rightarrow Q$	$\neg P$	$\neg Q$
0	0	0	1	1
0	1	1	1	0
1	0	0	0	1
1	1	1	0	0

(iii) Hypothetical syllogism:

If  $P \Rightarrow Q$  is true whenever  $P \Rightarrow Q$  is true

and  $Q \Rightarrow R$  is true

"If you have my home key then you can unlock my home."  $P \Rightarrow Q$

"If you can unlock my home then you can take my money"  $Q \Rightarrow R$

Conclusion: "If you have my home key then you can take my money"  $P \Rightarrow R$

$$\frac{P \Rightarrow Q, Q \Rightarrow R}{P \Rightarrow R}$$

⑩ Dinjunctive syllogism: If  $P \vee Q$  is true, and  $\neg P$  is true, then  $Q$  will be true.

Notation of Addition =  $\frac{P \vee Q, \neg P}{Q}$

Example: "Today is sunday or monday"  $\models P \vee Q$

"Today is not sunday"  $\models \neg P$

Conclusion: Today is monday.

⑪ Addition: If  $P$  is true then  $P$  or  $Q$  will be true." Notation:  $P / P \vee Q$

example: "I have a vanilla icecream"  $\models P$

"I have a chocolate icecream"  $\models Q$

Conclusion: I have vanilla or chocolate icecream.  $(P \vee Q) / P \vee Q$

vi) Simplification: If  $P \wedge Q$  is true, then  $Q$  or  $P$  will also be true.

Notation:  $P \wedge Q / P$  or  $P \wedge Q / Q$

vii) Resolution: If  $P$  or  $Q$  and  $\neg P \wedge R$  is true then  $Q \vee R$  will also be true.

Notation:  $\frac{P \vee Q, \neg P \wedge R}{Q \vee R}$

(4<sup>th</sup> part)

✓ KB for Wumpus world:

				A
				Gr
				OK
				P
				S
				✓
				W
				B
1,4	2,4	3,4	4,4	
1,3	2,3	3,3	4,3	
1,2	2,2	3,2	4,2	
1,1	2,1	3,1	4,1	

Atomic proposition variable for Wumpus world:  
 let,  $P_{i,j}$  be true if ~~agent perceive breeze~~ <sup>there is a pit in the room</sup> [i,j]

- \* let  $B_{i,j}$  true if agent perceive breeze in [i,j]. (dead or active)
- \* let  $W_{i,j}$  be true if there is wumpus in the square [i,j]

- ✓ let  $s_{i,j}$  be true if agent perceive stench is in the square  $[i,j]$
  - ✓ let  $g_{i,j}$  be true if gold in the square  $[i,j]$
  - ✓ let  $o_{i,j}$  be true if there room in safe
- propositional rules - for the wumpus world.
- R1 :  $\neg s_{1,1} \Rightarrow \neg w_{1,1} \wedge \neg w_{1,2} \wedge \neg w_{2,1}$
- R2 :  $\neg s_{2,1} \Rightarrow \neg w_{1,1} \wedge \neg w_{2,1} \vee \neg w_{2,2} \wedge \neg w_{3,1}$
- R3  $\neg s_{1,2} \Rightarrow \neg w_{1,1} \wedge \neg w_{1,2} \wedge \neg w_{2,2} \wedge \neg w_{1,3}$
- R4  $\neg s \Rightarrow w_{1,3} \vee w_{1,2} \vee w_{2,2} \vee w_{1,1}$

# Prove that umbras in room [1,3]

Sol =  $\vdash_1$ . Apply modus ponens with

$\neg S_{1,1}$  and  $R_1$

$\neg S_{1,1} \Rightarrow \neg w_{1,1} \wedge \neg w_{1,2} \wedge \neg w_{2,1}$

2. Apply and elimination rules:

$\neg w_{1,1}, \neg w_{1,2}, \neg w_{2,1}$

$\rightarrow \neg S_{2,1}$  and  $R_2$

$\neg S_{2,1} \Rightarrow \neg w_{1,1} \wedge \neg w_{2,1} \wedge \neg w_{2,2} \wedge \neg w_{3,1}$

$\neg w_{1,1}, \neg w_{2,1}, \neg w_{2,2}, \neg w_{3,1}$

$\rightarrow \neg S_{1,1}$  and  $R_3$

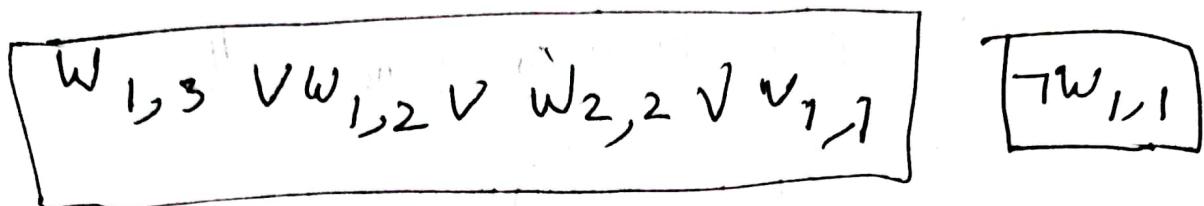
$\neg S_{1,2} \Rightarrow \neg w_{1,1} \wedge \neg w_{1,2} \vee \neg w_{2,1} \wedge \neg w_{1,3}$

