

Problem Set 10

Physics 104A

Due Wednesday December 1, 11:59 PM

No late HW will be accepted.

Primary topic: PDE

1. (Does not need to be turned in) Derive the Laplacian operator in cylindrical coordinates.
2. a) Find the electrostatic potential everywhere inside a hollow sphere of radius 1 with surface potential $35(\cos \theta)^2$.
b) Find the electrostatic potential everywhere outside the sphere of part a) (assuming there are no charges elsewhere in the universe).

For problems 3 and 4 below, you can leave your answer in terms of a suitable series as long as you give an integral formula for how the series coefficients will be obtained.

3. A rectangular plate has its edges lying on the lines $x = 0$, $x = 30$, $y = 0$, and $y = 40$. Find the steady-state temperature distribution in the plate, given that the temperature is 0° along the two long sides and along the short side at $y = 0$, while at $y = 40$ the temperature is 100° for $0 < x < 10$ and 0° for $10 < x < 30$.
4. Find the steady-state temperature distribution in a spherical shell of inner radius 1 and outer radius 2 if the inner surface is held at 0° and the outer surface has its upper half at 100° and its lower half at 0° . (Note that with neither 0 nor infinity in the region you are solving for, you need to keep *both* r^n and $\frac{1}{r^{n+1}}$ radial solutions, and solve paired equations for their coefficients.)