$\neg w_{1,1}, \neg w_{1,2}, \neg w_{2,2}, \neg w_{1,3}$

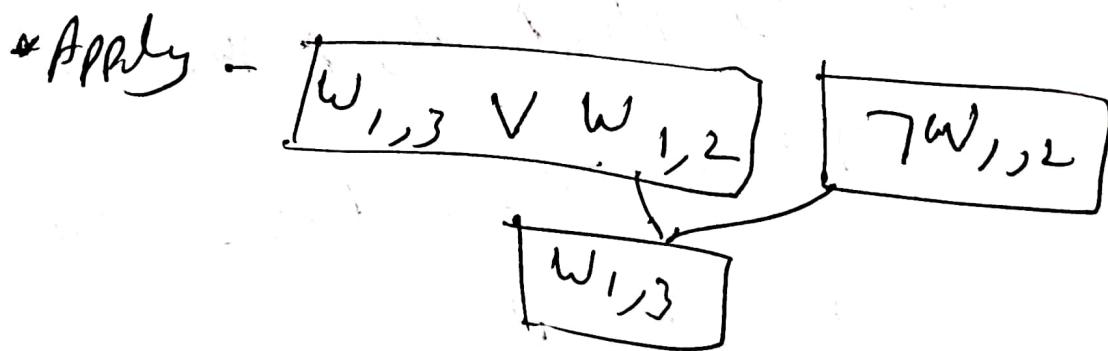
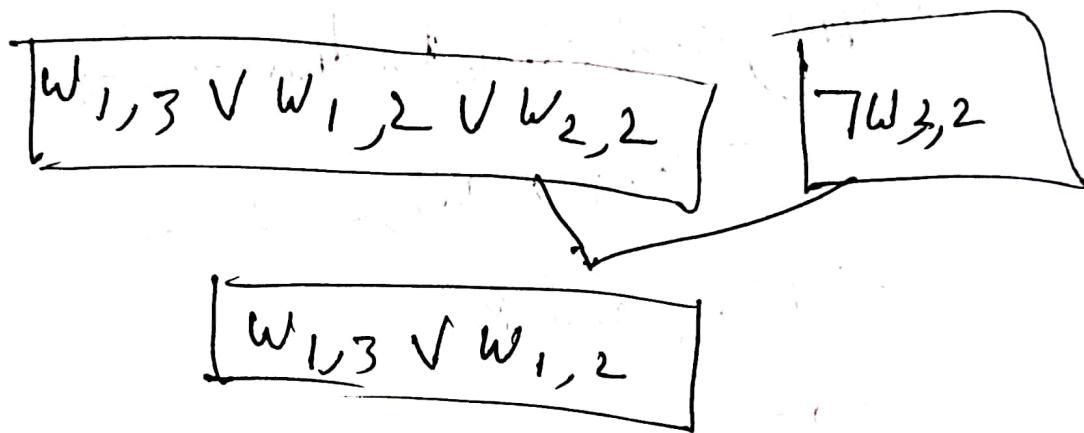
$\rightarrow S_{1,2} \& R4 : S_{1,2} \Rightarrow \frac{w_{1,3} \vee w_{1,2} \vee w_{2,2} \vee w_{1,1}}{w_{1,2}, w_{2,2}, w_{2,1}}$

Apply unit resolution on  $w_{1,3} \vee w_{1,2} \vee w_{2,2} \vee w_{1,1}$   
and  $w_{1,1}$

we will see  $w_{1,3} \vee w_{1,2} \vee w_{2,2}$



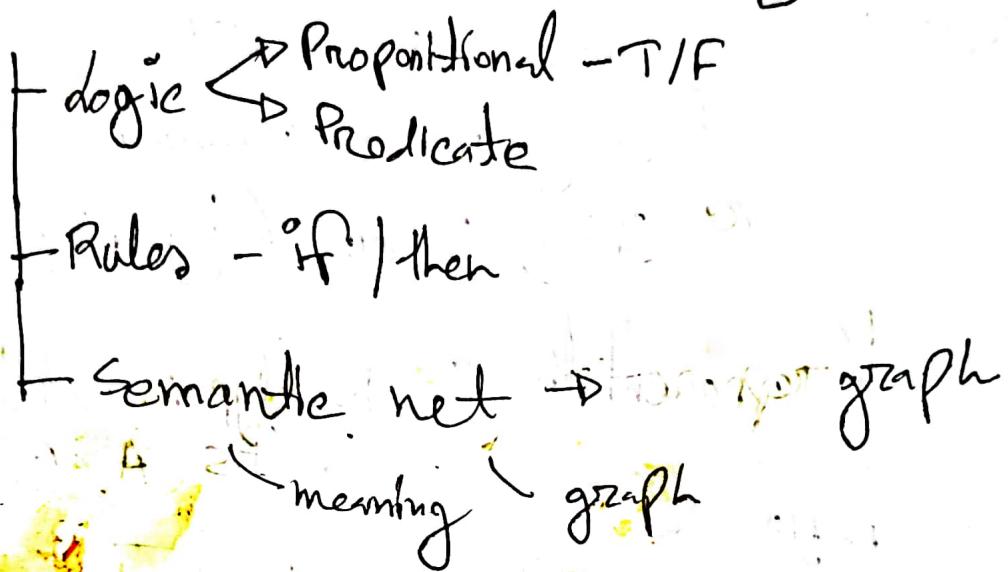
\* Apply unit resolution -



## Predicate

Plan-5

Knowledge representation and Reasoning :



Knowledge based Agents

Predicate logic:

Syntax      Semantics  
                    meaning

$\wedge$  conjunction  
 $\vee$  disjunction  
 $\neg$  negation  
 $\rightarrow$  implies  
 $\leftrightarrow$  biconditional

Semantic network representation:

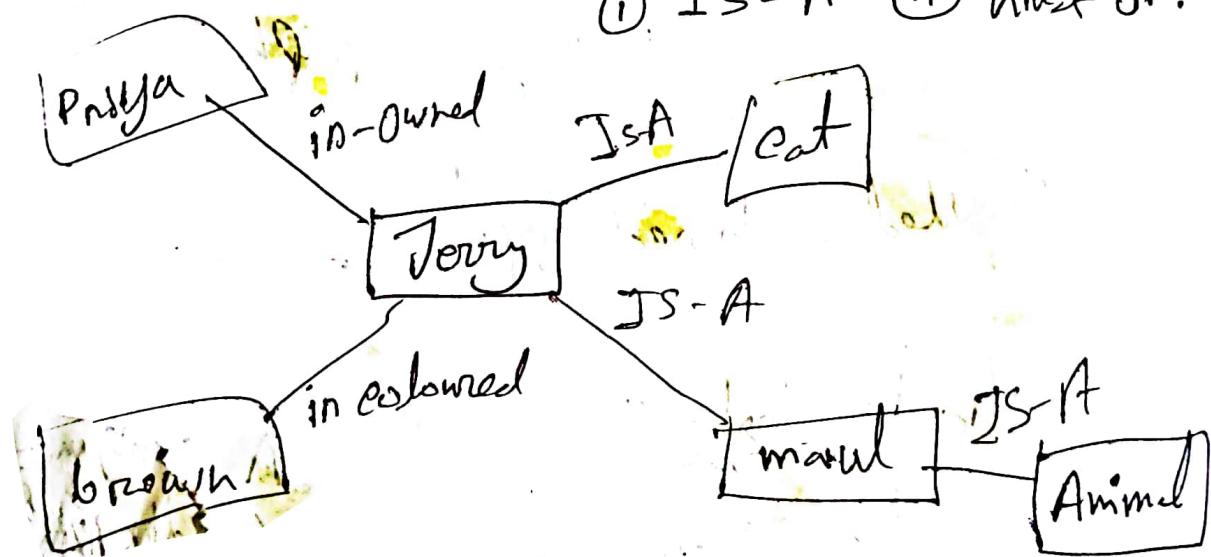
statement: (1) Jerry is a Cat.

(2) Jerry is a mammal

(3) Jerry is owned by Raja

Network representation: Two types relation  $\Rightarrow$

(1) IS-A (2) Kind of.



Statement: The artery is a particular kind of artery, which has a diameter of 2-5 cm.

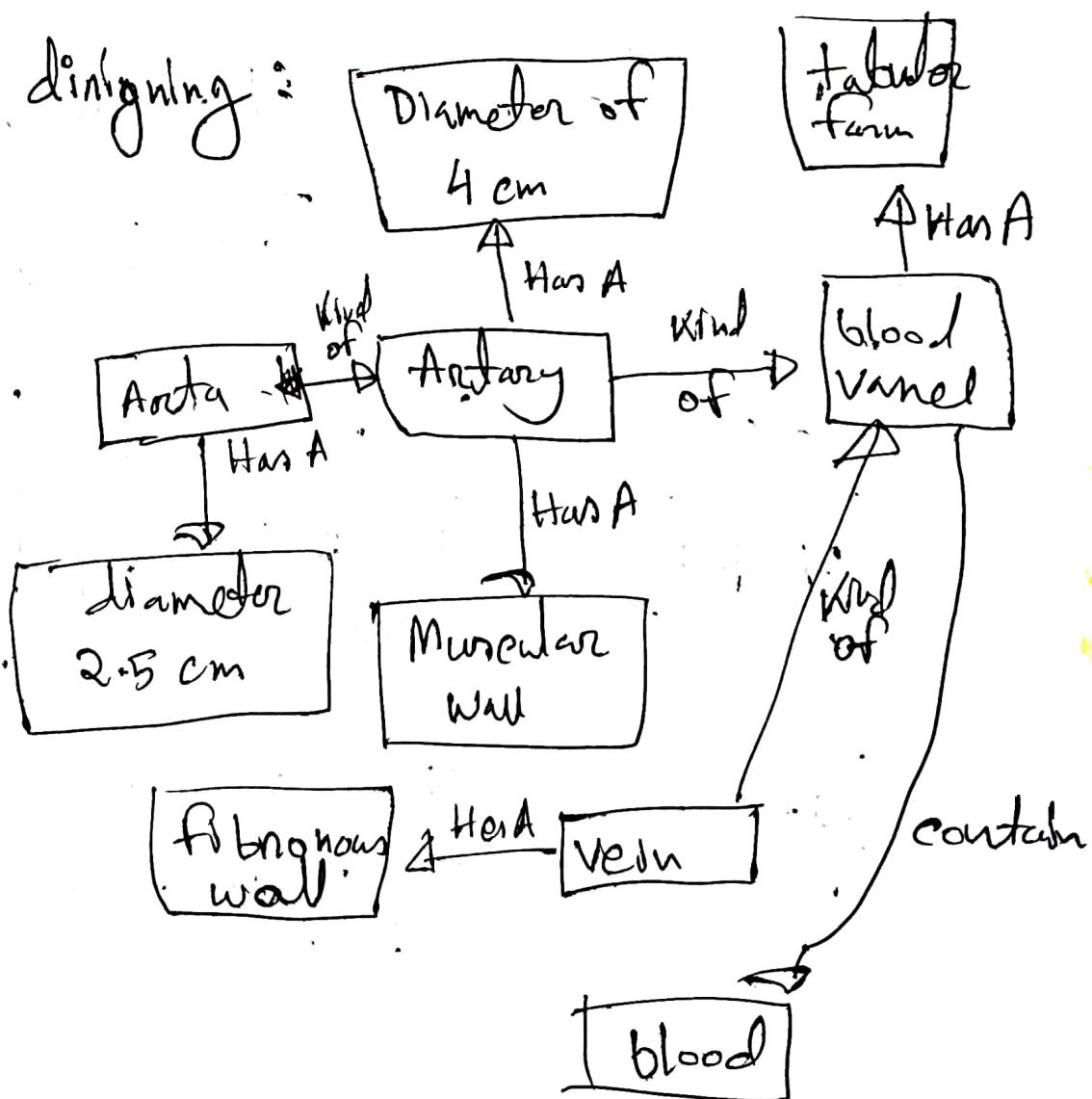
An artery is a kind of blood vessel. An artery always has a muscular wall and generally has

a diameter of 4 cm. A vein in a fibroid  
of blood vessel but has a ~~is~~ fibrous wall.

Blood vessels all have tubular form and contain blood.

relationship

## Network diagram



2 types of designing  $\Rightarrow$

① ~~frame~~ frame X  $\longrightarrow$  DDMMS System (Attribute, no)

② Production Rule: If condition then Action

statement: If (at the bus stop AND bus arrives)  
then (get into the bus)

✓ Predicate logic:  $\forall$  - Universal quantifier

$\exists$  - Existential quantifier

Statement	when true	when false
$\forall n P(n)$ Loop	$P(n)$ is true for every $n$	There is an $n$ for which $P(n)$ is false
$\exists n P(n)$ (and )	There is an $n$ for which $P(n)$ is true	$P(n)$ is false for every $n$ .

express the statement:

"Every student in the class has studied calculus" using predicate and quantifier.

student predicate  $S(x)$

calculus predicate  $C(x)$

Statement:  $\forall x(S(x) \Rightarrow C(x))$

"All Mon are fierce"

"Some Mon do not drink coffee -".

"some fierce creatures do not drink coffee!"

$P(x) = "x is a Mon"$

$Q(x) = "x is fierce"$

$R(x) = "x drinks coffee"$ .

$s_1 \models \forall (P(x) \Rightarrow Q(x))$

$s_2 \models \exists x(P(x) \wedge \neg R(x))$

$s_3 \models \exists x(Q(x) \wedge \neg R(x))$

Example:

# All birds fly.

$$\forall x \text{ Bird}(x) \rightarrow \text{fly}(x)$$

\* Not all student like both mathematics and Science.

Predicate question  $\text{like}(x, y)$

where  $x = \text{student}$  and  $y = \text{subject}$

$$\exists x [\text{student}(x) \rightarrow (\text{like}(x, \text{mathematics}) \wedge \text{like}(x, \text{Science}))]$$

logical inference

→ Notion of entailment

→ Model checking: x enumerate all possible models and check whether  $\alpha$  is true.

→ Sound (or truth preserving):

•  $i$  is a sound iff whenever  $K \models \alpha$  in  $i$   
if is also true that  $K \models \beta$ .

• Model checking is sound.

→ Complete

Proof Method

→ Application of inference rules

Proof Tree  
FOL

legitimate (sound) generation of new sentences

from old

→ Resolution - Proof by contradiction.

- forward and backward chaining.

→ Model Checking:

Searching through truth assignments

\* Improved backtracking (DPLL)

\* Heuristic search in model space:  
walksat

④

Conjunctive normal form:

$$P \rightarrow Q \equiv \neg P \vee Q$$

We would like to prove:  $KB \not\models \alpha$

equivalent to  $\neg KB \wedge \neg \alpha$ , unsatisfied.

$KB \wedge \neg \alpha$  into conjunctive normal form (CNF)



A "conjunction of disjunction"

Resolution: → Algorithm works using proof of contradiction.

→ To show  $KB \not\models \alpha$ , we know that  $KB \wedge \neg \alpha$  is not satisfied.

→ Apply resolution to  $KB \wedge \neg \alpha$  in CNF and resolve pairs with complementary literals

\* Statement: if the unicorn is mythical, then it is not immortal, but if it is not mythical, it is a mammal. If the unicorn is either immortal or a mammal, then it is horned.

Prove: the unicorn is horned.

Sol:  $M = \text{mythical}$ ,  $I = \text{immortal}$ ,  $A = \text{mammal}$ ,  $H = \text{horned}$ .

$$\textcircled{i} M \Rightarrow I, \underline{\text{CNF}}: \neg M \vee I$$

$$\textcircled{ii} \neg M \Rightarrow A, \underline{\text{CNF}}: M \vee A$$

$$\textcircled{iii} I \vee A \Rightarrow H, \underline{\text{CNF}}: \neg(I \vee A) \vee H,$$

Statement: ① If it is sunny & warm day you will enjoy. [Sunny  $\wedge$  Warm  $\Rightarrow$  enjoy]  $\rightarrow$  Prop. logic

② If it is raining you will get wet.  
[Raining  $\Rightarrow$  wet]

③ If it is a warm day. [warm]

④ It is raining [Raining]

⑤ It is sunny [sunny]

Prove: you will enjoy.

Solve: ① Sunny  $\wedge$  Warm  $\Rightarrow$  enjoy

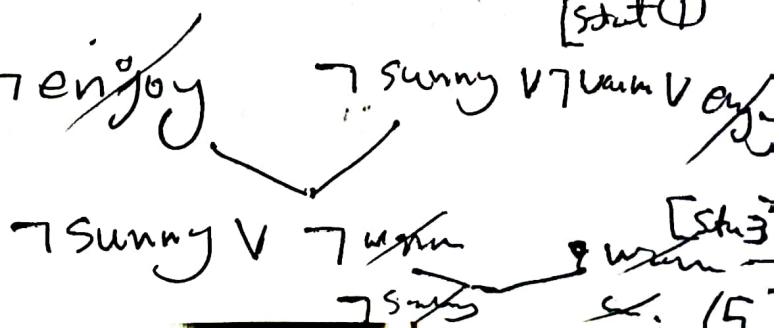
$$\equiv \neg(\text{Sunny} \wedge \text{Warm}) \vee \text{enjoy}$$

$$\equiv \neg \text{Sunny} \vee \neg \text{Warm} \vee \text{enjoy}$$

② Raining  $\Rightarrow$  wet

$$\equiv \neg \text{Raining} \vee \text{wet}$$

Draw resolution graph:  $\neg \text{enjoy}$        $\neg \text{Sunny} \vee \neg \text{Warm} \vee \text{enjoy}$



[Step 1]

[Step 2]

[Step 3]

[Step 4]

[Step 5]

[Step 6]

[Step 7]

[Step 8]

[Step 9]

[Step 10]

[Step 11]

[Step 12]

[Step 13]

[Step 14]

[Step 15]

7 sunny      8 sunny      [Statement 5]

$\Rightarrow \Rightarrow$  contradiction.

✗ Wampus Onev.

	1	1	1
	12		
	11		

Rules / Statement:

$$R_1 : \neg P_{1,1}$$

$$R_2 : B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})$$

$$R_3 : B_{2,1} \Leftrightarrow (P_{1,1} \vee P_{2,2} \vee P_{3,1})$$

$$R_4 : \neg B_{1,1}$$

$$R_5 : B_{2,1}$$

Is there a path in  $[1-2]$ ?

Sol: we have  $KB = R_1 \wedge R_2 \wedge R_3 \wedge R_4 \wedge R_5$ ,

we want to prove  $\neg P_{1,2}$

$$B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})$$

$$\equiv (B_{1,1} \Rightarrow (P_{1,2} \nmid V P_{2,1})) \wedge (P_{1,2} \vee P_{2,1}) \Rightarrow B_{1,1}$$

by bicondition elimination R 2.

$$\equiv (P_{1,2} \vee P_{2,1}) \Rightarrow B_{1,1} \text{ by AND elimination}$$

$$\equiv \neg B_{1,1} \Rightarrow \neg (P_{1,2} \vee P_{2,1}) \text{ by contraposition.}$$

$$\equiv \neg (P_{1,2} \vee P_{2,1}) \text{ by Modus Ponens.}$$

$$\equiv \neg P_{1,2} \wedge \neg P_{2,1}$$

That is neither no pit found both place.

Resolution:  $\text{KB} = (\beta_{-1,1} \Leftrightarrow (p_{1,2} \vee p_{2,1}))_{1,2,1}$

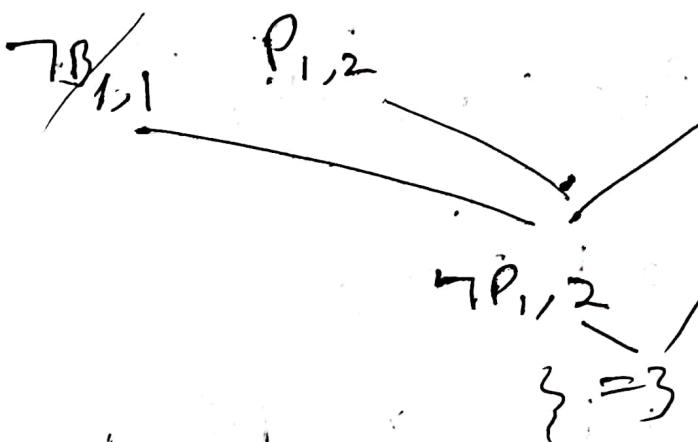
$$\alpha = \neg p_{1,2}$$

(HW)

=D:

Resolution graph:

$$\neg p_{2,1} \vee p_{1,1}, \quad \neg \beta_{1,1} \vee p_{1,2} \vee p_{2,1}, \quad \neg p_{1,2} \vee$$



(C-E)

Inference in first order logic:

#Rules of FOL:

\* Universal Generalization:  $\frac{P(c)}{\forall x P(x)}$

If we want to prove that every element

Example: let represent,  $P(c)$ : "A byte contains 8 bit,"

so "All bytes contain 8 bits" for  $\forall x P(x)$ , it will also be true.

$\xrightarrow{\text{Generalization}}$

\* Universal Instantiation (UI):

→ A valid inference in universal instantiation.  
 $\frac{(\forall B \neq \alpha)}{P(c)}$

→ We can infer any phrase by replacing a ground word for the variable.

→ The UI rule says that we can infer any sentence  $P(c)$  by substituting a ground term  $c$  (a constant

within domain  $x$ ) from  $\forall x P(x)$  for any object  
object in the universe of discourse.

exm: If "Every person like ice cream";  $\forall x P(x)$   
so we can infer that

"John likes ice-cream";  $P(c)$

exm: All kings who are greedy are Evil!

FOL statement:  $\forall n \text{ King}(n) \wedge \text{greedy}(n) \Rightarrow \text{Evil}(n)$

Infer statement:  $\text{King}(\text{John}) \wedge \text{Greedy}(\text{John}) \Rightarrow \text{Evil}(\text{John})$

/  $\text{King}(\text{Richard}) \wedge \text{Greedy}(\text{Richard}) \Rightarrow \text{Evil}(\text{Richard})$

$\text{father}(\text{John}) = \text{Richard}$

According to VI:  $\text{King}(\text{father}(\text{John})) \wedge \text{Greedy}(\text{father}(\text{John}))$   
 $\Rightarrow \text{Evil}(\text{father}(\text{John}))$ .

(3)  $\square$  Entailment Instantiation: this rules state that for a new constant symbol  $c$ , one can deduce  $P(c)$  from the formula given in the form of  $\exists x P(x)$ .

It can be represented as,  $\frac{\exists x P(x)}{P(c)}$

example: FOL ~~equivalent~~:  $\exists x \text{Crown}(x) \wedge \text{OnHead}(x, \text{John})$

so we can infer  $\text{Crown}(d) \wedge \text{OnHead}(d, \text{John})$

$\square$  Unification: It is the process of finding substitution that makes two separate logical atomic expression identical.

It accepts two literals as input and use substitution to make them identical.

let  $\phi_1$  and  $\phi_2$  be two atomic sentence and  $\alpha$  be a unifier such that  $\phi_1 \alpha \models \phi_2 \alpha$ ; then

$\text{unify}(\phi_1, \phi_2)$

Example: find the most general unifier (M.G.U) for

Unify  $\{ \text{King}(x), \text{King}(\text{John}) \}$

let  $\phi_1 = \text{King}(n)$ ,  $\phi_2 = \text{King}(\text{John})$

for two different expression,  $P(n, y) \& P(a, f(z))$

$$\phi_1 = P(n, y)$$

$$\phi_2 = P(a, f(z))$$

Substitute  $x$  with  $a$ ,  $y$  with  $f(z)$ ; it will be represented  $x/a$  and  $f(z)/y$ .

Final substitute set will be :  $P(x/a, f(z)/y)$ .

Unification Algorithm :- Step 1: Begin by making the substitution set empty.

Step 2: Unify atomic sentence in a recursive manner :-

i) check for expression that are identical.

ii) If one expression is a variable  $v_i$ , & the other is a term  $t_i$ , what does not contain variable  $v_i$ , then

② Substitute  $t_i/v_i$  in the entering substitute.

③ Add  $t_i/v_i$  to the substitution set  $S$ .

(E-7)

~~36GATE~~: Q) If both the expression are function, then function name must be similar, and the number of arguments must be same for both expression.

Q1: Find the most general unifier (M.G.U) of  $\{P(f(x), g(y)), P(x, x)\}$

$$\text{Sol: } \Psi_1 = P(f(u), g(v)), \Psi_2 = P(u, u)$$

Subst.:  $\{f(a)/u\}$

$$\Psi_1 = P(f(a), g(v)), \Psi_2 = P(f(a), f(a))$$

Subst.:  $\{f(a)/g(v)\}$  - Unification failed.

Unification not possible for this expression.

Q2: Unify  $(\text{Known}(\text{Richard}, n), \text{Known}(\text{Richard}, \text{John}))$

Sol:  $\Psi_1 = \text{Known}(\text{Richard}, n), \Psi_2 = \text{Known}(\text{Richard}, \text{John})$

Substitution:  $\{\text{John}/n\}$

$$S_1 = \{\text{Known}(\text{Richard}, \text{John}), \text{Known}(\text{Richard}, \text{John})\}$$

We can try to unify  $P(x,y) P(z,z)$  &  $P(y,z) \{y/z\}$   
 $\Rightarrow P(x,y), P(x,z) \text{ X} \text{ (X)}$   
✓ if  $P(x,y) P(z,z)$  then not possible = X

successful unif. sol.

unif. sol:  $\{x/n\}$

Q3: Unify  $\{P(b,n,f(g(z))) \& P(z,f(y),f(y))\}$

Sol:  $S_0 \Rightarrow \{P(b,n,f(g(z))), P(z,f(y),f(y))\}$

subst:  $\{b/z\}$

$S_1 \Rightarrow \{P(b,n,f(g/z)), P(b,f(y),f(y))\}$

~~$S_2 \Rightarrow \{P(b,n,f(g/y)), P(b,f(y),f(y))\}$~~  subst:  $\{f(y)/n\}$

$S_2 \Rightarrow \{P(b,n,f(g/z)), P(b,n,f(y))\}$

subst:  $\{g(b)/y\}$

$S_3 \Rightarrow \{P(b,f(g/b)), f(g/b); P(b,f(g/b), f(g/b))\}$

unif. sol:  $\{b/z, f(y)/n, g(b)/y\}$

Q4: Unify  $\{P(x_1, y), \text{ and } P(z_2, f(z))\}$

$$\text{unifiers} = \{x/z\}$$

$$S_0 \Rightarrow \{P(z/z), P(z, f(z))\}$$

and function substitution.

## Step by Resolution

1. Conversion of facts into FOL
2. Convert FOL statements into CNF
3. Negate the statement which needs to prove  
(proof by)
4. Draw resolution graph (Unification)

## Q problem:-

- (1) Anything anyone eats and not killed in food
- (2) Alex eats <sup>nuts</sup> peanut and still alive
- (3) John likes all kind of food
- (4) (3) Harry eats everything that Alex eat
- (5) Apple and vegetable are food

prove by resolution that John likes

Step 01

$\forall x \forall y \text{ eatn}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)$

Step 02 (without adding predicates) alive (Alex)

(a)  $\forall x \text{ eatn}(\text{Alex}, x) \rightarrow \text{alive}(\text{Herry}, x)$

(b)  $\forall x \neg \text{killed}(x) \rightarrow \text{alive}(\text{John}, x)$

(c) food (apple)  $\wedge$  food (vegetables)

added  
predicates

{ (d)  $\forall x \neg \text{killed}(x) \rightarrow \text{alive}(x)$   
(e)  $\forall x \text{ alive}(x) \rightarrow \neg \text{bleeding}(x)$   
(f)  $\text{alive}(\neg \text{John}, \text{Peanuts})$

Step 02 :-

Conversion of FOL into CNF

(a)  $\forall x \forall y \neg [\text{eatn}(x, y) \wedge (\neg \text{killed}(x) \wedge \text{food}(y))]$

$\vee \text{food}(y)$

(b)  $\text{eatn}(\text{Alex}, \text{peanuts}) \wedge \text{alive}(\text{Alex})$

(c)  $\forall x : \neg \text{eatn}(\text{Alex}, x) \vee \text{eatn}(\text{Herry}, x)$

(a)  $\forall n : \neg \text{food}(n) \vee \text{liker}(\text{John}, n)$

(b)  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$

(c)  $\forall n : [\neg \text{killed}(n)] \vee \text{alive}(n)$

(d)  $\forall n : \neg \text{alive}(n) \vee \neg \text{killed}(n)$

(e)  $\text{liker}(\text{John}, \text{peanuts})$

\* By dropping universal quantifiers -

1.  $\neg \text{eats}(y, z) \vee \text{killed} \vee \text{food}(z)$

2.  $\neg \text{eats}(\text{Alex}, w) \vee \text{eats}(\text{Honey}, w)$

3.  $\neg \text{food}(n) \vee \text{liker}(\text{John}, n)$

4.  $\neg \text{food}(\text{Apple})$

5.  $\text{food}(\text{vegetables})$

6.  $\text{eats}(\text{Alex}, \text{peanuts})$

7.  $\text{alive}(\text{Alex})$

8.  $\text{killed}(g) \vee \text{alive}(g)$

9.  $\neg$  alive (K) v  $\neg$  killed (K)

and gula  
around top  
large at  
on gula end  
down to

10. like (John, peanut)

Step 3

$\neg$  like (John, peanut)  $\neg$  food (n) v like (John, n)

{peanut/n}

$\neg$  food (Peanut)  $\neg$  eat(z) v kill  
food(z)

peanut/z

$\neg$  eatn (y, peanut) v  
y

killed (Alex)

alive (A)

v  $\neg$  killed

Alex (K)

$\neg$  Alive (Alex) alive (A)

ex

④ inference engine -

1. forward chaining
2. Backward chaining

Tree:

Definite clause - A clause which in a disjunction of literals with exactly one positive literal is known as a definite clause or unit clause.

- ct horn clauses

- eatn (Alex, peanut)

{A def/y}

Horn clause - A clause which in disjunction of literals with at most one positive literal is known as horn clause

of literals with at most one positive literal is known as horn clause

For example -  $(\neg p \vee \neg q \vee r)$ . It has only one positive literal  $r$ .

It is equivalent  $p \wedge q \rightarrow r$

Example:- Forward chaining:-

prob "As per the law, it is a crime for an American to sell weapons to hostile nations. Country A, an enemy of America has some missiles and all the missiles were sold to it by Robert who is an American citizen".

prove that using forward chaining:-

" Robert is criminal"

Sol'n: Fcn conversion into FOL:-

(a) It is a crime for an American to sell weapons to hostile nations.

1st Statement :-

(a) American (A) is weapon (P)  $\wedge$  hostile (H)  $\rightarrow$  Criminal (P)

(1)

(b) Country A has some missiles

Statement :-

Own (A, P)  $\wedge$  Missile (P)

Own (A, T<sub>1</sub>) - - (2)

Missile (T<sub>2</sub>) - - (3)

(c) All of the missiles were sold to Country  
by Robert Statement :-

Missile (P)  $\wedge$  Own (A, P)  $\Rightarrow$  Seller (Robert)

(d) Missiles are weapons

Statement :-

Missiles (P)  $\Rightarrow$  Weapons (P) - - (4)

(e) Enemy of America is known as hostile

Statement

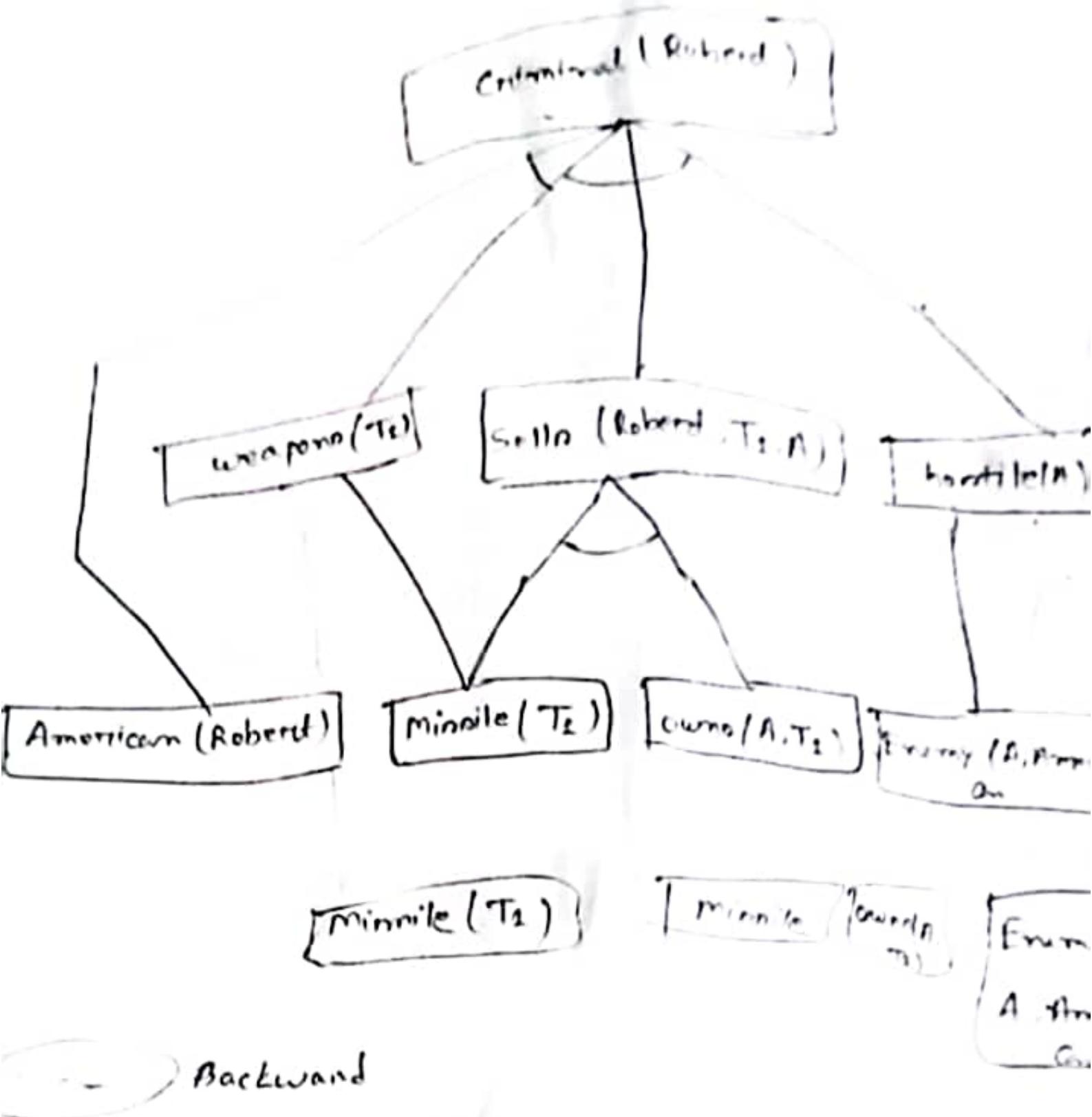
Enemy (P. America)  $\rightarrow$  Hostile (P). - (6)

(6) Country A is an enemy of America.

Enemy (A. America) - (7)

(7) Robert is American

American (Robert) - (8)



(Sunday)

- ML general setting:
- \* set of possible instances,  $x$
  - \* " " " labels,  $y$
  - \* unknown target func,  $f: x \rightarrow y$
  - \* set of function hypotheses,  $H = \{h | h: x \rightarrow y\}$   
each  $h$  in decision tree.

Input: Training examples of unknown target function of

$$\{(x_i, y_i)\}_{i=1}^n = \{(x_1, y_1), \dots, (x_n, y_n)\}$$

output: hypothesis  $h \in H$  that best approximates  $f$ .

Patient	Age	Edu	Prof	D
65	High	Driver		Y
30	IPHD	Program		N

How would we choose  
which feature to  
split the data?

Random: Choose any feature at random.

Least values: choose the feature with the fewest possible values.

Most-values: choose the features with most possible value

(impurity → mixed)  $\xrightarrow{\text{Pon/neg classes}}$

Max Gain: choose the feature with the largest expected information gain.  $\downarrow \text{Info}$

Learning bias: Ockham's Razor

ML  $\rightarrow$  "The simplest consistent explanation is the best!"

✓ Entropy (to measure impurity)  $H(Y) = -\sum P(x=i) \log_2 P(x=i)$

Info gain ( $X$ ; High BP) = Info ( $X$ ) - Info ( $X | \text{High BP}$ )

✓ Overfitting & Underfitting:



• K fold cross validation Method

Syllabus

→ T/F } Prop logic  
→ rules --  
→ inference  
→ resolution

✓ Predicate logic ]

✓ Unification apply resolution.

✓ backward forward chaining (Robert can) ]

✓ info gain ] ML .